

## CFG to PDA

$G = (V, \Sigma, R, S)$ . Corresponding PDA  
 $M = (K, \Sigma, \Gamma, \Delta, s, F)$  where:  
 $K = \{p, q\}$ ,  
 $\Gamma = V \cup \Sigma$ ,  
 $s = p$ ,  
 $F = \{q\}$ , and  $\Delta$  is defined as:

$((p, e, e)(q, S))$   
 $((q, e, A)(q, \alpha)) \forall \text{ rules of the form } A \rightarrow \alpha \text{ in } R$   
 $((q, a, a)(q, e)) \forall a \in \Sigma \rightarrow \text{Pop}$   
 $\rightarrow \text{Top Down parser.}$

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$((p, a, e)(p, a)) \forall a \in \Sigma \rightarrow \text{Push}$   
 $((p, e, \alpha^R)(p, A)) \forall \text{ rules of the form } A \rightarrow \alpha \text{ in } R$   
 $((p, e, S)(q, e))$   
 $\downarrow$   
 $\text{Orthogonal to the previous cons.}$

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$((p, e, e)(q, S)) \rightarrow \text{Start}$   
 $((q, e, A)(q, \alpha)) \forall \text{ rules of the form } A \rightarrow \alpha \text{ in } R$   
 $((q, a, a)(q, e)) \forall a \in \Sigma \rightarrow \text{Pop}$   
 $\rightarrow \text{Top Down parser.}$

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$((p, a, e)(p, a)) \forall a \in \Sigma$   
 $((p, e, \alpha^R)(p, A)) \forall \text{ rules of the form } A \rightarrow \alpha \text{ in } R$   
 $((p, e, S)(q, e))$   
 $\underline{\hspace{1cm}} \text{Non-deterministic}$

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 $s = p$ ,  
 $F = \{q\}$ , and  $\Delta$  is defined as:

$((p, e, e)(q, S)) \rightarrow \text{Shift}$   
 $((q, e, A)(q, \alpha)) \forall \text{ rules of the form } A \rightarrow \alpha \text{ in } R$   
 $((q, a, a)(q, e)) \forall a \in \Sigma \rightarrow \text{Pop}$   
 $\rightarrow \text{Top Down parser.}$

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 $M = (K, \Sigma, \Gamma, \Delta, s, F)$  where:  
 $K = \{p, q\}$ ,  
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$((p, a, e)(p, a)) \forall a \in \Sigma \rightarrow \text{Shift}$   
 $((p, e, \alpha^R)(p, A)) \forall \text{ rules of the form } A \rightarrow \alpha \text{ in } R$   
 $((p, e, S)(q, e))$   
 $\left. \begin{array}{l} \text{Shift} \\ \text{Reduce} \end{array} \right\} \text{Shift Reduce Transitions}$

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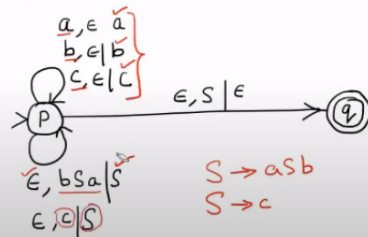
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## Example

$L = \{a^n c b^n \mid n \geq 0\}$

Grammar for L is  $S \rightarrow a S b \mid c$

Corresponding PDA becomes:  $(\{p, q\}, \{a, b, c\}, \{S, a, b, c\}, \Delta, p, \{q\})$ , where  $\Delta$  is given as:



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### Example

Parse the string aacbb using the given parser.

States and transitions:

- ①  $a, \epsilon \mid a$
- ②  $b, \epsilon \mid b$
- ③  $c, \epsilon \mid c$
- ④  $\epsilon, S \mid \epsilon$

Stack operations:

- Shift/Reduce

State	Input String	Stack	Action	Transition used	Rule of G
P	aacbb	--	Shift	①	--
P	cbb	aa	Shift	①	--
P	bb	caa	Shift	③	--
P	bb	Saa	Reduce	⑤	$S \rightarrow c$
P	b	bSaa	Shift	②	--
P	b	Sa	Reduce	④	$S \rightarrow asb$
P	--	bSa	Shift	②	--
P	--	S	Reduce	④	$S \rightarrow asb$

Final stack: S



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Theory of Computation CS F351 (2020-11-01 at 22:29 GMT-8)

### Example

Let  $L = \{1^k 0^i 1^j 0^k \mid i, j, k > 0\}$ .

Following is the CFG for L:

$S \rightarrow 1S0 \mid 1AA0$

$A \rightarrow 0A1 \mid 01$

Convert the above CFG to PDA which is suitable for bottom up parser. Also, make a parsing table for the string  $w = 1100110100$ .

**Sol:** Corresponding PDA is:  $\{(p, q), \{0, 1\}, \{S, A, 0, 1\}, \Delta, p, \{q\}\}$  such that  $\Delta$  is given by the following:

Transition	Transition Number
$(p, 0, \epsilon)(p, 0)$	1
$(p, 1, \epsilon)(p, 1)$	2
$(p, \epsilon, 0S1)(p, S)$	3
$(p, \epsilon, 0AA1)(p, S)$	4
$(p, \epsilon, 1A0)(p, A)$	5
$(p, \epsilon, 10)(p, A)$	6
$(p, \epsilon, S)(q, \epsilon)$	7



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## Example



Let  $L = \{1^k 0^i 1^j 0^k \mid i, j, k \geq 0\}$ . Bottom up parsing table for **1100110100** is as follows:

Transition	Transition Number
$(p, 0, e) (p, 0)$	1
$(p, 1, e) (p, 1)$	2
$(p, e, 0S1) (p, S)$	3
$(p, e, 0AA1) (p, S)$	4
$(p, e, 1A0) (p, A)$	5
$(p, e, 10) (p, A)$	6
$(p, e, S) (q, e)$	7

State	Unread input	Stack	Shift / Reduce	Transition No	Rule of G
p	1100110100	--	--	--	--
P	100110100	1	Shift	②	—
P	00110100	11	Shift	2	—
P	0110100	011	Shift	1	—
P	110100	0011	Shift	1	—
P	10100	10011	Shift	2	—
P	0100	A011	Reduce	6	$A \rightarrow 01$
P	0100	1A011	Shift	2	—
P	0100	A11	Reduce	5	$A \rightarrow 0A1$
P	100	0A11	Shift	—	—
P	00	10A11	Shift	—	—
P	00	AA11	Reduce	—	$A \rightarrow q$
P	0	0AA11	Shift	—	—
P	0	S1	Reduce	④	$S \rightarrow 1AA0$
P	—	0S1	Shift	1	—
P	—	S	Reduce	7	$S \rightarrow 1S0$
q	—	—	—	7	—



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