

sensor_fusion_3_30

March 30, 2021

```
[1]: import math
import numpy as np
import pandas as pd
import matplotlib.pyplot as plt
```

```
TEST_NAME = "euler_angles_2"
```

```
dt = 1/960
```

```
GRAVITY = 9.80665
```

```
RAD_TO_DEG = 180 / math.pi
```

```
DEG_TO_RAD = math.pi / 180
```

```
[2]: # read test params from CSV
csvp = open(f"data/{TEST_NAME}.csvp")

# create params array
params = np.array([eval(line) for line in csvp])

print(params)
```

```
[ 1 3848  0 300  0  1  30 960  96 16 2000  92  92  63
 63  14  14  86  86  0  0  0  0  0  0  0  0  0
 0  0  0]
```

```
[3]: # read data from CSV
data = pd.read_csv(f"data/{TEST_NAME}.csv", names=["AccelX", "AccelY", "
→"AccelZ", "GyroX", "GyroY", "GyroZ", "MagX", "MagY", "MagZ"],
→index_col=False)

sample_rate = params[7]

# add time axis to data set
time = np.arange(0, len(data)/sample_rate, 1/sample_rate)
data.insert(0, "Time", time)

# sign data
data = data.applymap(lambda x: x-65535 if x > 32767 else x)
```

```

# apply accel sensitivity
acc_cols = ["AccelX", "AccelY", "AccelZ"]
acc_sens = params[9]
data[acc_cols] = data[acc_cols].applymap(lambda x: x * acc_sens * GRAVITY / 32768)

# apply gyro sensitivity
gyro_cols = ["GyroX", "GyroY", "GyroZ"]
gyro_sens = params[10]
data[gyro_cols] = data[gyro_cols].applymap(lambda x: x * gyro_sens / 32768)

# apply mag sensitivity
mag_cols = ["MagX", "MagY", "MagZ"]
mag_sens = 4800
data[mag_cols] = data[mag_cols].applymap(lambda x: x * mag_sens / 8192)

# FIXME copy for debugging, remove later
original_mag_data = data[mag_cols]

# calculate offsets for each sensor (first 0.5s of data)
acc_offsets = data[acc_cols].head(480).mean()
gyro_offsets = data[gyro_cols].head(480).mean()
mag_offsets = data[mag_cols].mean()

# min/max method
# mag_offsets = (data[mag_cols].max() + data[mag_cols].min()) / 2

# apply offsets to each sensor (remove sensor bias)
# TODO: hold off on accel until actual IMU calibration is implemented
for i, axis in enumerate(gyro_cols):
    data[axis] = data[axis].map(lambda x: x - gyro_offsets[i])

for i, axis in enumerate(mag_cols):
    data[axis] = data[axis].map(lambda x: x - mag_offsets[i])

# create new mag dataframe by removing all NaNs
mag_data = data[mag_cols + ["Time"]].dropna()

# for some reason, the first mag data point is always erroneous, so remove it
mag_data = mag_data.iloc[1:]

print(acc_offsets, gyro_offsets, mag_offsets)
print(data.head(20))

```

```

AccelX    0.549230
AccelY    0.070439
AccelZ   -9.974224

```

```
dtype: float64 GyroX    -1.048406
GyroY    -5.921555
GyroZ    18.028132
dtype: float64 MagX    -255.593234
MagY     83.042161
MagZ    -79.244474
```

```
dtype: float64
      Time    AccelX    AccelY    AccelZ    GyroX    GyroY    GyroZ \
0  0.000000  0.517148  0.272939 -10.893618 -1.454035  3.602219 -0.694148
1  0.001042  0.699107 -0.526724  -8.231265  0.193914 -1.524734 -15.952937
2  0.002083  0.708684  1.134852 -10.189722  1.536687 -8.971024  1.625188
3  0.003125 -0.043096 -0.229843 -11.329362 -3.529231 16.053391 -2.097956
4  0.004167  2.183512  0.354342 -10.821792  3.428777 -16.844559 -0.938288
5  0.005208 -0.172383  0.770933  -9.251195 -0.843684 -2.867508 -20.164363
6  0.006250 -0.560243  0.019154 -10.218453  1.841863  5.250168 -0.999324
7  0.007292  0.847547 -0.833182 -10.611102 -3.529231 -5.736160  4.310735
8  0.008333  1.383849  0.354342 -10.275914  0.315984 -9.703445 -13.511531
9  0.009375  1.058237 -0.450110  -9.988609 -3.773371  0.428391 -3.929011
10 0.010417  0.071826 -0.383072 -10.802638 -4.383723 -1.341629 11.451848
11 0.011458  1.465251 -1.599327  -9.682152 -2.308528 13.917160  2.113469
12 0.012500 -0.565032  0.062249 -10.836157 -3.468196 -3.050613 11.146673
13 0.013542  1.953669  0.981623  -9.830592  3.733953 -1.158524 -0.511042
14 0.014583  0.138864  0.751779  -9.543288 -0.111262 -13.304520  0.953801
15 0.015625 -0.598550 -0.469264  -9.835380  8.372625  9.217453 -1.121394
16 0.016667  0.090980  0.430956  -8.169016 -0.050227  8.729172 11.818059
17 0.017708 -0.383072  0.814029 -10.199299  5.015691 -12.633133 -14.854304
18 0.018750  0.679953 -0.114922  -9.514557  1.475652  9.705734 -24.741999
19 0.019792  1.398214  0.421379  -9.485827 -5.970637  3.052902  8.888372
```

```
      MagX    MagY    MagZ
0 -26.242704 11.879714 -33.841463
1      NaN      NaN      NaN
2      NaN      NaN      NaN
3      NaN      NaN      NaN
4      NaN      NaN      NaN
5      NaN      NaN      NaN
6      NaN      NaN      NaN
7      NaN      NaN      NaN
8      NaN      NaN      NaN
9      NaN      NaN      NaN
10 -19.797391  7.778151 -29.739901
11      NaN      NaN      NaN
12      NaN      NaN      NaN
13      NaN      NaN      NaN
14      NaN      NaN      NaN
15      NaN      NaN      NaN
16      NaN      NaN      NaN
17      NaN      NaN      NaN
```

18	NaN	NaN	NaN
19	NaN	NaN	NaN

```
[4]: def show_plot(title=""):
    plt.title(title)
    plt.grid(b=True, which='major', color='#666666', linestyle='-')
    plt.minorticks_on()
    plt.grid(b=True, which='minor', color='#999999', linestyle='-', alpha=0.2)
    plt.legend()
    plt.show()
```

```
[5]: # denoising accelerometer
import scipy.signal

# calculate fft for AccelX
fourierTransform = np.fft.fft(data["AccelX"])/len(data["AccelX"])

tpCount = len(data["AccelX"])
values = np.arange(tpCount)
timePeriod = tpCount/sample_rate
frequencies = values/timePeriod

plt.plot(frequencies, abs(fourierTransform), label="AccelX")

# display the plot
plt.xlim(959.9,960)
show_plot("Accelerometer FFT")

# normalized cutoff frequency = cutoff frequency / (2 * sample rate)
ORDER = 10
# 959.93838386
CUTOFF_FREQ = 100
NORM_CUTOFF_FREQ = CUTOFF_FREQ / (2 * 960)

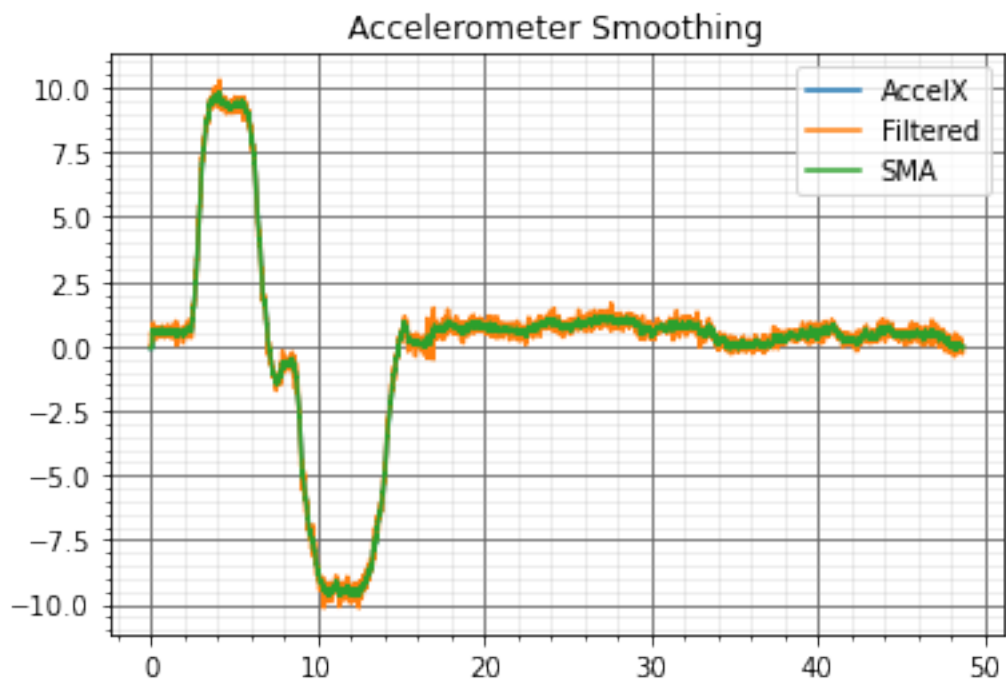
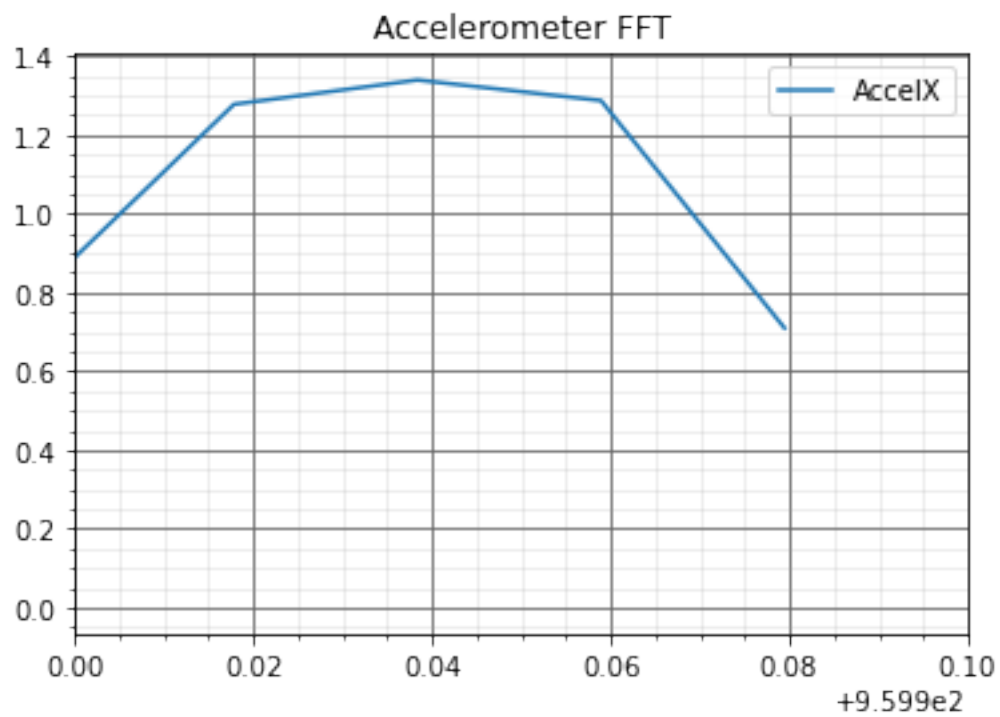
# Butterworth filter
num_coeffs, denom_coeffs = scipy.signal.butter(ORDER, NORM_CUTOFF_FREQ)
filtered_data = scipy.signal.lfilter(num_coeffs, denom_coeffs, data["AccelX"])

# simple moving average
rolling_data = data[acc_cols].rolling(window=100).mean().fillna(data[acc_cols].
    ↪iloc[49])

# apply simple moving average
data[acc_cols] = rolling_data

plt.plot(data["Time"], data["AccelX"], label="AccelX")
plt.plot(data["Time"], filtered_data, label="Filtered")
```

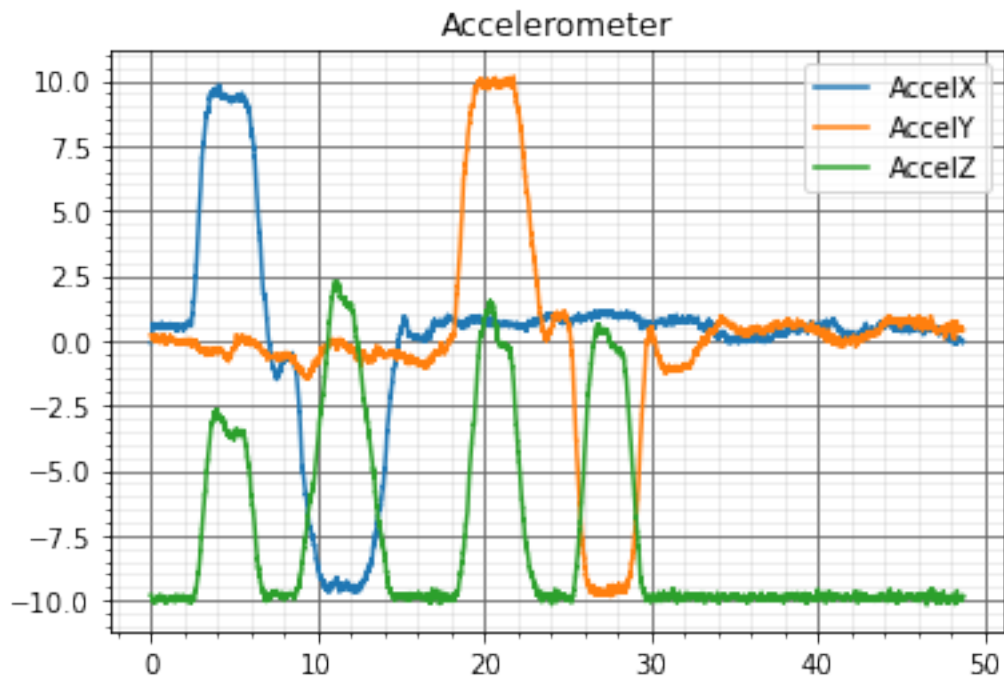
```
plt.plot(data["Time"], rolling_data["AccelX"], label="SMA")  
show_plot("Accelerometer Smoothing")
```

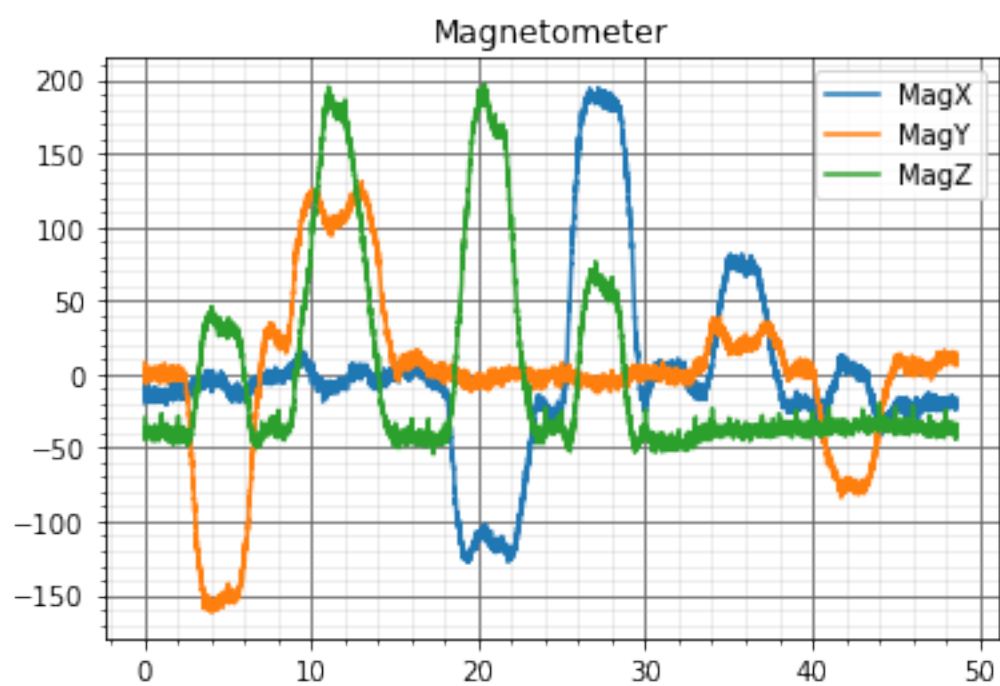
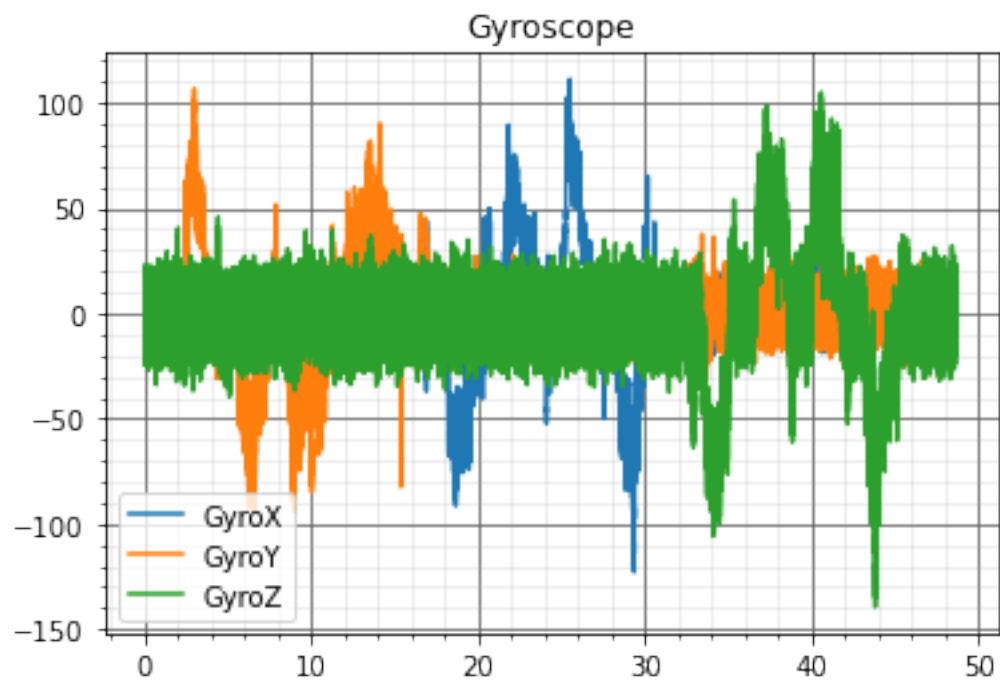


```
[6]: # plot acceleration
plt.plot(data["Time"], data["AccelX"], label="AccelX")
plt.plot(data["Time"], data["AccelY"], label="AccelY")
plt.plot(data["Time"], data["AccelZ"], label="AccelZ")
show_plot("Accelerometer")

# plot gyroscope
plt.plot(data["Time"], data["GyroX"], label="GyroX")
plt.plot(data["Time"], data["GyroY"], label="GyroY")
plt.plot(data["Time"], data["GyroZ"], label="GyroZ")
show_plot("Gyroscope")

# plot magnetometer
plt.plot(mag_data["Time"], mag_data["MagX"], label="MagX")
plt.plot(mag_data["Time"], mag_data["MagY"], label="MagY")
plt.plot(mag_data["Time"], mag_data["MagZ"], label="MagZ")
show_plot("Magnetometer")
```

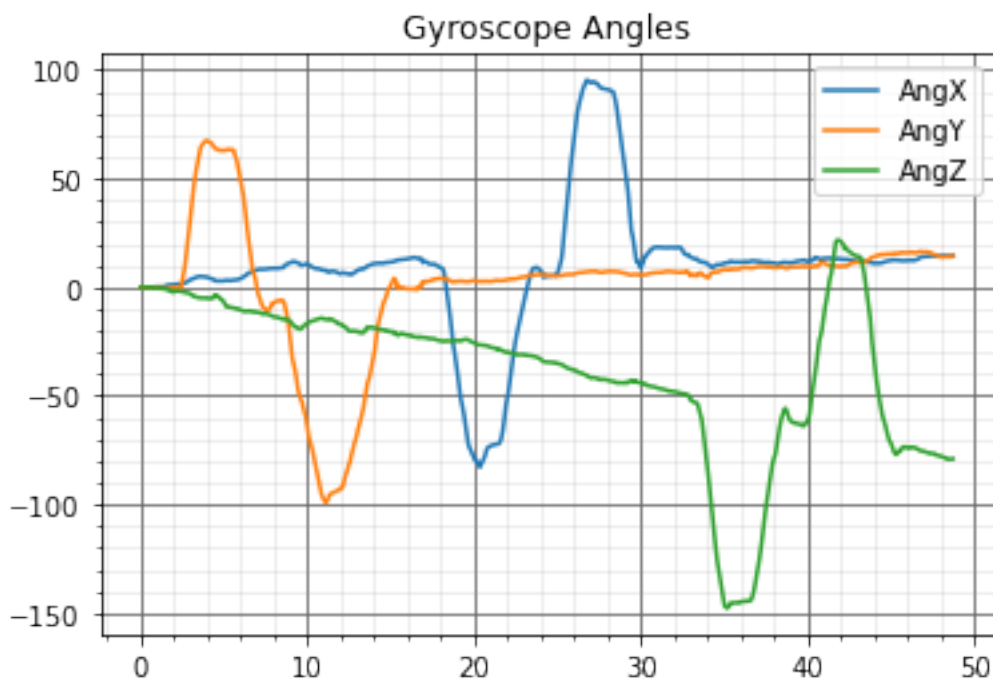




```
[7]: from scipy import integrate

# calculate angles from gyroscope
ang_x = integrate.cumtrapz(y=data["GyroX"], x=data["Time"], initial=0)
ang_y = integrate.cumtrapz(y=data["GyroY"], x=data["Time"], initial=0)
ang_z = integrate.cumtrapz(y=data["GyroZ"], x=data["Time"], initial=0)

# plot gyroscope angles
plt.plot(data["Time"], ang_x, label="AngX")
plt.plot(data["Time"], ang_y, label="AngY")
plt.plot(data["Time"], ang_z, label="AngZ")
show_plot("Gyroscope Angles")
```



```
[8]: # least squares ellipse fitting
# from https://www.hep.princeton.edu/~mumu/target/Yan/ellipse_fit.pdf
#
# (*) denotes tensor product,
# @ denotes matrix multiplication
def ellipse_fit(x_data, y_data):
    # create x and y vectors
    x = np.array(x_data)
    y = np.array(y_data)

    # X = [x (*) x, x (*) y, y (*) y, x, y]
```



```

# (transpose to account for x and y not being column vectors)
X = np.array([np.multiply(x, x), np.multiply(x, y), np.multiply(y, y), x,
→y])).T

# create n-dimensional column vector filled with 1s
ones = np.c_[[1] * len(x)]

# calculate coefficients [A,B,C,D,E] where:
#  $Ax^2 + Bxy + Cy^2 + Dx + Ey = 1$ 
beta = (np.linalg.inv(X.T @ X) @ X.T) @ ones
return beta

# fit data to 3D ellipsoid
# from: https://teslabs.com/articles/magnetometer-calibration/
def ellipsoid_fit(s):
    # D (samples)
    D = np.array([s[0]**2., s[1]**2., s[2]**2.,
                  2.*s[1]*s[2], 2.*s[0]*s[2], 2.*s[0]*s[1],
                  2.*s[0], 2.*s[1], 2.*s[2], np.ones_like(s[0])])

    # S, S_11, S_12, S_21, S_22 (eq. 11)
    S = np.dot(D, D.T)
    S_11 = S[:6,:6]
    S_12 = S[:6,6:]
    S_21 = S[6:,:6]
    S_22 = S[6:,6:]

    # C (Eq. 8, k=4)
    C = np.array([[-1, 1, 1, 0, 0, 0],
                  [1, -1, 1, 0, 0, 0],
                  [1, 1, -1, 0, 0, 0],
                  [0, 0, 0, -4, 0, 0],
                  [0, 0, 0, 0, -4, 0],
                  [0, 0, 0, 0, 0, -4]])

    # v_1 (eq. 15, solution)
    E = np.dot(np.linalg.inv(C),
                S_11 - np.dot(S_12, np.dot(np.linalg.inv(S_22), S_21)))

    E_w, E_v = np.linalg.eig(E)

    v_1 = E_v[:, np.argmax(E_w)]
    if v_1[0] < 0: v_1 = -v_1

    # v_2 (eq. 13, solution)
    v_2 = np.dot(np.dot(-np.linalg.inv(S_22), S_21), v_1)

```

```

# quadric-form parameters
M = np.array([[v_1[0], v_1[3], v_1[4]],
               [v_1[3], v_1[1], v_1[5]],
               [v_1[4], v_1[5], v_1[2]]])
n = np.array([v_2[0],
               v_2[1],
               v_2[2]])
d = v_2[3]

return M, n, d

```

```

[9]: # hard iron calibration
from scipy.linalg import sqrtm

# plot x-axis rotation (MagY, MagZ)
plt.scatter(data["MagY"], data["MagZ"], label="YZ (x-rotation)")

# plot y-axis rotation (MagX, MagZ)
plt.scatter(data["MagX"], data["MagZ"], label="XZ (y-rotation)")

# plot z-axis rotation (MagX, MagY)
plt.scatter(data["MagX"], data["MagY"], label="XY (z-rotation)")

# plot origin (0,0)
plt.scatter([0], [0], label="Origin")

# display the plot
plt.axis("square")
show_plot("Magnetometer Distribution")

def draw_mag_sphere(x_data, y_data, z_data):
    ax.scatter(x_data, y_data, z_data)
    limits = np.array([getattr(ax, f'get_{axis}lim')() for axis in 'xyz'])
    ax.set_box_aspect(np.ptp(limits, axis=1))
    ax.set_xlabel("Mag X")
    ax.set_ylabel("Mag Y")
    ax.set_zlabel("Mag Z")

def draw_unit_sphere(radius=1):
    u = np.linspace(0, np.pi, 30)
    v = np.linspace(0, 2 * np.pi, 30)
    x = np.outer(np.sin(u), np.sin(v))
    y = np.outer(np.sin(u), np.cos(v))
    z = np.outer(np.cos(u), np.ones_like(v))
    ax.plot_wireframe(x, y, z, color="r", alpha=0.25)

# calculate ellipsoid for data

```

```

s = np.array(mag_data[mag_cols]).T
M, n, d = ellipsoid_fit(s)

# calculate calibration parameters for:
#  $h_m = A @ h + b$  where  $h = A^{-1} @ (h_m - b)$ 
M_1 = np.linalg.inv(M)
b = -np.dot(M_1, n)
A_1 = np.real(1 / np.sqrt(np.dot(n.T, np.dot(M_1, n)) - d) * sqrtm(M))

# calculate  $h = A^{-1} @ (h_m - b)$ 
def calibrate_mag(row):
    res = A_1 @ np.c_[row] - b
    return res.flatten().tolist()

# calibrate magnetometer
mag_data[mag_cols] = mag_data[mag_cols].apply(calibrate_mag, axis=1,
→result_type='expand')

fig = plt.figure()
ax = fig.add_subplot(projection="3d")

# 3D plot of original mag data
draw_mag_sphere(original_mag_data["MagX"], original_mag_data["MagY"],
→original_mag_data["MagZ"])
draw_unit_sphere()
plt.show()

fig = plt.figure()
ax = fig.add_subplot(projection="3d")

# 3D plot of mag data
draw_mag_sphere(mag_data["MagX"], mag_data["MagY"], mag_data["MagZ"])
draw_unit_sphere()
plt.show()

# plot x-axis rotation (MagY, MagZ)
plt.scatter(mag_data["MagY"], mag_data["MagZ"], label="YZ (x-rotation)")

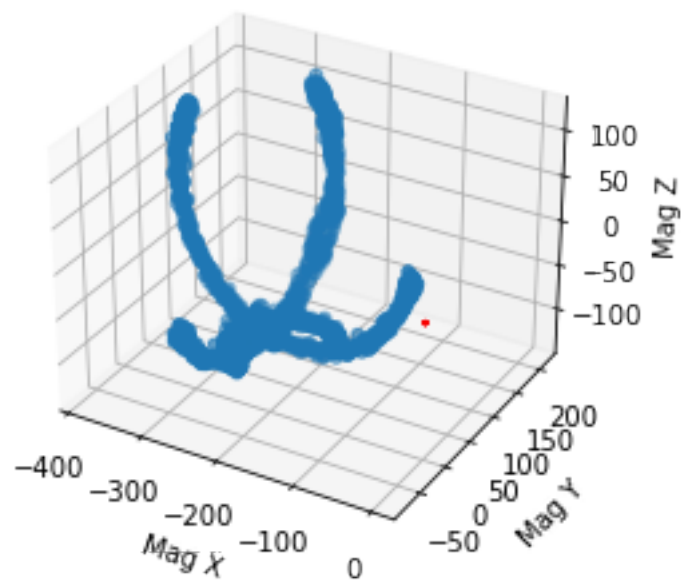
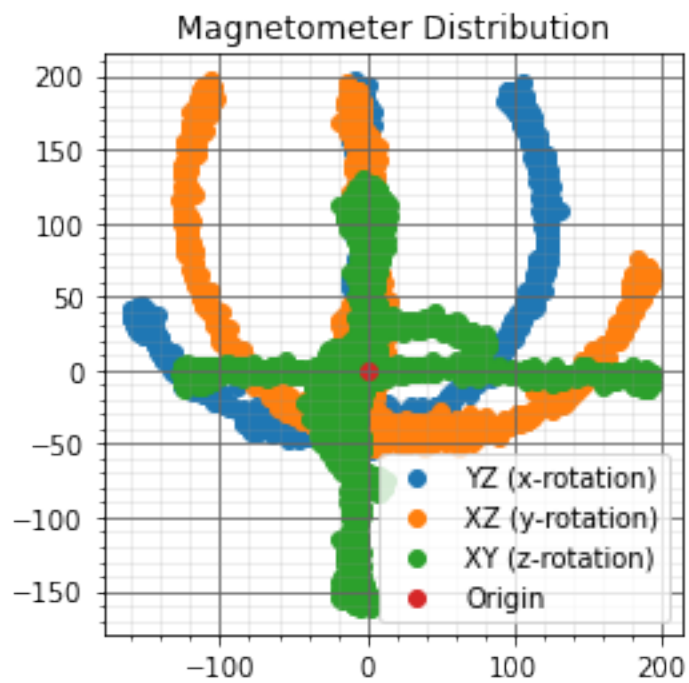
# plot y-axis rotation (MagX, MagZ)
plt.scatter(mag_data["MagX"], mag_data["MagZ"], label="XZ (y-rotation)")

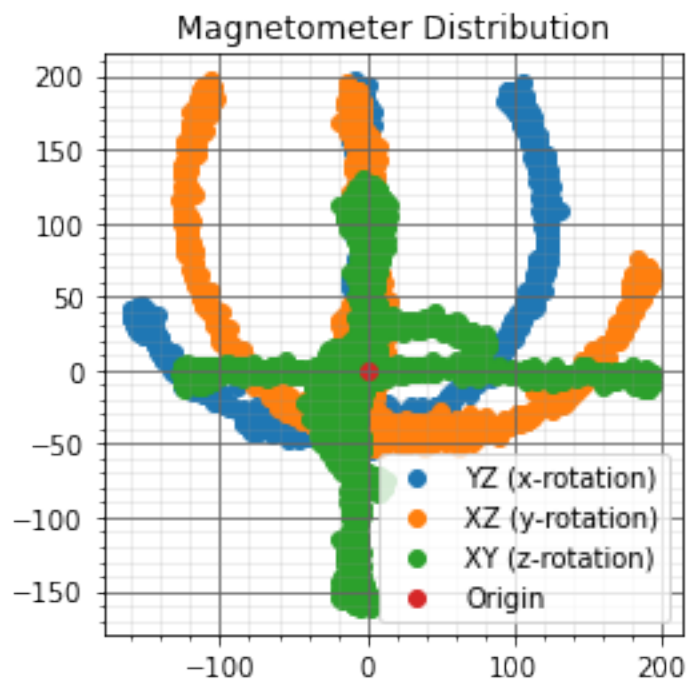
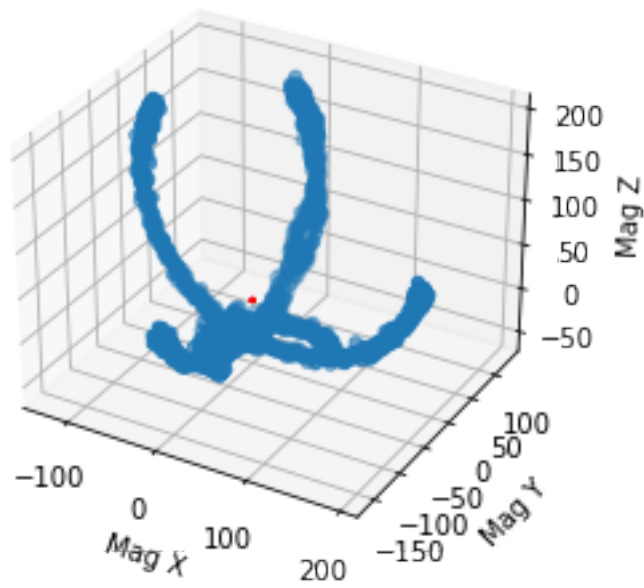
# plot z-axis rotation (MagX, MagY)
plt.scatter(mag_data["MagX"], mag_data["MagY"], label="XY (z-rotation)")

# plot origin (0,0)
plt.scatter([0], [0], label="Origin")

```

```
# display the plot
plt.axis("square")
show_plot("Magnetometer Distribution")
```





```
[10]: # plot x-axis rotation (MagY, MagZ)
plt.scatter(mag_data["MagY"], mag_data["MagZ"], label="YZ (x-rotation)")
```

```

# plot y-axis rotation (MagX, MagZ)
plt.scatter(mag_data["MagX"], mag_data["MagZ"], label="XZ (y-rotation)")

# plot z-axis rotation (MagX, MagY)
plt.scatter(mag_data["MagX"], mag_data["MagY"], label="XY (z-rotation)")
plt.plot()

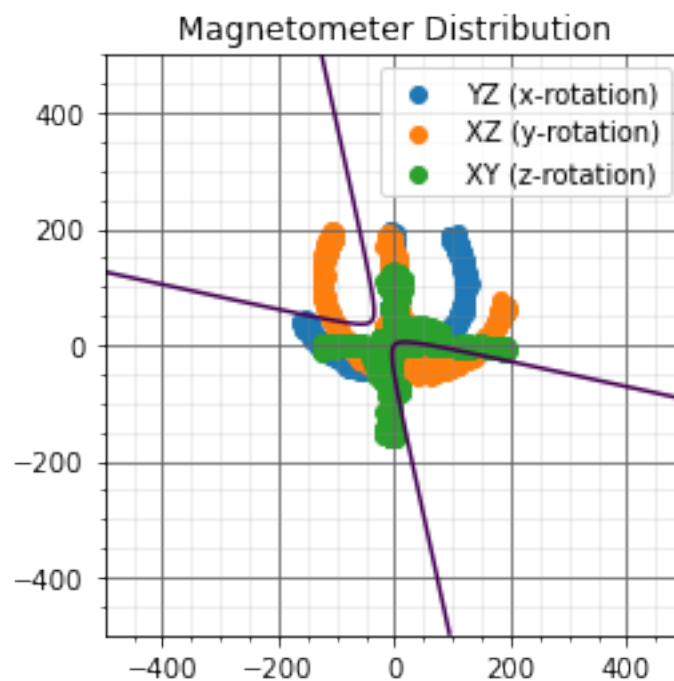
# calculate coefficients for ellipse fitting
A,B,C,D,E = ellipse_fit(mag_data["MagX"], mag_data["MagY"])

x = np.linspace(-500, 500, 1000)
y = np.linspace(-500, 500, 1000)
x, y = np.meshgrid(x, y)

plt.contour(x, y, A*x**2 + B*x*y + C*y**2 + D*x + E*y, [0])

# display the plot
plt.axis("square")
show_plot("Magnetometer Distribution")

```



```

[11]: # OLD: calculate angles from accelerometer
# acc_ang_x = np.arctan2(-data["AccelY"], -data["AccelZ"]) * RAD_TO_DEG
# acc_ang_y = np.arctan2(-data["AccelX"], np.sqrt(data["AccelY"]**2 +
↳ data["AccelZ"]**2)) * RAD_TO_DEG

```

```

MU = 0.01

# EXPERIMENTAL ANGLE CALCULATIONS
# TODO: added 2 negatives to acc_ang_x, doesn't work without it: why?
acc_ang_x = np.arctan2(-data["AccelY"], -np.sign(data["AccelZ"]) * np.
    ↳sqrt(data["AccelZ"]**2 + MU * data["AccelX"]**2))
acc_ang_y = np.arctan2(-data["AccelX"], np.sqrt(data["AccelY"]**2 +
    ↳data["AccelZ"]**2))

# calculate z-angle (yaw) from accelerometer & magnetometer
M_x = mag_data["MagX"] * np.cos(acc_ang_y) + mag_data["MagZ"] * np.
    ↳sin(acc_ang_y)
M_y = mag_data["MagX"] * np.sin(acc_ang_x) * np.sin(acc_ang_y) +
    ↳mag_data["MagY"] * np.cos(acc_ang_x) - mag_data["MagZ"] * np.sin(acc_ang_x)
    ↳* np.cos(acc_ang_y)

# remove NaNs from mag calculations
M_x = M_x[~np.isnan(M_x)]
M_y = M_y[~np.isnan(M_y)]

mag_ang_z = np.arctan2(M_y, -M_x)

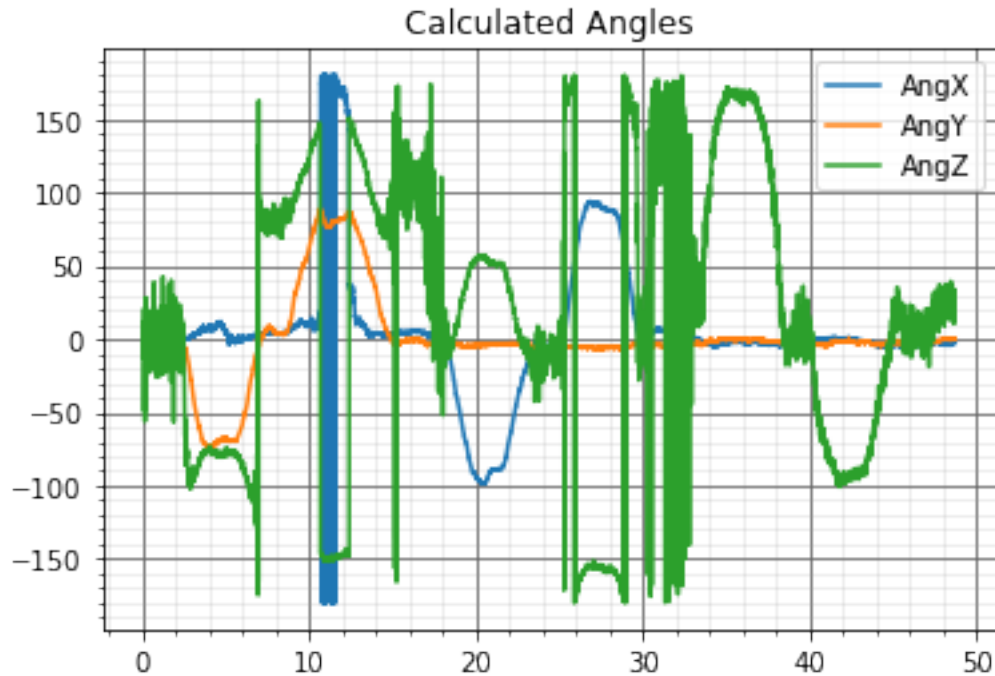
# convert all angles to degrees
acc_ang_x *= RAD_TO_DEG;
acc_ang_y *= RAD_TO_DEG;
mag_ang_z *= RAD_TO_DEG;

# plot accelerometer angles
plt.plot(data["Time"], acc_ang_x, label="AngX")
plt.plot(data["Time"], acc_ang_y, label="AngY")

# plot mag+accel z-axis angle
plt.plot(mag_data["Time"], mag_ang_z, label="AngZ")

# display the plot
show_plot("Calculated Angles")

```



```
[12]: # complementary filter
HP_weight = 0.98
LP_weight = 0.02

# create empty array w/ 3 axes
# set first elements to 0 (will be removed)
cf_ang = [[0],[0],[0]]

# group all axes of calculated angles together
gyro_ang = np.array([data["GyroX"].to_numpy(), data["GyroY"].to_numpy(),
    ↳data["GyroZ"].to_numpy()])
calc_ang = np.array([acc_ang_x, acc_ang_y, mag_ang_z], dtype=object)

# pair the calculated arrays for each axis together and loop
for i, (gyro_arr, calc_arr) in enumerate(zip(gyro_ang, calc_ang)):

    # pair the gyro & calc samples together and loop
    for j, (gyro, calc) in enumerate(zip(gyro_arr, calc_arr)):

        cf_ang_prev = cf_ang[i][-1]
        cf_ang_samp = HP_weight * (cf_ang_prev + gyro * dt) + LP_weight * calc
        cf_ang[i].append(cf_ang_samp)

    # if this is the magnetometer axis,
```



```

    # repeat sample 9x to ensure it lines up with accel/gyro
    if i == 2:
        for _ in range(9):
            cf_ang[i].append(cf_ang_samp)

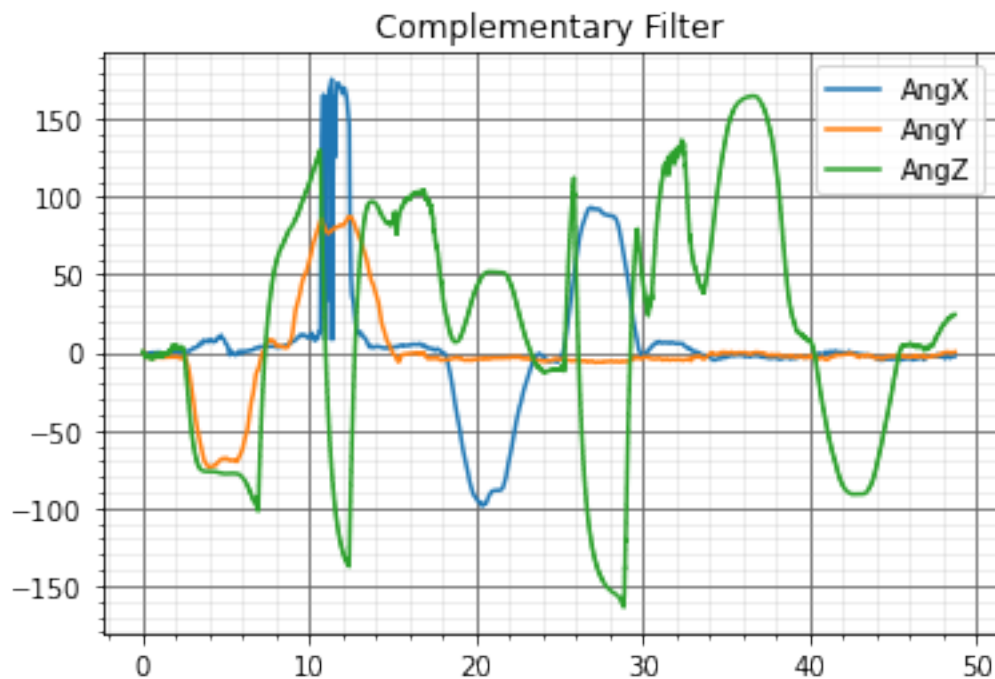
# since accel/gyro can have additional samples past 10 x mag,
# repeat the last sample to line up mag axis w/ accel/gyro
num_extra = len(cf_ang[0]) - len(cf_ang[2])
for _ in range(num_extra):
    cf_ang[2].append(cf_ang[2][-1])

# remove initial 0 values
for axis in cf_ang: del axis[0]

plt.plot(data["Time"], cf_ang[0], label="AngX")
plt.plot(data["Time"], cf_ang[1], label="AngY")
plt.plot(data["Time"], cf_ang[2], label="AngZ")

# display the plot
show_plot("Complementary Filter")

```



```

[13]: import csv

# save angle data as CSV

```

```
with open("out.csv", "w", newline="") as csvfile:

    # define CSV writer
    writer = csv.writer(csvfile, delimiter=",", quotechar='"', quoting=csv.
→QUOTE_MINIMAL)

    # loop over each row of (x,y,z),
    # and write each line to CSV
    for row in zip(*cf_ang):
        writer.writerow(row)
```

[]: