

Practice Problems: Top Down Parsing

Q1. Which of the following grammars are ambiguous?

- a) $\{\{S\}, \{a,b\}, P, S\}$
 $S \rightarrow aSb|ab|\epsilon$
- b) $\{\{S\}, \{a,b\}, P, S\}$
 $S \rightarrow SaSbS|ab$
- c) $\{\{S\}, \{+,-,*,(,),a\}, P, S\}$
 $S \rightarrow S+|S-|S*(S)|a|\epsilon$
- d) $\{\{S\}, \{a\}, P, S\}$
 $S \rightarrow S(S)|a|\epsilon$
- e) $\{\{S\}, \{0,1\}, P, S\}$
 $S \rightarrow 0S1S|1S0S|0|1$
- f) $\{\{S, E, S'\}, \{i,a,t,e,b\}, P, S\}$
 $S \rightarrow iEtSS'|a$
 $S' \rightarrow eS|\epsilon$
 $E \rightarrow b$

Q2. Write unambiguous grammar to the following grammar as per the following associativity and precedence order. The lowest precedence operators appear at the top, and the highest precedence operators appear at the bottom. Operators on the same line have the same associativity and precedence.

Left -associativity: * /
 Right-associativity: + -
 Left -associativity: ()

Grammar $\{\{E\}, \{+,-,*,/,(),\text{num}\}, P, E\}$:

$E \rightarrow E + E | E - E | E * E | E / E | (E) | \text{num}$

Q3. Check whether the following grammar $\{\{E\}, \{+,-,*,/,(),\text{num}\}, P, E\}$ is suitable for the predictive parsing. If it is not, then convert the grammar into suitable grammar and construct the predictive parsing table. (Consider C language operator associativity and precedence order).

$E \rightarrow E + E | E - E | E * E | E / E | (E) | \text{num}$

Q4. Write a procedure for each of the non-terminals of this grammar $\{\{D, F, S, E, A, T\}, \{\text{define, id, }, \{, \}, \text{return, int, float}\}, P, D\}$ using recursive descent parsing and parse the following input: `define int id(int id, float id){ return id(id(),)}`

$D \rightarrow \text{define } T \text{ id } (F) \{S\}$
 $F \rightarrow T \text{ id } , F | \epsilon$
 $S \rightarrow \text{return } E;$
 $E \rightarrow \text{id}(A)$

$A \rightarrow \epsilon \mid E, A$

$T \rightarrow \text{int} \mid \text{float}$

Q5. Write a procedure for each of the non-terminals of this grammar $\{ \{L, S\}, \{ \text{if}, \text{bexpr}, (,), \text{else}, \text{while} \mid \{, \}, \text{stmt}, ; \}, P, L \}$ using recursive descent parsing and parse the following input: $\{ \text{if}(\text{bexpr}) \{ \text{while}(\text{bexpr}) \{ \text{stmt}; \} \} \text{else stmt}; \}$

$L \rightarrow LS \mid S$

$S \rightarrow \text{if}(\text{bexpr}) S \mid \text{if}(\text{bexpr}) S \text{ else } S \mid \text{while}(\text{bexpr}) S \mid \{ L \} \mid \text{stmt};$

Q6. Calculate the first and follow of all non-terminals in the following grammar

1. $\{ \{S, A, B, C\}, \{a, b, g, h\}, P, S \}$.

$S \rightarrow ACBS \mid CbB \mid Ba$

$A \rightarrow daA \mid BC$

$B \rightarrow g \mid \epsilon$

$C \rightarrow h \mid \epsilon$

2. $\{ \{R\}, \{ ', *, (,), a, b, c \}, P, R \}$

$R \rightarrow R' \mid 'R \mid RR \mid R^*(R) \mid a \mid b \mid c$

3. $\{ \{S, E, S', E\}, \{a, e, t, i, b\}, P, S \}$

$S \rightarrow iEtSS' \mid a$

$S' \rightarrow eS \mid \epsilon$

$E \rightarrow b$

4. $\{ \{S, E\}, \{ \text{id}, =, , , ;, \text{if}, (,), \text{while}, \parallel, \&\&, \text{rel}, +, \text{id true}, \text{false} \} \}$

$S \rightarrow \text{id} = E; \mid \text{if} (E) S \mid \text{while} (E) S \mid S S$

$E \rightarrow E \parallel E \mid E \&\& E \mid E \text{ rel } E \mid E + E \mid (E) \mid \text{id} \mid \text{true} \mid \text{false}$

Q7. Eliminate the left recursion and write the first and follow for the following grammars

1. $\{ \{E, T, F\}, \{ +, -, *, /, (,), \text{id} \}, P, E \}$

$E \rightarrow E + T \mid E - T \mid T$

$T \rightarrow T * F \mid T / F \mid F$

$F \rightarrow (E) \mid \text{id}$

2. $\{ \{S, B\}, \{a, b, c, d\}, P, S \}$

$S \rightarrow Baa \mid bc \mid ab$

$B \rightarrow Bc \mid Sda \mid \epsilon$

3. $\{ \{S, A\}, \{a, b, c\}, P, A \}$

$S \rightarrow AA \mid a \mid c$

$A \rightarrow SSc \mid b$

4. $\{ \{S, A\}, \{a, b\}, P, S \}$

$S \rightarrow SAb \mid SA \mid b$

$A \rightarrow a$

Q8. Left factor the following grammars

1. $\{\{E\}, \{i, :, =, e, (,), a,)\}\}$
 $E \rightarrow i := e \mid i(e) \mid a$
2. $\{\{E, T\}, \{+, -, a, id, *\}\}$
 $E \rightarrow T + E \mid T - E \mid T \mid a$
 $T \rightarrow id * T \mid id$
3. $\{\{bexpr, bterm, bfactor\}, \{or, and, not, true, false\}, P, bexpr\}$
 $bexpr \rightarrow bexpr \text{ or } bterm \mid bterm$
 $bterm \rightarrow bterm \text{ and } bfactor \mid bfactor$
 $bfactor \rightarrow not \ bfactor \mid true \mid false$
4. $\{\{S\}, \{a, b, c, d, e\}, P, S\}$
 $S \rightarrow abd \mid ab \mid abcd \mid abcde \mid cd \mid e$

Q9. Do the suitable changes to the below grammar $\{\{S, T\}, \{a, ^, (,), , , \}, P, S\}$ and construct the predictive parsing table.

Obtain the moves for $(a, ^)$

$$S \rightarrow a \mid ^ \mid (T)$$

$$T \rightarrow T, S \mid S$$

Q10. Find whether the following grammar is LL(1) or not

$$S \rightarrow AB \mid PQx$$

$$A \rightarrow xy \mid m$$

$$B \rightarrow bC$$

$$C \rightarrow bC \mid e$$

$$P \rightarrow pP \mid \epsilon$$

$$Q \rightarrow qQ \mid \epsilon$$