Iris Dataset

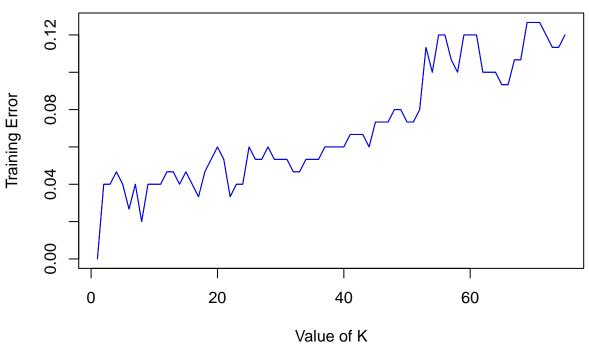
Shreya Kaul

```
# Load standard libraries
library(tidyverse)
library(datasets)
library(ggplot2)
library(MASS)
library(klaR)
library(stringr)
library(ISLR)
library(caret)
library(dummies)
library(class)
library(scales)
library(boot)
library(glmnet)
library(rpart)
library(rpart.plot)
#Dataset -Iris
data(iris)
my_x1 <- iris$Sepal.Length
my_x2 <- iris$Petal.Length</pre>
my_y <- as.factor(iris$Species)</pre>
#Classification Tress
tree_sample <- sample(1:110, replace=FALSE)</pre>
train_data <- iris[tree_sample,c('Species','Sepal.Length','Petal.Length')]</pre>
test_data <- iris[-tree_sample,c('Species','Sepal.Length','Petal.Length')]</pre>
train_tree <- rpart(train_data$Species~.,data = train_data, method = 'class')</pre>
rpart.plot(train_tree)
```

```
setosa
                             setosa
                                                                       versicolor
                           .45 .45 .09
                                                                       virginica
                              100%
                 versicolor
                                                    .00 .83 .17
                                                        55%
                                                Petal.Length < 5.1
    setosa
                                    versicolor
                                                                       virginica
                                    .00 .98 .02
 1.00 .00 .00
                                                                     .00 .10 .90
     45%
                                       45%
                                                                          9%
fit <- predict(train_tree, test_data, type='class')</pre>
table_mat <- table(test_data$Species , fit)</pre>
print(table_mat)
##
##
                setosa versicolor virginica
##
     setosa
                                 0
##
     versicolor
                     0
                                 0
                                           0
##
     virginica
                                          32
accu <- sum(diag(table_mat)) / sum(table_mat) * 100</pre>
print(paste0("Accuracy of the model: ", accu," %"))
## [1] "Accuracy of the model: 80 %"
set.seed(123)
k_seq <- seq(1:((nrow(iris)/2)))</pre>
train_error_seq <- vector('list', length = length(k_seq))</pre>
for (i in k_seq)
k \leftarrow k_seq[i]
training_prediction <- knn(train=data.frame(my_x1,my_x2),test=data.frame(my_x1,my_x2),cl=my_y,k=k)
training_error <- mean(training_prediction!=my_y)</pre>
train_error_seq[i] <- training_error</pre>
```

```
#Plotting of KNN Training Error for different values of K
plot(x = k_seq, y=unlist(train_error_seq), type='l', xlab='Value of K', ylab='Training Error', main='KN
lines(x = k_seq, y=unlist(train_error_seq), col = "blue")
```

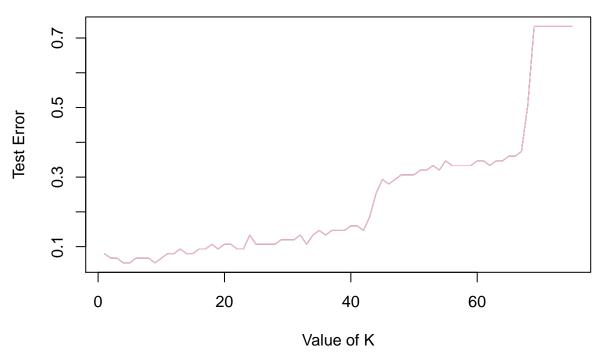
KNN Training Error



```
#Validation set approach
#Randomizing data and Splitting into test and train data
set.seed(123)
iris_random <- sample(1:nrow(iris), replace = FALSE)</pre>
iris_random_sample <- iris[iris_random,]</pre>
iris_random_train_class <- rbind(iris_random_sample[1:75,c('Species')])</pre>
iris_random_test_class <- rbind(iris_random_sample[76:150,c('Species')])</pre>
iris_random_train <- rbind(iris_random_sample[1:75,c('Sepal.Length','Petal.Length')])</pre>
iris_random_test <- rbind(iris_random_sample[76:150,c('Sepal.Length','Petal.Length')])</pre>
#Test error using Validation Set Approach
train_error_val <- vector()</pre>
k_seq <- seq(1:((nrow(iris)/2)))</pre>
for (i in k_seq)
{
k \leftarrow k_{seq[i]}
training_prediction_val <- knn(train=iris_random_train,test=iris_random_test,cl=iris_random_train_class
training_error_val <- mean(training_prediction_val!=iris_random_test_class)</pre>
train_error_val[i] <- training_error_val</pre>
```

```
#Plotting of test error using validation set approach
plot(x = k_seq, y=unlist(train_error_val), type='l', xlab='Value of K', ylab='Test Error', main='Test ellines(x = k_seq, y=unlist(train_error_val), col="pink")
```

Test error using Validation Set Approach



```
#Leave one out CV

train_error_loocv <- vector()
k_seq <- seq(1:((nrow(iris)/2)))
train_error <- vector()

#Loop for K-values
for (j in k_seq)
{
    #Train and test dataset
    for (i in 1:nrow(iris))
{
        iris_loocv_train_class <- rbind(iris[-i,c('Species')])
        iris_loocv_test_class <- rbind(iris[i,c('Species')])
        iris_loocv_train <- rbind(iris[i,c('Sepal.Length','Petal.Length')])
        iris_loocv_test <- rbind(iris[i,c('Sepal.Length','Petal.Length')])

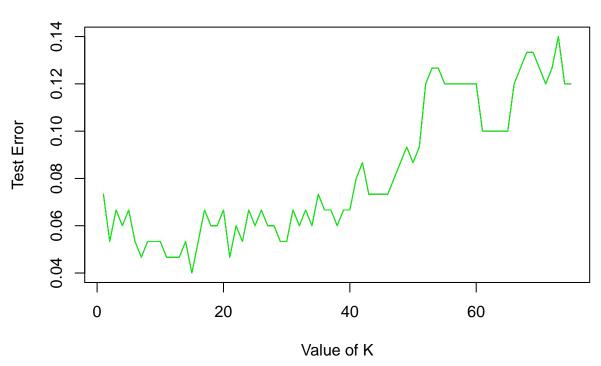
training_prediction_loocv <- knn(train=iris_loocv_train,test=iris_loocv_test,cl=iris_loocv_train_class,itraining_error_loocv <- mean(training_prediction_loocv!=iris_loocv_test_class)

train_error_loocv[i] <- training_error_loocv</pre>
```

```
train_error[j] <- mean(train_error_loocv)

#Plotting of test error using Leave one out approach
plot(x = k_seq, y=unlist(train_error), type='l', xlab='Value of K', ylab='Test Error', main='Test error
lines(x = k_seq, y=unlist(train_error), col="green")
</pre>
```

Test error using Leave-One-Out Approach



```
#5-Fold CV
training_error_kfold <- vector()
train_error_kfold <- vector()
kfold_error <- vector()
k_seq <- seq(1:((nrow(iris)/2)))

#Shuffling data randomly
set.seed(123)
iris_random_kfold <- sample(1:nrow(iris), replace = FALSE)
iris_sample_kfold <- iris[iris_random_kfold,]

#Creating 5 folds
folds <- cut(seq(1,nrow(iris_sample_kfold)),breaks=5,labels=FALSE)

for (j in k_seq) {

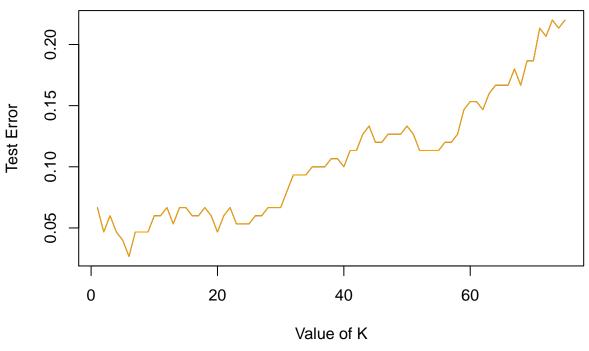
#Perform CV
for (i in 1:5) {
   test_index <- which(folds==i,arr.ind = TRUE)</pre>
```

```
kfold_test_data <- iris_sample_kfold[test_index,c('Sepal.Length','Petal.Length')]
kfold_train_data <- iris_sample_kfold[-test_index,c('Sepal.Length','Petal.Length')]
kfold_test_class <- iris_sample_kfold[test_index,c('Species')]
kfold_train_class <- iris_sample_kfold[-test_index,c('Species')]

training_prediction_kfold <- knn(train=kfold_train_data,test=kfold_test_data,cl=kfold_train_class,k=j
training_error_kfold <- mean(training_prediction_kfold!=kfold_test_class)

train_error_kfold[i] <- training_error_kfold
}
kfold_error[j] <- mean(train_error_kfold)
}
#Plotting of test error using 5-fold cross validation for different values of K
plot(x = k_seq, y=unlist(kfold_error), type='l', xlab='Value of K', ylab='Test_Error', main='Test_error_lines(x = k_seq, y=unlist(kfold_error), col="orange")</pre>
```

Test error using 5-Fold Cross validation



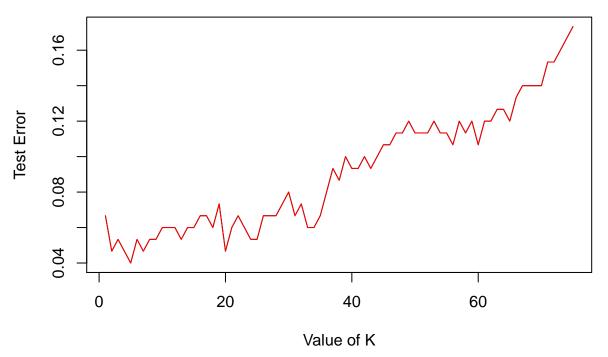
```
#10-Fold CV
training_error_kfold <- vector()
train_error_kfold <- vector()
kfold_error2 <- vector()
k_seq <- seq(1:((nrow(iris)/2)))

#Shuffling data randomly
set.seed(123)
iris_random_kfold <- sample(1:nrow(iris), replace = FALSE)
iris_sample_kfold <- iris[iris_random_kfold,]

#Creating folds</pre>
```

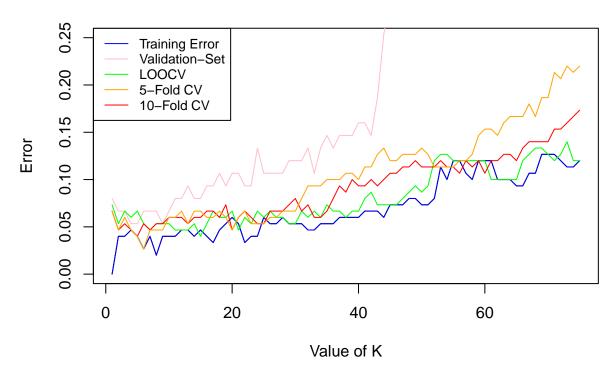
```
folds <- cut(seq(1,nrow(iris_sample_kfold)),breaks=10,labels=FALSE)</pre>
for (j in seq_along(k_seq)) {
#Perform CV
for (i in 1:10) {
  test_index <- which(folds==i,arr.ind = TRUE)</pre>
  kfold_test_data <- iris_sample_kfold[test_index,c('Sepal.Length','Petal.Length')]</pre>
  kfold_train_data <- iris_sample_kfold[-test_index,c('Sepal.Length','Petal.Length')]</pre>
  kfold_test_class <- iris_sample_kfold[test_index,c('Species')]</pre>
  kfold_train_class <- iris_sample_kfold[-test_index,c('Species')]</pre>
  training_prediction_kfold <- knn(train=kfold_train_data,test=kfold_test_data,cl=kfold_train_class,k=j
  training_error_kfold <- mean(training_prediction_kfold!=kfold_test_class)</pre>
train_error_kfold[i] <- training_error_kfold</pre>
}
  kfold_error2[j] <- mean(train_error_kfold)</pre>
#Plotting of test error using 10-fold cross validation for different values of K
plot(x = k_seq, y=unlist(kfold_error2), type='l', xlab='Value of K', ylab='Test Error', main='Test error
lines(x = k_seq, y=unlist(kfold_error2), col="red")
```

Test error using 10-Fold Cross validation



```
#Combining all the plots together
plot(x = k_seq, y=unlist(train_error_seq), type='l', xlab='Value of K', ylab='Error', main='K-Value vs lines(x = k_seq, y=unlist(train_error_seq), col = "blue")
lines(x = k_seq, y=unlist(train_error_val), col="pink")
```

K-Value vs Error

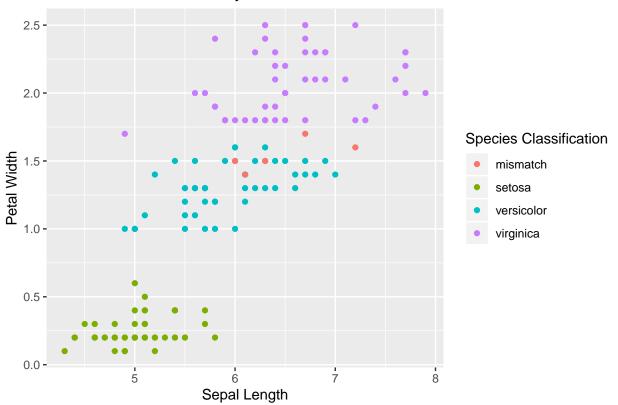


From the above plots, it can be seen that lowest test error will be for the values of K between 0-20.

```
#LDA
iris_df <- rbind(iris[,c('Sepal.Length', 'Petal.Width','Species')])</pre>
lda_iris <- lda(iris_df$Species~., iris_df)</pre>
lda_iris
## lda(iris_df$Species ~ ., data = iris_df)
##
## Prior probabilities of groups:
##
       setosa versicolor virginica
    0.3333333 0.3333333 0.3333333
##
##
## Group means:
##
              Sepal.Length Petal.Width
## setosa
                      5.006
                                  0.246
                      5.936
                                  1.326
## versicolor
## virginica
                      6.588
                                  2.026
##
## Coefficients of linear discriminants:
##
                                   LD2
                         LD1
## Sepal.Length -0.02715312 2.085884
```

```
## Petal.Width
                 4.91087360 -1.848948
##
## Proportion of trace:
##
      LD1
             LD2
## 0.9999 0.0001
iris_lda_value <- predict(lda_iris)</pre>
iris_df_plot_lda <- iris_df</pre>
for (i in 1:150) {
    iris_df_plot_lda$classification <- ifelse(iris_df$Species != iris_lda_value$class,"mismatch",
                                ifelse
                                (iris_df$Species == "setosa", "setosa",
                                   ifelse
                                   (iris_df$Species == "versicolor", "versicolor",
                                    ifelse
                                     (iris_df$Species == "virginica", "virginica", NA))))
}
gg <- ggplot(iris_df_plot_lda, aes(iris_df_plot_lda$Sepal.Length, iris_df_plot_lda$Petal.Width, col=iri
print(gg)
```

Linear Discriminant Analysis



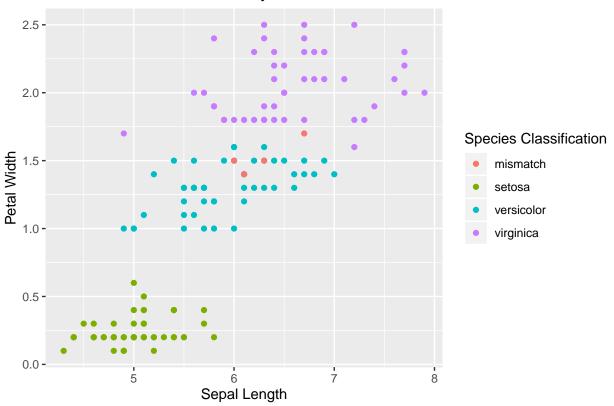
```
confusionMatrix(iris_lda_value$class, iris_df$Species)
```

```
## Confusion Matrix and Statistics
##
## Reference
## Prediction setosa versicolor virginica
```

```
50
##
     setosa
                                 0
                                           0
##
                     0
                                48
                                           4
     versicolor
##
     virginica
                     0
                                2
                                          46
##
## Overall Statistics
##
##
                  Accuracy: 0.96
                    95% CI : (0.915, 0.9852)
##
##
       No Information Rate: 0.3333
##
       P-Value [Acc > NIR] : < 2.2e-16
##
##
                     Kappa: 0.94
##
   Mcnemar's Test P-Value : NA
##
##
## Statistics by Class:
##
##
                         Class: setosa Class: versicolor Class: virginica
                                1.0000
                                                   0.9600
                                                                     0.9200
## Sensitivity
                                1.0000
## Specificity
                                                   0.9600
                                                                     0.9800
## Pos Pred Value
                                1.0000
                                                   0.9231
                                                                     0.9583
## Neg Pred Value
                                1.0000
                                                   0.9796
                                                                     0.9608
## Prevalence
                                0.3333
                                                   0.3333
                                                                     0.3333
## Detection Rate
                                0.3333
                                                   0.3200
                                                                     0.3067
## Detection Prevalence
                                0.3333
                                                   0.3467
                                                                    0.3200
## Balanced Accuracy
                                1.0000
                                                   0.9600
                                                                     0.9500
iris_df <- rbind(iris[,c('Sepal.Length', 'Petal.Width','Species')])</pre>
qda_iris <- qda(iris_df$Species~., iris_df)</pre>
qda_iris
## Call:
## qda(iris_df$Species ~ ., data = iris_df)
## Prior probabilities of groups:
       setosa versicolor virginica
  0.3333333 0.3333333 0.3333333
##
##
## Group means:
              Sepal.Length Petal.Width
## setosa
                     5.006
                                  0.246
                     5.936
                                  1.326
## versicolor
## virginica
                     6.588
                                  2.026
iris_qda_value <- predict(qda_iris)</pre>
for (i in 1:150) {
    iris_qda_value$classification <- ifelse(iris_df$Species != iris_qda_value$class,"mismatch",
                                ifelse
                                (iris_df$Species == "setosa", "setosa",
                                  ifelse
                                  (iris_df$Species == "versicolor", "versicolor",
                                    ifelse
                                    (iris_df$Species == "virginica","virginica",NA))))
```

```
iris_df_plot_qda <- iris_df
iris_df_plot_qda$classification <- iris_qda_value$classification
gg <- ggplot(iris_df, aes(iris_df_plot_qda$Sepal.Length, iris_df_plot_qda$Petal.Width, col=iris_df_plot
print(gg)</pre>
```

Quadratic Discriminant Analysis



confusionMatrix(iris_df\$Species, iris_qda_value\$class)

```
## Confusion Matrix and Statistics
##
               Reference
##
                setosa versicolor virginica
## Prediction
##
     setosa
                     50
                                 0
##
     versicolor
                      0
                                48
                                            2
     virginica
                      0
                                 3
                                           47
##
##
## Overall Statistics
##
##
                  Accuracy: 0.9667
##
                     95% CI: (0.9239, 0.9891)
       No Information Rate: 0.34
##
##
       P-Value [Acc > NIR] : < 2.2e-16
##
##
                      Kappa : 0.95
##
    Mcnemar's Test P-Value : NA
##
##
## Statistics by Class:
```

##							
##		Class:	setosa	Class:	versicolor	Class:	virginica
##	Sensitivity		1.0000		0.9412		0.9592
##	Specificity		1.0000		0.9798		0.9703
##	Pos Pred Value		1.0000		0.9600		0.9400
##	Neg Pred Value		1.0000		0.9700		0.9800
##	Prevalence		0.3333		0.3400		0.3267
##	Detection Rate		0.3333		0.3200		0.3133
##	Detection Prevalence		0.3333		0.3333		0.3333
##	Balanced Accuracy		1.0000		0.9605		0.9647

Out of the LDA and QDA models, QDA gave the smaller training error. QDA has more variance and therefore is more flexible. So, it fits better on the training data. If we consider bias-variance trade-off, then as the variance increases the training error decreases.

LDA is less flexible than QDA as in LDA the number of parameters are less. Due to more parameters, QDA has high variance. If the number of observations in training data are more then LDA will give a smaller test error as QDA will have higher variance and may result in overfitting of model. But if the classes have a different covariance matrix, then LDA will face high bias on the dataset and QDA will have lower test error.