

The screenshot shows a Beamer presentation slide titled "Virtual Memory". The slide is displayed within a Beamer window, which includes a sidebar on the left with a table of contents showing three slides: "Virtual Memory", "Background", and "Demand Paging". The main content area of the slide is currently blank, with the title "Virtual Memory" centered in a large green font. The Beamer window has a standard menu bar at the top and a status bar at the bottom.



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2:38 / 57:25

Background

- **Virtual memory –**
 - Only part of the program needs to be in memory for execution.
 - Logical address space can therefore be much larger than physical address space.
 - Allows address spaces to be shared by several processes.
 - Allows for more efficient process creation.
- Virtual memory can be implemented via:
 - Demand paging
 - Demand segmentation



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3:15 / 57:25

Demand Paging

- Bring a page into memory only when it is needed.
 - Less I/O needed
 - Less memory needed
 - Faster response
 - More users
- Page is needed \Rightarrow reference to it
 - invalid reference \Rightarrow abort
 - not-in-memory \Rightarrow bring to memory

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5:23 / 57:25

Valid-Invalid Bit

- With each page table entry a valid-invalid bit is associated
(1 \Rightarrow in-memory, 0 \Rightarrow not-in-memory)
- Initially valid-invalid bit is set to 0 on all entries.
- Example of a page table snapshot.

Frame #	valid-invalid bit
	1
	1
	1
	1
	0
⋮	
	0
	0

page table

- During address translation, if valid-invalid bit in page table entry is 0 \Rightarrow page fault.

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10:12 / 57:25

Page Fault

- If there is ever a reference to a page, first reference will trap to OS \Rightarrow page fault
- OS looks at another table to decide:
 - \rightarrow Invalid reference \Rightarrow abort.
 - \rightarrow Just not in memory.
- Get empty frame.
- Swap page into frame.
- Reset tables, validation bit = 1.
- Restart instruction:

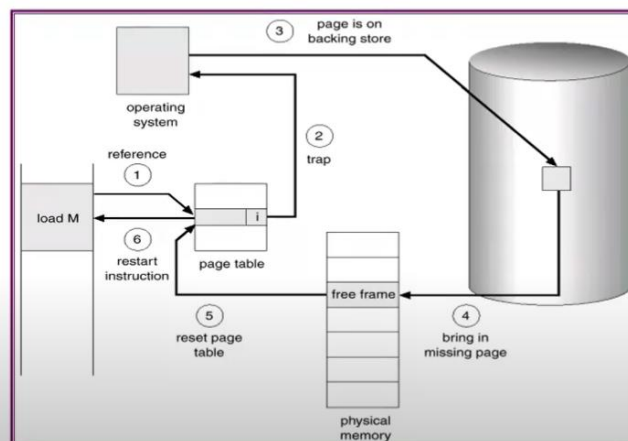
J

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11:59 / 57:25



Steps in Handling a Page Fault



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15:57 / 57:25



What happens if there is no free frame?

- Page replacement – find some page in memory, but not really in use, swap it out.
 - algorithm
 - performance – want an algorithm which will result in minimum number of page faults.
- Same page may be brought into memory several times.



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20:49 / 57:25

Performance of Demand Paging

- Page Fault Rate $0 \leq p \leq 1.0$
 - if $p = 0$ no page faults
 - if $p = 1$, every reference is a fault
- Effective Access Time (EAT)
$$\text{EAT} = (1 - p) \times \text{memory access} + p (\text{page fault overhead})$$

[swap page out + swap page in + restart overhead]



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24:35 / 57:25

Demand Paging Example

- Memory access time = 1 microsecond
- 50% of the time the page that is being replaced has been modified and therefore needs to be swapped out.
- Swap Page Time = 10 msec = 10,000 microsec
$$EAT = (1 - p) \times 1 + p (10000)$$
$$1 + 10000p$$



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27:13 / 57:25



Page Replacement

- Page-fault service routine includes page replacement.
- Use *modify (dirty) bit* to reduce overhead of page transfers – only modified pages are written to disk.
- Page replacement completes separation between logical memory and physical memory
 - large virtual memory can be provided on a smaller physical memory.



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Replacement Policy

- Which page to replaced?
- Page removed should be the page least likely to be referenced in the near future
- Most policies predict the future behavior on the basis of past behavior

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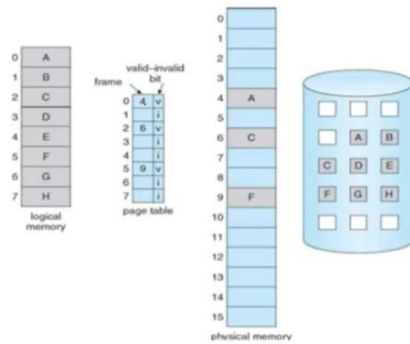
Replacement Policy

- Frame Locking
 - If frame is locked, it may not be replaced
 - Kernel of the operating system
 - Key control structures
 - I/O buffers
 - Associate a lock bit with each frame

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Page table when some pages are not in memory



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What is Page fault ?

- When the data (page) requested by program is not present in main memory , it is known as page fault
- Why page replacement required ?
 - ☞ System may not have enough RAM to store all required data

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Page Replacement Algorithms

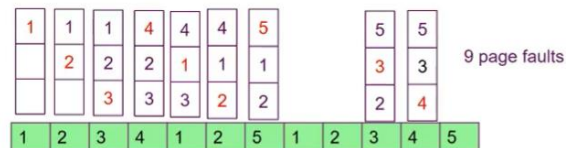
- Want lowest page-fault rate.
- Evaluate algorithm by running it on a particular string of memory references (reference string) and computing the number of page faults on that string.
- In all our examples, the reference string is
1, 2, 3, 4, 1, 2, 5, 1, 2, 3, 4, 5.

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First-In-First-Out (FIFO) Algorithm

- Reference string: 1, 2, 3, 4, 1, 2, 5, 1, 2, 3, 4, 5
- 3 frames (3 pages can be in memory at a time per process)



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First-In-First-Out (FIFO) Algorithm

- Reference string: 1, 2, 3, 4, 1, 2, 5, 1, 2, 3, 4, 5
- 4 frames (4 pages can be in memory at a time)
- In general more frames \Rightarrow less page faults
- FIFO Replacement – Belady's Anomaly

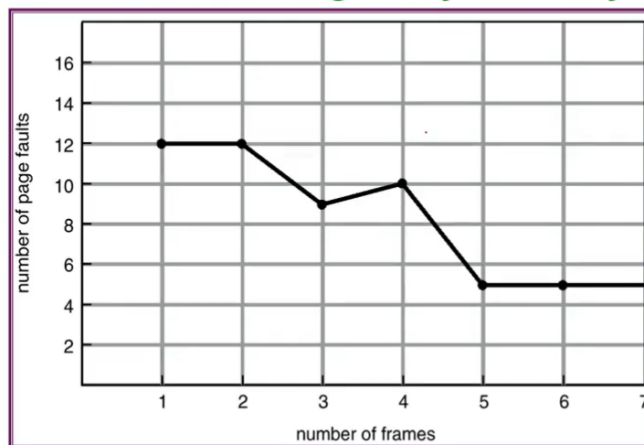
10 page faults

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FIFO Illustrating Belady's Anomaly



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Minimize # of PFs when # frames \geq # of unique pages

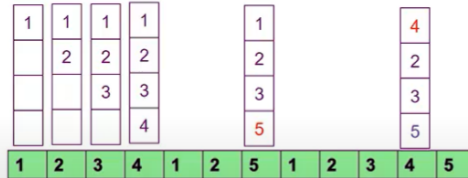
Operating systems (2020-11-23 at 21:28 GMT-8)

Optimal Algorithm

- Replace page that will not be used for longest period of time.

- 4 frames example

1, 2, 3, 4, 1, 2, 5, 1, 2, 3, 4, 5



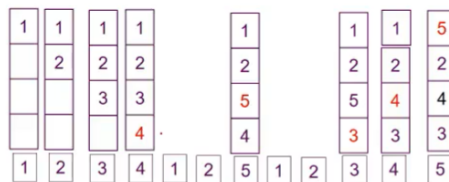
6 page faults

- Used for measuring how well algorithm performs.

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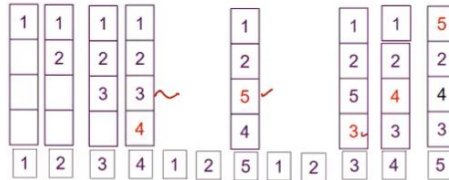
Least Recently Used (LRU) Algorithm

- Reference string: 1, 2, 3, 4, 1, 2, 5, 1, 2, 3, 4, 5



Least Recently Used (LRU) Algorithm

■ Reference string: 1, 2, 3, 4, 1, 2, 5, 1, 2, 3, 4, 5



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LRU Implementation

■ Counter implementation

- Every page entry has a counter; every time page is referenced through this entry, copy the clock into the counter.
- When a page needs to be replaced, look at the counters to determine which page to replace.

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LRU Algorithm (Cont.)

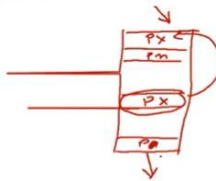
- Stack implementation
 - keep a stack of page numbers in a double link form:
 - whenever Page is referenced:
 - move it to the top
 - No search for replacement

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LRU Algorithm (Cont.)

- Stack implementation
 - keep a stack of page numbers in a double link form:
 - whenever Page is referenced:
 - move it to the top
 - No search for replacement



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LRU Approximation Algorithms

■ Reference bit

- With each page associate a bit, initially = 0
- When page is referenced bit set to 1.
- Replace the one which is 0 (if one exists). We do not know the order, however.

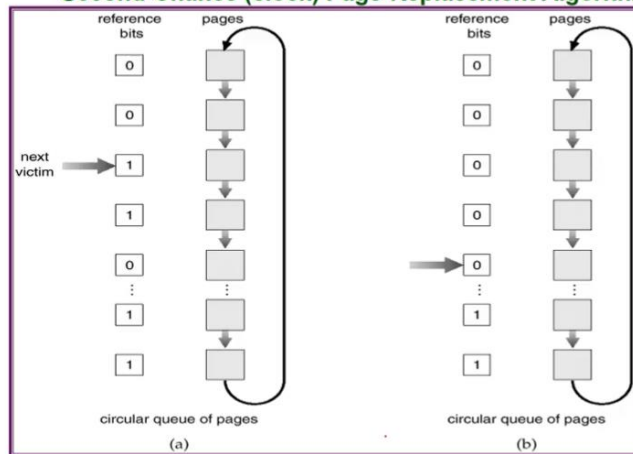
■ Second chance

- Need reference bit.
- If page to be replaced (in clock wise order) has reference bit = 1, then:
 - set reference bit 0.
 - leave page in memory.
 - replace next page (in clock wise order), subject to same rules.

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Second-Chance (clock) Page-Replacement Algorithm



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Enhanced Clock Policy

- In addition to reference bit use modify bit also
 - ☞ (0,0) not referenced not modified
 - ☞ (0, 1) Not recently used but modified
 - ☞ (1,0) recently used but not modified
 - ☞ (1,1) recently used and modified

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Comparison

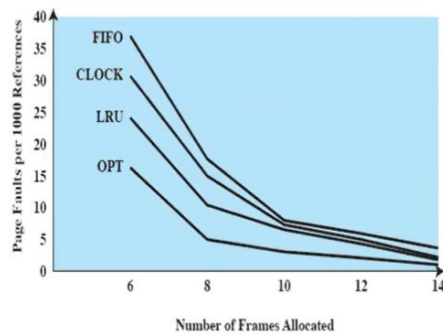


Figure 8.17 Comparison of Fixed-Allocation, Local Page Replacement Algorithms

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Counting Algorithms

- Keep a counter of the number of references that have been made to each page.
- LFU Algorithm: replaces page with smallest count.
- MFU Algorithm: based on the argument that the page with the smallest count was probably just brought in and has yet to be used.



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Allocation of Frames

- Each process needs **minimum** number of pages.
- Example:
 - MOV source, destination
 - instruction is 4 bytes, might span 2 pages.
 - 2 pages to handle **from**.
 - 2 pages to handle **to**.
- Two major allocation schemes.
 - fixed allocation
 - priority allocation



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Fixed Allocation

- Equal allocation – e.g., if 100 frames and 5 processes, give each 20 pages.
- Proportional allocation – Allocate according to the size of process.

s_i = size of process p_i

$S = \sum s_i$

m = total number of frames

a_i = allocation for $p_i = \frac{s_i}{S} \times m$

$$m = 64$$

$$s_1 = 10$$

$$s_2 = 127$$

$$a_1 = \frac{10}{137} \times 64 \approx 5$$

$$a_2 = \frac{127}{137} \times 64 \approx 59$$

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OS lect (2020-11-25 at 03:28 GMT-8)

Priority Allocation

- Use a proportional allocation scheme using priorities rather than size.
- If process P_i generates a page fault,
 - select for replacement one of its frames.
 - select for replacement a frame from a process with lower priority number.

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Global vs. Local Allocation

- **Global** replacement – process selects a replacement frame from the set of all frames; one process can take a frame from another.
 - Process cannot control its own Page fault rate
- **Local** replacement – each process selects from only its own set of allocated frames.
 - Number of frames allocated to a process do not change
 - Does not make use of less used pages belonging to other processes



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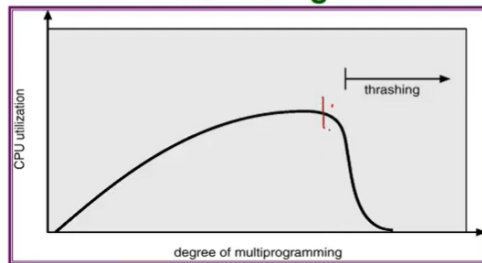
Thrashing

- If a process does not have “enough” pages, the page-fault rate is very high. This leads to:
 - low CPU utilization.
 - operating system thinks that it needs to increase the degree of multiprogramming.
 - another process added to the system.
- **Thrashing** ≡ a process is busy swapping pages in and out.
 - More pronounced for Global page replacement policy



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Thrashing



- Why does paging work?
 - Locality model
 - Process migrates from one locality to another.
 - Localities may overlap.
- Why does thrashing occur?
 - Σ size of locality > total memory size

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Working-Set Model

- Δ \equiv working-set window \equiv a fixed number of page references
 - Example: 10,000 instruction
- WSS_i (working set of Process P_i) = total number of pages referenced in the most recent Δ (varies in time)
 - if Δ too small will not encompass entire locality.
 - if Δ too large will encompass several localities.
 - if $\Delta = \infty \Rightarrow$ will encompass entire program.
- $D = \Sigma WSS_i \equiv$ total demand frames
- if $D > m$ (Total number of available frames) \Rightarrow Thrashing
- Policy if $D > m$, then suspend one of the processes.

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