

Chernoff

$$P(X \geq (1+\delta)\mu) \leq \left(\frac{e^\delta}{(1+\delta)^{1+\delta}} \right)^\mu$$

$$\mu = 25, \delta = 1$$

$$P(X \geq 50) \leq \left(\frac{e}{4} \right)^{25}$$

$$\leq 6.395 \times 10^{-5}$$

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Markov: $P(X \geq a) = \frac{E(X)}{a}$

$E(X) = np$ for a binomial distribution
 $= 100 \times \frac{1}{4}$ ($p = \frac{1}{4}$ \therefore there are 4 options)
 $= 25$

$$P(X \geq 50) = \frac{25}{50}$$
$$= \frac{1}{2} //$$

Chebyshev:

$$P(|X - \mu| \geq a) \leq \frac{\text{Var}(X)}{a^2}$$

$$P(|X - \mu| \geq 25) \leq \frac{100 \times \frac{1}{4} \times \frac{3}{4}}{25 \times 25}$$
$$\leq \frac{3}{100}$$

However, this includes $P(X \geq 50)$
and $P(X \leq 0)$

$$\therefore P(X \geq 50) \leq \frac{3}{100} - P(X \leq 0)$$
$$\leq \frac{3}{100} - \left(\frac{2}{4}\right)^{100} //$$