

# Network Intrusion Detection in an Adversarial Setting

*Report submitted in fulfillment of the requirements  
for the B.Tech Project of*

**Third Year B.Tech.**

*by*

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*Under the guidance of*  
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May 2019

Dedicated to  
*My parents, teachers*

# Declaration

We certify that

1. The work contained in this report is original and has been done by our team and the general supervision of my supervisor.
2. The work has not been submitted for any project.
3. Whenever we have used materials (data, theoretical analysis, results) from other sources, we have given due credit to them by citing them in the text of the thesis and giving their details in the references.
4. Whenever we have quoted written materials from other sources, we have put them under quotation marks and given due credit to the sources by citing them and giving required details in the references.

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# Certificate

*This is to certify that the work contained in this report entitled “**Network Intrusion Detection in an Adversarial Setting**” being submitted by **Shreyansh Singh** (Roll No. 16075052) and carried out in the Department of Computer Science and Engineering, Indian Institute of Technology (BHU) Varanasi, is a bona fide work of my supervision.*

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# Abstract

The origin of network-intrusion detection research was using signature-based detection approaches. But since the gain in the popularity of machine learning and anomaly detection techniques based on it, the domain of intrusion detection has also seen such techniques being used. The volume of attacks has been increasing everyday and the techniques adversaries are using for crafting the attacks is also evolving at a very fast pace. Hence with the improvements in big data analytics area, makes machine learning the go-to technique to solve the issue. The aim of this research is to show that although machine learning can prove to be a great tool for network intrusion detection, but the robustness of the classifiers should be evaluated before using such models in production.

The domain of Image classification has seen several adversarial techniques emerge from deep learning research. The main idea in such techniques is to make minor changes in the original input data that is not recognizable by humans but are enough to make a machine learning tool misclassify it. This research explores adversarial machine learning techniques that have emerged from the deep learning domain, against machine learning classifiers used for network intrusion detection.

In this study, we look at the well known and commonly used classifiers and study their performance under attack. The metrics we used are accuracy, F1-score and receiver operating characteristic (ROC). The approach used assumes no knowledge of the original classifier and examines targeted misclassification. Even using very simple methods for generating adversarial examples, we show that it is possible to lower the accuracy of intrusion detection classifiers from 2.5% to 32%. This is achieved by introducing a very small change (9.49% on average) in the original sample to create the adversarial sample, which makes it a candidate for practical adversarial attacks.

# Introduction

Although enterprise networks aim to deploy the best security measures, security breaches still remain a source of major concern. Malicious activities within a network can be categorized based on the origin of the attacker as:

- *External users*: These include the activities that are performed by external users and have the intention to get access to the internal network. Such activities could be successfully performed via a breach in the network perimeter using malware, social engineering, phishing attacks and so on. Getting inside the internal network is very dangerous as now it is difficult to distinguish the attacker from normal users since most often they use normal user or administrator credentials. The attackers can use such kind of access to install and run malicious software autonomously like bots, or install backdoors or rootkits on the system of the employees.
- *Internal users*: This is also known as “insider threat”. These include the activities that are performed by internal users and have the motive to misuse, attack or steal information.

## Intrusion Detection

Intrusion detection is dealing with unwanted access to systems and information by any type of user or software. An intrusion detection system (IDS) is a device or software application that monitors a network or systems for malicious activity or policy violations. An Intrusion Prevention System (IPS) is an IDS which also has the ability to stop attacks. There are two major categories of IDS:

- **Network IDS**, which monitors network segments and analyzes network traffic at different layers in order to detect intruders.
- **Host based IDS**, which are installed in host machines and analyze different indicators such as processes, log files, unexpected changes in the host to determine the presence of malicious activities.

Handling (gathering, storing and processing) the amount of network traffic that is generated on a daily basis by large enterprise networks, is a difficult task. One way to deal with this is to discard parts of the data or log less information, however the emergence of Big Data Analytics

(BDA) as well as the improvement in memory, computing power and the decrease in storage costs, transforms the situation into a big data problem.

Regardless of the specific data set used for Intrusion detection analysis, the nature of the data associated with this class of problems exhibits certain general characteristics:

- Data is generated constantly and there is a time series nature (continuous or discrete) based on the data set and the processing approach.
- *Class imbalance*, i.e. Very few positive labels or lack of labels
- Attack types change a lot over time, with attackers developing novel methods all the time.
- Variety in the type of data: packets, flows, numerical, unstructured text (URLs) and so on.

Traditional approaches in the area of intrusion detection mainly revolve around signature and rule based approaches. The limitations to those is that they work only with known attack patterns and that they require extensive domain knowledge [Chuvakin 2012]. Anomaly detection techniques based on statistical or machine learning approaches promise more flexibility and less dependency in domain knowledge and are more scalable when it comes to big data.

## Motivation of the Research Work

Network Intrusion Detection systems play an important role in ensuring the security of the networks of large enterprise systems or critical infrastructures. The aim of this research is to show how Adversarial Machine learning can be used to trick classifiers into misclassifying malicious network packets as legitimate ones. Most of the current work in Adversarial Machine Learning has been done for images like [Szegedy 2013b], [Goodfellow 2014b], [Nguyen 2015b], so our aim is to use the same attack techniques for Network Intrusion Detection systems as well.

## Organization of the Report

The organization of the report is as follows:

Chapter 1 gives a description of the past work that has been done in the domain of adversarial machine learning and the research papers we have gone through as a prerequisite for our study.

It also gives a description of the attack techniques that we will be using in our study.

Chapter 2 focuses on the dataset we have used and the preprocessing steps.

Chapter 3 provides the implementation details.

Chapter 4 discusses the results we obtained for every step in our study.

Chapter 5 gives an analysis of our results at every step.

Finally, we conclude our report in Chapter 6, and specify our future work.

# Chapter 1

## Literature Review

### 1.1 Introduction

We followed the framework proposed by [Vom Brocke 2009] for the literature review process. The first step involved defining the scope and creating a rough outline of the task to perform. This was followed by thorough literature survey and subsequent analysis of the work already done this field. Following these steps helped us to identify the research gaps that existed, and helped to formulate the research questions that we will attempt to answer through our work.

The literature review was conducted using exhaustive search over the following terms: “information security AND machine learning”, “machine learning AND IDS”, “anomaly detection AND IDS” and “adversarial machine learning”, “deep learning AND IDS”. Apart from keyword search and relevance, other selection criteria were the chronology of the papers and the quality of sources (peer reviewed journals and conferences).

The search engines utilized for this search were mainly the LTU library search and Google scholar search engines which aggregate results over a number of databases. The majority of the references comes from well known databases such as ACM, IEEE, Springer and Elsevier.

### 1.2 Intrusion Detection

The methodologies used in NIDS can be divided into various categories. The vast majority of the literature describe the following categorizations:

- **Misuse-based or signature based:** These types of systems perform simple signature matching using signatures or indicators extracted from previously known attacks. The problem with these types of systems is that they don’t perform well when they encounter new types of attacks and the task of maintaining the signatures given the rising number of attacks today, is also difficult.
- **Anomaly based:** These types of systems try to model normal behavior in a network in contrast to what is anomalous and potentially malicious. These are better than signature

based systems because of the fact that they are better at adapting to new attacks. but a major concern with such systems is whether the system “learns” a good definition of what is anomalous or not. The system should be able to classify malicious behaviour as anomalous.

- **Hybrid systems:** These types of systems are the combination of the above approaches.

In many of the research papers we surveyed, we find that the terms “machine learning” and “anomaly detection” are used interchangeably. [Bhuyan 2014] make a broader presentation that includes not only classifiers such as the ones used in Machine Learning and Data Mining but also pure anomaly detection techniques which include statistical methods, clustering and outlier based methods, knowledge based methods and combination learners.

Anomaly Detection based systems promise to solve the issue of adaptation to new attacks, however, the problem of generalization still exists, which makes it difficult to prove whether they can be used widely in practice. [Sommer 2010a] present some challenges that are relevant even today. These challenges include:

- the data used to train the models is very unbalanced, which makes it difficult to apply unsupervised classification techniques,
- High False Positive rate (FPR) can become a problem because that would result in a large number of alarms to be analyzed that are generated by the NIDS, therefore, time and fatigue can be a problem
- interpretation of the results and taking action is not always possible with some ML techniques,
- the lack of high quality representative datasets can lead to problems in the evaluation of different approaches.

[Milenkoski 2015] identified four major categories of evaluation metrics that are used in majority of the studies:

- Attack detection accuracy with most common metrics the False Positive, False Negative, True Positive and True Negative rates, the Positive Predictive Value (PPV) or Precision and the Negative Predictive Value (NPV). The False Positive Rate (FPR) and the True Positive Rate (TPR) are used in the construction of Receiver Operating Characteristic (ROC) curves and the calculation of the Area Under the Curve (AUC).
- Performance overhead which the IDS is adding to the overall network environment.
- Attack coverage, which is the detection accuracy of the IDS without benign traffic.
- Workload processing, which is the amount of traffic that can be processed by an IDS vs. the amount of network traffic the IDS discards.

### 1.2.1 IDS Datasets

One of the most used dataset is KDD'99 [KDD ] which was derived from the DARPA'98 dataset. The dataset was used in a competition that was held during the Fifth International Conference on Knowledge Discovery and Data Mining and the main competition task was to create a predictive model that can be used in network intrusion detection. The KDD'99 dataset had some problems which were analyzed by researchers such as [McHugh 2000], [Sommer 2010b], [Brugger 2007], [Tavallae 2009a]. The major issues were -

- There is a huge number of redundant records for about 78% and 75% are duplicated in the train and test set, respectively.
- This redundancy makes the machine learning training quite biased.

This led to the creation of an improved version of the KDD'99 dataset, which was called the NSL-KDD dataset [NSL-KDD ] by [Tavallae 2009a]. This dataset did not solve all the problems in the KDD'99 dataset and more importantly it did not erase the fact that it is quite outdated. Still, the NSL-KDD dataset has been used in many Network Intrusion Detection based works due to the lack of public datasets for network-based IDSs. It provides a good analysis on various machine learning techniques for intrusion detection. The advantages of using this dataset are -

- No redundant records in the train set, so the classifier will not produce any biased results
- No duplicate record in the test set which have better reduction rates.
- The number of selected records from each difficult level group is inversely proportional to the percentage of records in the original KDD data set.

## 1.3 Adversarial Machine Learning

Adversarial Machine Learning (AML) is the study of machine learning in the presence of an adversary that works against the ML system in an effort to reduce its effectiveness or extract information from it.

All aspects and phases of the machine learning process can be attacked by an adversary as can be seen in Figure 1.1.

### 1.3.1 Attack Types

If we see the problem from the attacker's perspective, we can define two types of attacks as poisoning attacks or evasion attacks. [Biggio 2012] and [Xiao 2015] describe different poisoning attacks. [Xiao 2015] devised attacks against the Ridge and Lasso linear classifiers by maximizing the classification error with regards to the training points. [Biggio 2012] performed poisoning

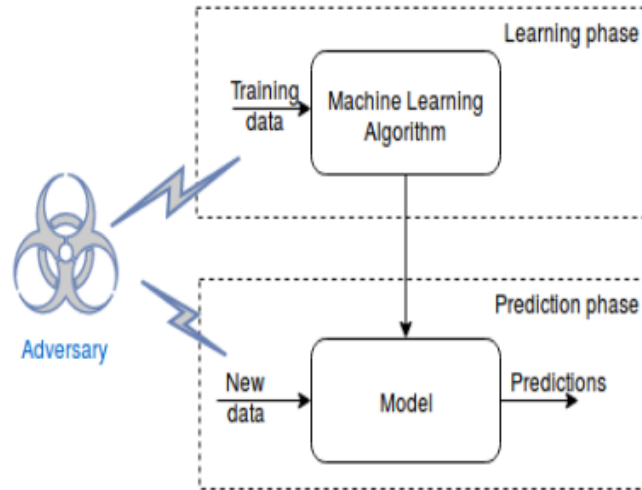


Figure 1.1: Adversarial Machine Learning [Maria Rigaki 2017]

attack on SVMs (Support Vector Machines). They injected samples to the training set in order to find the attack point that will maximize the classification error.

Evasion attacks were studied in the works of [Biggio 2013], [Biggio 2014] and [Ateniese 2015]. The latter, i.e. [Ateniese 2015] proposed a method in which a meta-classifier is created by training several classifiers on multiple training sets. This meta-classifier is used in order to extract statistical properties from the data but not the features themselves, which makes it an attack against privacy.

### 1.3.2 Adversarial Deep Learning

Deep Learning has become very successful in the recent years in the field of Natural Language Processing and Computer Vision. This also led to the development of Adversarial Deep Learning which was initially centered around the Computer Vision domain.

One of the first breakthroughs came in 2013, when [Szegedy 2013a] successfully demonstrated how one can fool Deep Learning classifiers by introducing small variations in an image. These variations were so small that they were imperceptible to humans but enough to fool the classifiers. Some examples of such images are shown in Figure 1.2. Another work [Nguyen 2015a], generated random images which appeared or had patterns in it, which did not mean anything, but the images were able to fool the Deep Learning classifiers into predicting them into valid object classes. Some reference images have been shown in Figure 1.3.

Although many different explanations have been given for the reason as to why this is possible, [Goodfellow 2014a] explains, contrary to the intuition of many people, that the main cause is the high degree of linearity of the Deep Learning components. The linearity is brought about by the use of piece wise linear activation functions such as Rectified Linear Units (ReLUs). Such functions are used to achieve faster optimization as well as help to create decision boundaries





Figure 1.2: Adversarial example produced by image perturbation. The neural network believes the images on the right are ostriches. [Szegedy 2013a]

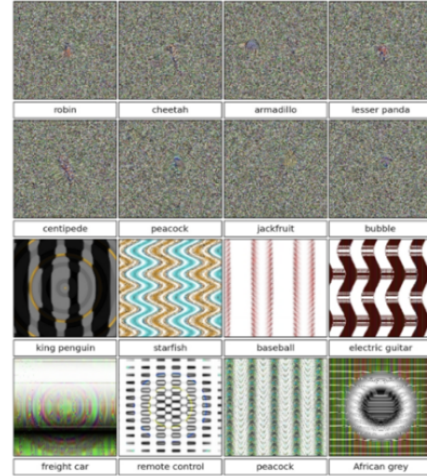


Figure 1.3: Images generated using evolutionary algorithms. [Nguyen 2015a]

that define much larger areas than the training data. This is the reason why when these classifiers encounter new examples (images), that have certain specific properties, they are misclassified ([Goodfellow 2014a] and [Nguyen 2015a]). Another very interesting property that was discovered by [Szegedy 2013a], [Goodfellow 2014a] and [Nguyen 2015a] was that the images that show adversarial properties for one neural network can transfer these properties to other neural networks trained separately.

The only models that have shown some resistance to adversarial examples are the Radial Basis Function (RBF) networks but they are not used often as they don't generalize well [Goodfellow 2014a]. Other than those, even shallow linear models are also affected by the same problem and so are model ensembles.

The methods and algorithms to generate adversarial examples has also been researched upon. There are many such methods which have a trade-off on speed of production, performance and complexity. Some of the methods that have been proposed are given below -

- Evolutionary algorithms, proposed in [Nguyen 2015a]. But this method is very slow compared to the other two alternatives.
- Fast Gradient Sign Method (FGSM) proposed in [Goodfellow 2014a].
- Jacobian-based Saliency Map Attack (JSMA) [Papernot 2016c] is more computationally expensive than FGSM but it has the ability to create adversarial samples with less degree of distortion.

Both the FGSM and JSMA methods try to generate a small perturbation in the original sample so that it will exhibit adversarial characteristics. In FGSM a perturbation  $\delta$  is generated by

computing the gradient of the cost function  $J$  in respect to the input  $x$ :

$$\delta = \epsilon \text{sign}(\nabla_x J(\theta, x, y)) \quad (1.1)$$

where  $\theta$  are model parameters,  $x$  is the input to the model,  $y$  are the labels associated with  $x$ ,  $\epsilon$  is a very small value and  $J(\theta, x, y)$  is the cost function used when training the neural network. This method is very fast because it requires the gradient which can be computed very efficiently using backpropagation. The perturbation is then added to the initial sample and the final result produces a misclassification. An example is shown in Figure 1.4.

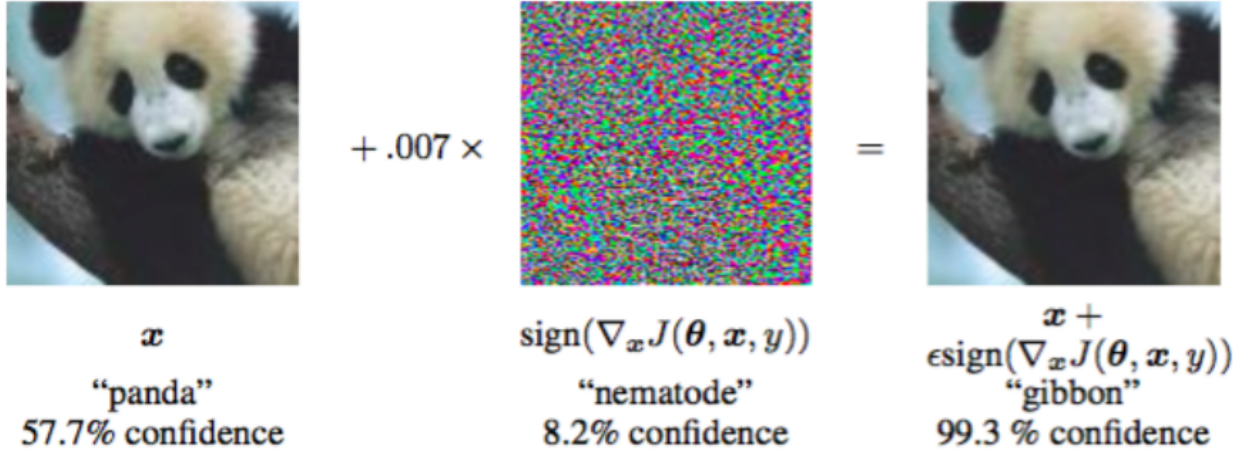


Figure 1.4: Generating adversarial samples with FGSM [Goodfellow 2014a]

JSMA, as the name suggests, generates adversarial sample perturbations based on the concept of saliency maps. The direction sensitivity of the sample in regards to the target class is calculated using a saliency map. [Papernot 2016c] designed an efficient saliency adversarial map under the  $L_0$  distance (i.e. the number of features  $i$  such that  $x'_i \neq x_i$ ). The Jacobian matrix computed for a given sample  $x$  is expressed as -

$$J_f(x) = \frac{\partial f(x)}{\partial x} = \left[ \frac{\partial f_j(x)}{\partial x_i} \right]_{i \times j} \quad (1.2)$$

In this way, the input features of  $x$  that made most significant changes to the output can be identified. Basically, the algorithm works by trying to determine which input features will be most likely to create a targeted class change. Using this sensitivity map one or more features are chosen as the possible perturbations and the model is checked to establish whether or not this change resulted in a misclassification. If it does not result in a misclassification, the next most sensitive feature is selected and a new iteration occurs until an adversarial sample that can fool the network is generated [Papernot 2016c]. The process is illustrated in Figure 1.5. Since the method usually takes a number of iterations, it is not as fast as FGSM.

Both FGSM and JSMA operate under the threat model of a strong attacker, e.g. an attacker that has knowledge of at least the underlying model. However if the attacker is not aware of the underlying model, it does not mean that the system cannot be exploited. If the attacker has only access to the model output and has some knowledge of the input to be provided, he can use the output of the model with different inputs to create an approximation of the model. And since the adversarial attacks have the transferability property, it is possible for the attacker to craft adversarial samples on the approximated model which can later be used as attack vectors against the original model [Papernot 2016b].

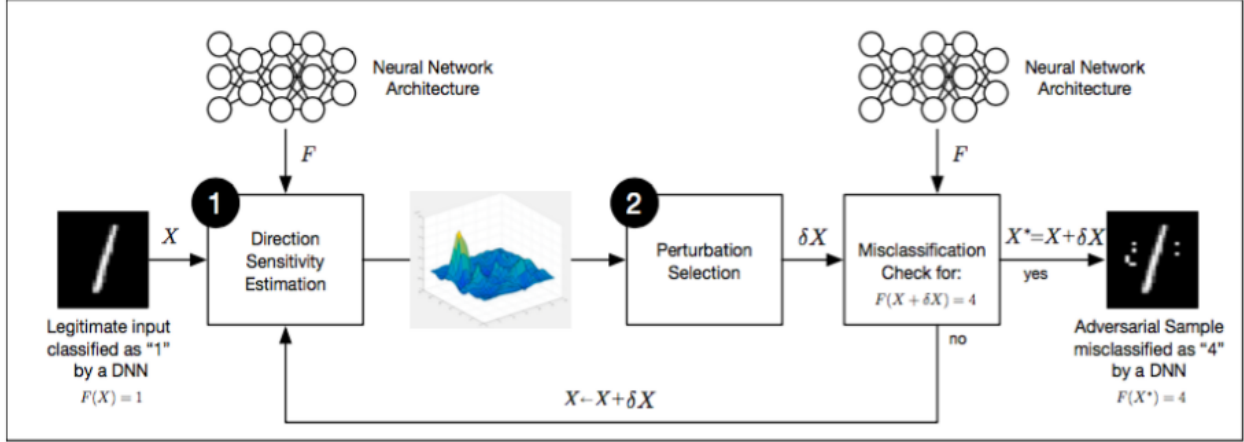


Figure 1.5: Generating adversarial samples with JSMA [Papernot 2016c]

An even weaker threat model is that in which the attacker has no access to the underlying model. These types of situations arise in face or voice recognition systems, i.e. in the physical domain. An attacker that can craft adversarial samples without access or knowledge of the underlying model or system could potentially fool these systems. [Kurakin 2016] demonstrated a successful attempt of such type of an attack.

[Papernot 2016a] thoroughly tested the concept of transferability. The authors tested several classifiers both as source for adversarial sample generation as well as target models. One thing to note, however, is that the testing was confined to image classifiers.

# Chapter 2

## Data Collection and Analysis

The most popular datasets in the domain of Intrusion Detection as discussed in Section 1.2.1 are the KDD'99 and the NSL-KDD datasets. These are the only ones that are labeled, include a variety of attacks and hence are widely used. Although these datasets are severely outdated, they have been chosen as a basis for this study mainly due to lack of better alternatives and secondly because the purpose of the study is the robustness of classifiers and not to make claims about prediction capabilities and generalization of our models.

### 2.1 KDD'99 and NSL-KDD

KDD'99 is one of the most widely used datasets in the literature related to Intrusion Detection. The attacks that are present in the dataset can be divided into four major categories: **Denial of Service (DoS)**, **User to Root (U2R)**, **Remote to Local (R2L)** and **Probing** attacks. A short description of these categories are given below -

- **DoS** attacks are an interruption in an authorized user's access to a computer network, in other words, they are attacks against availability. This category contains attacks such as *smurf*, *neptune*, *mailbomb*, *udpstorm*, etc.
- **U2R** attacks indicate attempts of privilege escalation. Some attacks of this type in the dataset are *buffer overflow*, *loadmodule*, *sqlattack* and *rootkit*.
- **R2L** attacks aim to gain remote access to a system by exploiting a vulnerability. Some examples of this type of attacks are *multihop*, *guesspasswd*, *httptunnel* and *xsnoop*.
- **Probe** attacks aim to gather information by using enumeration techniques like scanning or probing different parts of the network, for e.g. the ports. Although strictly speaking, they are not attacks but they are the first set of steps that an attacker will perform before attacking a network. Some examples of such types of attacks are *ipsweep*, *portsweep*, *nmap* and *mscan*.

Feature	Type	Feature	Type
duration	cont.	is_guest_login	sym.
protocol_type	sym.	count	cont.
service	sym.	srv_count	cont.
flag	sym.	serror_rate	cont.
src_bytes	cont.	rerror_rate	cont.
dest_bytes	cont.	srv_rerror_rate	cont.
land	sym.	diff_srv_rate	cont.
wrong_fragment	cont.	srv_diff_host_rate	cont.
urgent	cont.	dst_host_count	cont.
hot	cont.	dst_host_srv_count	cont.
num_failed_logins	cont.	dst_host_same_srv_rate	cont.
logged_in	sym.	dst_host_diff_srv_rate	cont.
num_compromised	cont.	dst_host_same_src_port_rate	cont.
root_shell	cont.	dst_host_srv_diff_host_rate	cont.
su_attempted	cont.	dst_host_serror_rate	cont.
num_root	cont.	dst_host_srv_serror_rate	cont.
num_file_creations	cont.	dst_host_rerror_rate	cont.
num_access_files	cont.	dst_host_srv_rerrorv_rate	cont.
num_outbound_cmds	cont.	is_host_login	sym.

Table 2.1: KDD'99 and NSL-KDD features

The detailed list of features is given in Table 2.1. The original dataset description used the term “symbolic” for categorical variables and the term “continuous” for numerical ones. The features in the dataset can be divided into three main categories: **Basic**, **Traffic** and **Content** related ones, as described in [Tavallae 2009b].

**Basic** features are the ones related to connection information such as hosts, ports, protocols and services used.

**Traffic** features are calculated during a window interval as an aggregate. A further subdivision is “aggregates based on the same host” and “aggregates over the same service”. In the NSL-KDD dataset, the time window (in KDD'99) was substituted with a connection window of the last 100 connections.

**Content** features are extracted from the payload or packet data and they are related to the content of specific applications or protocol used.

The NSL-KDD dataset [NSL-KDD] has the same number of features as the KDD'99, but improved some shortcomings as described by [Tavallae 2009a] which included the removal of redundant records in the training and testing sets and also adjusting the difficulty of classification for some attacks.

## 2.2 Data Preprocessing

For data preprocessing, the following steps were followed-

1. One-Hot encoding was used to convert the categorical features to numerical features.
2. All the features (now all numerical) were normalized using Min-Max Scaler as very large values can dominate the dataset and affect the performance of certain classifiers like SVM and the MLP.
3. The dataset had labels consisting of 39 distinct attack categories. These attacks were grouped into four major families - “DoS”, “U2R”, “R2L” and “Probe”. Hence the problem was transformed into a five-class classification problem (including the “normal” class).

After preprocessing, the final number of features are 122. The number of data points in the training set are 1,25,973 and in the test set 22,544.

# Chapter 3

## Implementation Details

This section will highlight the libraries used and the implementation details. The code is written in Python language.

### 3.1 Libraries Used

Following are the major libraries used in the project -

- **Keras**: Deep Learning library for creating and training the model
- **Cleverhans**: For implementing adversarial attacks and adversarial example generation
- **Scikit-learn**: For making Machine Learning models for testing purposes
- **Numpy**: For storing the train and test data
- **Pandas**: For reading the train and test data
- **Matplotlib**: For visualisation in the form of plots and graphs

### 3.2 Description of functions

#### 3.2.1 Jacobian-based Saliency Map Attack

To implement JSMA, we use the *SaliencyMapMethod* function present in the Cleverhans python library.

```
1 models = KerasModelWrapper(model)
2 jsma = SaliencyMapMethod(models, sess=sess)
3 jsma_params = {'theta': 1., 'gamma': 0.1, 'clip_min': 0., 'clip_max': 1., 'y_target': None}
4
5 for sample_ind in range(0, source_samples):
6     sample = X_test_scaled[sample_ind: (sample_ind+1)]
```

```

7         # We want to find an adversarial example for each possible target class
8         # (i.e. all classes that differ from the label given in the dataset)
9         current_class = int(np.argmax(y_test[sample_ind]))
10
11         # Only target the normal class
12         for target in [0]:
13             if current_class == 0:
14                 break
15
16             print('Generating adv. example for target class {} for sample {}'.format(\
17                 target, sample_ind), end='\r')
18
19             # Run the Jacobian-based saliency map approach
20             one_hot_target = np.zeros((1, FLAGS.nb_classes), dtype=np.float32)
21             one_hot_target[0, target] = 1
22             jsma_params['y_target'] = one_hot_target
23             adv_x = jsma.generate_np(sample, **jsma_params)
24
25             # Check if success was achieved
26             res = int(model_argmax(sess, x, predictions, adv_x) == target)
27
28             # Compute number of modified features
29             adv_x_reshape = adv_x.reshape(-1)
30             test_in_reshape = X_test_scaled[sample_ind].reshape(-1)
31             nb_changed = np.where(adv_x_reshape != test_in_reshape)[0].shape[0]
32             percent_perturb = float(nb_changed) / adv_x_reshape.shape[0]
33
34             X_adv[sample_ind] = adv_x
35             results[target, sample_ind] = res
36             perturbations[target, sample_ind] = percent_perturb
37
38     print()
39     print(X_adv.shape)

```

### 3.2.2 Fast Gradient Sign Method

To implement FGSM, we use the *FastGradientMethod* function present in the Cleverhans python library.

```

1 models = KerasModelWrapper(model)
2 # Craft adversarial examples using Fast Gradient Sign Method (FGSM)
3 fgsm = FastGradientMethod(models, sess=sess)
4 fgsm_params = {'eps': 0.3}
5 adv_x_f = fgsm.generate(x, **fgsm_params)
6 # adv_x_f = tf.stop_gradient(adv_x_f)
7 X_test_adv, = batch_eval(sess, [x], [adv_x_f], [X_test_scaled])

```

### 3.2.3 Adversarial Feature Statistics

To get the statistics of the Adversarial examples that were generated, followed by plotting the most important features in the case of JSMA, we use the following piece of code.

```

1 print("===== Adversarial Feature Statistics =====")
2
3 feats = dict()
4 total = 0
5 orig_attack = X_test_scaled - X_adv
6 for i in range(0, orig_attack.shape[0]):
7     ind = np.where(orig_attack[i, :] != 0)[0]

```



```

8         total += len(ind)
9         for j in ind:
10             if j in feats:
11                 feats[j] += 1
12             else:
13                 feats[j] = 1
14
15 # The number of features that were changed for the adversarial samples
16 print("Number of unique features changed with JSMA: {}".format(len(feats.keys())))
17 print("Number of average features changed per datapoint with JSMA: {}".format(total/len(
    orig_attack)))
18
19 top_10 = sorted(feats, key=feats.get, reverse=True)[:10]
20 top_20 = sorted(feats, key=feats.get, reverse=True)[:20]
21 print("Top ten features: ", X_test.columns[top_10])
22
23 top_10_val = [100*feats[k] / y_test.shape[0] for k in top_10]
24 top_20_val = [100*feats[k] / y_test.shape[0] for k in top_20]
25
26 plt.figure(figsize=(12, 6))
27 plt.bar(np.arange(20), top_20_val, align='center')
28 plt.xticks(np.arange(20), X_test.columns[top_20], rotation='vertical')
29 plt.title('Feature participation in adversarial examples')
30 plt.ylabel('Percentage (%)')
31 plt.xlabel('Features')
32 plt.savefig('Adv_features.png', bbox_inches = "tight")

```

### 3.2.4 Plotting ROC curves

ROC curves were plotted for four ML based classifiers which are shown later. The general sample code for plotting ROC curves is given below -

```

1 dt = OneVsRestClassifier(DecisionTreeClassifier(random_state=42))
2 dt.fit(X_train_scaled, y_train)
3 y_pred = dt.predict(X_test_scaled)
4
5 fpr_dt, tpr_dt, _ = roc_curve(y_test[:, 0], y_pred[:, 0])
6 roc_auc_dt = auc(fpr_dt, tpr_dt)
7 print("Accuracy score: {}".format(accuracy_score(y_test, y_pred)))
8 print("F1 Score: {}".format(f1_score(y_test, y_pred, average='micro')))
9 print("AUC score: {}".format(roc_auc_dt))
10
11 y_pred_adv = dt.predict(X_adv)
12 fpr_dt_adv, tpr_dt_adv, _ = roc_curve(y_test[:, 0], y_pred_adv[:, 0])
13 roc_auc_dt_adv = auc(fpr_dt_adv, tpr_dt_adv)
14 print("Accuracy score adversarial: {}".format(accuracy_score(y_test, y_pred_adv)))
15 print("F1 Score adversarial: {}".format(f1_score(y_test, y_pred_adv, average='micro')))
16 print("AUC score adversarial: {}".format(roc_auc_dt_adv))
17
18 plt.figure()
19 lw = 2
20 plt.plot(fpr_dt, tpr_dt, color='darkorange', lw=lw, label="ROC Curve (area = %0.2f)" %
    roc_auc_dt)
21 plt.plot(fpr_dt_adv, tpr_dt_adv, color='green', lw=lw, label="ROC Curve adv. (area = %0.2f" %
    roc_auc_dt_adv))
22 plt.plot([0, 1], [0, 1], color='navy', lw=lw, linestyle='--')
23 plt.xlim([0.0, 1.0])
24 plt.ylim([0.0, 1.05])
25 plt.xlabel("False Positive Rate")
26 plt.ylabel("True Positive Rate")
27 plt.title("ROC Decision Tree (class=Normal)")
28 plt.legend(loc="lower right")
29 plt.savefig('ROC_DT.png', bbox_inches = "tight")

```

# Chapter 4

## Results

### 4.1 Baseline Models

A number of different were trained and tested on the NSL-KDD dataset to establish a baseline. The results on the test set are given in Table 4.1.

Method	Accuracy	F1-Score	AUC (normal)
Decision Tree	0.989	0.992	0.992
Random Forest	0.993	0.994	0.994
Linear SVM	0.945	0.958	0.954
Voting Ensemble	0.993	0.993	0.746
MLP	0.985	-	-

Table 4.1: Test set results for 5-class classification

The variation of the accuracy with the epochs while training the MLP on the clean dataset is shown in Figure 4.1.

### 4.2 Adversarial Test Set Generation

Both the FGSM and JSMA methods were used in order to generate adversarial test sets from the original test set. The underlying model used to generate the adversarial examples was a pre-trained MLP. The architecture of the model is shown in figure 4.2. Table 4.2 below, shows the difference between the two methods in terms of changed features on average as well as the unique features changed for all data points in the test set.

Tables 4.3 and 4.4 show the transformation required for selected features using the JSMA method in order to for the specific data point to become “normal”. Some of the altered features for that data point are shown.

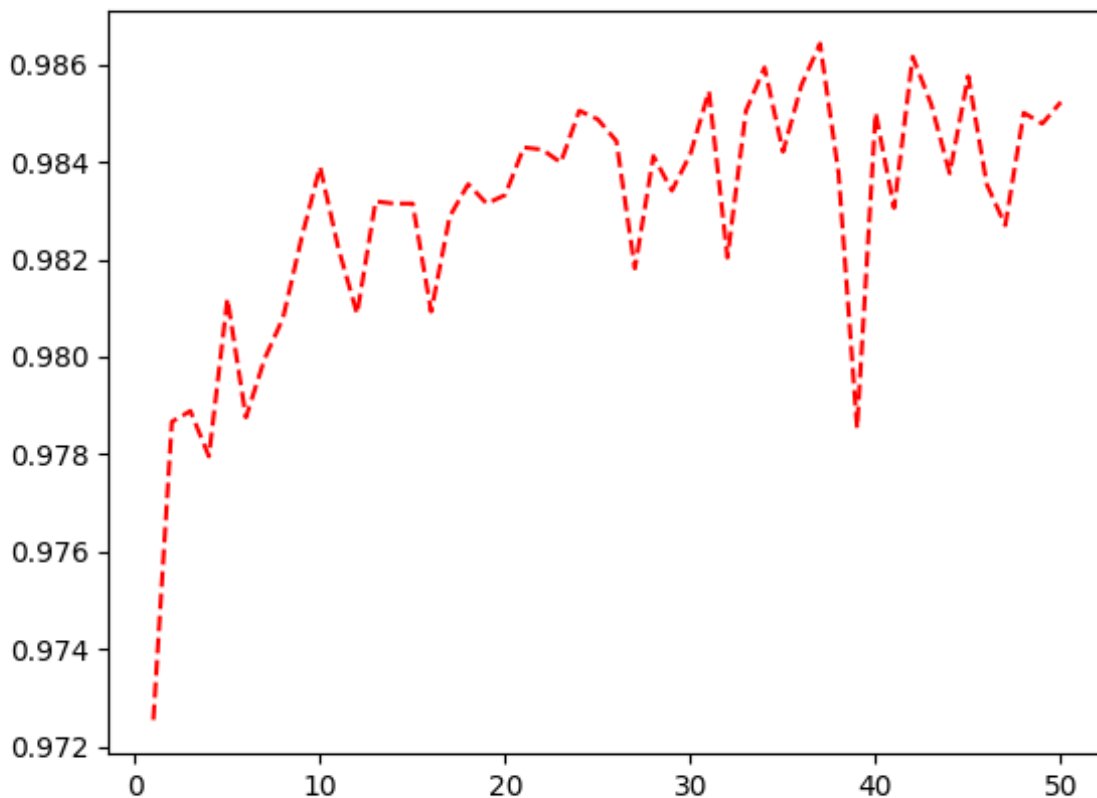


Figure 4.1: MLP Training - accuracy vs. epochs

Method	Num. of unique altered features	Avg. features changed per data point	Percentage of altered features
FGSM	122	76.47	62.68
JSMA	89	11.58	9.49

Table 4.2: Adversarial feature statistics

...	F26	...	F29	F30	...	F41	...	label
...	0.7	...	0.7	0.7	...	0.7	...	dos

Table 4.3: Data point  $x^{(17)}$  in original test set

## 4.3 Model Evaluation on Adversarial Data

This section presents the results of the baseline models on the adversarial test set generated by the JSMA method in terms of Accuracy, F1-score and AUC (Table 4.5). One thing to note here

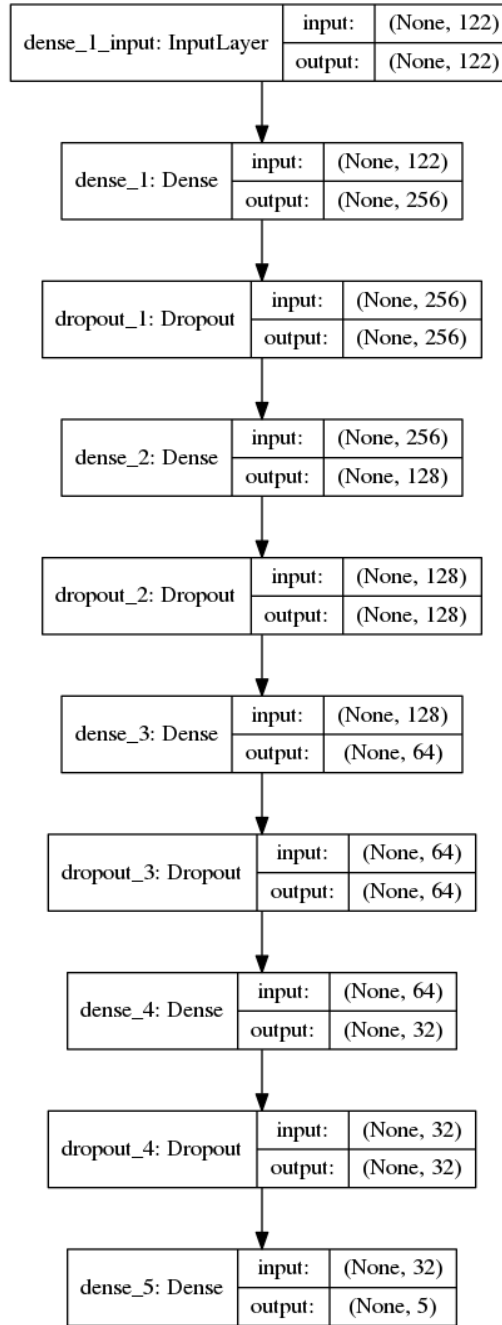


Figure 4.2: Architecture of underlying MLP

...	F26	...	F29	F30	...	F41	...	label
...	1.0	...	1.0	1.0	...	1.0	...	normal

Table 4.4: Transformation of data point  $x_{\text{adv}}^{(17)}$  using JSMA

is that both the AUC results as well as the ROC curves in the figures below, are only presented for the the “normal” class, while the F1-score is an average score over all classes.

Method	Accuracy	F1-Score	AUC (normal)
Decision Tree	0.660	0.802	0.744
Random Forest	0.968	0.977	0.986
Linear SVM	0.810	0.846	0.949
Voting Ensemble	0.914	0.914	0.723
MLP	0.670	-	-

Table 4.5: Adversarial test set results for 5-class classification

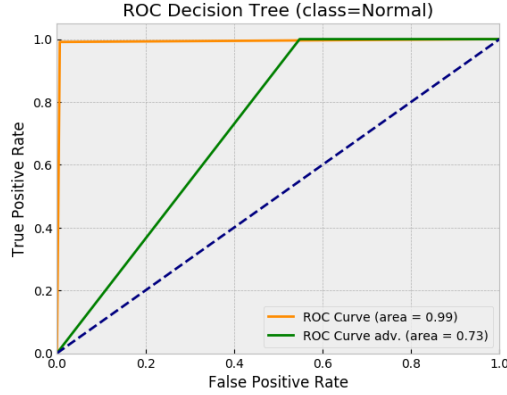


Figure 4.3: Decision Tree ROC curves

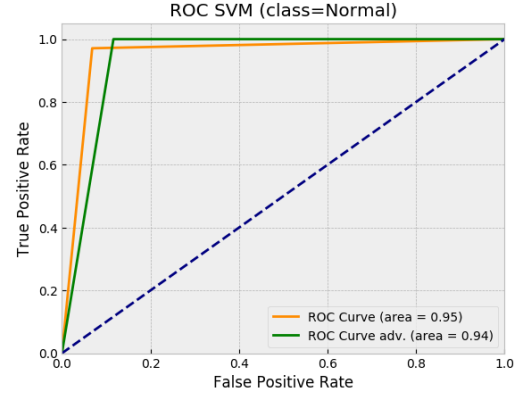


Figure 4.4: SVM ROC curves

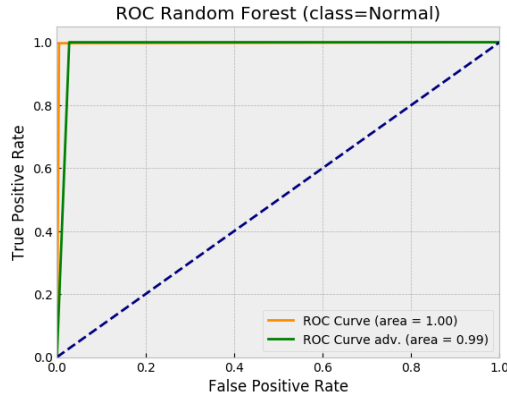


Figure 4.5: Random Forest ROC curves

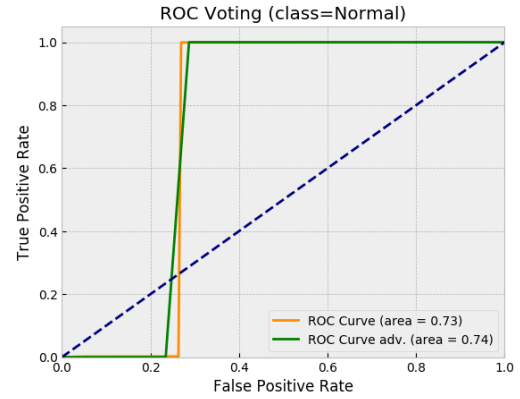


Figure 4.6: Voting Ensemble ROC curves

## 4.4 Feature Evaluation

After generating the adversarial test set using JSMA, a ranking of the features in terms of frequency with which they appear in the adversarial test set as changed was created. This was calculated by subtracting the original test set from the adversarial test set

$$\delta = X^* - X_{\text{test}}$$

where  $X^*$  is the adversarial test set and  $X_{\text{test}}$  is the original test set. In order to find which

features were altered for each data point  $\delta^{(i)}$  we need to find the feature indexes  $j$  where feature  $\delta_j^{(i)} = 0$ .

The top ten features and their description are presented in Table 4.6. Figure 4.7 shows the top 20 features and their percentages.

Feature	Description
srv_count	number of connections to the same service as the current connection in the past 100 connections
count	number of connections to the same host as the current connection in the past 100 connections
dst_host_srv_count	number of connections to the same service and destination host as the current connection in the past 100 connections
dst_host_same_srv_rate	% of connections to the same service and destination host
src_bytes	number of data bytes from source to destination
same_srv_rate	% of connections to the same service
dst_bytes	number of data bytes from destination to source
dst_host_diff_srv_rate	% of different services on the current host
dst_host_count	number of connections to the same destination host as the current connection in the past 100 connections
duration	duration of the connection

Table 4.6: Top 10 adversarial features using JSMA

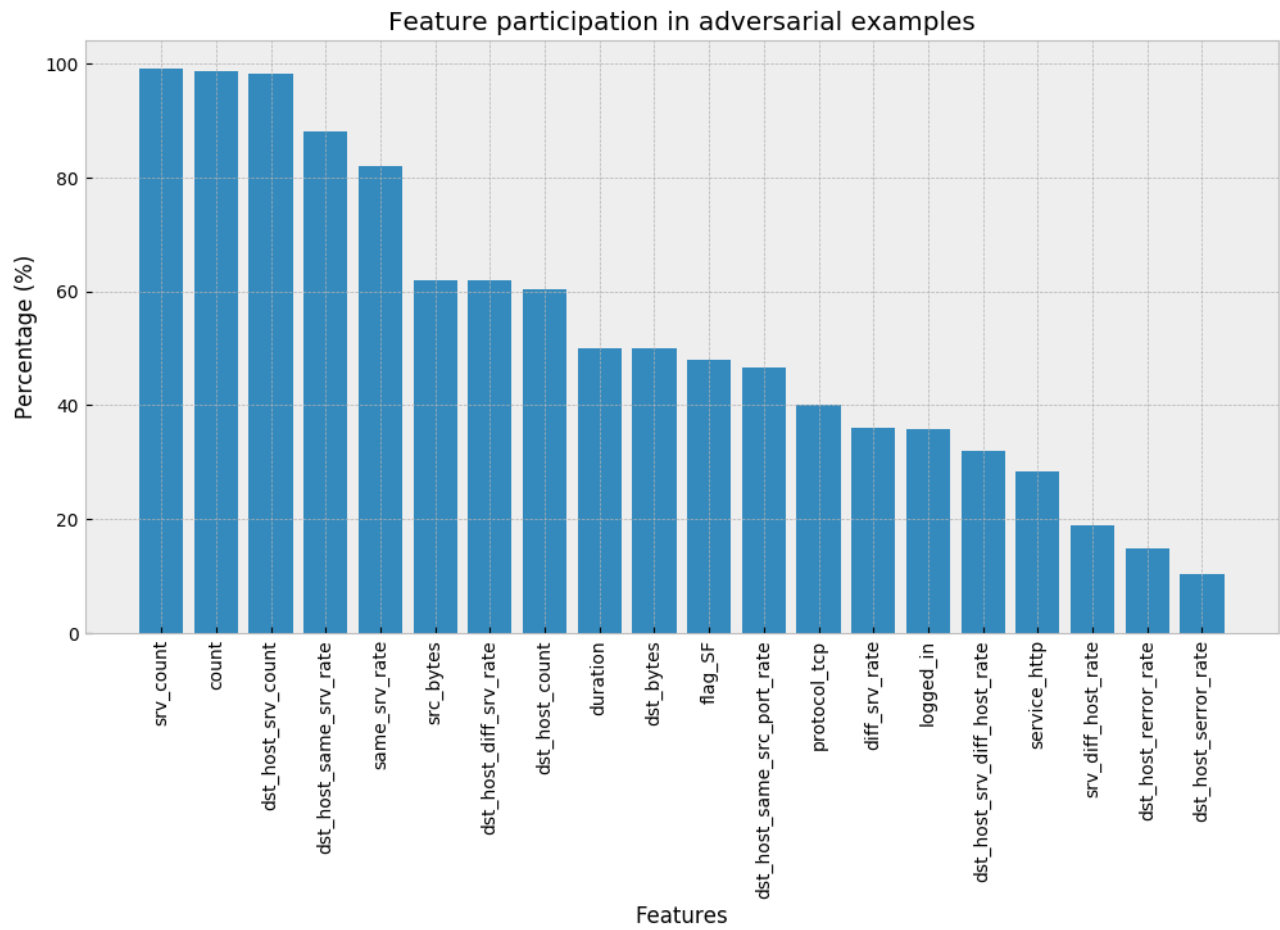


Figure 4.7: Most used features in adversarial sample generation

# Chapter 5

## Discussion

### 5.1 Data Modelling

Table 4.1 shows that all the models have an overall accuracy and F1-score around 99%. The AUC scores however show a major difference where we observe that the Decision Tree and the Random Forest classifier outperform the SVM and the Voting ensemble. This implies that the first two methods are performing slightly better in classifying the “normal” test samples exhibiting a lower False Positive Rate (FPR). This can also be observed in the ROC-AUC curves shown in Figures 4.3 to 4.6.

### 5.2 Adversarial Test Set Generation

As it was explained earlier, the FGSM method changes each feature very slightly while JSMA searches through the features of each data point and changes one at each iteration in order to produce an adversarial sample. This means that FGSM is not suitable for tasks like NIDS since the features are generated from network traffic and controlling them in a fine grained manner would not be possible for an adversary. On the contrary, JSMA changes only a few features at a time and although it takes more time to generate adversarial examples as it is iterative, it can form the basis for a practical attack due to the lower number of features that have to be changed. This is totally inline with the observations in [Huang 2011] where the importance of domain applicability is highlighted as a potential problem for an attacker.

### 5.3 Model Evaluation on Adversarial Data

In terms of overall classification accuracy all classifiers were affected. The most severely affected is the Decision Tree with a drop of 32.9% and the Decision Tree whose accuracy dropped by 13.5%. The Random Forest classifier showed some robustness with an accuracy drop of 2.5%.

When it comes to F1-score, the Decision Tree was affected the most and its score was reduced



by 19%. Linear SVM saw an F1-score reduction of 11.2%. The other two classifiers did not suffer as much and again the Random Forest showed the highest robustness by dropping only 1.7%.

The AUC over the normal class is an indicator of how robust were the classifiers against targeted misclassification towards the normal class. It provides a measure on how much was the increase on the FPR compared to the TPR, in other words, how many attacks were misclassified as normal traffic. The best performing classifier was the the Linear SVM, which only dropped 0.5%, followed by the Random Forest which dropped 0.8%. The Decision Tree classifier was severely affected, losing 24.8% percentage points.

Based on the results, it seems that the only method that was robust across all metrics was the Random Forest. The Decision Tree was the worst performing classifier, which also corresponds with the result of [Papernot 2016a], in which also, Decision Tree was one of the worst performing methods.

## 5.4 Feature Evaluation

Table 5.6 gives an idea of the top-10 features which contribute most during the generation of adversarial samples. Among those features, the top two are about the number of connections to the same service/host as the current connection in the past 100 connections. The next two features are about the rate and the count of the connections to the same host and port. This tells us that one way an attacker could get around the detection would be to lessen the number of requests they generate. Exploiting this can be very helpful for running bots as one can generate connections to external command and control servers and can hide their traffic under normal traffic that a user creates. A similar type of reasoning can also be applied to other count and rate types of features. This type of discussion is also relevant to the Denial of Service (DoS) type of attacks and while this dataset is quite old, historically, there have been attacks that followed the “low and slow” approach in order to appear as close to legitimate traffic as possible. When it comes to features related to service types, using common protocols like HTTP or HTTPS can be a good strategy in order to hide into other normal traffic, instead of using protocols that might be easier to get discovered.

# Chapter 6

## Conclusion

From the results and discussion presented previously we can say that JSMA is more preferable in the intrusion detection domain in terms of applicability of attacks in terms of as compared to FGSM which cannot be used in a practical manner. We also observed the robustness exhibited by different classifiers which is also shown in [Papernot 2016a]. Also, it is clear that using a substitute model to generate adversarial samples can be successful and it is worth looking at adversarial security when deploying machine learning classifiers. This means that even when attackers do not have access to the training data, adversarial samples can transfer to different models under certain circumstances. This means that when machine learning is used, it should be accompanied with relevant adversarial training and testing and strengthening.

Also, one important thing to note is that in our case, we had a preprocessed dataset and not raw data which made it easier to attack. A physical attack would require some idea on how the raw network data are processed and the types of features that are generated. So, if we were to deal with raw data some knowledge would be required about how the data is preprocessed and how features are generated.

Finally, even if we know the features used, it would still require work to adjust the traffic profiles of the specific attack. Contrary to the image classification problem, where each bit in the image can be considered a feature which can be easily altered, not all traffic related characteristics can be changed, even when an adversary has the ability to craft specific network packets and payloads. To protect against adversaries, NIDS classifiers will have to use features that can not be easily manipulated by an attacker.

### 6.1 Future Work

This study presented an attempt to transfer adversarial methods from the Deep Learning image classification domain to the NIDS domain. While defenses have been proposed against these methods in several studies, these defenses do not generalize very well. A future study would be to examine some of these defenses and establish whether they improve the situation or not especially in the NIDS domain.

---

In our study a neural net was used as the source model for preparing the adversarial examples. An extension of this study could be to use other models as the source as well.

Finally, further study is also required to understand the effect of the adversarial methods in different attack classes which would potentially yield a better overview of which features are more important for each attack type when it comes to adversarial sample generation. This can eventually be used by adversaries to select strategies that would allow them to hide their malicious traffic depending on the chosen attack.

# Appendices



# Appendix A

## Source Code

```
1  import numpy as np
2  import pandas as pd
3  import sys
4  from keras.models import Sequential
5  from keras.layers import Dense, Dropout
6  from keras.optimizers import RMSprop, adam
7  from keras import backend as K
8  from keras.utils import plot_model
9  from cleverhans.attacks import FastGradientMethod, SaliencyMapMethod
10 from cleverhans.utils_tf import model_train, model_eval, batch_eval, model_argmax
11 from cleverhans.attacks_tf import jacobian_graph
12 from cleverhans.utils import other_classes
13 from cleverhans.utils_keras import KerasModelWrapper
14
15 import tensorflow as tf
16 from tensorflow.python.platform import flags
17
18 from sklearn.multiclass import OneVsRestClassifier
19 from sklearn.tree import DecisionTreeClassifier
20 from sklearn.ensemble import RandomForestClassifier, VotingClassifier
21 from sklearn.linear_model import LogisticRegression
22 from sklearn.svm import SVC, LinearSVC
23
24 from sklearn.metrics import accuracy_score, roc_curve, auc, f1_score
25 from sklearn.preprocessing import LabelEncoder, MinMaxScaler
26 import matplotlib.pyplot as plt
27 import pickle
28 plt.style.use('bmh')
29
30 K.set_learning_phase(1)
31
32 FLAGS = flags.FLAGS
33
34 flags.DEFINE_integer('nb_epochs', 50, 'Number of epochs to train model')
35 flags.DEFINE_integer('batch_size', 64, 'Size of training batches')
36 flags.DEFINE_integer('learning_rate', 0.005, 'Learning rate for training')
37 flags.DEFINE_integer('nb_classes', 5, 'Number of classification classes')
38 flags.DEFINE_integer('source_samples', 10, 'Nb of test set examples to attack')
39
40 print()
41 print()
42 print("===== Start of preprocessing stage \n
43      =====")
44
45 names = ['duration', 'protocol', 'service', 'flag', 'src_bytes', 'dst_bytes', 'land', '\n
46         wrong_fragment', 'urgent', 'hot', 'num_failed_logins', 'logged_in', 'num_compromised', '\n
```

```

    'root_shell', 'su_attempted', 'num_root', 'num_file_creations', 'num_shells', 'num_access_files', 'num_outbound_cmds', 'is_host_login', 'is_guest_login', 'count', 'srv_count', 'serror_rate', 'srv_serror_rate', 'error_rate', 'srv_error_rate', 'same_srv_rate', 'diff_srv_rate', 'srv_diff_host_rate', 'dst_host_count', 'dst_host_srv_count', 'dst_host_same_srv_rate', 'dst_host_diff_srv_rate', 'dst_host_same_src_port_rate', 'dst_host_srv_diff_host_rate', 'dst_host_serror_rate', 'dst_host_srv_serror_rate', 'dst_host_error_rate', 'dst_host_srv_error_rate', 'attack_type', 'other']
45
46 df_train = pd.read_csv('../NSL_KDD/KDDTrain+.txt', names=names, header=None)
47 df_test = pd.read_csv('../NSL_KDD/KDDTest-21.txt', names=names, header=None)
48 print("Initial training and test data shapes: ", df_train.shape, df_test.shape)
49
50 full = pd.concat([df_train, df_test])
51 assert full.shape[0] == df_train.shape[0] + df_test.shape[0]
52
53 full['label'] = full['attack_type']
54
55 # Denial-of-Service (DoS) Attacks
56 full.loc[full.label == 'neptune', 'label'] = 'dos'
57 full.loc[full.label == 'back', 'label'] = 'dos'
58 full.loc[full.label == 'land', 'label'] = 'dos'
59 full.loc[full.label == 'pod', 'label'] = 'dos'
60 full.loc[full.label == 'smurf', 'label'] = 'dos'
61 full.loc[full.label == 'teardrop', 'label'] = 'dos'
62 full.loc[full.label == 'mailbomb', 'label'] = 'dos'
63 full.loc[full.label == 'processtable', 'label'] = 'dos'
64 full.loc[full.label == 'udpstorm', 'label'] = 'dos'
65 full.loc[full.label == 'apache2', 'label'] = 'dos'
66 full.loc[full.label == 'worm', 'label'] = 'dos'
67
68 # User-to-root (U2R) Attacks
69 full.loc[full.label == 'buffer_overflow', 'label'] = 'u2r'
70 full.loc[full.label == 'loadmodule', 'label'] = 'u2r'
71 full.loc[full.label == 'perl', 'label'] = 'u2r'
72 full.loc[full.label == 'rootkit', 'label'] = 'u2r'
73 full.loc[full.label == 'sqlattack', 'label'] = 'u2r'
74 full.loc[full.label == 'xterm', 'label'] = 'u2r'
75 full.loc[full.label == 'ps', 'label'] = 'u2r'
76
77 # Remote-to-local (R2L) Attacks
78 full.loc[full.label == 'ftp_write', 'label'] = 'r2l'
79 full.loc[full.label == 'guess_passwd', 'label'] = 'r2l'
80 full.loc[full.label == 'imap', 'label'] = 'r2l'
81 full.loc[full.label == 'multihop', 'label'] = 'r2l'
82 full.loc[full.label == 'phf', 'label'] = 'r2l'
83 full.loc[full.label == 'spy', 'label'] = 'r2l'
84 full.loc[full.label == 'warezclient', 'label'] = 'r2l'
85 full.loc[full.label == 'warezmaster', 'label'] = 'r2l'
86 full.loc[full.label == 'xlock', 'label'] = 'r2l'
87 full.loc[full.label == 'xsnoop', 'label'] = 'r2l'
88 full.loc[full.label == 'snmpgetattack', 'label'] = 'r2l'
89 full.loc[full.label == 'httptunnel', 'label'] = 'r2l'
90 full.loc[full.label == 'snmpguess', 'label'] = 'r2l'
91 full.loc[full.label == 'sendmail', 'label'] = 'r2l'
92 full.loc[full.label == 'named', 'label'] = 'r2l'
93
94 # Probe attacks
95 full.loc[full.label == 'satan', 'label'] = 'probe'
96 full.loc[full.label == 'ipsweep', 'label'] = 'probe'
97 full.loc[full.label == 'nmap', 'label'] = 'probe'
98 full.loc[full.label == 'portsweep', 'label'] = 'probe'
99 full.loc[full.label == 'saint', 'label'] = 'probe'
100 full.loc[full.label == 'mscan', 'label'] = 'probe'
101
102 full = full.drop(['other', 'attack_type'], axis=1)

```

```

103 print("Unique labels", full.label.unique())
104 full = full.sample(frac=1).reset_index(drop=True)
105
106 # Generate One - Hot encoding
107 full2 = pd.get_dummies(full, drop_first=False)
108
109 # Separate training and test sets again
110 features = list(full2.columns[:-5]) # Due to One-Hot encoding
111 y_train = np.array(full2[0: df_train.shape[0]][['label_normal', 'label_dos', 'label_probe',
112         'label_r2l', 'label_u2r']])
112 X_train = full2[0: df_train.shape[0]][features]
113
114 y_test = np.array(full2[df_train.shape[0]: ][['label_normal', 'label_dos', 'label_probe',
115         'label_r2l', 'label_u2r']])
115 X_test = full2[df_train.shape[0]: ][features]
116
117 # Scale data
118 scaler = MinMaxScaler().fit(X_train)
119 X_train_scaled = np.array(scaler.transform(X_train))
120 X_test_scaled = np.array(scaler.transform(X_test))
121
122 # Generate label encoding for Logistic regression
123 labels = full.label.unique()
124 le = LabelEncoder()
125 le.fit(labels)
126 y_full = le.transform(full.label)
127 y_train_l = y_full[0: df_train.shape[0]]
128 y_test_l = y_full[df_train.shape[0]: ]
129
130 print("Training dataset shape", X_train_scaled.shape, y_train.shape)
131 print("Test dataset shape", X_test_scaled.shape, y_test.shape)
132 print("Label encoder y shape", y_train_l.shape, y_test_l.shape)
133
134 print("===== End of preprocessing stage \n
135         =====")
136
137 print()
138 print()
139
140 print("===== Start of adversarial sample generation \n
141         =====")
142
143 print()
144 print()
145
146 def mlp_model():
147     """
148     Generate a Multilayer Perceptron model
149     """
150     model = Sequential()
151     model.add(Dense(256, activation='relu', input_shape=(X_train_scaled.shape[1], )))
152     model.add(Dropout(0.4))
153     model.add(Dense(256, activation='relu'))
154     model.add(Dropout(0.4))
155     model.add(Dense(FLAGS.nb_classes, activation='softmax'))
156     model.compile(loss='categorical_crossentropy', optimizer='adam', metrics=['\
157         accuracy'])
158
159     model.summary()
160     return model
161
162 def mlp_model2():
163     """
164     Generate a Multilayer Perceptron model
165     """
166     model = Sequential()
167     model.add(Dense(256, activation='relu', input_shape=(X_train_scaled.shape[1], )))
168     model.add(Dropout(0.2))

```



```

164     model.add(Dense(128, activation='relu'))
165     model.add(Dropout(0.2))
166     model.add(Dense(64, activation='relu'))
167     model.add(Dropout(0.2))
168     model.add(Dense(32, activation='relu'))
169     model.add(Dropout(0.2))
170     model.add(Dense(FLAGS.nb_classes, activation='softmax'))
171     model.compile(loss='categorical_crossentropy', optimizer='adam', metrics=['accuracy'])
172
173     model.summary()
174     return model
175
176 acc_list = []
177 count = 0
178 def evaluate():
179     """
180     Model evaluation function
181     """
182     global count
183     count += 1
184
185     eval_params = {'batch_size': FLAGS.batch_size}
186     accuracy = model_eval(sess, x, y, predictions, X_test_scaled, y_test, args=
187         eval_params)
188     global acc_list
189     acc_list.append((count, accuracy))
190     print("Test accuracy on legitimate test samples: " + str(accuracy))
191
192 # Tensorflow placeholder variables
193 x = tf.placeholder(tf.float32, shape=(None, X_train_scaled.shape[1]))
194 y = tf.placeholder(tf.float32, shape=(None, FLAGS.nb_classes))
195
196 tf.set_random_seed(42)
197 model = mlp_model2()
198 plot_model(model, show_shapes=True, to_file='model.png')
199 sess = tf.Session()
200 predictions = model(x)
201 init = tf.global_variables_initializer()
202 sess.run(init)
203
204 # Train the model
205 train_params = {'nb_epochs': FLAGS.nb_epochs, 'batch_size': FLAGS.batch_size, '
206     learning_rate': FLAGS.learning_rate, 'verbose': 0}
207
208 model_train(sess, x, y, predictions, X_train_scaled, y_train, evaluate=evaluate, args=
209     train_params)
210
211 file = open("scores.pkl", "wb")
212 pickle.dump(acc_list, file)
213 file.close()
214
215 # Generate adversarial samples for all test datapoints
216 source_samples = X_test_scaled.shape[0]
217
218 # Jacobian-based Saliency Map Attack
219 results = np.zeros((FLAGS.nb_classes, source_samples), dtype='i')
220 perturbations = np.zeros((FLAGS.nb_classes, source_samples), dtype='f')
221 grads = jacobian_graph(predictions, x, FLAGS.nb_classes)
222
223 X_adv = np.zeros((source_samples, X_test_scaled.shape[1]))
224
225 models = KerasModelWrapper(model)
226 jsma = SaliencyMapMethod(models, sess=sess)
227 jsma_params = {'theta': 1., 'gamma': 0.1, 'clip_min': 0., 'clip_max': 1., 'y_target': None
228     }

```

```

226
227 for sample_ind in range(0, source_samples):
228     sample = X_test_scaled[sample_ind: (sample_ind+1)]
229     # We want to find an adversarial example for each possible target class
230     # (i.e. all classes that differ from the label given in the dataset)
231     current_class = int(np.argmax(y_test[sample_ind]))
232
233     # Only target the normal class
234     for target in [0]:
235         if current_class == 0:
236             break
237
238         print('Generating adv. example for target class {} for sample {}'.format(\
                target, sample_ind), end='\r')
239
240         # Run the Jacobian-based saliency map approach
241         one_hot_target = np.zeros((1, FLAGS.nb_classes), dtype=np.float32)
242         one_hot_target[0, target] = 1
243         jsma_params['y_target'] = one_hot_target
244         adv_x = jsma.generate_np(sample, **jsma_params)
245
246         # Check if success was achieved
247         res = int(model_argmax(sess, x, predictions, adv_x) == target)
248
249         # Compute number of modified features
250         adv_x_reshape = adv_x.reshape(-1)
251         test_in_reshape = X_test_scaled[sample_ind].reshape(-1)
252         nb_changed = np.where(adv_x_reshape != test_in_reshape)[0].shape[0]
253         percent_perturb = float(nb_changed) / adv_x_reshape(-1).shape[0]
254
255         X_adv[sample_ind] = adv_x
256         results[target, sample_ind] = res
257         perturbations[target, sample_ind] = percent_perturb
258
259 print()
260 print(X_adv.shape)
261
262 print("===== Evaluation of MLP Performance \
        =====")
263 print()
264
265 eval_params = {'batch_size': FLAGS.batch_size}
266 accuracy = model_eval(sess, x, y, predictions, X_test_scaled, y_test, args=eval_params)
267 print("Test accuracy on normal examples: {}".format(accuracy))
268
269 accuracy_adv = model_eval(sess, x, y, predictions, X_adv, y_test, args=eval_params)
270 print("Test accuracy on adversarial examples: {}".format(accuracy_adv))
271 print()
272
273 print("===== Decision tree Classifier \
        =====")
274 dt = OneVsRestClassifier(DecisionTreeClassifier(random_state=42))
275 dt.fit(X_train_scaled, y_train)
276 y_pred = dt.predict(X_test_scaled)
277
278 # Calculate FPR for normal class only
279 fpr_dt, tpr_dt, _ = roc_curve(y_test[:, 0], y_pred[:, 0])
280
281 roc_auc_dt = auc(fpr_dt, tpr_dt)
282 print("Accuracy score: {}".format(accuracy_score(y_test, y_pred)))
283 print("F1 Score: {}".format(f1_score(y_test, y_pred, average='micro')))
284 print("AUC score: {}".format(roc_auc_dt))
285
286 # Predict using adversarial test samples
287 y_pred_adv = dt.predict(X_adv)
288 fpr_dt_adv, tpr_dt_adv, _ = roc_curve(y_test[:, 0], y_pred_adv[:, 0])

```

```

289 roc_auc_dt_adv = auc(fpr_dt_adv, tpr_dt_adv)
290 print("Accuracy score adversarial: {}".format(accuracy_score(y_test, y_pred_adv)))
291 print("F1 Score adversarial: {}".format(f1_score(y_test, y_pred_adv, average='micro')))
292 print("AUC score adversarial: {}".format(roc_auc_dt_adv))
293
294 plt.figure()
295 lw = 2
296 plt.plot(fpr_dt, tpr_dt, color='darkorange', lw=lw, label="ROC Curve (area = %0.2f)" % \
roc_auc_dt)
297 plt.plot(fpr_dt_adv, tpr_dt_adv, color='green', lw=lw, label="ROC Curve adv. (area = %0.2f\
)" % roc_auc_dt_adv)
298 plt.plot([0, 1], [0, 1], color='navy', lw=lw, linestyle='--')
299 plt.xlim([0.0, 1.0])
300 plt.ylim([0.0, 1.05])
301 plt.xlabel("False Positive Rate")
302 plt.ylabel("True Positive Rate")
303 plt.title("ROC Decision Tree (class=Normal)")
304 plt.legend(loc="lower right")
305 plt.savefig('ROC_DT.png', bbox_inches = "tight")
306 print()
307
308 print()
309 print("===== Random Forest Classifier \
=====")
310 rf = OneVsRestClassifier(RandomForestClassifier(n_estimators=200, random_state=42))
311 rf.fit(X_train_scaled, y_train)
312 y_pred = rf.predict(X_test_scaled)
313
314 # Calculate FPR for normal class only
315 fpr_rf, tpr_rf, _ = roc_curve(y_test[:, 0], y_pred[:, 0])
316
317 roc_auc_rf = auc(fpr_rf, tpr_rf)
318 print("Accuracy score: {}".format(accuracy_score(y_test, y_pred)))
319 print("F1 Score: {}".format(f1_score(y_test, y_pred, average='micro')))
320 print("AUC score: {}".format(roc_auc_rf))
321
322 # Predict using adversarial test samples
323 y_pred_adv = rf.predict(X_adv)
324 fpr_rf_adv, tpr_rf_adv, _ = roc_curve(y_test[:, 0], y_pred_adv[:, 0])
325 roc_auc_rf_adv = auc(fpr_rf_adv, tpr_rf_adv)
326 print("Accuracy score adversarial: {}".format(accuracy_score(y_test, y_pred_adv)))
327 print("F1 Score adversarial: {}".format(f1_score(y_test, y_pred_adv, average='micro')))
328 print("AUC score adversarial: {}".format(roc_auc_rf_adv))
329
330 plt.figure()
331 lw = 2
332 plt.plot(fpr_rf, tpr_rf, color='darkorange', lw=lw, label="ROC Curve (area = %0.2f)" % \
roc_auc_rf)
333 plt.plot(fpr_rf_adv, tpr_rf_adv, color='green', lw=lw, label="ROC Curve adv. (area = %0.2f\
)" % roc_auc_rf_adv)
334 plt.plot([0, 1], [0, 1], color='navy', lw=lw, linestyle='--')
335 plt.xlim([0.0, 1.0])
336 plt.ylim([0.0, 1.05])
337 plt.xlabel("False Positive Rate")
338 plt.ylabel("True Positive Rate")
339 plt.title("ROC Random Forest (class=Normal)")
340 plt.legend(loc="lower right")
341 plt.savefig('ROC_RF.png', bbox_inches = "tight")
342 print()
343
344 print()
345 print("===== Linear SVC Classifier \
=====")
346 sv = OneVsRestClassifier(LinearSVC(C=1., random_state=42, loss='hinge'))
347 sv.fit(X_train_scaled, y_train)
348 y_pred = sv.predict(X_test_scaled)

```

```

349
350 # Calculate FPR for normal class only
351 fpr_sv, tpr_sv, _ = roc_curve(y_test[:, 0], y_pred[:, 0])
352
353 roc_auc_sv = auc(fpr_sv, tpr_sv)
354 print("Accuracy score: {}".format(accuracy_score(y_test, y_pred)))
355 print("F1 Score: {}".format(f1_score(y_test, y_pred, average='micro')))
356 print("AUC score: {}".format(roc_auc_sv))
357
358 # Predict using adversarial test samples
359 y_pred_adv = sv.predict(X_adv)
360 fpr_sv_adv, tpr_sv_adv, _ = roc_curve(y_test[:, 0], y_pred_adv[:, 0])
361 roc_auc_sv_adv = auc(fpr_sv_adv, tpr_sv_adv)
362 print("Accuracy score adversarial: {}".format(accuracy_score(y_test, y_pred_adv)))
363 print("F1 Score adversarial: {}".format(f1_score(y_test, y_pred_adv, average='micro')))
364 print("AUC score adversarial: {}".format(roc_auc_sv_adv))
365
366 plt.figure()
367 lw = 2
368 plt.plot(fpr_sv, tpr_sv, color='darkorange', lw=lw, label="ROC Curve (area = %0.2f)" % \
roc_auc_sv)
369 plt.plot(fpr_sv_adv, tpr_sv_adv, color='green', lw=lw, label="ROC Curve adv. (area = %0.2f" \
%)" % roc_auc_sv_adv)
370 plt.plot([0, 1], [0, 1], color='navy', lw=lw, linestyle='--')
371 plt.xlim([0.0, 1.0])
372 plt.ylim([0.0, 1.05])
373 plt.xlabel("False Positive Rate")
374 plt.ylabel("True Positive Rate")
375 plt.title("ROC SVM (class=Normal)")
376 plt.legend(loc="lower right")
377 plt.savefig('ROC_SVM.png', bbox_inches = "tight")
378 print()
379
380 print()
381 print("===== Voting Classifier =====")
382 vot = VotingClassifier(estimators=[('dt', dt), ('rf', rf), ('sv', sv)], voting='hard')
383 vot.fit(X_train_scaled, y_train_l)
384 y_pred = vot.predict(X_test_scaled)
385
386 # Calculate FPR for normal class only
387 fpr_vot, tpr_vot, _ = roc_curve(y_test_l, y_pred, pos_label=1, drop_intermediate=False)
388
389 roc_auc_vot = auc(fpr_vot, tpr_vot)
390 print("Accuracy score: {}".format(accuracy_score(y_test_l, y_pred)))
391 print("F1 Score: {}".format(f1_score(y_test_l, y_pred, average='micro')))
392 print("AUC score: {}".format(roc_auc_vot))
393
394 # Predict using adversarial test samples
395 y_pred_adv = vot.predict(X_adv)
396 fpr_vot_adv, tpr_vot_adv, _ = roc_curve(y_test_l, y_pred_adv, pos_label=1, \
drop_intermediate=False)
397 roc_auc_vot_adv = auc(fpr_vot_adv, tpr_vot_adv)
398 print("Accuracy score adversarial: {}".format(accuracy_score(y_test_l, y_pred_adv)))
399 print("F1 Score adversarial: {}".format(f1_score(y_test_l, y_pred_adv, average='micro')))
400 print("AUC score adversarial: {}".format(roc_auc_vot_adv))
401
402 plt.figure()
403 lw = 2
404 plt.plot(fpr_vot, tpr_vot, color='darkorange', lw=lw, label="ROC Curve (area = %0.2f)" % \
roc_auc_vot)
405 plt.plot(fpr_vot_adv, tpr_vot_adv, color='green', lw=lw, label="ROC Curve adv. (area = \
%0.2f)" % roc_auc_vot_adv)
406 plt.plot([0, 1], [0, 1], color='navy', lw=lw, linestyle='--')
407 plt.xlim([0.0, 1.0])
408 plt.ylim([0.0, 1.05])
409 plt.xlabel("False Positive Rate")

```

```

410 plt.ylabel("True Positive Rate")
411 plt.title("ROC Voting (class=Normal)")
412 plt.legend(loc="lower right")
413 plt.savefig('ROC_Vot.png', bbox_inches = "tight")
414 print()
415
416
417 # Print overall ROC curves
418 plt.figure(figsize=(12, 6))
419 plt.plot(fpr_dt_adv, tpr_dt_adv, label = 'DT (area = %0.2f)' % roc_auc_dt_adv)
420 plt.plot(fpr_rf_adv, tpr_rf_adv, label = 'RF (area = %0.2f)' % roc_auc_rf_adv)
421 plt.plot(fpr_sv_adv, tpr_sv_adv, label = 'SVM (area = %0.2f)' % roc_auc_sv_adv)
422 plt.plot(fpr_vot_adv, tpr_vot_adv, label = 'Vot (area = %0.2f)' % roc_auc_vot_adv)
423
424 plt.xlabel('False positive rate')
425 plt.ylabel('True positive rate')
426 plt.title('ROC curve (adversarial samples)')
427 plt.legend(loc = 'best')
428 plt.savefig('ROC_curves_adv.png', bbox_inches = "tight")
429
430
431 plt.figure(figsize=(12, 6))
432 plt.plot(fpr_dt, tpr_dt, label = 'DT (area = %0.2f)' % roc_auc_dt)
433 plt.plot(fpr_rf, tpr_rf, label = 'RF (area = %0.2f)' % roc_auc_rf)
434 plt.plot(fpr_sv, tpr_sv, label = 'SVM (area = %0.2f)' % roc_auc_sv)
435 plt.plot(fpr_vot, tpr_vot, label = 'Vot (area = %0.2f)' % roc_auc_vot)
436
437 plt.xlabel('False positive rate')
438 plt.ylabel('True positive rate')
439 plt.title('ROC curve (normal samples)')
440 plt.legend(loc = 'best')
441 plt.savefig('ROC_curves.png', bbox_inches = "tight")
442 print()
443
444 print("===== Adversarial Feature Statistics =====")
445
446 feats = dict()
447 total = 0
448 orig_attack = X_test_scaled - X_adv
449 for i in range(0, orig_attack.shape[0]):
450     ind = np.where(orig_attack[i, :] != 0)[0]
451     total += len(ind)
452     for j in ind:
453         if j in feats:
454             feats[j] += 1
455         else:
456             feats[j] = 1
457
458 # The number of features that were changed for the adversarial samples
459 print("Number of unique features changed with JSMA: {}".format(len(feats.keys())))
460 print("Number of average features changed per datapoint with JSMA: {}".format(total/len(\
orig_attack)))
461
462 top_10 = sorted(feats, key=feats.get, reverse=True)[:10]
463 top_20 = sorted(feats, key=feats.get, reverse=True)[:20]
464 print("Top ten features: ", X_test.columns[top_10])
465
466 top_10_val = [100*feats[k] / y_test.shape[0] for k in top_10]
467 top_20_val = [100*feats[k] / y_test.shape[0] for k in top_20]
468
469 plt.figure(figsize=(12, 6))
470 plt.bar(np.arange(20), top_20_val, align='center')
471 plt.xticks(np.arange(20), X_test.columns[top_20], rotation='vertical')
472 plt.title('Feature participation in adversarial examples')
473 plt.ylabel('Percentage (%)')
474 plt.xlabel('Features')

```

```

475 plt.savefig('Adv_features.png', bbox_inches = "tight")
476
477 # Craft adversarial examples using Fast Gradient Sign Method (FGSM)
478 fgsm = FastGradientMethod(models, sess=sess)
479 fgsm_params = {'eps': 0.3}
480 adv_x_f = fgsm.generate(x, **fgsm_params)
481 # adv_x_f = tf.stop_gradient(adv_x_f)
482 X_test_adv, = batch_eval(sess, [x], [adv_x_f], [X_test_scaled])
483
484 # Evaluate accuracy
485 eval_par = {'batch_size': FLAGS.batch_size}
486 accuracy = model_eval(sess, x, y, predictions, X_test_adv, y_test, args=eval_par)
487 print("Test accuracy on adversarial examples: {}".format(accuracy))
488
489 # Comparison of adversarial and original test samples (attack)
490 feats = dict()
491 total = 0
492 orig_attack = X_test_scaled - X_test_adv
493
494 for i in range(0, orig_attack.shape[0]):
495     ind = np.where(orig_attack[i, :] != 0)[0]
496     total += len(ind)
497     for j in ind:
498         if j in feats:
499             feats[j] += 1
500         else:
501             feats[j] = 1
502
503 # The number of features that were changed for the adversarial samples
504 print("Number of unique features changed with FGSM: {}".format(len(feats.keys())))
505 print("Number of average features changed per datapoint with FGSM: {}".format(total/len(\
    orig_attack)))

```

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