HW3 - 20 Points

You have to submit two files for this part of the HW

```
(1) ipynb (colab notebook) and(2) pdf file (pdf version of the colab file).**
```

Files should be named as follows:

```
FirstName_LastName_HW_3**
```

Task 1 - Tensors and Autodiff - 5 Points

```
In [1]:
    import torch
    import torch.nn as nn
    from torch.utils import data
    import torch.functional as F
    from torch.utils.data import DataLoader, TensorDataset, Dataset
```

Q1: Create Tensor (1/2 Point)

Create a torch Tensor of shape (5, 3) which is filled with zeros. Modify the tensor to set element (0, 2) to 10 and element (2, 0) to 100.

```
In [2]: ten = torch.zeros(5, 3)
        print(ten)
        # Manually set the value at the first row and third column to 10,
        # and the value at the third row and first column to 100 in the tensor named "my te
        # code here
        ten[0,2] = 10
        ten[2, 0] = 100
        ten
      tensor([[0., 0., 0.],
              [0., 0., 0.],
              [0., 0., 0.],
              [0., 0., 0.],
              [0., 0., 0.]])
Out[2]: tensor([[ 0., 0., 10.],
                [0., 0., 0.]
                [100., 0., 0.],
                [ 0., 0., 0.],
                [ 0.,
                       0.,
                             0.]])
In [3]: ten.shape
```

```
Out[3]: torch.Size([5, 3])
```

Q2: Reshape tensor (1/2 Point)

You have following tensor as input:

```
x=torch.tensor([0, 1, 2, 3, 4, 5, 6, 7, 8, 9, 10, 11, 12, 13, 14, 15, 16, 17, 18, 19, 20, 21, 22, 23])
```

Using only reshaping functions (like view, reshape, transpose, permute), you need to get at the following tensor as output:

x = torch.transpose(x, 0, 1)

Χ

Q3: Slice tensor (1/2 Point)

- Slice the tensor x to get the following
 - last row of x
 - fourth column of x
 - first three rows and first two columns the shape of subtensor should be (3,2)
 - odd valued rows and columns

```
In [8]: # Student Task: Retrieve the Last row of the tensor 'x'
         # Hint: Negative indexing can help you select rows or columns counting from the end
         # Think about how you can select all columns for the desired row.
         last row = x[-1]
         last_row
 Out[8]: tensor([11, 12, 13, 14, 15])
 In [9]: # Student Task: Retrieve the fourth column of the tensor 'x'
         # Hint: Pay attention to the indexing for both rows and columns.
         # Remember that indexing in Python starts from zero.
         fourth column = x[:,-2]
         fourth_column
 Out[9]: tensor([ 4, 8, 14])
In [10]: # Student Task: Retrieve the first 3 rows and first 2 columns from the tensor 'x'.
         # Hint: Use slicing to extract the required subset of rows and columns.
         first_3_rows_2_columns = x[0:3, 0:2]
         first_3_rows_2_columns
Out[10]: tensor([[ 1, 2],
                  [6, 7],
                 [11, 12]])
In [11]: # Student Task: Retrieve the rows and columns with odd-indexed positions from the t
         # Hint: Use stride slicing to extract the required subset of rows and columns with
         odd_valued_rows_columns = x[::2, ::2]
         odd valued rows columns
Out[11]: tensor([[ 1, 3, 5],
                 [11, 13, 15]])
```

Q4 -Normalize Function (1/2 Points)

Write the function that normalizes the columns of a matrix. You have to compute the mean and standard deviation of each column. Then for each element of the column, you subtract the mean and divide by the standard deviation.

```
torch.Size([3, 4])
torch.float32

In [15]: # Compute and display the mean and standard deviation of each column for reference
    X.mean(axis = 0)
    X.std(axis = 0)

Out[15]: tensor([ 4.3589, 20.8167, 404.1452, 404.1452])

In [16]: X.std(axis = 0)

Out[16]: tensor([ 4.3589, 20.8167, 404.1452, 404.1452])
```

- Your task starts here
- Your normalize matrix function should take a PyTorch tensor x as input.
- It should return a tensor where the columns are normalized.
- After implementing your function, use the code provided to verify if the mean for each column in Z is close to zero and the standard deviation is 1.

```
In [17]: def normalize_matrix(x):
           # Calculate the mean along each column (think carefully , you will take mean alon
           mean = x.mean(axis=0)
           # Calculate the standard deviation along each column
           std = x.std(axis=0)
           # Normalize each element in the columns by subtracting the mean and dividing by t
           y = (x-mean)/std
           return y # Return the normalized matrix
In [18]: Z = normalize_matrix(X)
         Ζ
Out[18]: tensor([[ 0.6882, 0.8006, -1.0722, 1.0722],
                 [0.4588, -1.1209, 0.1650, -0.1650],
                 [-1.1471, 0.3203, 0.9073, -0.9073]])
In [19]: Z.mean(axis = 0)
Out[19]: tensor([ 0.0000e+00, 4.9671e-08, 3.9736e-08, -3.9736e-08])
In [20]: Z.std(axis = 0)
Out[20]: tensor([1., 1., 1., 1.])
```

Q5 -Calculate Gradients 1 Point

Compute Gradient using PyTorch Autograd - 2 Points

$$f(x,y) = rac{x + \exp(y)}{\log(x) + (x-y)^3}$$

Compute dx and dy at x=3 and y=4

```
In [21]: def fxy(x, y):
           # Calculate the numerator: Add x to the exponential of y
           num = x+torch.exp(y)
           # Calculate the denominator: Sum of the logarithm of x and cube of the difference
           den = torch \cdot log(x) + (x-y)**3
           # Perform element-wise division of the numerator by the denominator
           return num/den
In [22]: # Create a single-element tensor 'x' containing the value 3.0
         # make sure to set 'requires_grad=True' as you want to compute gradients with respe
         x = torch.tensor([3.0], requires_grad = True)
         # Create a single-element tensor 'y' containing the value 4.0
         # Similar to 'x', we want to compute gradients for 'y' during backpropagation, hence
         y = torch.tensor([4.0], requires_grad = True)
In [23]: # Call the function 'fxy' with the tensors 'x' and 'y' as arguments
         # The result 'f' will also be a tensor and will contain derivative information beca
         f = fxy(x, y)
Out[23]: tensor([584.0868], grad_fn=<DivBackward0>)
In [24]: # Perform backpropagation to compute the gradients of 'f' with respect to 'x' and '
         # Hint use backward() function on f
         f.backward()
In [25]: # Display the computed gradients of 'f' with respect to 'x' and 'y'
         # These gradients are stored as attributes of x and y after the backward operation
         # Print the gradients for x and y
         print('x.grad =', x.grad)
         print('y.grad =', y.grad)
        x.grad = tensor([-19733.3965])
        y.grad = tensor([18322.8477])
```

Q6. Numerical Precision - 2 Points

Given scalars x and y, implement the following log_exp function such that it returns

$$-\log\left(\frac{e^x}{e^x + e^y}\right)$$

```
In [26]: #Question
def log_exp(x, y):
    ## add your solution here and remove pass
    log_output = torch.tensor([-1]) * (torch.log(torch.div(torch.exp(x), torch.add(
    return log_output
```

Test your codes with normal inputs:

```
In [27]: # Create tensors x and y with initial values 2.0 and 3.0, respectively
x, y = torch.tensor([2.0]), torch.tensor([3.0])

# Evaluate the function log_exp() for the given x and y, and store the output in z
z = log_exp(x, y)

# Display the computed value of z
z
```

Out[27]: tensor([1.3133])

Now implement a function to compute $\partial z/\partial x$ and $\partial z/\partial y$ with autograd

```
In [28]: def grad(forward_func, x, y):
             # Enable gradient tracking for x and y, set reauires_grad appropriately
             x.requires_grad_(True)
             y.requires_grad_(True)
           # CODE HERE
           # Evaluate the forward function to get the output 'z'
             z = forward_func(x, y)
           # Perform the backward pass to compute gradients
           # Hint use backward() function on z
             z.backward()
           \# Print the gradients for x and y
             print('x.grad =', x.grad)
             print('y.grad =', y.grad)
           \# Reset the gradients for x and y to zero for the next iteration
             x.grad = x.grad.fill (0)
             y.grad = y.grad.fill_(0)
```

Test your codes, it should print the results nicely.

But now let's try some "hard" inputs

In [30]: x, y = torch.tensor([50.0]), torch.tensor([100.0])

```
In [31]: # you may see nan/inf values as output, this is not an error
          grad(log_exp, x, y)
        x.grad = tensor([nan])
        y.grad = tensor([nan])
In [32]: # you may see nan/inf values as output, this is not an error
          torch.exp(torch.tensor([100.0]))
Out[32]: tensor([inf])
          Does your code return correct results? If not, try to understand the reason. (Hint, evaluate
          exp(100)). Now develop a new function stable_log_exp that is identical to log_exp
          in math, but returns a more numerical stable result.
          Hint: (1) \log\left(\frac{x}{y}\right) = log(x) - log(y)
          Hint: (2) See logsum Trick - https://www.xarg.org/2016/06/the-log-sum-exp-trick-in-
          machine-learning/
In [33]: def stable_log_exp(x, y):
             z = torch.max(x, y)
              stable_log = -x + z + torch_log(torch_add(torch_exp(x - z), torch_exp(y - z)))
              \#torch.subtract((torch.log(x)), torch.log(y))
              return stable_log
In [34]: log_exp(x, y)
Out[34]: tensor([inf], grad_fn=<MulBackward0>)
In [35]: stable_log_exp(x, y)
Out[35]: tensor([50.], grad_fn=<AddBackward0>)
In [36]: grad(stable_log_exp, x, y)
        x.grad = tensor([-1.])
        y.grad = tensor([1.])
```

Task 2 - Linear Regression using Batch Gradient Descent with PyTorch- 5 Points

Regression using Pytroch

Imagine that you're trying to figure out relationship between two variables x and y . You have some idea but you aren't quite sure yet whether the dependence is linear or quadratic.

Your goal is to use least mean squares regression to identify the coefficients for the following three models. The three models are:

- 1. Quadratic model where $y = b + w_1 \cdot x + w_2 \cdot x^2$.
- 2. Linear model where $y = b + w_1 \cdot x$.
- 3. Linear model with no bias where $y = w_1 \cdot x$.
- You will use Batch gradient descent to estimate the model co-efficients.Batch gradient descent uses complete training data at each iteration.
- You will implement only training loop (no splitting of data in to training/validation).
- The training loop will have only one for loop. We need to iterate over whole data in each epoch. We do not need to create batches.
- You may have to try different values of number of epochs/ learning rate to get good results.
- You should use Pytorch's nn.module and functions.

Data

```
In [37]: x = torch.tensor([1.5420291, 1.8935232, 2.1603365, 2.5381863, 2.893443, \
                             3.838855, 3.925425, 4.2233696, 4.235571, 4.273397, \
                             4.9332876, 6.4704757, 6.517571, 6.87826, 7.0009003, \
                             7.035741, 7.278681, 7.7561755, 9.121138, 9.728281])
         y = torch.tensor([63.802246, 80.036026, 91.4903, 108.28776, 122.781975, \
                             161.36314, 166.50816, 176.16772, 180.29395, 179.09758, \
                             206.21027, 272.71857, 272.24033, 289.54745, 293.8488, \
                             295.2281, 306.62274, 327.93243, 383.16296, 408.65967])
In [38]: # Reshape the y tensor to have shape (n, 1), where n is the number of samples.
         # This is done to match the expected input shape for PyTorch's loss functions.
         y = y.reshape(y.size()[0], 1)
         \# Reshape the x tensor to have shape (n, 1), similar to y, for consistency and to w
         x = x.reshape(x.size()[0], 1)
         # Compute the square of each element in x.
         # This may be used for polynomial features in regression models.
         x2 = x * x
In [39]: # Concatenate the original x tensor and its squared values (x2) along dimension 1 (
         \# This creates a new tensor with two features: the original x and x2 (its square) .
         x_{combined} = torch.cat((x, x2), 1)
In [40]: print(x_combined.shape, x.shape)
        torch.Size([20, 2]) torch.Size([20, 1])
```

```
In [41]: x_combined.shape[-1]
Out[41]: 2
```

Loss Function

```
In [42]: # Initialize Mean Squared Error (MSE) loss function with mean reduction
# 'reduction="mean"' averages the squared differences between predicted and target
loss_function = nn.MSELoss(reduction = 'mean')
```

Train Function

```
In [43]: def train(epochs, x, y, loss function, log interval, model, optimizer):
             Train a PyTorch model using gradient descent.
             Parameters:
             epochs (int): The number of training epochs.
             x (torch.Tensor): The input features.
             y (torch.Tensor): The ground truth labels.
             loss_function (torch.nn.Module): The loss function to be minimized.
             log_interval (int): The interval at which training information is logged.
             model (torch.nn.Module): The PyTorch model to be trained.
             optimizer (torch.optim.Optimizer): The optimizer for updating model parameters.
             Side Effects:
             - Modifies the input model's internal parameters during training.
             - Outputs training log information at specified intervals.
             for epoch in range(epochs):
                 # Step 1: Forward pass - Compute predictions based on the input features
                 y hat = model(x)
                 # Step 2: Compute Loss
                 loss = loss function(y hat,y)
                 # Step 3: Zero Gradients - Clear previous gradient information to prevent a
                 optimizer.zero_grad()
                 # Step 4: Calculate Gradients - Backpropagate the error to compute gradient
                 loss.backward()
                 # Step 5: Update Model Parameters - Adjust weights based on computed gradie
                 optimizer.step()
                 # Log training information at specified intervals
                 if epoch % log interval == 0:
                     print(f'epoch: {epoch + 1} --> loss {loss.item()}')
```

Part 1

- For Part 1, use x_combined (we need to use both x and x^2) as input to the model, this means that you have two inputs.
- Use linear_reg function to specify the model, think carefully what values the three arguments (n_ins, n_outs, bias) will take..
- In PyTorch, the nn.Linear layer initializes its weights using Kaiming initialization by default, which is well-suited for ReLU activation functions. The bias terms are initialized to zero.

• In this assignment you will use nn.init functions like nn.init.normal_ and nn.init.zeros_, to explicitly override these default initializations to use your specified methods.

Run the cell below twice

In the first attempt

Use LEARNING_RATE = 0.05 What do you observe?

Write your observations HERE:

In the second attempt

Now use a LEARNING_RATE = 0.0005, What do you observe?

Write your observations HERE:

```
In [44]: # model 1
         LEARNING RATE = 0.0005
         EPOCHS = 100000
         LOG_INTERVAL= 10000
         # Use PyTorch's nn.Linear to create the model for your task.
         # Based on your understanding of the problem at hand, decide how you will initializ
         # Take into consideration the number of input features, the number of output featur
         # print(x combined.shape[-1])
         # print(y.size()[-1])
         model = nn.Linear(in_features = x_combined.shape[-1], out_features = y.size()[-1],
         # Initialize the weights of the model using a normal distribution with mean = 0 and
         # Hint: To initialize the model's weights, you can use the nn.init.normal_() functi
         # You will need to provide the 'model.weight' tensor and specify values for the 'me
         nn.init.normal_(model.weight, mean = 0, std = 0.01)
         # Initialize the model's bias terms to zero
         # Hint: To set the model's bias terms to zero, consider using the nn.init.zeros ()
         # You'll need to supply 'model.bias' as an argument.
         nn.init.zeros_(model.bias)
         # Create an SGD (Stochastic Gradient Descent) optimizer using the model's parameter
         optimizer = torch.optim.SGD(model.parameters(), LEARNING_RATE)
         # Start the training process for the model with specified parameters and sett
         train(EPOCHS, x_combined, y, loss_function, LOG_INTERVAL, model, optimizer)
```

```
epoch: 1 --> loss 57629.94921875
epoch: 10001 --> loss 5.004045486450195
epoch: 20001 --> loss 3.09553861618042
epoch: 30001 --> loss 2.1379129886627197
epoch: 40001 --> loss 1.6573289632797241
epoch: 50001 --> loss 1.4161760807037354
epoch: 60001 --> loss 1.294985055923462
epoch: 70001 --> loss 1.2341334819793701
epoch: 80001 --> loss 1.2036077976226807
epoch: 90001 --> loss 1.1882110834121704
In [45]: print(f' Weights {model.weight.data}, \nBias: {model.bias.data}')
Weights tensor([[4.1796e+01, 1.4833e-02]]),
Bias: tensor([0.9774])
```

Part 2

- For Part 1, use x as input to the model, this means that you have only one input.
- Use linear_reg function to specify the model, think carefully what values the three arguments (n_ins, n_outs, bias) will take..

```
In [46]: # model 2
         LEARNING RATE = 0.01
         EPOCHS = 1000
         LOG_INTERVAL= 10
         # Use PyTorch's nn.Linear to create the model for your task.
         # Based on your understanding of the problem at hand, decide how you will initializ
         # Take into consideration the number of input features, the number of output featur
         model = nn.Linear(in_features = x.shape[-1], out_features = y.size()[-1], bias = Tr
         # Initialize the weights of the model using a normal distribution with mean = 0 and
         # Hint: To initialize the model's weights, you can use the nn.init.normal_() functi
         # You will need to provide the 'model.weight' tensor and specify values for the 'me
         nn.init.normal_(model.weight, mean = 0, std = 0.01)
         # Initialize the model's bias terms to zero
         # Hint: To set the model's bias terms to zero, consider using the nn.init.zeros ()
         # You'll need to supply 'model.bias' as an argument.
         nn.init.zeros_(model.bias)
         # Create an SGD (Stochastic Gradient Descent) optimizer using the model's parameter
         optimizer = torch.optim.SGD(model.parameters(), LEARNING_RATE)
         # Start the training process for the model with specified parameters and settings
         # Note that we are passing x as an input for this part
         train(EPOCHS, x, y, loss_function, LOG_INTERVAL, model, optimizer)
```

epoch: 1 --> loss 57931.1484375 epoch: 11 --> loss 6.970406532287598 epoch: 21 --> loss 6.596502780914307 epoch: 31 --> loss 6.246757984161377 epoch: 41 --> loss 5.919557094573975 epoch: 51 --> loss 5.613437175750732 epoch: 61 --> loss 5.327097415924072 epoch: 71 --> loss 5.059176445007324 epoch: 81 --> loss 4.808563709259033 epoch: 91 --> loss 4.574114799499512 epoch: 101 --> loss 4.354766368865967 epoch: 111 --> loss 4.149575233459473 epoch: 121 --> loss 3.957587718963623 epoch: 131 --> loss 3.7780089378356934 epoch: 141 --> loss 3.6100101470947266 epoch: 151 --> loss 3.4528374671936035 epoch: 161 --> loss 3.305802583694458 epoch: 171 --> loss 3.168247938156128 epoch: 181 --> loss 3.039552688598633 epoch: 191 --> loss 2.9191665649414062 epoch: 201 --> loss 2.8065433502197266 epoch: 211 --> loss 2.7011678218841553 epoch: 221 --> loss 2.602609157562256 epoch: 231 --> loss 2.5104026794433594 epoch: 241 --> loss 2.424147129058838 epoch: 251 --> loss 2.343447208404541 epoch: 261 --> loss 2.267942190170288 epoch: 271 --> loss 2.197319746017456 epoch: 281 --> loss 2.131227493286133 epoch: 291 --> loss 2.0694172382354736 epoch: 301 --> loss 2.0115818977355957 epoch: 311 --> loss 1.9574825763702393 epoch: 321 --> loss 1.906874656677246 epoch: 331 --> loss 1.8595330715179443 epoch: 341 --> loss 1.8152427673339844 epoch: 351 --> loss 1.773810625076294 epoch: 361 --> loss 1.735033392906189 epoch: 371 --> loss 1.698767900466919 epoch: 381 --> loss 1.6648380756378174 epoch: 391 --> loss 1.6331119537353516 epoch: 401 --> loss 1.6034069061279297 epoch: 411 --> loss 1.5756254196166992 epoch: 421 --> loss 1.549647569656372 epoch: 431 --> loss 1.525327444076538 epoch: 441 --> loss 1.5025887489318848 epoch: 451 --> loss 1.4813003540039062 epoch: 461 --> loss 1.4614076614379883 epoch: 471 --> loss 1.4427732229232788 epoch: 481 --> loss 1.425364375114441 epoch: 491 --> loss 1.4090664386749268 epoch: 501 --> loss 1.3938236236572266 epoch: 511 --> loss 1.3795610666275024 epoch: 521 --> loss 1.3662116527557373 epoch: 531 --> loss 1.353738784790039 epoch: 541 --> loss 1.3420501947402954 epoch: 551 --> loss 1.3311245441436768

```
epoch: 561 --> loss 1.3209110498428345
        epoch: 571 --> loss 1.3113486766815186
        epoch: 581 --> loss 1.3023998737335205
        epoch: 591 --> loss 1.2940291166305542
        epoch: 601 --> loss 1.2862087488174438
        epoch: 611 --> loss 1.2788854837417603
        epoch: 621 --> loss 1.2720317840576172
        epoch: 631 --> loss 1.2656220197677612
        epoch: 641 --> loss 1.2596298456192017
        epoch: 651 --> loss 1.2540167570114136
        epoch: 661 --> loss 1.248769998550415
        epoch: 671 --> loss 1.2438617944717407
        epoch: 681 --> loss 1.2392655611038208
        epoch: 691 --> loss 1.234969973564148
        epoch: 701 --> loss 1.2309528589248657
        epoch: 711 --> loss 1.2271960973739624
        epoch: 721 --> loss 1.2236711978912354
        epoch: 731 --> loss 1.2203744649887085
        epoch: 741 --> loss 1.2173010110855103
        epoch: 751 --> loss 1.2144218683242798
        epoch: 761 --> loss 1.211728811264038
        epoch: 771 --> loss 1.2092041969299316
        epoch: 781 --> loss 1.2068431377410889
        epoch: 791 --> loss 1.2046411037445068
        epoch: 801 --> loss 1.202578067779541
        epoch: 811 --> loss 1.2006373405456543
        epoch: 821 --> loss 1.198833703994751
        epoch: 831 --> loss 1.1971498727798462
        epoch: 841 --> loss 1.1955734491348267
        epoch: 851 --> loss 1.1940834522247314
        epoch: 861 --> loss 1.192704677581787
        epoch: 871 --> loss 1.1914142370224
        epoch: 881 --> loss 1.1901978254318237
        epoch: 891 --> loss 1.1890780925750732
        epoch: 901 --> loss 1.1880154609680176
        epoch: 911 --> loss 1.1870167255401611
        epoch: 921 --> loss 1.186085820198059
        epoch: 931 --> loss 1.185221791267395
        epoch: 941 --> loss 1.1844091415405273
        epoch: 951 --> loss 1.1836483478546143
        epoch: 961 --> loss 1.18294358253479
        epoch: 971 --> loss 1.182273268699646
        epoch: 981 --> loss 1.181653380393982
        epoch: 991 --> loss 1.1810722351074219
In [47]: print(f' Weights {model.weight.data}, \nBias: {model.bias.data}')
        Weights tensor([[41.9377]]),
        Bias: tensor([0.7467])
```

Part 3

Part 3 is similar to part 2, the only difference is that model has no bias term now.

 You will see that we are now running the model for only ten epochs and will get similar results

```
In [48]: # model 3
         LEARNING RATE = 0.01
         EPOCHS = 10
         LOG_INTERVAL= 1
         # Use PyTorch's nn.Linear to create the model for your task.
         # Based on your understanding of the problem at hand, decide how you will initializ
         # Take into consideration the number of input features, the number of output featur
         model = nn.Linear(in_features = x.shape[-1], out_features = y.size()[-1], bias = Fa
         # Initialize the weights of the model using a normal distribution with mean = 0 and
         # Hint: To initialize the model's weights, you can use the nn.init.normal_() functi
         # You will need to provide the 'model.weight' tensor and specify values for the 'me
         nn.init.normal_(model.weight, mean = 0, std = 0.01)
         # We do not need to initilaize the bias term as there is no bias term in this model
         # Create an SGD (Stochastic Gradient Descent) optimizer using the model's parameter
         optimizer = torch.optim.SGD(model.parameters(), LEARNING_RATE)
         # Start the training process for the model with specified parameters and settings
         # Note that we are passing x as an input for this part
         train(EPOCHS, x, y, loss_function, LOG_INTERVAL, model, optimizer)
        epoch: 1 --> loss 57945.9453125
        epoch: 2 --> loss 6893.7275390625
        epoch: 3 --> loss 821.08251953125
        epoch: 4 --> loss 98.74296569824219
        epoch: 5 --> loss 12.821006774902344
        epoch: 6 --> loss 2.600693702697754
        epoch: 7 --> loss 1.3849643468856812
        epoch: 8 --> loss 1.240365743637085
        epoch: 9 --> loss 1.2231651544570923
        epoch: 10 --> loss 1.2211220264434814
In [49]: print(f' Weights {model.weight.data}')
```

Task 3 - MultiClass Classification using Mini Batch Gradient Descent with PyTorch- 5 Points

Data

```
In [50]: # Import the make_classification function from the sklearn.datasets module
# This function is used to generate a synthetic dataset for classification tasks.
```

Weights tensor([[42.0557]])

```
from sklearn.datasets import make_classification

# Import the StandardScaler class from the sklearn.preprocessing module
# StandardScaler is used to standardize the features by removing the mean and scali
from sklearn.preprocessing import StandardScaler
```

- In [51]: # Import the main PyTorch library, which provides the essential building blocks for import torch

 # Import the 'optim' module from PyTorch for various optimization algorithms like S import torch.optim as optim

 # Import the 'nn' module from PyTorch, which contains pre-defined layers, loss func import torch.nn as nn

 # Import the 'functional' module from PyTorch; incorrect import here, it should be # This module contains functional forms of layers, loss functions, and other operat import torch.functional as F # Should be 'import torch.nn.functional as F'

 # Import DataLoader and Dataset classes from PyTorch's utility library.
 # DataLoader helps with batching, shuffling, and loading data in parallel.
 # Dataset provides an abstract interface for easier data manipulation.
 from torch.utils.data import DataLoader, Dataset
- In [52]: # Generate a synthetic dataset for classification using make_classification functio
 # Parameters:
 # n_samples=1000: The total number of samples in the generated dataset.
 # n_features=5: The total number of features for each sample.
 # n_classes=3: The number of classes for the classification task.
 # n_informative=4: The number of informative features, i.e., features that are ac
 # n_redundant=1: The number of redundant features, i.e., features that can be lin
 # random_state=0: The seed for the random number generator to ensure reproducibil

 X, y = make_classification(n_samples=1000, n_features=5, n_classes=3, n_informative)

In this example, you're using make_classification to generate a dataset with 1,000 samples, 5 features per sample, and 3 classes for the classification problem. Of the 5 features, 4 are informative (useful for classification), and 1 is redundant (can be derived from the informative features). The random_state parameter ensures that the data generation is reproducible.

```
In [53]: # Initialize the StandardScaler object from the sklearn.preprocessing module.
# This will be used to standardize the features of the dataset.
preprocessor = StandardScaler()

# Fit the StandardScaler on the dataset (X) and then transform it.
# The fit_transform() method computes the mean and standard deviation of each featu # and then standardizes the features by subtracting the mean and dividing by the st
X = preprocessor.fit_transform(X)
```

Dataset and Data Loaders

```
In [57]: # Convert the numpy arrays X and y to PyTorch Tensors.
         # For X, we create a floating-point tensor since most PyTorch models expect float i
         # This is a multiclass classification problem.
         # IMPORTANT: # Consider what cost function you will use and whether it expects the
         # -----
         x_tensor = torch.tensor(X)
         y_tensor = torch.tensor(y)
In [58]: # Define a custom PyTorch Dataset class for handling our data
         class MyDataset(Dataset):
            # Constructor: Initialize the dataset with features and labels
            def __init__(self, X, y):
                self.features = X
                self.labels = y
            # Method to return the Length of the dataset
            def __len__(self):
                return self.labels.shape[0]
            # Method to get a data point by index
            def __getitem__(self, index):
                x = self.features[index]
                y = self.labels[index]
                return x, y
In [59]: # Create an instance of the custom MyDataset class, passing in the feature and labe
         # This will allow the data to be used with PyTorch's DataLoader for efficient batch
         train_dataset = MyDataset(x_tensor, y_tensor)
In [60]: # Access the first element (feature-label pair) from the train_dataset using indexi
         # The __getitem__ method of MyDataset class will be called to return this element.
         train dataset[0]
```

Out[60]: (tensor([-0.3944, -0.7803, -0.2501, 0.0912, -0.5691], dtype=torch.float64),

tensor(2, dtype=torch.int32))

```
In [61]: # Create Data Loader from Dataset
         # Use a batch size of 16
         # Use shuffle = True
         train loader = data.DataLoader(train dataset, batch size = 16, shuffle = True)
In [62]: for X batch, y batch in train loader:
             print(X_batch, '\n', y_batch)
             break
       tensor([[-0.2185, 0.9655, -1.3025, 1.1737, -0.4569],
               [-0.8762, 0.9241, -0.0717, 0.4633, -1.2034],
               [0.9676, -0.9052, 1.0567, 0.6395, 0.4591],
               [0.6487, -0.8149, -0.4108, -0.0971, 0.8600],
               [0.6102, -1.0195, 0.8864, 0.1992, 0.2890],
               [-0.7050, -2.6669, -0.8674, -1.6803, -0.0552],
               [-1.8729, 1.4647, -1.1924, -0.3540, -1.6296],
               [0.5527, -0.1956, 0.2116, -0.1725, 0.6984],
               [-0.0641, -0.7978, -0.6218, -1.0031, 0.5330],
               [-0.4552, -0.7291, 1.3423, 0.3070, -1.1682],
               [0.8297, 1.4415, 1.3723, 0.4348, 0.6096],
               [2.5057, 0.4694, 0.9073, 3.2727, 1.1241],
               [-0.2374, -3.0383, -0.9911, -0.9811, 0.1251],
               [-1.5176, 0.3580, 0.0854, -0.7736, -1.4282],
               [-0.5085, 0.4061, 0.1271, -1.5419, 0.2346],
               [ 0.1211, 0.1431, -0.1639, 0.1702, 0.1164]], dtype=torch.float64)
         tensor([1, 2, 0, 1, 0, 0, 2, 2, 0, 2, 1, 1, 0, 2, 0, 2], dtype=torch.int32)
```

Model

```
In [63]: # Student Task: Define your neural network model for multi-class classification.
# Think through what layers you should add. Note: Your task is to create a model th
# classification but doesn't include any hidden layers.
# You can use nn.Linear or nn.Sequential for this task
model = nn.Linear(5, 3) #, nn.Softmax(dim = 1)
# result = model(train_loader)
# print(f'output:{result}\n')
```

Loss Function

```
In [64]: # Student Task: Specify the loss function for your model.
# Consider the architecture of your model, especially the last layer, when choosing
# Reminder: The last layer in the previous step should guide your choice for an app

loss_function = nn.CrossEntropyLoss()
```

Initialization

Create a function to initilaize weights.

Initialize weights using normal distribution with mean = 0 and std = 0.05

• Initilaize the bias term with zeros

```
In [65]: # Function to initialize the weights and biases of a neural network layer.
# This function specifically targets layers of type nn.Linear.
def init_weights(layer):
    # Check if the layer is of the type nn.Linear.
    if type(layer) == nn.Linear:
        # Initialize the weights with a normal distribution, centered at 0 with a stand torch.nn.init.normal_(layer.weight, mean=0, std=0.05)
    # Initialize the bias terms to zero.
        torch.nn.init.zeros_(layer.bias)
```

Training Loop

Model Training involves five steps:

- Step 0: Randomly initialize parameters / weights
- Step 1: Compute model's predictions forward pass
- Step 2: Compute loss
- Step 3: Compute the gradients
- Step 4: Update the parameters
- Step 5: Repeat steps 1 4

Model training is repeating this process over and over, for many **epochs**.

We will specify number of *epochs* and during each epoch we will iterate over the complete dataset and will keep on updating the parameters.

Learning rate and **epochs** are known as hyperparameters. We have to adjust the values of these two based on validation dataset.

We will now create functions for step 1 to 4.

```
In [66]: # Function to train a neural network model.
# Arguments include the number of epochs, loss function, learning rate, model archi

def train(epochs, loss_function, learning_rate, model, optimizer):

# Loop through each epoch
for epoch in range(epochs):

# Initialize variables to hold aggregated training loss and correct prediction
running_train_loss = 0
running_train_correct = 0

# Loop through each batch in the training dataset using train_loader
for x, y in train_loader:

# Move input and target tensors to the device (GPU or CPU)
device = torch.device('cuda:0' if torch.cuda.is_available() else 'cpu')
```

```
x = x.to(device, dtype = torch.float32)
  targets = y.to(device, dtype = torch.long)
  # print(x.dtype)
  # Step 1: Forward Pass: Compute model's predictions
 output = model(x)
  # Step 2: Compute Loss
 loss = loss_function(output, targets)
  # Step 3: Backward pass - Compute the gradients
  # Zero out gradients from the previous iteration
 optimizer.zero_grad()
  # Backward pass: Compute gradients based on the loss
 loss.backward()
  # Step 4: Update the parameters
 optimizer.step()
  # Accumulate the loss for the batch
  running_train_loss += loss.item()
  # Evaluate model's performance without backpropagation for efficiency
  # `with torch.no_grad()` temporarily disables autograd, improving speed and a
 with torch.no_grad():
      y_pred = output.argmax(dim=1) # Find the class index with the maximum pre
      correct = (y_pred == targets).sum().item() # Compute the number of correct
      running_train_correct += correct # Update the cumulative count of correct
# Compute average training loss and accuracy for the epoch
train_loss = running_train_loss / len(train_loader)
train_acc = running_train_correct / len(train_loader.dataset)
# Display training loss and accuracy metrics for the current epoch
print(f'Epoch : {epoch + 1} / {epochs}')
print(f'Train Loss: {train_loss:.4f} | Train Accuracy: {train_acc * 100:.4f}%')
```

```
In [67]: # Fix the random seed to ensure reproducibility across runs
    torch.manual_seed(100)

# Define the total number of epochs for which the model will be trained
    epochs = 5

# Detect if a GPU is available and use it; otherwise, use CPU
    device = torch.device('cuda:0' if torch.cuda.is_available() else 'cpu')
    print(device) # Output the device being used

# Define the learning rate for optimization; consider its impact on model performan
    learning_rate = 1

# Student Task: Configure the optimizer for model training.
# Here, we're using Stochastic Gradient Descent (SGD). Think through what parameter
# Reminder: Utilize the learning rate defined above when setting up your optimizer.
```

```
optimizer = torch.optim.SGD(model.parameters(), learning_rate)
         # Relocate the model to the appropriate compute device (GPU or CPU)
         model.to(device)
         # Apply custom weight initialization; this can affect the model's learning trajecto
         # The `apply` function recursively applies a function to each submodule in a PyTorc
         # In the given context, it's used to apply the `init_weights` function to initializ
         # The benefit is that it provides a convenient way to systematically apply custom w
         # potentially improving model convergence and performance.
         model.apply(init_weights)
         # Kick off the training process using the specified settings
         train(epochs, loss_function, learning_rate, model, optimizer)
        Epoch : 1 / 5
        Train Loss: 0.8130 | Train Accuracy: 65.4000%
        Epoch : 2 / 5
        Train Loss: 0.8005 | Train Accuracy: 66.7000%
        Epoch : 3 / 5
        Train Loss: 0.7915 | Train Accuracy: 67.0000%
        Epoch : 4 / 5
        Train Loss: 0.7978 | Train Accuracy: 67.9000%
        Epoch : 5 / 5
        Train Loss: 0.8008 | Train Accuracy: 67.0000%
In [68]: # Output the Learned parameters (weights and biases) of the model after training
         for name, param in model.named_parameters():
           # Print the name and the values of each parameter
           print(name, param.data)
        weight tensor([[ 0.4345, -0.9407, -0.5891, -0.4591, 0.7364],
                [0.0557, 1.0332, 0.1920, 0.4732, 0.0554],
```

```
Task 4 - MultiLabel Classification using Mini Batch Gradient Descent with PyTorch- 5 Points
```

[-0.6367, -0.0987, 0.2159, 0.0453, -0.8418]])

bias tensor([-0.2508, -0.0254, 0.2762])

Data

```
In [69]: # Import the function to generate a synthetic multilabel classification dataset
from sklearn.datasets import make_multilabel_classification

# Import the StandardScaler for feature normalization
from sklearn.preprocessing import StandardScaler
In [70]: # Import PyTorch library for tensor computation and neural network modules
import torch
```

```
# Import PyTorch's optimization algorithms package
         import torch.optim as optim
         # Import PyTorch's neural network module for defining layers and models
         import torch.nn as nn
         # Import PyTorch's functional API for stateless operations
         import torch.functional as F
In [71]: # Generate a synthetic multilabel classification dataset
         # n_samples: Number of samples in the dataset
         # n_features: Number of feature variables
         # n classes: Number of distinct labels (or classes)
         # n_labels: Average number of labels per instance
         # random_state: Seed for reproducibility
         X, y = make multilabel classification(n samples=1000, n features=5, n classes=3, n
In [72]: # Initialize the StandardScaler for feature normalization
         preprocessor = StandardScaler()
         # Fit the preprocessor to the data and transform the features for zero mean and uni
         X = preprocessor.fit_transform(X)
In [73]: # Print the shape of the feature matrix X and the label matrix y
         # Students: Pay attention to these shapes as they will guide you in defining your n
         print(X.shape, y.shape)
        (1000, 5) (1000, 3)
In [74]: X[0:5]
Out[74]: array([[ 1.65506353, 0.2101857, 0.51570947, -2.00177184, 0.40001786],
                [-0.02349989, -0.51376047, 2.34771468, 0.78787635, -1.04334554],
                [1.09554239, 0.93413188, -0.09495894, -0.00916599, -0.01237169],
                [-0.58302103, 1.17544727, 0.21037527, -0.80620833, 0.8124074],
                [ 1.09554239, 0.69281649, -1.92696415, 1.18639752, -1.24954031]])
# IMPORTANT: # NOTE: The y in this case is one hot encoded.
         # This is different from Multiclass Classification.
         # The loss function we use for multiclass classification handles this internally
         # For multilabel case we have to provide y in this format
         print(y[0:10])
        [[0 0 1]
        [1 0 0]
         [1 \ 1 \ 1]
         [0 1 1]
         [1 1 0]
        [0 1 0]
        [1 \ 1 \ 1]
         [1 0 1]
         [1 \ 1 \ 1]
         [1 1 0]]
```

Dataset and Data Loaders

```
In [76]: # Student Task: Create Tensors from the numpy arrays.
         # Earlier, we focused on multiclass classification; now, we are dealing with multil
         # -----
         # IMPORTANT: # Consider what cost function you will use for multilabel classificati
         x tensor = torch.tensor(X)
         y_tensor = torch.tensor(y)
In [77]: # Define a custom PyTorch Dataset class for handling our data
         class MyDataset(Dataset):
             # Constructor: Initialize the dataset with features and labels
             def __init__(self, X, y):
                self.features = X
                 self.labels = y
             # Method to return the length of the dataset
             def __len__(self):
                 return self.labels.shape[0]
             # Method to get a data point by index
             def __getitem__(self, index):
                x = self.features[index]
                y = self.labels[index]
                 return x, y
In [78]: # Initialize an instance of the custom MyDataset class
         # This will be our training dataset, holding our features and labels as PyTorch ten
         train_dataset = MyDataset(x_tensor, y_tensor)
In [79]: # Access the first element (feature-label pair) from the train_dataset using indexi
         # The getitem method of MyDataset class will be called to return this element.
         # This is useful for debugging and understanding the data structure
         train_dataset[0]
Out[79]: (tensor([ 1.6551, 0.2102, 0.5157, -2.0018, 0.4000], dtype=torch.float64),
          tensor([0, 0, 1], dtype=torch.int32))
In [80]: # Create Data LOader from Dataset
         # Use a batch size of 16
         # Use shuffle = True
         train_loader = data.DataLoader(train_dataset, batch_size = 16, shuffle = True)
```

Model

```
In [81]: # Student Task: Specify your model architecture here.
# This is a multilabel problem. Think through what layers you should add to handle
# Remember, the architecture of your last layer will also depend on your choice of
```

```
# Additional Note: No hidden layers should be added for this exercise.
# You can use nn.Linear or nn.Sequential for this task
model = nn.Linear(5, 3)
```

Loss Function

```
In [82]: # Student Task: Specify the loss function for your model.
# Consider the architecture of your model, especially the last layer, when choosing
# This is a multilabel problem, so make sure your choice reflects that.

loss_function = nn.BCEWithLogitsLoss()
```

Initialization

Create a function to initilaize weights.

- Initialize weights using normal distribution with mean = 0 and std = 0.05
- Initilaize the bias term with zeros

```
In [83]: # Function to initialize the weights and biases of the model's layers
# This is provided to you and is not a student task
def init_weights(layer):
    # Check if the layer is a Linear layer
    if type(layer) == nn.Linear:
        # Initialize the weights with a normal distribution, mean=0, std=0.05
        torch.nn.init.normal_(layer.weight, mean = 0, std = 0.05)
        # Initialize the bias terms to zero
        torch.nn.init.zeros_(layer.bias)
```

Training Loop

Model Training involves five steps:

- Step 0: Randomly initialize parameters / weights
- Step 1: Compute model's predictions forward pass
- Step 2: Compute loss
- Step 3: Compute the gradients
- Step 4: Update the parameters
- Step 5: Repeat steps 1 4

Model training is repeating this process over and over, for many **epochs**.

We will specify number of **epochs** and during each epoch we will iterate over the complete dataset and will keep on updating the parameters.

Learning rate and **epochs** are known as hyperparameters. We have to adjust the values of these two based on validation dataset.

We will now create functions for step 1 to 4.

```
In [84]: # Install the torchmetrics package, a PyTorch library for various machine learning
# to facilitate model evaluation during and after training.
#!pip install torchmetrics

In [85]: # Import HammingDistance from torchmetrics
# HammingDistance is useful for evaluating multi-label classification problems.
from torchmetrics import HammingDistance
```

Hamming Distance is often used in multi-label classification problems to quantify the dissimilarity between the predicted and true labels. It does this by measuring the number of label positions where predicted and true labels differ for each sample. It is a useful metric because it offers a granular level of understanding of the discrepancies between the predicted and actual labels, taking into account each label in a multi-label setting.

Unlike accuracy, which is all-or-nothing, Hamming Distance can give partial credit by considering the labels that were correctly classified, thereby providing a more granular insight into the model's performance.

Let us understand this with an example:

```
In [86]: target = torch.tensor([[0, 1], [1, 1]])
    preds = torch.tensor([[0, 1], [0, 1]])
    hamming_distance = HammingDistance(task="multilabel", num_labels=2)
    hamming_distance(preds, target)
```

Out[86]: tensor(0.2500)

In the given example, the Hamming Distance is calculated for multi-label classification with two labels (0 and 1).

- 1. The target tensor has shape (2, 2): [[0, 1], [1, 1]]
- 2. The prediction tensor also has shape (2, 2): [[0, 1], [0, 1]]

Let's examine the individual sample pairs to understand the distance:

- For the first sample pair (target = [0, 1], prediction = [0, 1]), the Hamming Distance is 0 because the prediction is accurate.
- For the second sample pair (target = [1, 1], prediction = [0, 1]), the Hamming Distance is 1 for the first label (predicted 0, true label 1).

To calculate the overall Hamming Distance, we can take the number of label mismatches and divide by the total number of labels:

• Total Mismatches = 1 (from the second sample pair)

Total Number of Labels = 2 samples * 2 labels per sample = 4

Therefore, the overall Hamming Distance is (1/4 = 0.25), which matches the output tensor (0.2500).

Hamming Distance is a good metric for multi-label classification as it can capture the difference between sets of labels per sample, thereby providing a more granular measure of the model's performance.

```
In [87]: def train(epochs, loss_function, learning_rate, model, optimizer, train_loader, dev
             train_hamming_distance = HammingDistance(task="multilabel", num_labels=3).to(de
             for epoch in range(epochs):
                 # Initialize train_loss at the start of the epoch
                 running_train_loss = 0.0
                 # Iterate on batches from the dataset using train_loader
                 for x, y in train_loader:
                     # Move inputs and outputs to GPUs
                     device = torch.device('cuda:0' if torch.cuda.is_available() else 'cpu')
                     x = x.to(device, dtype=torch.float32)
                     y = y.to(device, dtype=torch.float32)
                     # Step 1: Forward Pass: Compute model's predictions
                     output = model(x)
                     # Step 2: Compute Loss
                     loss = loss_function(output, y)
                     # Step 3: Backward pass - Compute the gradients
                     # Zero out gradients from the previous iteration
                     optimizer.zero grad()
                     # Backward pass: Compute gradients based on the loss
                     loss.backward()
                     # Step 4: Update the parameters
                     optimizer.step()
                     # Update running Loss
                     running_train_loss += loss.item()
                     with torch.no grad():
                         # Correct prediction using thresholding
                         y_pred = (output > 0.9).float()
                         # Update Hamming Distance metric
                         train_hamming_distance.update(y_pred, y)
                 # Compute mean train loss for the epoch
                 train_loss = running_train_loss / len(train_loader)
                 # Compute Hamming Distance for the epoch
```

```
epoch_hamming_distance = train_hamming_distance.compute()

# Print the train loss and Hamming Distance for the epoch
print(f'Epoch: {epoch + 1} / {epochs}')
print(f'Train Loss: {train_loss:.4f} | Train Hamming Distance: {epoch_hammi

# Reset metric states for the next epoch
train_hamming_distance.reset()
```

```
In [88]: # Set a manual seed for reproducibility across runs
         torch.manual seed(100)
         # Define hyperparameters: Learning rate and the number of epochs
         learning_rate = 1
         epochs = 20
         # Determine the computing device (GPU if available, otherwise CPU)
         device = torch.device('cuda:0' if torch.cuda.is_available() else 'cpu')
         print(f"Using device: {device}")
         # Student Task: Configure the optimizer for model training.
         # Here, we're using Stochastic Gradient Descent (SGD). Think through what parameter
         # Reminder: Utilize the learning rate defined above when setting up your optimizer.
         optimizer = torch.optim.SGD(model.parameters(), lr=learning_rate)
         # Transfer the model to the sel ected device (CPU or GPU)
         model.to(device)
         # Apply custom weight initialization function to the model layers
         # Note: Weight initialization can significantly affect training dynamics
         model.apply(init_weights)
         # Call the training function to start the training process
         # Note: All elements like epochs, loss function, learning rate, etc., are passed as
         train(epochs, loss function, learning rate, model, optimizer, train loader, device)
```

Using device: cpu

```
Epoch: 1 / 20
        Train Loss: 0.5126 | Train Hamming Distance: 0.3363
        Epoch: 2 / 20
        Train Loss: 0.4856 | Train Hamming Distance: 0.2877
        Epoch: 3 / 20
        Train Loss: 0.4825 | Train Hamming Distance: 0.2817
        Epoch: 4 / 20
        Train Loss: 0.4833 | Train Hamming Distance: 0.2833
        Epoch: 5 / 20
        Train Loss: 0.4866 | Train Hamming Distance: 0.2823
        Epoch: 6 / 20
        Train Loss: 0.4829 | Train Hamming Distance: 0.2867
        Epoch: 7 / 20
        Train Loss: 0.4856 | Train Hamming Distance: 0.2757
        Epoch: 8 / 20
        Train Loss: 0.4843 | Train Hamming Distance: 0.2790
        Epoch: 9 / 20
        Train Loss: 0.4858 | Train Hamming Distance: 0.2840
        Epoch: 10 / 20
        Train Loss: 0.4860 | Train Hamming Distance: 0.2787
        Epoch: 11 / 20
        Train Loss: 0.4846 | Train Hamming Distance: 0.2817
        Epoch: 12 / 20
        Train Loss: 0.4842 | Train Hamming Distance: 0.2773
        Epoch: 13 / 20
        Train Loss: 0.4845 | Train Hamming Distance: 0.2840
        Epoch: 14 / 20
        Train Loss: 0.4848 | Train Hamming Distance: 0.2800
        Epoch: 15 / 20
        Train Loss: 0.4833 | Train Hamming Distance: 0.2800
        Epoch: 16 / 20
        Train Loss: 0.4846 | Train Hamming Distance: 0.2840
        Epoch: 17 / 20
        Train Loss: 0.4847 | Train Hamming Distance: 0.2830
        Epoch: 18 / 20
        Train Loss: 0.4854 | Train Hamming Distance: 0.2800
        Epoch: 19 / 20
        Train Loss: 0.4828 | Train Hamming Distance: 0.2783
        Epoch: 20 / 20
        Train Loss: 0.4822 | Train Hamming Distance: 0.2747
In [89]: # Loop through the model's parameters to display them
         # This is helpful for debugging and understanding how well the model has learned
         for name, param in model.named_parameters():
             # 'name' will contain the name of the parameter (e.g., 'layer1.weight')
             # 'param.data' will contain the parameter values
             print(name, param.data)
        weight tensor([[ 0.9856, -0.1141, -0.2715, 0.0869, -0.9284],
                [-0.9591, 0.7973, 0.5119, 0.1237, -1.4677],
                [0.1281, 0.7948, -0.0565, -1.6264, 0.5559]])
        bias tensor([-0.2102, 0.4204, 0.0613])
```