



adedalic's blog

Codeforces Round #421 Editorial

By [adedalic](#), [history](#), 10 days ago,  

First, I apologize for problems with round and serious problem with Div1A/Div2C. It was very important round for me and, as always, something goes wrong. **KAN** have already [wrote about this](#).

Anyway, there are problems, so editorial must exist. Due some circumstances, Editorial will be upload in parts. Also, most of tutorials will contain main ideas how to solve task, not ready algorithm.

820A - Mister B and Book Reading

All that needed - is to accurately simulate process.

Create variable, which will contain count of read pages, subtract l , add v_0 , check, what you still have unread pages, make $v_0 = \min(v_1, v_0 + a)$ and again.

Complexity is $O(c)$.

```
code
....
```

820B - Mister B and Angle in Polygon

Since polygon is regular, all vertices of a regular polygon lie on a common circle (the circumscribed circle), so all possible angles are inscribed angles. And all inscribed angles subtending the same arc have same measure.

More over, minor and major arcs between vertices v_i and v_k equals to minor and major arcs between vertices v_{i+1} and v_{k+1} .

And finally, length of arc can be calculated with formula as sum of minor arcs between consecutive vertices. Length of minor arcs between consecutive vertices equals to $360 / n$.

Length of inscribed angle is half of arc it based on.

In other words $\angle v_1 v_2 v_3 = \frac{180 \cdot (n - (v_3 - v_1))}{n}$ if $v_1 < v_2 < v_3$ or $\frac{180 \cdot (v_3 - v_1)}{n}$ in other case.

In the end, this task can be solved by checking all different $(v_3 - v_1)$ (v_1 can be fixed as 1), or by formula, if we put in $|\angle v_1 v_2 v_3 - a|$ formula above.

In result finding closest angle can be done in $O(n)$ or even $O(1)$ time.

```
code
....
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819A - Mister B and Boring Game

Tutorial is not available

```
code
....
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819B - Mister B and PR Shifts


Let's see, how p_k ($1 \leq k \leq n$) affects different shifts.

Let's denote d_i is deviation of the i -th shift. At first all $d_i = 0$.


Then p_k affects it in following way:

→ Pay attention

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shreyansh.barodiya

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Handle:

- $d_0 + = |p_k - k|$,
- $d_1 + = |p_k - (k + 1)|$,
- ...
- $d_{n-k} + = |p_k - n|$,
- $d_{n-k+1} + = |p_k - 1|$,
- ...
- $d_{n-1} + = |p_k - (k - 1)|$.

Then there are 2 cases: $p_k \geq k$ or not.

If $p_k \geq k$ after removing modules we will get 3 query:

- to add $p_k - (k + i)$ to d_i where $0 \leq i \leq p_k - k$,
- to add $(k + i) - p_k$ to d_i where $p_k - k < i \leq n - k$ and
- to add $p_k - i$ to d_{n-k+i} where $0 < i < k$.

Else if $p_k < k$ we need to perform next operation:

- to add $(k + i) - p_k$ to d_i where $0 \leq i \leq n - k$,
- to add $p_k - i$ to d_{n-k+i} where $1 \leq i \leq p_k$ and
- to add $i - p_k$ to d_{n-k+i} where $p_k < i < k$.

But in both cases we must add 3 arithmetic progression to the segment of array d . Or make operation of adding $k \cdot (x - l) + b$ to segment $[l, r]$. Its known task, which can be done by adding/subtracting values in start and end of segment offline.

To make such operation we need to remember, how to add value b to segment $[l, r]$ of array d offline. We can just do next operations: $d[l] + = b$ and $d[r + 1] - = b$. Now value in position i $ans_i = \sum_{j=0}^{j=i} d[j]$.

So what is adding progression with coef k ? it's only adding to array d value k to all positions in segment $[l, r]$. That's why we need other array, for example df and making $df[l] + = k$ and $df[r + 1] - = k$. In result, $d[i] = d[i] + \sum_{j=0}^{j=i-1} df[j]$.

So algorithm to add $k \cdot (x - l) + b$ to segment $[l, r]$ is next:

- $d[l] + = b$,
- $d[r + 1] - = k \cdot (r - l + 1)$,
- $df[l] + = k$,
- $df[r + 1] - = k$.

After all queries we need recover array d with formula $d[i] = d[i] + \sum_{j=0}^{j=i-1} df[j]$. And after that get answer with formula $ans_i = \sum_{j=0}^{j=i} d[j]$.

So complexity is $O(n)$.

code

819C - Mister B and Beacons on Field

There 2 stages in this task: moving of first beacon and moving of second.

But at first we need factorization of n and s . Since n and s are product of integers $\leq 10^6$, it can be done in $O(\log(n) + \log(s))$ time by "Sieve of Eratosthenes".

Start from **second stage**, when second beacon is moving:

Position of beacons will look like pair of points: $(0, 0)$, $(0, k)$, where $0 \leq k \leq n$.

We need to check existing of point (x, y) such, that area of triangle $(0, 0)$, $(0, k)$, (x, y) equals to s . Using cross product $|((0, k) - (0, 0)) \cdot ((x, y) - (0, 0))| = 2 \cdot s$. After simplifying we get $|k \cdot x| = 2 \cdot s$ where $0 \leq k \leq n$.

So we can iterate all divisors of $2 \cdot s$, using factorization of s and recursive algorithm.

Complexity of second stage is $O(\sigma(s))$, where $\sigma(s)$ — number of divisors of s and for $s \leq 10^{18}$ $\sigma(s) \leq \approx 10^5$.

In the **first stage** we have such points: $(k, 0)$, $(0, n)$, where $1 \leq k \leq m$.

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We need to check existing of point (x, y) such, that area of triangle $(k, 0), (0, n), (x, y)$ equals to s . Using cross product $|((k, 0) - (0, n)) \cdot ((x, y) - (0, n))| = 2 \cdot s$ we can get next equation: $|k \cdot (y - n) + n \cdot x| = 2 \cdot s$. Then solution exists iff $\gcd(k, n) \mid 2 \cdot s$ ($2s \% \gcd(k, n) = 0$).

And we need to calculate how many $1 \leq k \leq m$ such, that $\gcd(k, n) \mid 2 \cdot s$.

We will solve it in next way: let's $n = p_1^{n_1} p_2^{n_2} \dots p_l^{n_l}$ and $2s = p_1^{s_1} p_2^{s_2} \dots p_l^{s_l}$ ($n_i, s_i \geq 0$).

Look at all p_i , that $n_i > s_i$. It's obvious, that if $p_i^{s_i+1}$ is divisor of k , then $2s$ doesn't divide at $\gcd(k, n)$.

In result, we have some constrains on k , like k doesn't divide at $a_j = p_i^{s_i+1}$.

Finally, we have next task: calculate number of k ($1 \leq k \leq n$) such, that k doesn't divide any of a_j . It can be done with inclusion-exclusion principle, where number of k which divides $a_{i_1}, a_{i_2}, \dots, a_{i_b}$ is $\frac{n}{a_{i_1} a_{i_2} \dots a_{i_b}}$.

Complexity of first stage is $O(2^{z(n)})$, where $z(x)$ — number of prime divisors of x , $z \leq 15$ for integers up to 10^{18} .

Result complexity is $O(\sigma(s) + 2^{z(n)})$ per test.

`code`

819D - Mister B and Astronomers

Let's construct slow but clear solution and then, speed it up.

Let's denote $s = \sum_{i=1}^n a_i$. We can see, that, at first, all operation with time are modulo T and the i -th astronomer checks moments $st_i, (st_i + s) \% T, (st_i + 2s) \% T, \dots$, where $st_i = \sum_{j=2}^i a_j$. More over, every astronomer, who checks moment t will check moment $(t + S) \% T$ by next time.

So we now constructed functional graph with T vertices. But this graph has very special type, since it can be divided on some cycles. More specifically, This graph consists of $\gcd(T, s)$ oriented cycles and each cycle has length exactly $\frac{T}{\gcd(T, s)}$. Even more, vertices u and v belong to same cycle iff $u \equiv v \pmod{\gcd(T, s)}$.

So we can work with cycles independently.

Let's look closely on one cycle. It's obviously, that all astronomers will walk on their cycles from their starting positions $st_i \% T$. But what the answer for them.

Answer for the i -th astronomer is number of vertices, including starting vertex, to the nearest starting vertex of any other astronomer if count along the orientation of cycle, because if two astronomers came to same vertex, lucky is one, who came first. Other astronomer has this vertex as start, his time is st_j , i -th time is $st_i + k \cdot s$, $k \geq 1$ and $st_i + k \cdot s > st_j$. If $st_i \equiv st_j \pmod T$ and $st_i < st_j$ then answer for the j -th astronomer is always 0.

So we must effectively calculate distance between two positions on cycle.

For that, let's numerate vertices along the orientation of cycle using vertex with minimal label as 0. If we will know position of $st_i \% T$ for every astronomer calculation of distance between consecutive is trivial (sort, or set or other).

For the i -th astronomer let's denote vertex with label 0 in his cycle as z_i . $z_i = st_i \% \gcd(T, s)$. But cycles very specific, because vertex with label 0 is z_i , vertex with label 1 is $(z_i + s) \% T$, vertex with label 2 is $(z_i + 2s) \% T$. In other words, vertex with label k is $(z_i + k \cdot s) \% T$.

If we want to know position k of st_i , we need to find v such, that $v \equiv (v \% \gcd(T, s)) + k \cdot s \pmod T$ which is diofant equation and can be calculated in $O(\log(T))$ time.

Result complexity is $O(n \cdot \log(T))$.

`code`

819E - Mister B and Flight to the Moon

There are different constructive solutions in this problem. Here is one of them.

Consider odd and even n separately. Let n be even. Let's build for each even $n \geq 4$ a solution such that there are triangles $1-2-x$, $3-4-y$, $5-6-z$ and so on. For $n = 4$ it's easy to construct such a solution. Then let's add two vertices at a time: $a = n - 1$ and $b = n$. Instead of triangle $1-2-x$ let's add triangle $1-a-2-x$, square $1-a-2-b$ and square $1-2-b$. The same with $3-4-y$, $5-6-z$ and so on. Only one edge $a-b$ is remaining, we should add it twice. To do this let's replace the square $1-a-2-b$ with triangles $a-b-1$ and $a-b-2$. Easy to see that the condition on triangles is satisfied, so we can proceed to adding two more vertices and so on.

To deal with odd n let's keep triangles $2-3-x$, $4-5-y$ and so on. To add two more vertices replace each of these triangles with two squares and one triangle in the same way as for even n , and also add two triangles $1-a-b$.

code

Tutorial of Codeforces Round #421 (Div. 1)

Tutorial of Codeforces Round #421 (Div. 2)

+205



[adedalic](#)

10 days ago

33



Comments (33)

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[adedalic](#)

10 days ago, # | ☆

+12

Auto comment: topic has been updated by [adedalic](#) (previous revision, new revision, compare).

→ [Reply](#)



[ibrahim5253](#)

10 days ago, # | ☆

+8

But in both cases we must add 3 arithmetic progression to the segment of array d . It's well known task, which can be done by adding/subtracting values in start and end of segment offline.

Can you please elaborate a bit(or point to some reference) on this *well known task*?

→ [Reply](#)



[Hailo](#)

10 days ago, # ^ | ☆

← Rev. 2 0

I a general case when you need to add progressions and answer queries you can use a Lazy Fenwick tree, see this [tutorial](#). Maybe someone knows how to solve it without this structure, I don't.

But in this specific case, you made updates but you have to answer the query just after all modifications are made. So you can make the updates using just 2 arrays

→ [Reply](#)



[adedalic](#)

10 days ago, # ^ | ☆

+5

Yes, i will elaborate this with next update

→ [Reply](#)



[8shubham](#)

10 days ago, # ^ | ☆

+1

[Reference](#) for offline addition(407C)

→ [Reply](#)



[forerunner](#)

10 days ago, # | ☆

← Rev. 4 +6

A "if...else if" solution for div2 C... [28115691](#)

→ [Reply](#)



shreyash390

10 days ago, # ^ | ☆

▲ +6 ▼

can you please explain your code??

→ [Reply](#)

forerunner

9 days ago, # ^ | ☆

▲ 0 ▼

sorry that I failed to prove it when $b < a$, seems complex...I just think it will be a loop; and when $b \geq a$ or the length is short, the answer is sure. there are some mistakes before, now corrected and some comments added

→ [Reply](#)

ranjanvittal

9 days ago, # ^ | ☆

▲ +1 ▼

A loop come brute force solution must work I guess. Basically logic I tried out is checking all strings where the repeating character introduced by B is any of the last $\max(1, a-b)$ characters.

<http://codeforces.com/contest/820/submission/28126243>→ [Reply](#)

meeeep

9 days ago, # | ☆

▲ +5 ▼

An alternative to handle the even case of 1E is to split the graph into 2 equal disjoint sets A and B. Label the elements a_1 to a_m , b_1 to b_m .

Use induction to construct for A and B separately. What remains is the complete bipartite graph, which can be done using cycles of length 4, all of form $a_i - b_{(i+j)} - a_{(i+1)} - b_{(i+j+1)}$, where i and j run from 1 to m, and indices are taken modulo m.

→ [Reply](#)

Aronzx

9 days ago, # | ☆

← Rev. 2 ▲ 0 ▼

Can someone please help me understand how Div2 Problem B can be solved in $O(1)$?

→ [Reply](#)

Sina_Imani

9 days ago, # ^ | ☆

▲ 0 ▼

[Here's my submission](#) Well, if you want to find closest angle to a, you just need to find an arc with angle most close to $2 \cdot a$ which its vertices are vertices of polygon. For doing this, you make your ideal arc (with angle $2 \cdot a$) and find the vertex in polygon which is closest to end of arc.

→ [Reply](#)

joker_in

9 days ago, # | ☆

▲ +4 ▼

can anyone explain div2d div1 b more thoroughly . i am not getting it

→ [Reply](#)

usernameson

9 days ago, # | ☆

▲ +3 ▼

The solution for Div 2 B is really nice. My solution was to construct the polygon then use dot products and a binary search to find the best end point with two other points fixed. It was really tedious and time consuming to code and had a worse complexity of $O(n \log(n))$.

→ [Reply](#)

HossamDoma

9 days ago, # | ☆

▲ 0 ▼

Can someone elaborate more accurately on Div2 D?

→ [Reply](#)

haleyk100198

9 days ago, # | ☆

▲ +18 ▼

For Div2D / Div1B, one could also keep the amount of elements which holds $a[i] \geq i$ to update the difference in $O(1)$ time.

Code with comments : <http://codeforces.com/contest/819/submission/28113390>→ [Reply](#)

end83

9 days ago, # ^ | ☆

▲ 0 ▼

Can you explain your solution a bit more?

→ [Reply](#)

9 days ago, # ^ | ☆

▲ +7 ▼

To calculate the weighted sum of the $(i+1)$ -th shift from the i -th shift, the elements which holds $i \geq a[i]$ (named as gt in the code) contributes $+1$ to the sum and $i < a[i]$ contributes -1 . That being said, we could solve the problem by simply maintaining the amount of elements which holds true on the above cases.



haleyk100198

For non-tail elements, we could easily tell the moment of $i < a[i]$ becomes $i \geq a[i]$ is $a[i] - i$, meaning that we need to account for this moments later.

For the tail element at the moment, we shall recalculate its contribution and placing a new update for it. Note that as $a[i] \leq n$, it is guaranteed that $n > a[\text{tail}]$ holds true, so we shall remove one from gt before the update. Same for updating lt for the tail.

→ [Reply](#)

R_ash

9 days ago, # ^ | ☆

▲ 0 ▼

Can you please tell me what does $\text{upd}[i]$ hold? Actually I don't understand what this operation " $\text{upd}[a[i]+i]++$ " is doing.

→ [Reply](#)

8 days ago, # ^ | ☆

▲ +1 ▼

As $\text{upd}[\text{time}]$ stores the pended update for moment "time", $\text{upd}[\text{time}]++$ means that there will be one extra element will switch from contributing -1 to $+1$. As we are placing $a[\text{tail}]$ back to the front, after $a[\text{tail}]$ iterations it will hit $a[\text{index}] == \text{index}$, therefore we shall place an update on $\text{time} = a[\text{tail}] + \text{current_time} = a[\text{tail}] + i$.

→ [Reply](#)

nikich340

8 days ago, # ^ | ☆

▲ 0 ▼

I did it more stupid using segment tree, but calculating indexes carefully is a bit difficult, and each update in log time :P

<http://codeforces.com/contest/820/submission/28132944>→ [Reply](#)

s_jindal00

7 days ago, # ^ | ☆

▲ 0 ▼

Awesome solution! Thanks. I understood it and coded myself but it's giving TLE! I don't understand how a $O(n)$ solution gets TLE?! [Code](#) Can you please check it once why it's happening

→ [Reply](#)

7 days ago, # ^ | ☆

▲ +1 ▼

[Editted version](#)

I interchanged line 10 & 11 of the original code and it passed all cases, the TLE is most likely caused by initializing the array with size $n+2$ before n is properly initialized.

For the sake of competitive programming, I would recommend you to use array that has fixed size instead of referring their sizes to variables -- This increases memory usage in practical cases but we only care about the worse case scenario here.

→ [Reply](#)

haleyk100198



s_jindal00

7 days ago, # ^ | ☆

▲ 0 ▼

Yea. I figured it out just after submitting the solution in java. In c++ uninitialized variables contain garbage values and no compilation error, however in java you need initialise it. **BTW thanks for giving this nice concept to solve the problem**

→ [Reply](#)

madn

9 days ago, # | ☆

← Rev. 2 ▲ +11 ▼

I think my solution of div2D/div1B is a bit easier. We can see that after a cyclic shift our array is always divided into two parts: shifted part and not shifted part. So i just simulated the process. All we need is to maintain two values for each of two parts: number of such elements that $|p[i] - i|$ will increase after shifting, and number of elements for which this value will decrease. Complexity is $O(n)$. My explanation isn't very good, but code may help you [28121452](#)

→ [Reply](#)

arman.t

9 days ago, # ^ | ☆

▲ 0 ▼

I did something similar: <http://codeforces.com/contest/820/submission/28127444>

→ [Reply](#)

adedalic

9 days ago, # | ☆

▲ 0 ▼

Auto comment: topic has been updated by adedalic (previous revision, new revision, compare).

→ [Reply](#)

9 days ago, # | ☆

← Rev. 2 ▲ +38 ▼

Abstract.

Another (and probably more simple) approach to Div1E.

Here I will suggest a way of constructing a solution for n , given **any** solution for $n - 2$. No properties are requested and required to be preserved by such induction.

You still need to solve cases for $n = 3$ and $n = 4$ to get the full solution.

The method:

Let's take two nodes, let them be $s = n - 1$ and $t = n$ for simplicity of numbering.

Consider following paths:

- $s \rightarrow 1 \rightarrow t$
- $s \rightarrow 2 \rightarrow t$
- ...
- $s \rightarrow (n - 2) \rightarrow t$
- $s \rightarrow t$ (this one is special from above).

Taking any two of such pathes you form a valid cycle of length 3 or 4. Match listed paths into cycles the following way: first with second, second with third, ..., pre-last with last, and last with first (in other words, match by neighbourhood).

Add such cycles to the answer. Note, that each listed path was used twice by construction above, this way all edges connected to s or t were used twice too.

Continue with $n = n - 2$ here.

→ [Reply](#)

cdkrot

7 days ago, # ^ | ☆

▲ 0 ▼



geniucos

This solution is absolutely brilliant! Thanks for sharing it with us. It's unexpectedly elegant and easy to understand. I've looked for an induction approach but failed to think about it for long because it was hard for me to imagine that I might be able to keep the old construction in its exact form, without some strange alterations.

→ [Reply](#)

8 days ago, # | ☆

▲ 0 ▼



joker_in

why editorial link is not there on contest page . I know there is issue with div2-c question but rest of the question are good , i learned and solved div2-d and e(almost done) . good work in editorial and contest **adedalic** . thumbs up for good work.

→ [Reply](#)

7 days ago, # | ☆

← Rev. 2 ▲ 0 ▼



XuYipei

There is my solution to [819A - Mister B and Boring Game](#) First of all, I guess the color for each segment a is ascending or descending. And for each segment b its color is the minimum or maximum value of the previous paragraph a. We can easily make the interval between l and r no more then $5 \cdot (a+b)$. Thus, you can enumerate the status of each segment and calculate the current answer. Maybe I can't describe it clearly. This is my submission: [28097355](#)

→ [Reply](#)

minson123

7 days ago, # ^ | ☆

▲ 0 ▼

The description said: "From multiple variants of t lexicographically minimal is chosen." Why each segment a is descending?

→ [Reply](#)

7 days ago, # ^ | ☆

▲ 0 ▼

Your solution inspire me.



minson123

This is [my solution](#).

For each segment a is increasing then as you said: "for each segment b its color is the minimum or maximum value of the previous paragraph a.", so I separate it to two situation: If $a \leq b$ then get the minimum/maximum value in section $[l+1, l+a]$ else get it in section $[l+b+1, l+a]$.

→ [Reply](#)

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