# CS F364: Design & Analysis of Algorithm



### Knapsack Problem Greedy Algorithm



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## Activity Selection Problem

### Activity Selection Problem:

- Consider a set  $S = \{1, 2, 3, ..., n\}$  of n activities that can happen one activity at a time. Activity i takes place during interval  $[s_i, f_i)$ .
- Activity i and j are compatible if  $[s_i, f_i)$  and  $[s_j, f_j)$  do not overlap
  - Select maximum size set of mutually comparable activities.

Consider following set of activity

- {3, 9, 11} is a compatible activity
- {1, 4, 8, 11} is larger compatible activity. In fact it is the largest
- Another largest compatible activity is {2, 4, 9, 11}

# Activity Selection Problem

### Greedy Algorithm

- Strategy to solve constrained optimization problem
- Make sequence of choices [with] What looks best at the moment
  - Incremental thus Efficient
- A greedy algorithm makes a locally optimal choice in the hope that the choice will lead to a globally optimal solution
  - Caution: does NOT always yields optimal solutions •
- Determine the problem has optimal substructure

### Key ingredients

- Greedy-choice property: we can assemble a globally optimal solution by making locally optimal (greedy) choices. 9
  - Optimal substructure: if an optimal solution to the problem contains within it optimal solutions to subproblems.

## Activity Selection Problem

Assume that activities are in increasing order of their finishing time. If not, then sort it in  $O(n \lg n)$  time.



### Knapsack Problem

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- A thief robbing a store finds n items.
- The ith item is worth v, dollars and weighs w<sub>i</sub> pounds. The thief wants to take as valuable a load as possible, but he can carry at most W pounds in his knapsack (consider v<sub>i</sub>, w<sub>i</sub>, and W as integer)
  - Which items should he take?

### Fractional knapsack problem: He can take fraction of an items

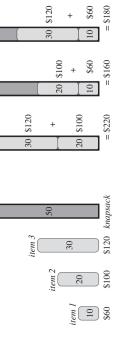
He can either take complete 0-1 knapsack problem:

- Fractional knapsack problem can be solved with greedy
  - 0-1 knapsack problem needs Dynamic Programming

$$V(i, w) = max(V(i-1, w), V(i-1, w-w[i]) + P[i])$$

# 0-1 knapsack problem needs DP

Let knapsack can have 50kg 3 items of wt 10, 20, 30 of price Rs 60, 100 and 120 respectively



\$120

9\$

### Thank You!

Thank you very much for your attention! (Reference¹) Queries?

Lecture-06(Jan 29, 2021) 8/8 | 11 Book - Introduction to Algorithm, By THOMAS H. CORMEN, CHARLES E. LEISERSON, RONALD L. RIVEST, CLIFFORD STEIN

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