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Using the following algorithm:

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n = length[p] - 1
for i = 1 to n do
    m[i][i] = 0
for l = 2 to n do
    for i = 1 to n - l + 1 do
        j = i + l - 1
        m[i][j] = ∞
        for k = i to j - 1 do
            q = m[i][k] + m[k+1][j] + p[i] * p[k] * p[j]
            if q < m[i][j] then
                m[i][j] = q
                s[i][j] = k
    
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	1	2	3	4	5	6		1	2	3	4	5	6
1	0	6						1	1				
2		0	24					2		2			
3			0	60				3			3		
4				0	120			4				4	
5					0	210		5					5
6						0							

$l=2$   $j = 1+2-1=2$   
 $i=1$   $m[1,2] = m[1,1] + m[2,2] + p[1] * p[2] * p[3]$   
 $= 6$   $s[1,2] = 1$   
 $i=2, j=3$   $m[2,3] = 24$   $s[2,3] = 2$   
 $i=3, j=4$   $m[3,4] = 60$   $s[3,4] = 3$   
 $i=4, j=5$   $m[4,5] = 120$   $s[4,5] = 4$   
 $i=5, j=6$   $m[5,6] = 210$   $s[5,6] = 5$

$l=3$   
 $i=1, j=3$

$i=2, j=4$   
 $i=3, j=5$

	1	2	3
1	0	6	18
2		0	24
3			0
4			
5			
6			

$l=4$   
 $i=1, j=5$

$i=2, j=6$   
 $i=3, j=6$

	1	2
1	0	6
2		0
3		
4		
5		
6		

$$l=3$$

$$i=1, j=3 \quad m[1,3] = 0 + 24 + 16 = 32$$

$$\downarrow$$

$$m[1,3] = 6 + 0 + 12 = 18$$

$$\therefore m[1,3] = 18, \quad s[1,3] = 2$$

$$i=2, j=4 \quad m[2,4] = 64, \quad s[2,4] = 3$$

$$i=3, j=5 \quad m[3,5] = 150, \quad s[3,5] = 4$$

$$i=4, j=6 \quad m[4,6] = 288, \quad s[4,6] = 5$$

	1	2	3	4	5	6
1	0	6	18			
2		0	24	64		
3			0	60	150	
4				0	120	288
5					0	210
6						0

$$l=4$$

$$i=1, j=4 \quad m[1,4] = 0 + 64 + 16 = 70$$

$$= 6 + 18 + 15 = 39$$

$$= 18 + 0 + 20 = 38$$

$$\therefore m[1,4] = 38, \quad s[1,4] = 3$$

$$i=2, j=5 \quad m[2,5] = 124, \quad s[2,5] = 4$$

$$i=3, j=6 \quad m[3,6] = 270, \quad s[3,6] = 5$$

	1	2	3	4	5	6
1	0	6	18	38		
2		0	24	64	124	
3			0	60	150	270
4				0	120	288
5					0	210
6						0



$$l=5$$

$$i=1, j=5 \quad m[1,5] = 0 + 124 + 12 = 136$$

$$= 6 + 150 + 18 = 174$$

$$= 18 + 120 + 24 = 162$$

$$= 38 + 10 + 30 = 68$$

$$\therefore m[1,5] = 68, \quad s[1,5] = 4$$

$$i=2, j=6 \quad m[2,6] = 208, \quad s[2,6] = 5$$

$$l=6$$

$$i=4, j=6 \quad m[4,6] = 0 + 108 + 2 \times 7$$

$$= 6 + 276 + 14 = 292$$

$$= 18 + 288 + 4 \times 7 = 308$$

$$= 38 + 210 + 5 \times 7 = 355$$

$$= 68 + 0 + 6 \times 7 = 110$$

$$m[1,6] = 110, \quad s[1,6] = 5$$

	1	2	3	4	5	6		1	2	3	4	5	6
1	0	6	18	38	68	110		1		2	3	4	5
2			0	24	64	124	208	2		2	3	4	5
3				0	60	150	274	3			2	4	5
4					0	120	288	4				4	5
5						0	210	5					5
6							0						

$$\text{min cost} = 110$$

Order of parenthesis =

$$((A \times B) \times C) \times D \times E \times F, \quad s[1,6] = 5$$

$$= ((A \times B \times C) \times D) \times E \times F, \quad s[1,5] = 4$$

$$= (((A \times B) \times C) \times D) \times E \times F, \quad s[1,4] = 3$$

$$= (((A \times B) \times C) \times D) \times E \times F, \quad s[1,3] = 2$$