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LR(1) Parsers

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Algorithm for CLR (1) Parsing Table



- Construct $C = \{I_0, \dots, I_n\}$ the sets of LR(1) items.
- If $[A \rightarrow \alpha.a\beta, b]$ is in I_i and $\text{goto}(I_i, a) = I_j$ then $\text{action}[i, a] = \text{shift } j$
- If $[A \rightarrow \alpha., a]$ is in I_i then $\text{action}[i, a] = \text{reduce } A \rightarrow \alpha$
- If $[S' \rightarrow S., \$]$ is in I_i then $\text{action}[i, \$] = \text{accept}$
- If $\text{goto}(I_i, A) = I_j$ then $\text{goto}[i, A] = j$ for all non terminals A

More Examples

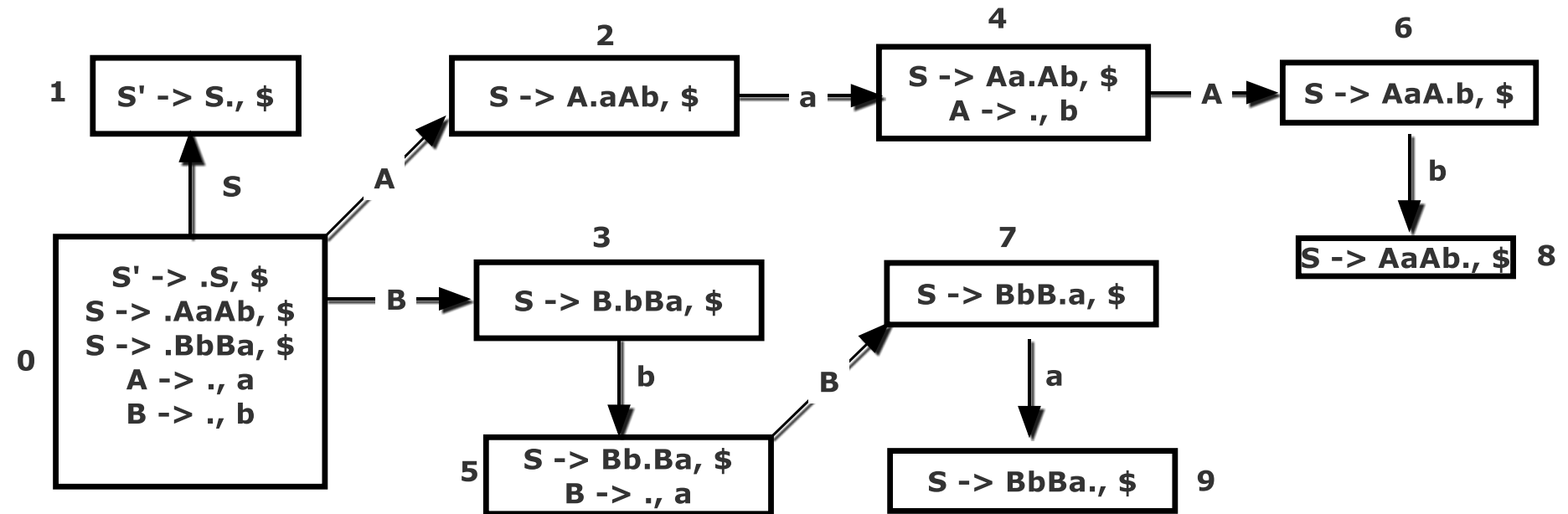
Construct the LR(1) collection of items for the following Grammar and design the CLR(1) parsing table and find out whether this grammar is CLR(1) or not.

$S \rightarrow AaAb \mid BbBa$

$A \rightarrow \epsilon$

$B \rightarrow \epsilon$

GOTO GRAPH



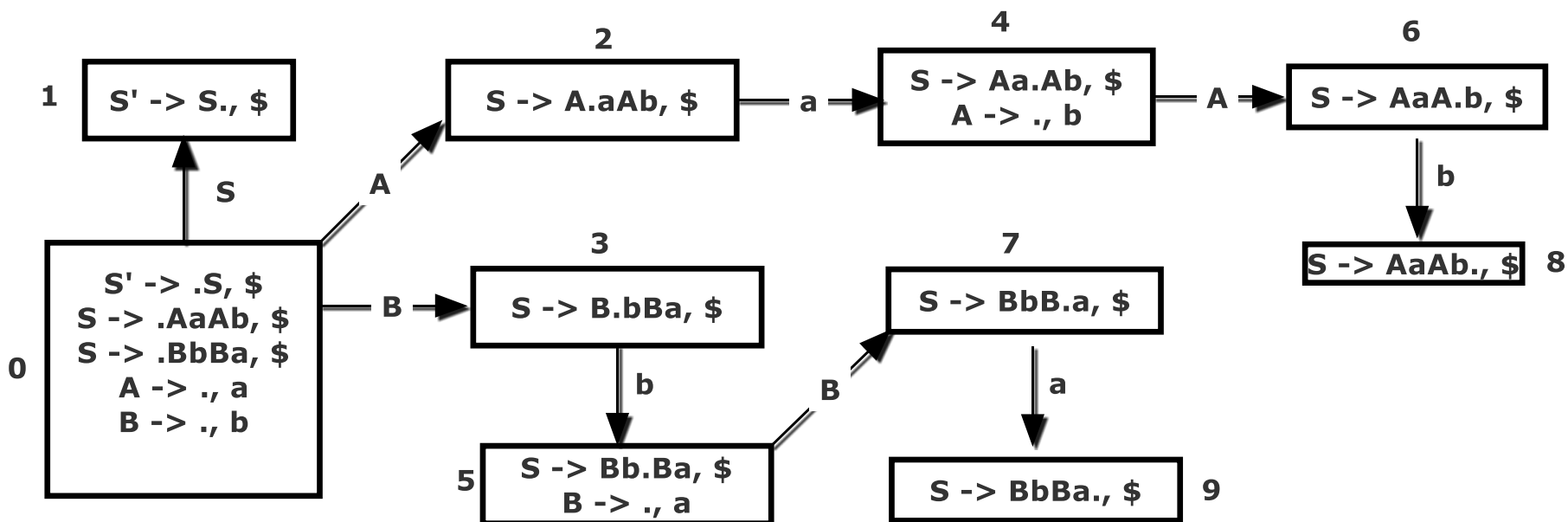
0 $S' \rightarrow S$
 1 $S \rightarrow AaAb$
 2 $S \rightarrow BbBa$
 3 $A \rightarrow \epsilon$
 4 $B \rightarrow \epsilon$

CLR(1) Parsing Table

$0 S' \rightarrow S$
 $1 S \rightarrow AaAb$
 $2 S \rightarrow BbBa$
 $3 A \rightarrow \epsilon$
 $4 B \rightarrow \epsilon$

BLANK CELLS ARE ERROR
ENTRIES

| | ACTION | | | GOTO | | |
|---|--------|----|--------|------|---|---|
| | a | b | \$ | S | A | B |
| 0 | R3 | R4 | | 1 | 2 | 3 |
| 1 | | | ACCEPT | | | |
| 2 | S4 | | | | | |
| 3 | | S5 | | | | |
| 4 | | R3 | | | 6 | |
| 5 | R4 | | | | | 7 |
| 6 | | S8 | | | | |
| 7 | S9 | | | | | |
| 8 | | | R1 | | | |
| 9 | | | R2 | | | |



CLR(1) Parser

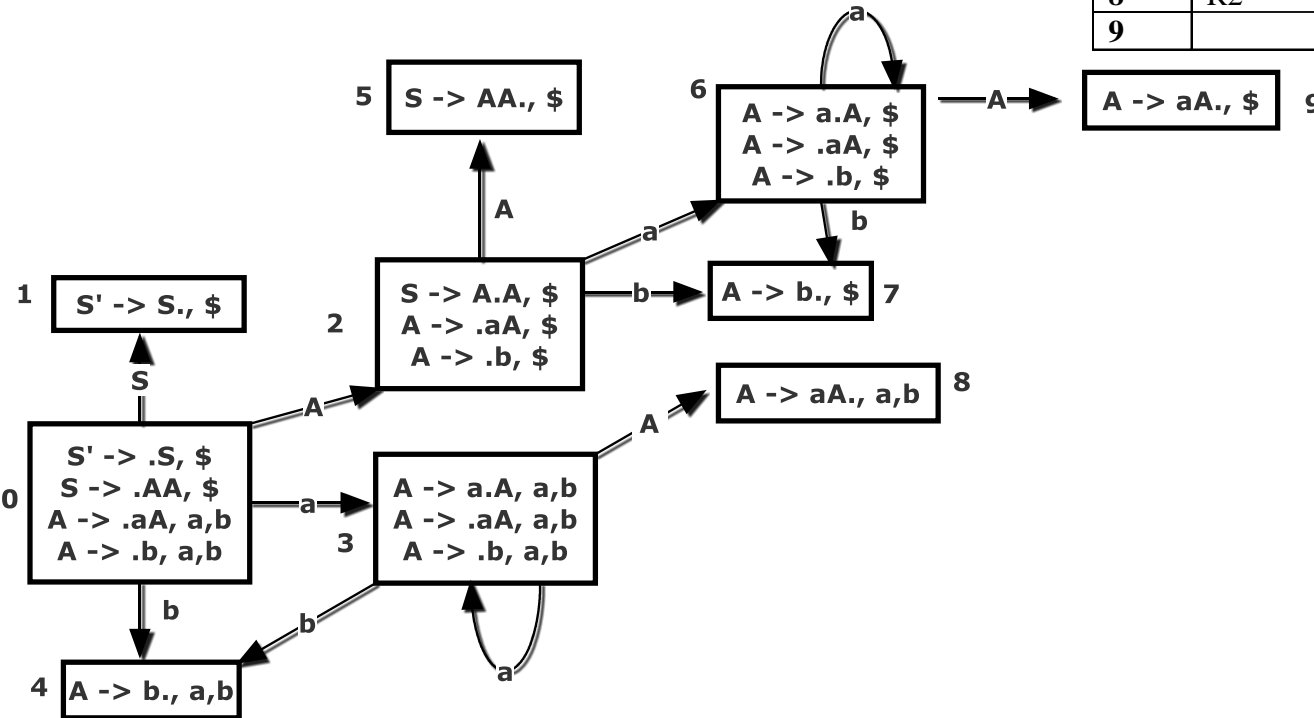
On an error canonical LR parser never makes a wrong shift/reduce move. It immediately declares an error.

Problem: Canonical LR parse table has a large number of states

Revisiting CLR (1) Parsing Table

BLANK CELLS ARE ERROR
ENTRIES

| | ACTION | | | GOTO | |
|---|--------|----|--------|------|---|
| | a | b | \$ | S | A |
| 0 | S3 | S4 | | 1 | 2 |
| 1 | | | accept | | |
| 2 | S6 | S7 | | | 5 |
| 3 | S3 | S4 | | | 8 |
| 4 | R3 | R3 | | | |
| 5 | | | R1 | | |
| 6 | S6 | S7 | | | 9 |
| 7 | | | R3 | | |
| 8 | R2 | R2 | | | |
| 9 | | | R2 | | |



0 S' -> S
1 S -> AA
2 A -> aA
3 A -> b

LookAhead (LALR(1) Parser)

Consider a pair of similar looking states (same core and different lookaheads) in the set of LR(1) items

- $I_4 : A \rightarrow b. , a/b$ $I_7 : A \rightarrow b. , \$$

Replace I_4 and I_7 by a new state I_{47} consisting of ($A \rightarrow b. , a/b/\$$)

- Similarly I_3 & I_6 and I_8 & I_9 form pairs.
- Merge LR(1) items having the same core.

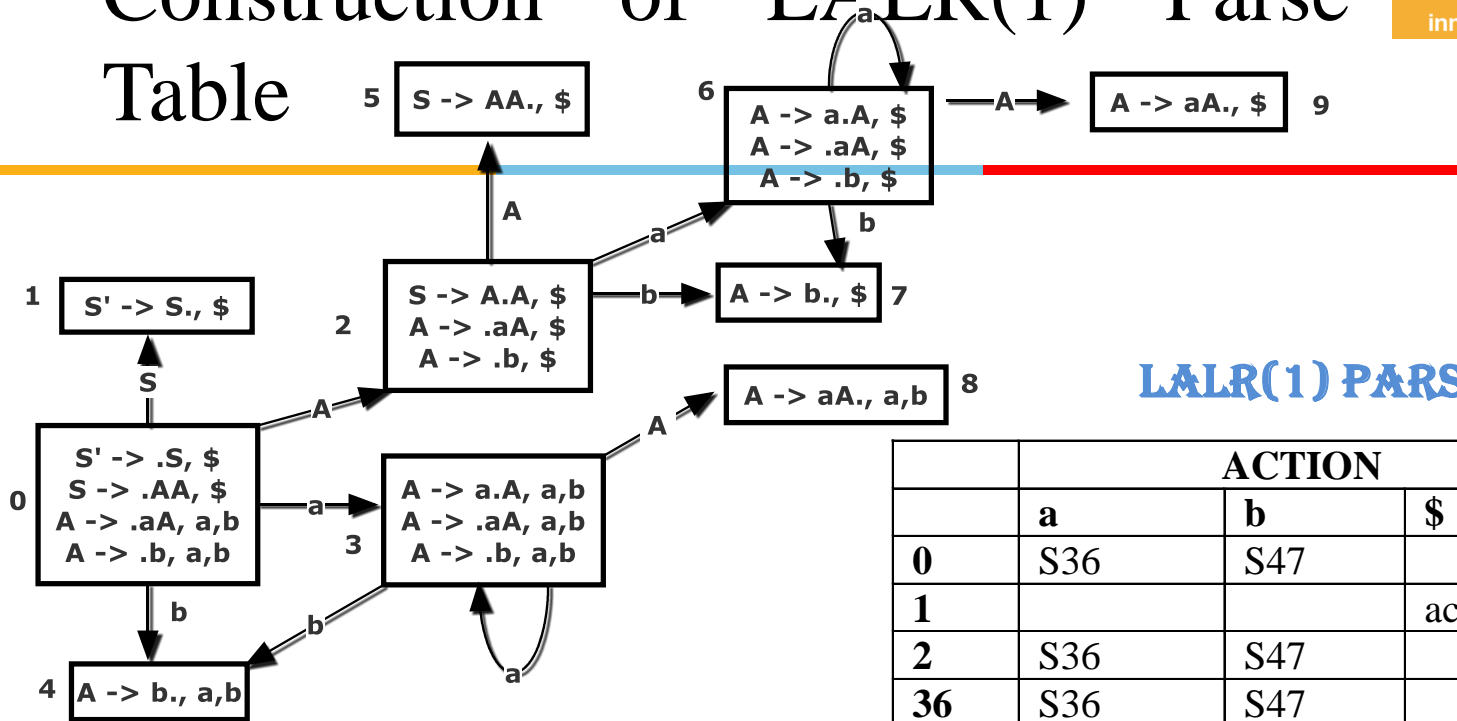
Construction of LALR(1) Parse Table



Construct $C = \{I_0, \dots, I_n\}$ set of LR(1) items

For each LR(0) item present in LR(1) items find all sets having the same LR(0) item and replace these sets by their union.

Construction of LALR(1) Parse Table



LALR(1) PARSE TABLE

| | ACTION | | | GOTO | |
|---|--------|----|--------|------|---|
| | a | b | \$ | S | A |
| 0 | S3 | S4 | | 1 | 2 |
| 1 | | | accept | | |
| 2 | S6 | S7 | | | 5 |
| 3 | S3 | S4 | | | 8 |
| 4 | R3 | R3 | | | |
| 5 | | | R1 | | |
| 6 | S6 | S7 | | | 9 |
| 7 | | | R3 | | |
| 8 | R2 | R2 | | | |
| 9 | | | R2 | | |

| | ACTION | | | GOTO | |
|----|--------|-----|--------|------|----|
| | a | b | \$ | S | A |
| 0 | S36 | S47 | | 1 | 2 |
| 1 | | | accept | | |
| 2 | S36 | S47 | | | 5 |
| 36 | S36 | S47 | | | 89 |
| 47 | R3 | R3 | R3 | | |
| 5 | | | R1 | | |
| 89 | R2 | R2 | R2 | | |

Construction of LALR(1) Parse Table



Let $C' = \{J_0, \dots, J_m\}$ be the resulting set of items.

- Construct action table as was done earlier.

Let $J = I_1 \cup I_2 \dots \cup I_k$ since I_1, I_2, \dots, I_k have same core, $\text{goto}(J, X)$ will have the same core.

- Let $K = \text{goto}(I_1, X) \cup \text{goto}(I_2, X) \dots \text{goto}(I_k, X)$ the $\text{goto}(J, X) = K$

LALR(1) Parse Table

In general core is a set of LR(0) items and LR(1) grammar may produce more than one set of items with the same core.

Merging items in LALR(1) parsing table may produces conflicts.

- SLR and LALR parse tables have same number of states

LALR(1) Parse Table



Merging items may result into conflicts in LALR parsers which did not exist in LR parsers

New conflicts may arise in LALR(1) Parsers.

LALR parser can have new conflicts

- Assume states $\{[X \rightarrow \alpha., a], [Y \rightarrow \beta., b]\}$ and $\{[X \rightarrow \alpha., b], [Y \rightarrow \beta., a]\}$
- Merging the two states produces

$\{[X \rightarrow \alpha., a/b], [Y \rightarrow \beta., a/b]\}$

More Examples

Consider the following Grammar and find out whether it is LALR(1) or not.

$S \rightarrow aEa \mid bEb \mid aFb \mid bFa$

$E \rightarrow e$

$F \rightarrow e$

**GRAMMAR IS NOT LALR(1)
BECAUSE OF CONFLICT IN SOME
OF ITS STATES.**