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a) $M(i, w) = \max(M(i-1, w), M(i-1, w-w_i) + p_i)$

i \ p_i w_i	0	1	2	3	4	5	6	7	8
1 5 1	0	5	5	5	5	5	5	5	5
2 4 2	0	5	5	9	9	9	9	9	9
3 3 3	0	5	5	9	9	9	12	12	12
4 2 4	0	5	5	9	9	9	12	12	12
5 1 5	0	5	5	9	9	9	12	12	12

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b) The item with the greatest value should always be picked

If there did exist an item x with more value than some other item y , y could simply replace it with x and it would fit and increase the value.

~~Therefore we can remove the items~~
~~and the complexity is $O(n \log n)$~~

1) Sort the weights in ascending order
time complexity $O(n \log n)$

2) Set x, i, p to 0
while ($x \leq w$ & $i \leq n$)
if ($w_i \leq w - x$)
 $p = p + p_i$, $x = x + w_i$
else
 exit
solution is p

\therefore Algorithm takes $O(n \log n)$ time to sort
+ $O(n)$ to find solution
 \Rightarrow complexity is $O(n \log n)$