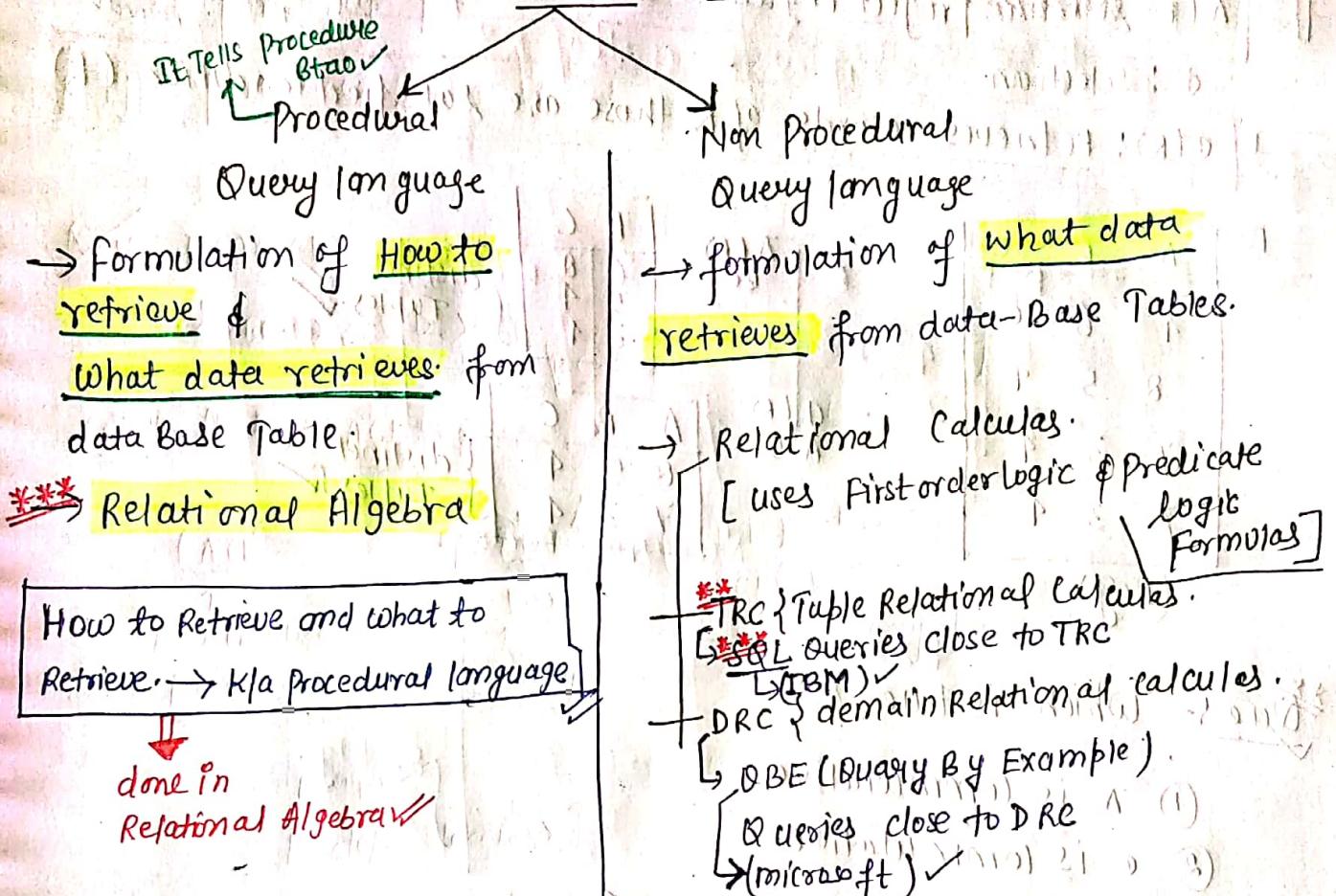


Lecture - 7 :-

Queries (4 marks)



Relational Algebra :-

Basic Operators

unary operator

binary operator

unary operator

- ① Projection (π)
- ② Selection (σ)
- ③ Cross product (\times)
- ④ Union (U)
- ⑤ Set difference (-)
- ⑥ Rename (δ)

7

Derived operators

- ① Join (\bowtie) $\rightarrow \{ \times, \sigma, \pi \}$
- ② Intersection (\cap) $\rightarrow \{ - \}$
- ③ division ($/$ or $\frac{\sigma}{\pi}$) $\rightarrow \{ \times, \pi, - \}$

π : Projection

$\pi(R)$: selection Project required attributes from R

→ Also select
distinct tuple
or record ✓

σ : Selection.

$\sigma(R)$: Retrieves records of R those are satisfied condition (R)

R	A	B	C
4	6	8	
8	5	4	
7	3	4	
7	3	4	

$\pi(R)$	B	C
π_{BC}	6	8
	5	4
	-3	4

$\sigma(R)$	A	B	C
$\sigma_{A>5}$	8	5	4
	7	3	4

(Bag)

distinct
Tuples ✓

distinct
Tuples ✓

Ques- Which is true?

- ① π is commutative
- ② σ is commutative
- (a) (i), (b) (ii), (c) i & ii (d) None ✓

$$\text{So } ① \pi_{U_{A,B}}(\pi_{i,i+1}(R)) = \pi_{i,i+1}(\pi_{U_{A,B}}(R))$$

$$\boxed{\pi_{AB}(\pi_{ABC}(R)) \neq \pi_{ABC}(\pi_{AB}(R))}$$

Ex1) $\pi_{AB}(\pi_{ABC}) \neq \pi_{ABC}(\pi_{AB})$

Ex2) $\sigma_{xy}(\sigma_{yz}) = \sigma_{yz}(\sigma_{xy})$

Not commutative

$$② \sigma_{C_2}(\sigma_{C_1}(R)) = \sigma_{C_1}(\sigma_{C_2}(R)) = \sigma(R)$$

↑
Stream = CS ↑
Stream = CS ↑
Centre = Delhi Centre = Delhi

* σ is commutative while π is Not holding commutative property.

Cross Product :-

$R \times S$:- All attributes of R followed by all attributes of S .
 & Each record of R pairs with Every record of S .

R	A	B	C
	4	2	5
	6	5	8
	3	4	5

S	C	D
	5	7
	7	8

Find $R \times S$

A	B	C	C	D.
4	2	5	5	7
4	2	5	7	8
6	5	8	5	7
6	5	8	7	8
3	4	5	5	7
3	4	5	7	8

If ① 1st table have x No. of attributes;

② 2nd table have y No. of attributes;

Then $I \times II$ have $(x+y)$ attributes.

If ② - ① Ist Relⁿ have m distinct Tuples

②. IInd Relⁿ have n distinct Tuples

Then $I \times II$ have $(m * n)$ o Tuples

Ques: Relation R with "n" distinct tuples, Relation S with "0" tuples.

Then how many tuples in result of $R \times S$:

Ans

'0' zero

Eg

A	B
4	2
7	2

B	C

} 0 tuples.

No pairing occurs

$R \times S$

A	B	B	C

} empty.

So, $R \times S$ result empty record set if either R or S rel with 0 tuples.

JOINS! - (Various joins are there)

- ↗ Natural Join
- ↗ Conditional Join
- ↗ Left Outer Join
- ↗ Right Outer Join
- ↗ Full Outer Join.

① Natural Join (\bowtie)

$$R \bowtie S = \pi(\sigma_{\text{equality b/w common attributes of } R \& S}(R \times S))$$

distinct attributes

Example:-

R	A	B	C
4	2	5	
6	5	8	
3	4	5	

S	C	D
5	7	
7	9	

**

$M \rightarrow (X, \sigma, \pi)$

**

$N \rightarrow (X, \pi, -)$

$$R \bowtie S = \pi_{ABCD} (\sigma_{R.C=S.C} (R \times S))$$

(1)

A	B	C	C	D
4	2	5	5	7
4	2	5	7	8
6	5	8	5	7
6	5	8	7	8
3	4	5	5	7
3	4	5	7	5

(2)

A	B	C	C	D
4	2	5	5	7
3	4	5	5	7

(3)

A	B	C	D
4	2	5	7
3	4	5	7

Example

(2) If $R(ABC)$, $S(BGDE)$

if $R(AB)$, $S(CD)$

$R \bowtie S = ??$

Sol: If No common attributes.

then

$$R \bowtie S = R \times S$$

→ when No common attribute are their.

$$\pi_{ABCDE} (\sigma_{R.B=S.B} (\sigma_{R.C=S.C} (R \times S)))$$

Conditional Join :- (Mc)

$$R \bowtie_C S = \pi(\sigma_C(R \times S))$$

* Example

R	A	B	C
4	2	5	
6	5	8	
3	4	5	

S	C	D
5	7	
7	8	

find $R \bowtie_C S$

$R.C > S.C$

Not merging

Solⁿ

A	B	C	D
6	5	8	5 7
6	5	8	7 8

$$R \bowtie_C S$$

$R.C > S.C$

Outer Joins :-

① left outer join (\bowtie) Natural Join

$$(R \bowtie S) = (R \bowtie S) \cup$$

records of R those are failed
join condition with Null
condition in remaining attr

Ex for above R & S Table

$$R \bowtie S \Rightarrow$$

A	B	C	D
4	2	5	7
3	4	5	8
6	5	8	Null

Extra attached due to Left outer join

② Right Outer Join

$$R \times^R S = (R \bowtie S) \cup \text{records of } S \text{ those are failed join condition with null cond in remaining attributes}$$

from Previous Table :-

$R \times^R S =$	A	B	C	D
	4	2	5	7
	3	4	5	7
	N	N	7	8

③ Full Outer Join :- (Left Outer Join \cup Right Outer Join)

$$R \times^F S = (R \bowtie S) \cup (R \times^R S)$$

from Previous Table :-

$R \times^F S =$	A	B	C	D
	4	2	5	7
	3	4	5	7
	6	5	8	Null
	Null	Null	7	8

Ex from previous R & S Tables

$$R \times^F S \\ R.C > S.C$$

A	B	C	D
6	5	8	5
6	5	8	7
4	2	5	Null
3	4	5	Null

Join Queries :-



RCA), SC(B)

Retrieve "A" Values of R, those are more than some "B" Value of S.

(any/at least one)

Soln

R	A	S	B
X	10		15
	20		25
	30		30
	40		

$\pi_A(R \times S) \rightarrow$

$R.A$

$B.B$

$\pi_A(R \bowtie S) \rightarrow$

$R.A$

$S.B$

A	B
20	15
30	15
30	25
40	15
40	25
40	30

~~Learn~~

For at least one / some / any /

use $R \bowtie S$

$R \bowtie_C S$

$\sigma_C(R \times S)$

Rename :- (f) used to rename table names (or) attribute names

To avoid ambiguity we go for Renaming.

Ex	$\pi(\sigma(stud \times stud)) \rightarrow$	sid age sid age
	stud.sid stud.age stud.age stud.age	

Ambiguity so Renaming use here

f(temp, stud)

One student Table rename as Temp

I	N	A

attribute rename

f(stud) \rightarrow I, N, A

Temp	sid	sname	age

(88)

$f(\text{stud}) \Rightarrow$

stud.

I	Sname	A

Renaming { Instance } Sid → I
Some attribute age → A
Renaming

Our Emp (eid sal gen)

Retrieve female emp id's whose salary more than

Salary of some male employee.

$\text{Teid} \left(\sigma_{\text{sal} > s} \left(\sigma_{\text{EMP}} \text{ gen=female} \right) \text{ IX } f: \left(\sigma_{\text{gender}}^{\text{male}} \right) \right)$
 or
 $\text{Teid} \left(\sigma_{\text{EMP}} \text{ gen=female} \text{ sal} > s \text{ IX } f: \left(\sigma_{\text{gen}}^{\text{male}} \right) \right)$

Ques Emp (eid sal dNo)

Retrieve eid whose salary more than salary of some department "5" employee.

Sol"

$\exists eid \left(\text{Emp} \bowtie_{\text{Sal} > s}^{\exists} \text{I, S, D} \left(\begin{array}{l} \vdash (\text{Emp}) \\ dNo = 5 \end{array} \right) \right)$

Conditional Join going for :-

(\exists) \Rightarrow Some / any / at least one.

Ques :- stud (sid, age) Dept (did, age)

Retrieve sid's whose age is more than age of some department

Sol"

$\exists sid \left(\text{stud} \bowtie_{\text{age} > \text{Dept. age}} \text{Dept} \right)$

(lecture - 8)

for ① $R(A) \times S(B)$

Some.

$R(A)$ $S(B)$

Retrieve 'A' value's of R those are more than some B

Value of S.

$$\hookrightarrow \pi_A(R(A) \times S(B))$$

$R > S_B$

~~for ②~~

$R(A) \times S(B)$

Retrieve A values of R those are more than every B value

of S.

soln

$R(A) = \{ \text{value of } A \text{ which is less than every value of } B \}$

$$\Rightarrow R(A) = \{ \pi_A(R(A) \times R(B)) \}$$

R.A.
R.B

• [All values of A] - [A ≤ some B] ✓

Example

for $R(A)$

A
10
20
30
40

$S(B)$

B
15
25
30

A
10
20
30
40

10
20
30

$$= (40) \text{ Ans} \quad \checkmark$$

~~V.Imp~~

Emp (eid dno sal)

Retrieve eid's whose salary are more than every emp salary of dept 5.

Solⁿ

Emp (eid dno sal) Emp (eid dno sal)

Choose dept 5 employee

$\sigma_{dept=5} [Emp]$

(All Employees) - $\neg (sal > \text{every sal of dept } 5)$

(All employees) - (eid sal \leq Some salary of dept 5)

$\pi_{eid} (emp) - \pi_{eid} \left(emp \underset{\substack{sal \leq s \\ I, D, S}}{\bowtie} f(\sigma_{dept=5} [emp]) \right)$

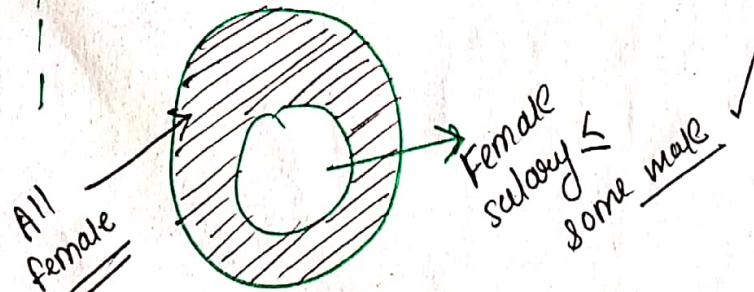
~~V.Imp~~

Emp (eid, sal, gender)

Retrieve eid's of female employee's whose salary is more than every salary of male employees.

Solⁿ - $\pi_{eid} (\sigma_{g=f} [emp]) - \pi_{eid} \left(\sigma_{g=f} [emp] \underset{\substack{sal \leq s \\ I, S, G}}{\bowtie} f(\sigma_{g=m} [emp]) \right)$

(All female eid) - (female emp sal \leq Some sal of male employee)



Ques $\text{Emp}(eid, sal)$

Retrieve eid 's whose gets maximum salary

Soln $\left\{ \begin{array}{l} eid's \text{ whose salary} \\ \text{maximum} \end{array} \right\}$

$$\left\{ \begin{array}{l} eid's \text{ whose salary} \\ \geq \text{every salary of emps} \end{array} \right\} = \left\{ \begin{array}{l} \text{all} \\ eid's \text{ of} \\ \text{emp} \end{array} \right\} - \left\{ \begin{array}{l} eid's \text{ whose} \\ \text{salary < some} \\ \text{salary of emps} \end{array} \right\}$$

$$= \pi_{eid}(\text{emp}) - \pi_{eid}(\text{Emp} \setminus f_{I,s}(\text{Emp}))$$

$\cdot A \geq \text{every } B \equiv \{ \text{All } A \} - \{ A < \text{some } B \}$

$\cdot A \geq \text{every } B \equiv \{ \text{All } A \} - \{ A < \text{some } B \}$

$\cdot R(A) \vdash \neg \exists A$

max value of A

~~A value~~ $\geq \text{every } A \equiv$

$\{ \text{All } A \text{ values} \} - \{ A < \text{some } B \}$

example:-

Emp		
	eid	sal
✓	e1	40
✗	e2	80
✓	e3	60
✓	e4	40
✗	e5	80

Emp	
I	S
e1	40
e2	80
e3	60
e4	40
e5	80

All eid

↓
e1
e2
e3
e4
e5

eid

e1
e3
e4

$$= (e2, e5) \checkmark$$

Ques $\exists \text{Emp}(\text{eid}, \text{sal})$

eid's whose gets min salary.

Sol

$\{ \text{eid}'s \text{ whose salary} \}$.

$\{ \text{every emp salary} \}$.

$\{ \text{min salary} \}$

$\{ \text{min salary} \}$

$\{ \text{All emp's} \} - \{ \text{eid}'s \text{ whose salary} > \}$.

of emp

$\{ \text{some emp salary} \}$.

$$\Rightarrow \pi_{\text{eid}}(\text{Emp}) - \pi_{\text{eid}}(\text{Emp} \setminus \underset{\text{sal} > \text{min}}{\text{f}_{I,S}(\text{Emp})})$$

Ques $\exists \text{Emp}(\text{eid}, \text{sal}, \text{dno})$

Eid's who gets maximum salary for each department.

Sol

$\{ \text{eid}'s \text{ whose} \}$ = $\{ \text{all} \}$ - $\{ \text{eid}'s \text{ whose sal.} \}$

$\{ \text{sal} > \text{every emp} \}$

$\{ \text{Emp id's} \}$

$\{ \text{eid}'s \text{ whose sal.} \}$

$\{ \text{some emp of same} \}$

dept

$$\Rightarrow \pi_{\text{eid}}(\text{emp}) - \pi_{\text{eid}}(\text{Emp} \setminus \underset{\substack{\text{sal} > \text{max} \\ \wedge \\ \text{Dno} = D}}{\text{f}_{I,S,D}(\text{Emp})})$$

One family (Parent child child dob)

Parent	child	child dob
A	B	1995
A	C	1998
A	D	1996
E	F	1990
E	G	1996

Retrieve youngest child of each parent

$$\text{Sol}^M \left\{ \pi_{\text{child}}^{(\text{family})} \left(\pi_{\text{child}}^{(\text{family})} \bowtie_{\substack{\text{child dob} \\ \leq \text{cd}}} \pi_{\substack{P, \text{cd}}}^{(\text{family})} \right) \right\}$$

parent = P

→ { Retrieve child whose DOB > Every child DOB of same parent } \equiv { all child } - { child whose DOB < some child DOB of same parent }

Division (/ or \div)

Enroll (sid, cid)
S1 C1
S1 C2
S1 C3
S2 C1
S2 C2
S3 C1

Course (cid)
C1
C2
C3

all courses

uses in division

{ Retrieve sid's Enrolled every course of course relation. }

π_{Enroll}		π_{course}		\equiv	Result
sid	cid	cid			sid s1
s1	c1	c1			
s2	c2	c2			
s1	c3	c3			
x { s2 } c1					
x { s3 } c1					

Expansion of Division (/)

$$\left\{ \begin{array}{l} \pi(E) / \pi_{\text{cid}}(C) \\ \text{sid} \end{array} \right\} \rightarrow \left\{ \begin{array}{l} \text{sid's enrolled} \\ \text{Every course} \end{array} \right\}$$

These steps are very much important please concentrate on this your division operator problem will be finished within one minute

a) sid's not enrolled for Every course

[sid's enrolled proper subset of all courses]

$$\pi_{\text{sid}} (\pi_{\text{sid}}(E) \times \pi_{\text{cid}}(C) - \pi_{\text{sidcid}}(E))$$

sid		cid
s1	X	c1
s2		c2
s3		c3

All Possible pair b/w sid's of enroll rel & all courses.

sid	cid
s1	c1
s1	c2
s1	c3
s2	c1
s2	c2
s2	c3
s3	c1
s3	c2
s3	c3

sid	cid
s1	c1
s1	c2
s1	c3
s2	c1
s2	c2
s2	c3
s3	c1
s3	c2
s3	c3

sid	cid
s2	c3
s3	c2
s3	c3

sid
s2
s3

std
Not enrolled
course

Division can Express :-

Using $\pi, \times, -$ basic operation

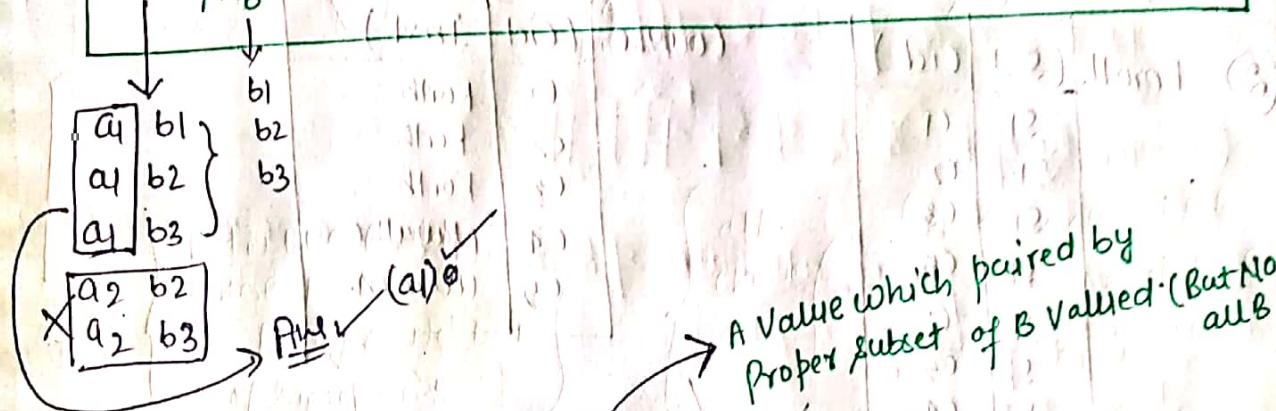
(1) (2) (3)

(b) $\{ \text{sid's enrolled} \}_{\text{Every courses}} = \{ \text{sid enrolled some courses} \} - \{ \text{sid not enrolled for every course} \}$

$$\pi_{\text{sid}(\text{cid})}^{(F)} / \pi_{\text{cid}(c)} = \pi_{\text{sid}}^{(F)} - \pi_{\text{sid}} (\pi_{\text{sid}}^{(E)} \times \pi_{\text{cid}(c)} - \pi_{\text{sid}(\text{cid})}^{(E)})$$

$\xrightarrow{\text{finally}}$

$\pi_{AB}^{(R)} / \pi_B^{(S)} \Rightarrow$ it gives A Value which Pairs with Every value of B.



$$\pi_{AB(R)} / \pi_{B(S)} = \pi_{(R)} - \pi_A (\pi_{A(R)} \times \pi_{B(S)} - \pi_{AB})$$

$\checkmark \begin{cases} a_1 b_1 \\ a_1 b_2 \\ a_1 b_3 \\ \otimes \{ a_2 b_2 \\ a_2 b_3 \} \end{cases}$

$\xrightarrow{\text{all } (AB) \text{ value}}$

$\xrightarrow{\text{No Paired with CD gives from R to S - Actual Rel}}$

$\xrightarrow{\text{Total Relation}}$

$\xrightarrow{\text{After doing } "-", \text{ we get those NOT enrolled}}$

$\xrightarrow{\text{For given Pair all correctly Think}}$

$$\pi_{ABCD}^{(R)} / \pi_{CD}^{(S)} = \left\{ \pi_{(R)} - \pi_{AB} (\pi_{AB} \times \pi_{CD} - \pi_{ABC}^{(R)}) \right\}$$

$\checkmark \begin{cases} a_1 b_1 c_1 d_1 \\ a_1 b_1 c_1 d_2 \\ a_1 b_1 c_2 d_1 \\ \otimes \{ a_2 b_2 c_1 d_2 \} \end{cases}$

A	B
a ₁	b ₁

~~V.1.1~~ ~~Ques~~ Enroll(sid, cid) Course(cid, Inst)

- ① Retrieve sid's who enrolled for some course taught by KORTH.
- ② Retrieve sid's who enrolled for every course taught by KORTH.

Sol ① $\pi_{\text{sid}} \left(\sigma_{\substack{\text{Enroll} \\ \text{cid}}} \left(\text{Enroll} \times \sigma_{\substack{\text{course} \\ \text{Inst}=\text{Korth}}} \right) \right)$

(OR)

$\pi_{\text{sid}} \left(\text{Enroll} \bowtie \sigma_{\substack{\text{course} \\ \text{Inst}=\text{Korth}}} \right)$

②

Enroll

<u>sid</u>	<u>cid</u>
S1	C1
S1	C2
S1	C3
S1	C5
S2	C2
S2	C5
S3	C4

Course

<u>cid</u>	<u>Inst</u>
C1	Korth
C2	Korth
C3	Korth
C4	Navathe
C5	Ullman

$\Rightarrow \pi_{\text{sid}}^{\text{(Enroll)}} / \pi_{\text{cid}}^{\text{(course Inst=Korth)}}$

gives

<u>sid</u>
S1

(OR)

$\pi_{\text{sid}}^{\text{(Enroll)}} - \pi_{\text{sid}}^{\left(\pi_{\text{sid}}^{\text{(Enroll)}} \times \pi_{\text{cid}}^{\text{(course Inst=Korth)}} \right)} - \pi_{\text{sid}}^{\text{(Enroll)}}$

V. Imp

Example:-

Workfor(Eid Pid) Project(Pid Pname)

- ① Retrieve eid's whose work for some DB project
- ② Retrieve eid's who work for Every DB Project.

Soln:-

① $\pi_{Eid} \left(\text{Workfor} \bowtie \sigma_{Pname=DB} (\text{Projects}) \right)$

② $\pi_{EidPid} \left/ \pi_{Pid} \left(\sigma_{Pname=DB} (\text{Project}) \right) \right.$

(or)

$\pi_{Eid} - \pi_{Eid} \left\{ \pi_{Eid}(w) \times \pi_{Pid} \left(\sigma_{Pname=DB} (\text{Project}) \right) - \pi_{EidPid}(w) \right\}$

↑ possible
Every eid of Workfor
rel pairs with all DB projects

actual
givenTable

Employee Id who Not Work for all data-base Project

Eid's Works some project

use

\bowtie	: Some
$/$: Every

Lecture - 9

Set Operators

Union : \cup

Set difference : -
(Minus)

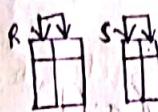
Intersection : \cap

~~Same in SQL~~ To apply $R \cup S$, $R \cap S$, & $R - S$ Relation R & S must be union compatible

Com patable.

$\Rightarrow R$ & S is union compatible iff ①

① Arity of $R =$ Arity of S



~~Arity \Rightarrow #attribute
 \Rightarrow #columns~~

② Domain of each attributes of R must be same as attributes of S respectively.

Ex ① $\pi_{sid, sname}()$

$\pi_{sid}()$

Arity = 2

Arity = 1

→ cannot apply ($\cup, \cap, -$) ✓

② $\pi_{sid, sname}() \cup \pi_{sid, age}()$

Not same domain → cannot

apply ($\cup, \cap, -$) ✓

③ $\pi_{sid, same}()$ $\pi_{studID, studName}()$

Everything fine

✓ Apply ($\cup, \cap, -$) ✓

RUS, RNS, R-S set

Operations:-

① schema for & result same as schema of R

② Resulted record set is distinct record set

Same for
SQL

Ex

R

A	B	C
2	4	6
3	5	7
3	5	7
4	5	6

S

D	E	F
2	4	6
2	4	6
4	5	6
3	5	9

RUS

A	B	C
2	4	6
3	5	7
4	5	6
3	5	9

} either record
from R (or) S

RNS

A	B	C
2	4	6
4	5	6

} records from
R and S

R-S

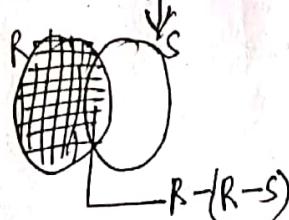
A	B	C
3	5	7

} Records of R
but not S

• U → Basic operator

• ∩ → Derived operator. → $(R \cap S) = R - (R - S)$

$$(R \cap S) = R - (R - S)$$



$$\textcircled{1} \quad R \cap S = R \setminus S \xrightarrow{\text{Same as } (\text{NOR})} \text{Same IP} \leftarrow \underline{\text{High IP}}$$

R $A \quad B$
 $\begin{array}{|c|c|}\hline & 4 & 6 \\ \hline 2 & 5 & \\ \hline\end{array}$

$\bigcap \quad \bigcap \quad R \cap S = R \setminus S$

$$\textcircled{2} \quad |(R \cup S)| = R \setminus S \xrightarrow{|X| = M \cup \text{left remaining} \cup \text{right remaining}}$$

$R \quad S$
 $\bigcap \quad \bigcap \quad R \cup S = R \setminus S$

When No common attributes in Tables:-

$R(AB) \quad S(CD)$

$$\textcircled{1} \quad R \cap S = R - (R - S) \xrightarrow{R \setminus S = R \times S}$$

$\Leftrightarrow \textcircled{2} \quad R \setminus S \neq R \cap S$ // attribute names are not same for R & S Tables

$$\textcircled{3} \quad R \cap S = R \setminus f(S) \xrightarrow[C \rightarrow A, D \rightarrow B]$$

$$\textcircled{4} \quad R \cap S \neq R \setminus f(S) = R \times S$$

$$\textcircled{5} \quad R \cap S = R \setminus f(S) \xrightarrow[C \rightarrow A, D \rightarrow B]$$

for the division formula

$$\frac{\pi_{AB}(R)}{\pi_B(S)} = \frac{\pi_A(R) - \pi_A(\pi_A(R) \times \pi_B(S) - \pi_{AB}(R))}{\pi_B(S)}$$

↑ ↑
 union Union
 compatible compatible

Means
 ↳ M Tabhi N ki Tareh kaam
 ↳ Krega Jis Keval attribute Name
 ↳ Ismein
 ↳ Agar attribute Names same Nhi hain
 to same kiske $M \times N$ ka use 'KRO'
 otherwise simple 'X' {cross product}
 ki Tareh kaam krye. Igne.

Queries by using setop^n

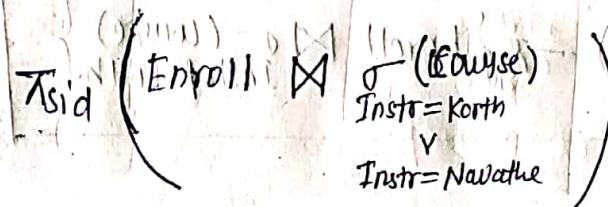
Stud (sid sname age) Course (cid cname instr) Enroll (sid cid fee)

Q1) Retrieve sid's enrolled for some course taught by Korth or some course taught by Navathe.

Q2) Retrieve sid's enrolled for some course taught by Korth and some course taught by Navathe.

Ans:-

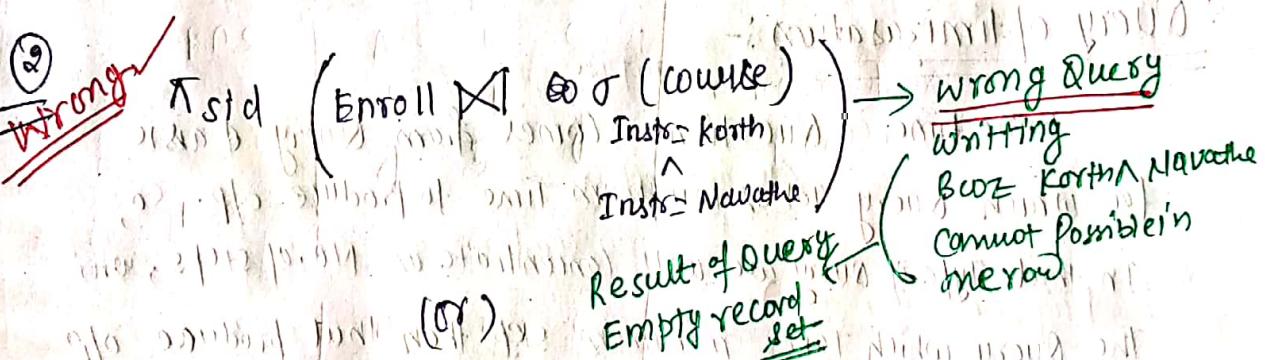
①



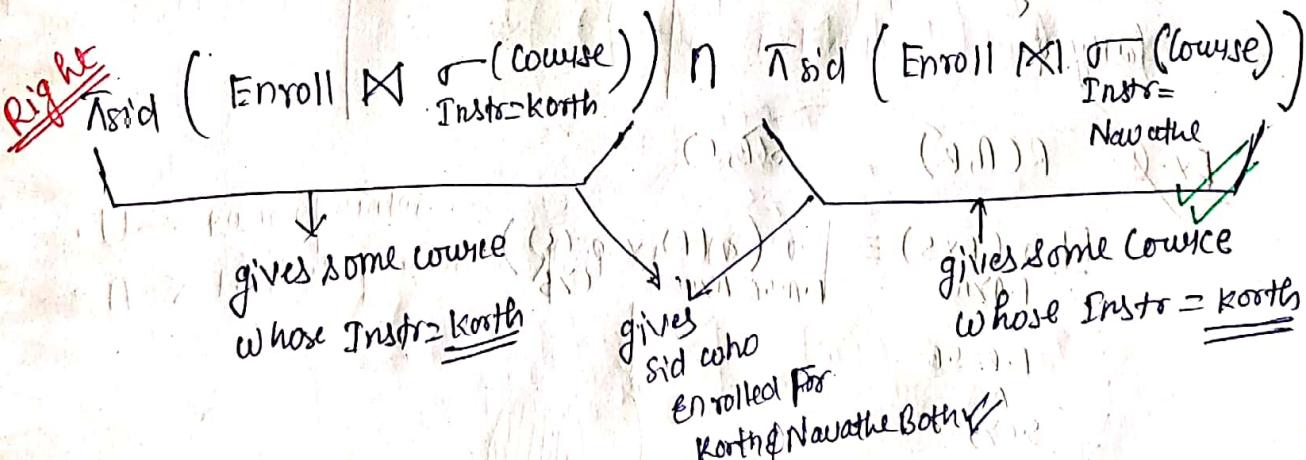
(or)

$$\pi_{\text{sid}} (\text{Enroll} \bowtie \sigma_{\text{course}}) \cup \pi_{\text{sid}} (\text{Enroll} \bowtie \sigma_{\text{course}})$$

②



Right



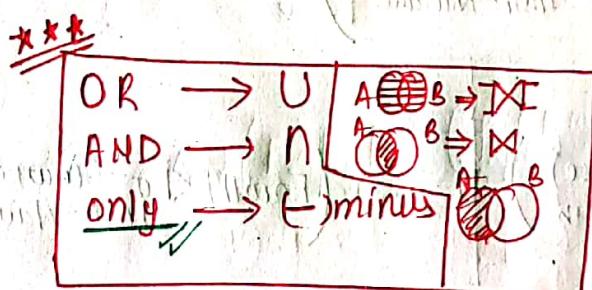
~~Ques~~ Enroll (sid cid) Course (cid Instr)

Retrieves sid enrolled only courses taught by Korth.

② Retrieve sid's enrolled some course taught by Korth.

Ans ① {sid's enrolled} - {sid's enrolled some course} Non Korth courses

$$\Rightarrow \pi_{\text{sid}}(\text{Enroll}) - \pi_{\text{sid}}[\text{Enroll} \bowtie \sigma_{\text{Instr} = \text{Korth}} (\text{course})]$$



Query optimization :-

Some time Questions comes from Query & ask for which query takes minimum time to produce o/p. So, In that Type of query we will concentrate on NO. of steps, etc
The query which takes minimum step then that produce o/p

Ex-~~R~~ R(A,B) S(B,C)

$$\sigma(R \times S) \equiv \sigma(\sigma(R) \times \sigma(S))$$

R.A > 10 R.A = S.B A > 10 C > 5

R.B = S.B

S.C > 5

A	B	C
1	2	3

~~Ex-2~~ I) $\sigma(R \bowtie S)$

$R.A > 10$



II) $\sigma(R) \bowtie S$ optimal

$A > 10$

join cost reduces.

~~Ex-3~~ I) $\sigma(R \bowtie S)$

$R.A > 10$

$S.C > 5$



II) $\sigma(R) \bowtie \sigma(S)$ optimal

$A > 10$

$C > 5$

~~Ex-4~~ Enroll (sid cid)

so optimise $\sigma(Enroll \bowtie Course)$

$Instr =$
KORTH

solⁿ Method-I
 $\sigma(Enroll \bowtie Course)$
 $Instr =$
KORTH

10 Lacks Records

$\sigma(\sigma(Exc)) \Rightarrow 2 Lacks Comp.$

10 Lacks Comp.

Method 2

Enroll $\bowtie \sigma(Course) = \sigma(Enroll \times \sigma(Course))$

50,000 Comp

10,000

5 Tuples

method-2
in optimised
method

~~5~~ Emp (eid, dno, Sal)
 Assume 100 Emp &
~~10(dept-5)Emp.~~

Plan 1

$\pi_{eid}(\text{Emp} \bowtie_{\substack{\text{Sal} \geq s \\ \wedge D=5}} f(\text{Emp}))$

100 Tuples 100 Tuples.

10,000 Tuples
cross product

Cost of Query: 20000 comp.

Plan 2

$\pi_{eid}(\text{Emp} \bowtie_{\substack{\text{Sal} \geq s \\ \wedge D=5}} (\sigma_{\substack{\text{D}=5 \\ \text{from dept5}}}(\text{EMP})))$

from dept5 ← 100 Employee

100 Tuples

10 Tuples

10,000 Tuples

1000 comparison

~~6~~ Emp (eid, gen, sal)

$\pi_{eid}(\text{Emp} \bowtie_{\substack{\text{gen=Fem} \\ \wedge \text{G=Male} \\ \wedge \text{Sal} \geq s}} f(\text{Emp})) \equiv$

gen=Fem
G=Male

$\pi_{eid}(\text{Emp} \bowtie_{\substack{\text{gen=Fem} \\ \wedge \text{Sal} \geq s}} f(\text{Emp}))$

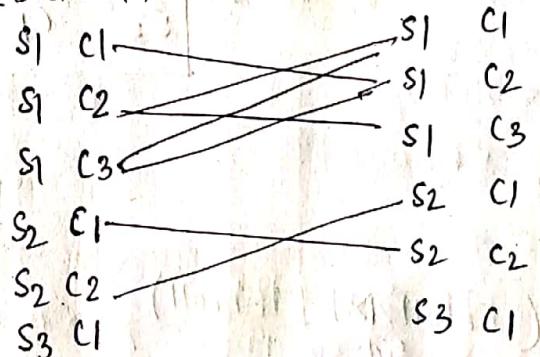
$\pi_{eid}(\sigma_{\substack{\text{gen=Fem} \\ \text{Sal} \geq s}}(\text{Emp}) \bowtie_{\substack{\text{gen=Male} \\ \text{Sal} \geq s}} \sigma_{\substack{\text{gen=Male} \\ \text{Sal} \geq s}}(f(\text{Emp})))$

-lecture-10:-

Queries related to At least / only / atmost

~~good one~~ • Enroll (sid cid); Retrieve sid's enrolled for at least two courses.

$T_1 \rightarrow \text{Enroll}(sid, cid) \quad T_2 \rightarrow \text{Enroll}(cid, sid)$



~~good one ✓~~

$\pi_{T_1.sid} (f(T_1, \text{Enroll}) \bowtie f(T_2, \text{Enroll}))$

$T_1.sid = T_2.sid$

$T_1.cid \neq T_2.cid$

Tricks:-

- For Finding & at least 2 Then do cross product Two Times & For
- Finding atleast 3 Then do cross product Three Times. So on-
- Then apply cond'

$\pi_{sid} (\text{Enroll} \bowtie_{sid=sid} f_{sid,cid} (\text{Enroll}))$

$\wedge \wedge$
 $cid \neq cid$

~~good one~~ ★★★★ Retrive sid's enrolled for at least three courses.

$\pi_{sid} (f(T_1, \text{Enroll}) \times f(T_2, \text{Enroll}) \times f(T_3, \text{Enroll}))$

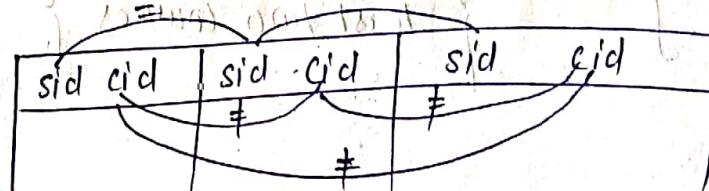
$T_1.sid = T_2.sid \wedge T_2.sid = T_3.sid \wedge$

$T_1.cid \neq T_2.cid \wedge T_2.cid \neq T_3.cid \wedge$

$T_1.cid \neq T_3.cid$

16:30

$T_1 \times T_2 \times T_3$



Ques Sid's enrolled "only one" course.

↓ logic

{ Sid's enrolled }
at least one course } — { Sid Enrolled at }
least two courses }

$$\underline{s_3} \equiv s_1 - s_2$$

E	sid	cid
S1	s1	c1
S1	s1	c2
S1	s1	c3
S2	s2	c1
S2	s2	c2
S3	s3	c1

$$\pi_{\text{sid}}(\text{Enroll}) - \pi_{\text{sid}}(\text{Enroll} \Delta f_{s,c}(\text{Enroll}))$$

$\Delta f_{s,c}(\text{Enroll})$
 $\text{sid} = s$
 $\wedge \text{cid} \neq c$

Ques Sid enrolled "only two" courses.

↓ logic

{ Sid's Enrolled at }
at least two courses } — { Sid's Enroll at least }
three courses }

$$\underline{s_2} \equiv s_1 - s_1$$

Ques Sid enrolled at most one courses.

Ans

stud (sid sname) Enroll (sid cid)

$\Delta f_{s,c}(\text{Enroll})$

s_1

s_2

s_3

s_4

s_1 c1

s_1 c2

s_1 c3

s_2 c1

s_2 c2

s_3 c1

s_4 c1

$$\{s_3, s_4\} = \{ \text{All stud} \} - \{ \text{Sid Enrolled at } \\ \text{least two courses} \}$$

$\Delta f_{s,c}(\text{Enroll})$

s_1

s_2

s_3

s_4

Ques sid Enrolled "at most" two course.

$$\text{Soln} \quad \{ \text{All student} \} \vdash \{ \text{Sid's Enrolled at least three course} \}$$

V.t.mpl Ques Relⁿ R with x set of attributes & n distinct tuples

Rel^m S with y set of attributes & m distinct tuples.

a) Condition Required to use R/S (division op)

b) Resulted Attribute set of R/S

c) Cardinality of R/S.

Soln :- a) Condⁿ required for R/S $\Rightarrow R \supseteq S$

b) Resulted attr. Set of R/S $\rightarrow (x-y)$

c) Cardinality of R/S $\rightarrow (0 - [n/m])$ Tuples

$$\text{Ex } \frac{\pi(R)}{\pi(S)} = \begin{array}{c|c} AB & B \\ \hline a_1 b_1 & b_1 \\ a_1 b_2 & b_2 \\ a_2 b_2 & b_3 \\ a_2 b_3 & b_3 \end{array} \Rightarrow (0)$$

min NO. of Tuples.

Rel R with n distinct Tuples.

Rel S with m distinct Tuples.

means minimum & maximum Tuples in the relation

R.A Expression | Cardinality (min, max) | Commutative.

①	$\pi_A(R)$	i) atmost n tuples ii) depend on the # of distinct A value	NO
②	$\sigma_A(R)$	(0 to n) Tuples	✓
③	$R \times S$	(n*m) Tuples	✓
④	$R \bowtie S, R \bowtie CS$	(0 to n*m) Tuples	✓
⑤	$R \bowtie S$	(m to n*m) Tuples	NP
⑥	$R \bowtie S$	(m to n*m) Tuples	X {order change + result change}
⑦	$R \bowtie S$	(max(n,m) to n*m) Tuples	✓
⑧	$R \cup S$	* (max(m,n) to n*m) Tuples	✓
⑨	$R \cap S$	(0 to min(n,m))	✓
⑩	$R - S$	{0 to n}	X
⑪	R / S	{0 to [n/m]}	X

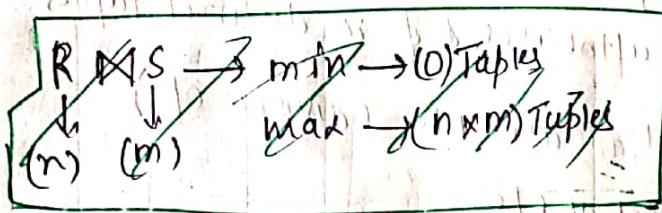
~~Imp
Date~~

Stud (sid sname) sid Primary Key with 100 Tuples.

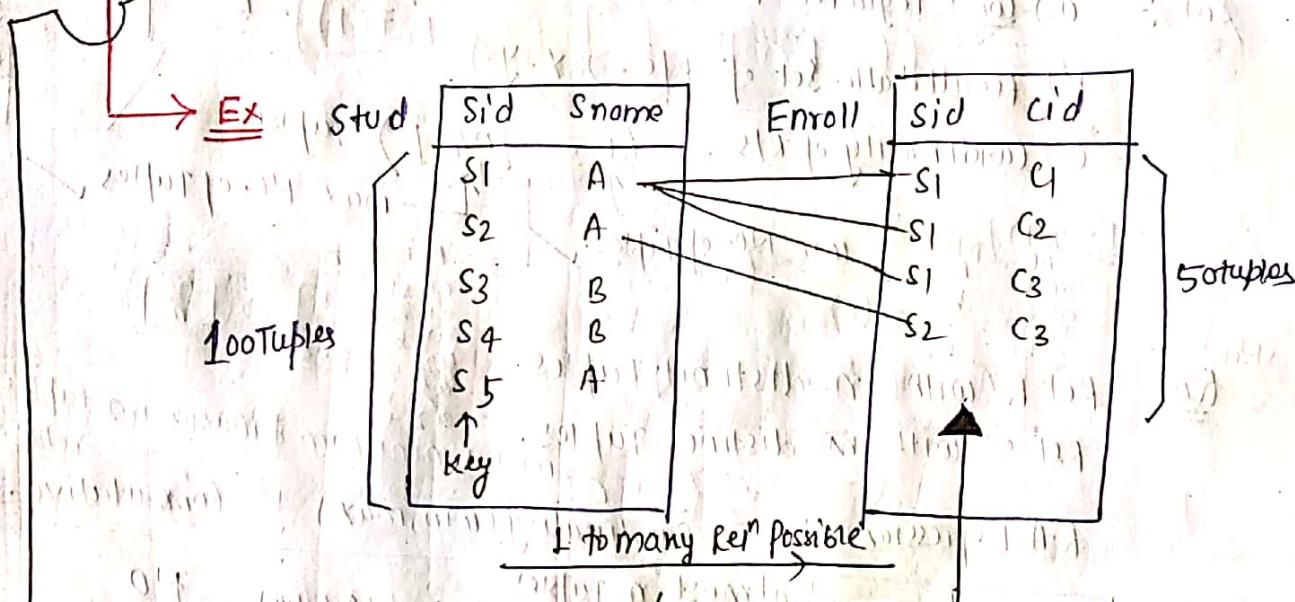
Enroll (sid cid) sid Primary Key with 50 tuples.

How many (max, min) tuples in result of Stud \bowtie Enroll?

- Soln.
- (a) (100, 50) (b) (100, 0) (c) (50, 50) (d) (5000, 0)



max tuples, S \bowtie E \Rightarrow 50 tuples
min tuples S \bowtie E \Rightarrow 50 tuples [FK exists]



If NO foreign key given
then sid of Enroll table
Not match with and stud Id
In this case min Tuples will be "0"

all will join with

stud \rightarrow max \rightarrow 50

min \rightarrow 50

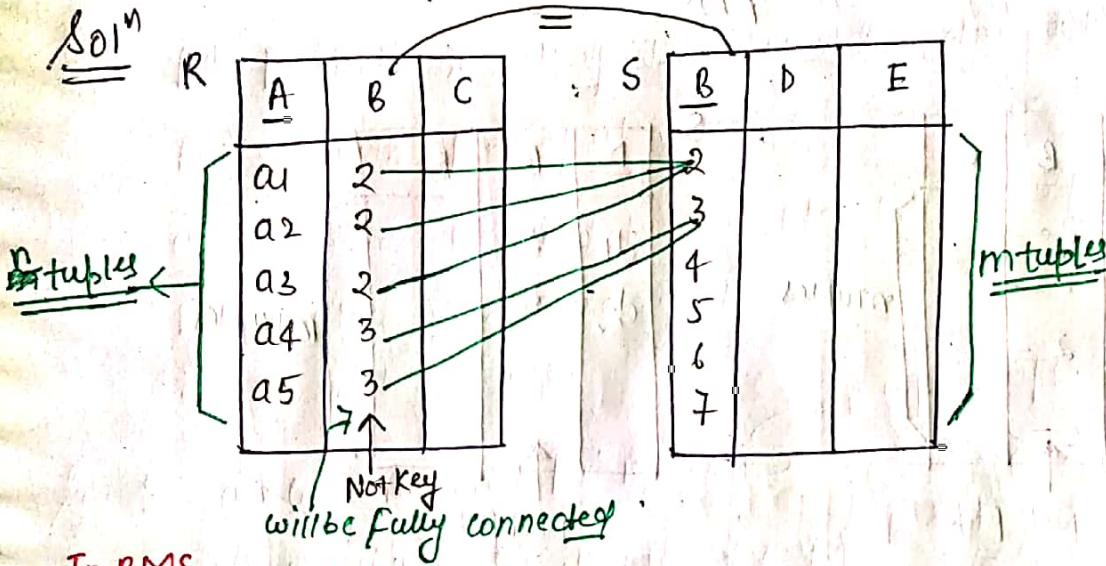
V. Imp ~~Ques~~ R (A B C) No Null with n tuples

S (B D E) with m tuples.

How many max tuples in Result of $R \bowtie S$:

How many min tuples in Result of $R \bowtie S$:

Solⁿ



In $R \bowtie S$

max Tuples $\rightarrow n \times n$

min Tuples $\rightarrow 0 \rightarrow$ (No foreign key)

$n \times n \rightarrow$ (with foreign key)

V. Imp ~~Ques~~

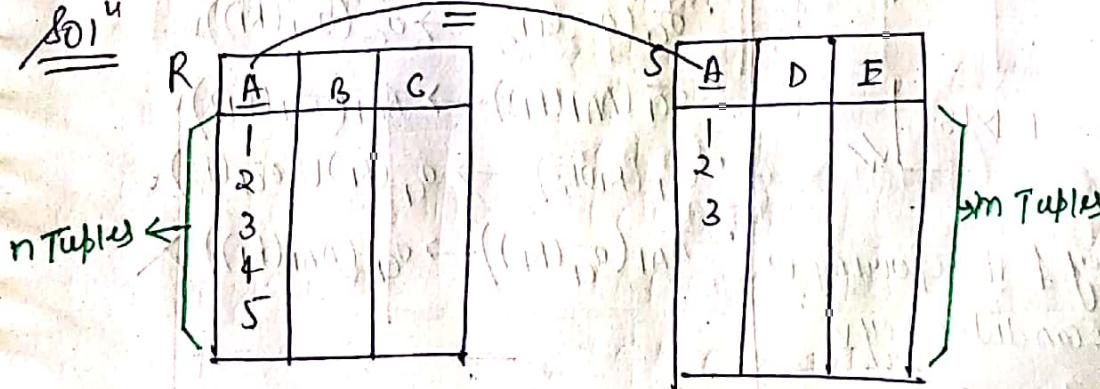
R (A B C) with n tuples

S (A D E) with m tuples

max tuples in result of $R \bowtie S$:

min tuples in result of $R \bowtie S$:

Solⁿ



In $R \bowtie S$

① max Tuples $\rightarrow \min(n, m)$

② min Tuples $\rightarrow \min(n, m) \leftarrow$ with FK

0 \leftarrow 0 (No FK)

V. Imp
★

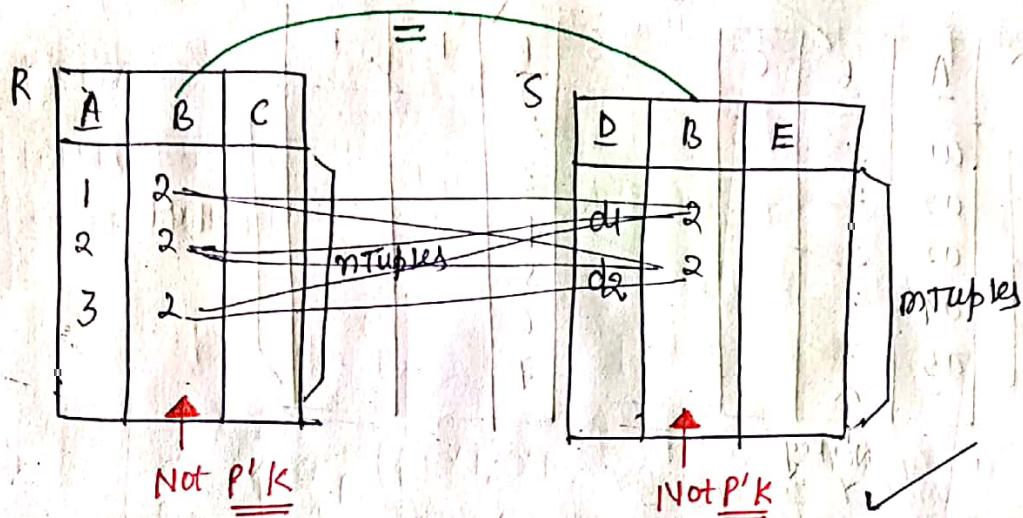
$R(A B C)$ with n tuples

$S(D B E)$ with m tuples.

max tuples in result of $R \setminus S$ _____

min in $R \setminus S$ _____

Solⁿ



In $R \setminus S$

• max tuples = $n \times m$

• min tuples = 0

Important Concept

- Have same Expressive power

→ Relational Algebra

→ TRC Restricted to safe Expression

→ DRC Restricted to safe expression

$$R - (R - S) = R \setminus S = R \setminus S$$

- If B is a foreign key & it referring to "C" → then C will be candidate key ✓

- Jb Tk SQL Ke Question me Ye Na Khajee kidustinct selection Tb Tk distinct Na maanovi ✓

$$R \setminus S = R - (R - S)$$

- $\sigma_{C_1}(\sigma_{C_2}(R_1)) \rightarrow \sigma_{C_2}(\sigma_{C_1}(R_1))$ ✓
- $\sigma_{C_1}(\pi_{A_1}(R_1)) \rightarrow \pi_{A_1}(\sigma_{C_1}(R_1))$ ✓
- $\sigma_{C_1}(R_1 \cup R_2) \rightarrow \sigma_{C_1}(R_1) \cup \sigma_{C_1}(R_2)$ ✓
- $\pi_{A_1}(\sigma_{C_1}(R_1)) \rightarrow \sigma_{C_1}(\pi_{A_1}(R_1))$ ✗

Lecture - 11

SQL { Structured Query Language }.

Sub languages of SQL →

- DDL (Data definition language)
- DML (Data manipulation language)
- DCL (Data control language)

Data definition Language (DDL)

- used to define structure/definition of DB table.
- ⇒ CREATE TABLE --
- ⇒ DROP TABLE
- ⇒ ALTER TABLE
 - (add/remove attributes)
- ⇒ PRIMARY KEY
- ⇒ UNIQUE (Alternate Key)
- ⇒ Foreign Key (FK constraints)
- ⇒ NOT NULL
- ⇒ Check etc
 - (used to set range for attribute value)

Data Manipulation Language (DML)

Used to modify Data records & access required data from DB tables.

- ⇒ INSERT INTO --
- ⇒ DELETE FROM --
- ⇒ UPDATE -- SET

⇒ SELECT * FROM Tables WHERE Cond,

Data control language (DCL)

- ① Data control from for transaction mgmt
- [To Avoid inconsistency bcoz concurrent user]

⇒ Roll Back ↑

- ⇒ Commit
- commit
- ⇒ Check Point etc.

- ② Data control for user authentication (Security)

↳ Grant Access --

↳ Revoke Access etc

SQL Query Vs Relational Algebra(RA) Query :-

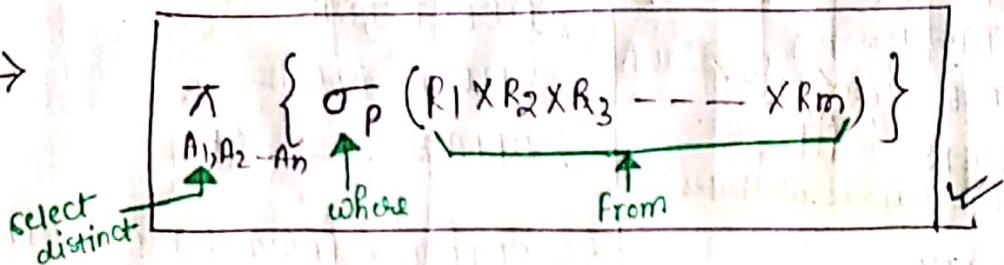
SQL 1-

{ SELECT DISTINCT A₁, A₂ -- A_n
from R₁, R₂, R₃ -- R_m where P;

FROM → cross product (X)

WHERE → selection (σ)

SELECT DISTINCT → projection (π) ✓



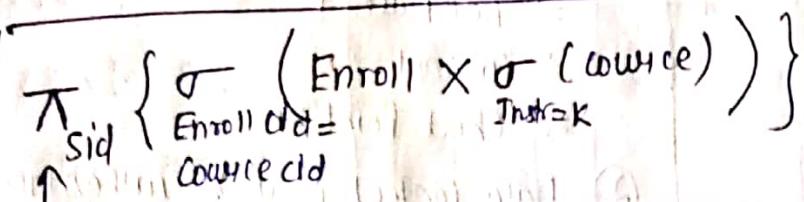
Enroll

Sid	Cid
S1	C1
S1	C2
S2	C2
S2	C3

course

Cid	Instr
C1	K
C2	K
C3	N
C4	N

Retrieve sid's enrolled some course Taught by korth.



gives

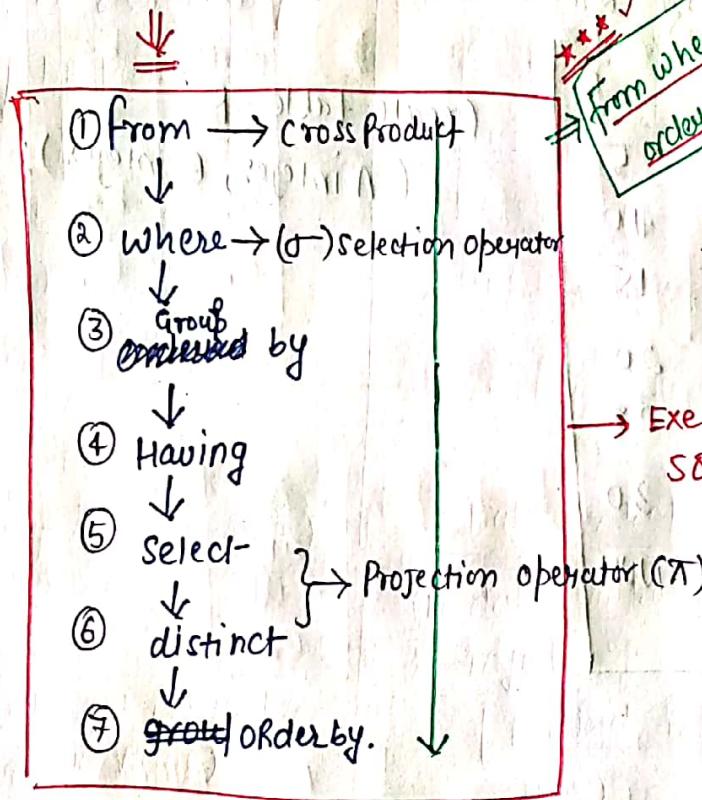
S1
S2

SQL

• Select distinct sid from Enroll,
course where Instr = Korth &
Enroll.Cid = course.Cid

Basic SQL clauses :-

- ⑤ SELECT [DISTINCT] / A₁, A₂ -- A_n
- ⑥ FROM R₁, R₂, -- R_m
- ② [WHERE condition]
- ③ [Group By (attributes)]
- ④ [HAVING condition]
- ⑦ [ORDER BY (attributes) [DESC]];



About Group by clause :-

Used to group records based on specific attributes.
Values.

SELECT "X" Agg(Y)
from R
Grouped by (X)

- ① If **group by** clause used then
 - I All attribute of group by clause must be in **select** clause.
 - II Can use **Aggregate fun.** option in **select** clause.
 - III Not allowed to select any other attribute in **select** clause.

Aggregate function :-

- ① min()
- ② max()
- ③ sum()
- ④ Avg()
- ⑤ count()

Aggregate Function

Computes aggregation of
Non Null Values of A

→ maintained by SQL.

Row ID	A	B
1	20	5
2	40	10
3	NULL	15
4	20	20
5	60	25
6	80	30
7	NULL	NULL

create table R
(A integer, B Integer);

*** Count:-

Count(*) :- # of Records

Count(A) :- # of Non Null Values of Attr A.

Count(distinct A) :- # of distinct Non Null Value of A.

Ques:-

R

Row ID	A	B
1	20	5
2	40	10
3	NULL	15
4	20	20
5	60	25
6	80	30
7	NULL	NULL
8	1	1
9	1	1

a) select Count(*) A1,
Count(A) A2,
Count(DISTINCT A) A3,
from R;

b) Select Sum(A) A1, sum (DISTINCT A) A2,
AVG(A) A3, AVG(DISTINCT A) A4,
MIN(A) A5, MAX(A) A6
from R;

Soln :-
a)

A1	A2	A3
77	5	4

b)

A1	A2	A3	A4	A5	A6
220	200	44	50	20	80

$$\text{AVG}(A) = \frac{\text{sum}(A)}{\text{Count}(A)} = \frac{220}{5} = 44$$

$$\boxed{\text{AVG}(\text{DISTINCT } A) = \frac{\text{sum}(\text{DISTINCT } A)}{\text{Count}(\text{DISTINCT } A)}}$$

$$= \frac{200}{4} = 50$$

GROUP BY:-

Used to group records based on specific attribute values.

Query Based on GROUP BY :-

R	A	B	C
c1	b1	80	
a2	b4	90	
Null	b3	60	
a2	b4	60	
a1	b1	90	
Null	b3	40	
a1	b2	NULL	

Group by "A"

A	B	C
a1	b1	80
a1	b1	90
a1	b2	NULL
Null	b3	60
Null	b3	40
a2	b4	90
a2	b4	60

Query -

(1) ③ Select A

① from R

② GROUP BY A;

A
a1
Null
a2

(2) ③ Select A , AVG(C)

① from R

② Group By A

Each group

A	AVG(C)
a1	85
Null	50
a2	75

(3) ~~Select A, B~~

from R

Group By A;

→ Invalid Query

(4) ~~Select B~~

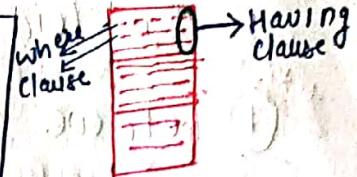
from R

Group By A;

→ Invalid Query.

Having clause Conditions :-

Where clause Tested for each record
 & Having clause Tested for each Group.



Order by clause form the values either in Ascending order or in descending order.

Having clause is used to select groups based on condition.



Ex ~~Food~~

A	B	C
a1	b1	80
a1	b1	90
a1	b2	NULL
null	b3	60
null	b3	40
a2	b4	90
a2	b4	60

① Select A
from R
Group By A
Having $\text{Avg}(C) > 60$

A
a1
a2

② Select A
from R
Group By A
Having $\text{some}(C) > 80$

A
a1
a2

③ Select A
from R
Group By A

Having $C > 60$

direct
Attr
Comb.

Not possible
in Having clause

Either takes
aggregation/comparison
or special comparison
like some, all
etc.

Query practice :-

1) Emp(eid sal)

① Retrieve eid who gets maximum salary.

→ Relational Query

$$\left(\pi_{eid}^{(Emp)} - \pi_{eid}^{(Emp \bowtie f(Emp))} \right)$$

Sal < I.S

SQL Query :- (without Aggregation)

Select Eid from Emp. } All Emp

→ except

except means (-)

Select Eid
from Emp T₁, Emp T₂ }
where T₁.sal < T₂.sal }
eid's
whose sal
< some Emp sal

By using Aggregation CLAUSE :-

① Select Eid from Emp.

where sal = (select max(sal) from Emp);

gives constant

Nested Query used in Aggregation clause

② select Eid

from Emp, (select max(salary), msal
from Emp), temp;

where Emp.sal = temp.msal;

~~Ques :- Emp (eid sal)~~

V. V. Smirnov ✓

~~From~~ Retrieve emp's who gets second highest salary.

Solⁿ

$f(\text{femp}, \exists_{\text{eidsal}} (\text{Emp} \sqcap_{\text{sal}} s \sqcap_{\text{I,s}} f(\text{Emp})))$

Theory

$$\nabla_{\text{eid}}(\text{Temp}) - \nabla_{\text{eid}}(\text{Temp} \times \frac{\delta(\text{temp})}{\text{sales}_{I,S}})$$

13

emp	
eid	sal
e1	70
e2	50
e3	80
e4	60

eid	sal
e1	70
e2	50
e4	60

V. V. 3ml

SQL Query:-

- Select emp
from Emp

where Sal = (Select max(Sal)
from Emp)

from Emb

from Emp

Select max (S)
from (Emp)

Lecture → 12

Nested Queries

- Nested Query without Correlation ✓
- Nested Query with Correlation ✓

① Nested Query without Correlation.

move ↑
 Select eid
 From Emp
 Where sal = (Select max(sal) from Emp);

⇒ Inner Query independent

⇒ Bottom-top move.

⇒ Inner Query computes only once

SELECT
 from
 WHERE
 GROUP BY
 HAVING
 ORDER BY

② Nested Query with Correlation :-

R(A---) S(B---)

select *

from R

where

(Select count(*) from R where R.A > S.B) < 20
 from S
 where R.A > S.B) &

Solⁿ for Previous Ques

R	S	60 X S.B	40 X S.B	30 Y S.B	50 X S.B	10 Y S.B
A	B					
60	50	✓	X	X	X	X
40	10	✓	✓	X	✓	X
30	60	X	X	X	X	X
50	40	✓	X	X	✓	X
10	30	✓	✓	✓	✓	X

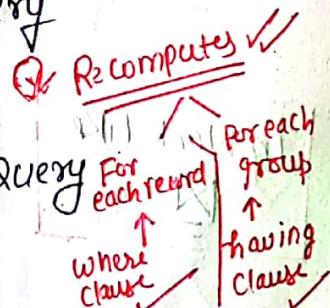
for Nested Query with Co-relation :-

⇒ Inner Query uses attribute of Outer Query

⇒ Execution flow from Top-Bottom-Top

⇒ If Co-relation in WHERE clause Inner Query

re-computes for each record of Outer Query



⇒ If co-relation in having clause then Inner Query recomputes for each group of outer query.

- Nested Queries functions will be used where more than one comparison occurs with one value in inner (Nested) loop.

Ex:-

Select *
from Emp.
where sal > (select sal
from Emp
where dno=5)

Sal
60
80
40

cannot compare
so Error occurs.

(select + sal
from Emp
where dno=5)

Function:

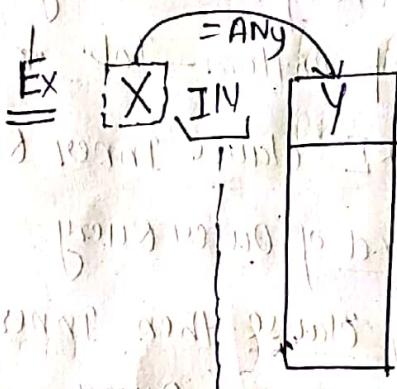
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Functions used for Nested Queries :-

- ① $\text{IN} / \text{NOT IN} (\bowtie)$
 - ② ANY
 - ③ ALL
 - ④ Exists / Not Exists.
- } Best Suitable
for Nested Query without
Co-relation
- } Best suitable For Correlated
Nested Query

IN Function : Used For membership Test.

↳ (\bowtie)



In Work Like

\bowtie

True if x value is member of y set

↳ x value must be "equal" to "some"

(at least one) value of y set.

$\boxed{\text{IN}}$ can be used as —

equir^o join (\bowtie) Queries

$\pi_{R.A} (R \bowtie S)$

$R.A = S.B$

= Some

$RCA(B)$

$S(CBC)$

$(R \bowtie S)$

$\rightarrow \pi_{AB} (R \bowtie S) \equiv \text{Select DISTINCT } R*$
from R

where $R.B \text{ IN } (\text{Select } B \text{ from } S)$

~~Ex~~ $\rightarrow R(A) \times S(B)$

$\pi_A(R \bowtie S) \Rightarrow$ Select distinct A
from R
 $R.A = S.B.$

where $R.AIN(S)$ (Select B from S)

~~Ex~~ $R(A, B) \times S(C, D)$

$\pi_{AB}(R \bowtie S) \Rightarrow$ Select distinct A, B
from R
 $R.A = S.C$
 $\wedge R.B = S.D$

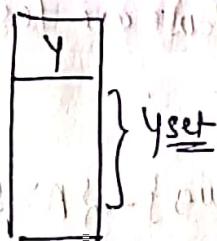
where $(A, B) \in (C, D)$ (Select (C, D) from S)

ANY & ALL Function :-

Preceded by operator.

{ $<$, \leq , $>$, \geq , $=$, \neq }

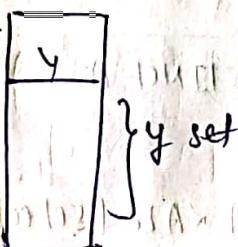
~~Ex~~ $x < ANY$



True if x Value \ll some Value of y set.

So, Here we can use \bowtie_c operator.

~~Ex~~ $x < ALL$



True iff ~~not~~ x Value \ll every Value of y set.

- (ANY) fun can used For Conditional Join (\bowtie_c) Queries.

Ex

$$R(A---) \cdot S(B---)$$

Retrieve "A" Value of R those are less than some "B" Value of S.

$$\pi_A(R \setminus S)_{R.A < S.B}$$

\equiv Select distinct A
from R
where R.A < ANY (select B value from S)

or

Select distinct A
from R, S
where R.A < S.B.

Ex

$$R(A---) \cdot S(B---)$$

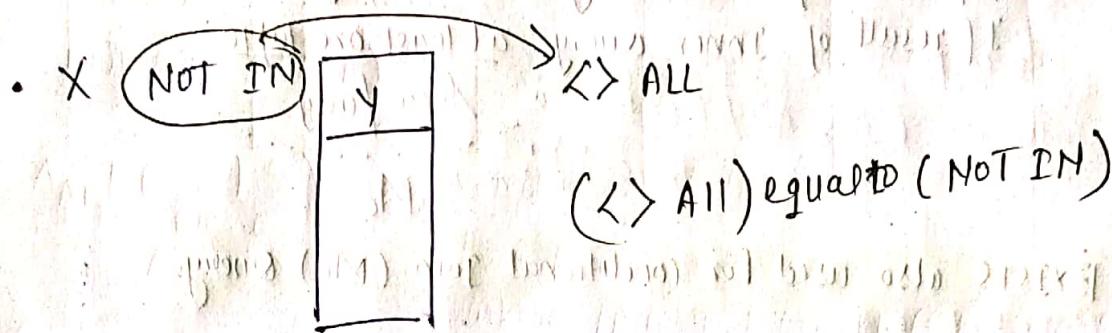
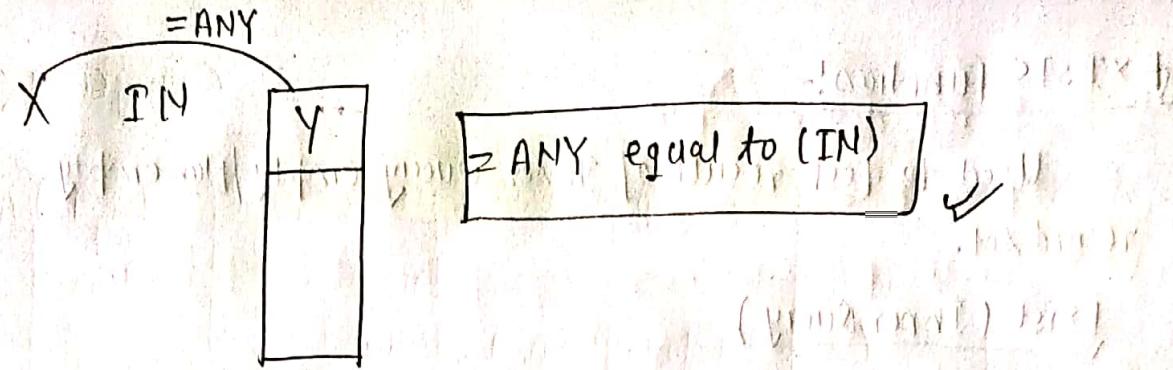
Retrieve "A" Values of R those are less than every B Values of S.

Sol $\{A < \text{Every } B\} \equiv \{\text{all } A \text{ values}\} - \{A > \text{some } B\}.$

$$= \pi_A(R) - \pi_A(R \setminus S)_{R.A > S.B}$$

SOL \rightarrow

Select DISTINCT A
from R
where R.A < ALL (select B from S);



✓ $R(A) S(B)$

$\pi_A(R \bowtie S) \Rightarrow$ select distinct A from R
 $\begin{array}{l} R.A = \\ S.B \end{array}$ where $A =\text{ANY}$ (select B from S);

✓ $R(A, B) S(C, D)$

$\pi_{AB}(R \bowtie S) \Rightarrow$ Select distinct A, B
 $\begin{array}{l} R.A = S.C \\ R.B = S.D \end{array}$ from R

where $(A, B) \text{ IN } (\text{select } C, D \text{ from } S)$

BUT it
have
two
value
comparison
↑
can't replace
by
 $=\text{ANY}$

$\text{IN} \Rightarrow =\text{ANY}$
 $\text{NOT IN} \Rightarrow \nexists \text{ ALL}$

$(A, B) = (C, D)$ ← used for
2 Value
comp like
A < B
used for only
on Value comp.

$\text{IN} \Rightarrow \bowtie$
 $\text{ANY} \Rightarrow \bowtie$
 $\text{All} \Rightarrow \pi - \pi(\)$
 $\text{Exist} \Rightarrow \bowtie_c$

EXISTS Function:-

Used to test result of Inner query empty / Non empty record set.

Exist (Inner Query)

True if result of inner query is not empty.

If result of inner query at least one tuple

Some / any

Mc

EXISTS also used for conditional join (Mc) Query.

Example:-

$\exists \text{emp}(\text{eid} \text{ duo } \text{sal})$

Retrieve eid's whose salary less than some emp salary
of dept 5.

$\rightarrow \exists \text{eid} (\text{Emp} \bowtie_{\text{Sales}} f(\text{T}_{\text{dept}, \text{S}}(\text{Emp}))$



SQL Query

select eid
① from Emp, T1

③ where Exist

② (Select *
from Emp T2
where T2.dNo=5
& T1.sal < T2.sal);

Emp T1			
	eid	dno	sal
✓	e1	4	10
✓	e2	5	20
✓	e3	4	30
✗	e4	5	40
✗	e5	4	80

emp T2			
	eid	dno	sal
	e1	4	10
	e2	5	20
	e3	4	30
	e4	5	40
	e5	4	80

	eid	dno	sal
	e1	4	10
	e2	5	20
	e3	4	30

• Exist clause behaves like N_c Queries where it has this is used in inner part of query of where clause which is related with outer query.

~~Ques~~ 6-7 Timegate Example comes
Emp (eid dno sal)

Retrieve eid's whose salary less than every emp of dept 5.

Solⁿ RA: $\exists_{eid} \text{ Emp}(eid) - \forall_{eid} (\text{Emp} \underset{\text{Sal} > S}{\bowtie} \{ \sigma_{dno=5}(\text{Emp}) \})$

↳ SQL Correlated Query

Select eid
from Emp T₁

Where Not exists

→ Exist gives true
→ Not Exist gives true
Not Empty / Empty

Select *
from Emp T₂
where T₁.sal > T₂.sal and
(T₂.d NO = 5);

Exist \leftrightarrow Some
Not Exist \leftrightarrow Every

R(A ---) S(B ---)

Retrieve "A" Values of R which are more than some "B" Values of S

Solⁿ R.A !- $\forall_A (R \bowtie S)$
 $R.A \in S$

SOL:

P. T. O

SQL

Select distinct R.A

From R, S

Where R.A > S.B.;

(OR)

Select R.A

from R

Where R.A > ANY (Select B
from S);

Nested Query

Select R.A

from R

Where Exists (Select *
from S
Where R.A > S.B.);

V. Imp
Ques

R(A —) S(B —)

Retrieve 'A' values of R which are more than every B

Values of S.

$$\Delta \underset{R}{\underset{A}{\underset{\exists}{\rightarrow}}} \left[\underset{A \leq B}{\pi_A(R) - \pi_A(R \setminus S)} \right] \checkmark$$

SQL

① Select A

From R

EXCEPT

Select A

From R, S

WHERE A <= B.;

JOIN QUERY

② select A

from R

Nested
Query

where $A > \text{ALL} (\text{Select } B)$

from S;

③

Select A

from R

Co-related
Nested
Query

where $\text{NOT EXISTS} (\text{Select } * \text{ from } S$

where $R.A \leq S.B);$

$\neg(A \leq \text{some } B)$

$\equiv (A > \text{every } B)$

V. Impl

Ans Emp (eid, sal)

1] Retrieve eid's who gets minimum salary

Sol " RA $\Rightarrow \text{All eid}(\text{Emp}) / - \text{All eid}(\text{Emp}, \bigcap_{\text{Sal} \in S} f_{I,S}(\text{Emp}))$

SQL \Rightarrow

Select eid

from emp

where sal $\leq \text{ALL} (\text{select sal}$

from Emp);

Nested
Query.

\Rightarrow Select eid

from Emp T₁

where Not Exist (Select *

from Emp T₂

where T₁.sal $> T_2.\text{sal});$

gives (T₁.sal $> \text{some } \text{Sal of } T_2) \Leftrightarrow$

Related
Nested
Query.

Q. 1 Emp (e_id & sal duo)

Retrieve e_id's whose get min salary for each dept.

80%

R.A : $\pi_{e_id}(\text{Emp}) - \pi_{e_id}(\text{Emp} \bowtie_{\substack{\text{sal} > s \\ \wedge \text{dno} = D}} \rho_{I, I, S, D}(\text{Emp}))$

SQL: Using group by & Aggregation.

Ex \Rightarrow Emp

e_id	sal	d_no
e1	40	3
e2	70	3
e3	50	3
e4	80	4
e5	60	4

dno	m_sal
3	40
4	30

Create another Table in which only minimum salary of Each dept is placed & then do cross product.

① Select e_id

{ from Emp,

(select d_no, min(sal) m_sal
from Emp
Group by d_no) temp

Then
Then
② { where

Emp.dno = temp.dno,
and sal = m_sal;

③ Select e_id

from Emp T1,

where not exist (select * from Emp T2

where T1.sal > T2.sal and ~~d_no = T1.d_no = T2.d_no~~)

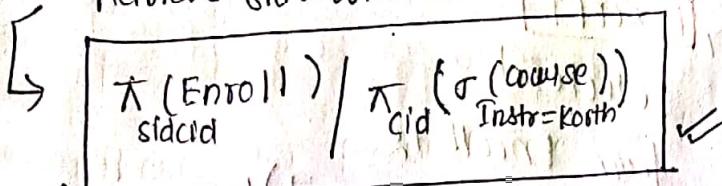
> some salary
gives ✓

Lecture - 13.

SQL Query which is equal to Division of R.A.

Enroll (sid cid) Course (cid Instructor)

Retrieve sid's who enrolled every course taught by KORTH.



But in SQL there is NO RELATED DIVISION
 division operator \rightarrow so, we have some standard procedure for it

SQL \rightarrow (Correlated Nested Query)
 kyun ki baar-2 si ki value
 check krra hai
 lekr ki wo poora course liya hai ki nhii.

Concept

Enroll
T₁

sid	cid
S1	C1
S1	C2
S1	C3
S2	C1
S2	C4
S3	C4

Course

cid	Inst
C1	Korth
C2	Korth
C3	Korth
C4	Navathe

Enroll
T₂

sid	cid
S1	C1
S1	C2
S1	C3
S2	C1
S2	C4
S3	C4

Retrieve T₁.sid from Enroll (T₁)

if { all cid's of Korth courses } - { cid's of Enroll (T₂) which are enrolled by T₁.sid }

Ex: T₁.sid = S₁ \Rightarrow {C₁, C₂, C₃} - {C₁, C₂, C₃} = \emptyset \leftarrow It means S₁ Enrolled all Korth courses

T₁.sid = S₂ \Rightarrow {C₁, C₂, C₃} - {C₁, C₄} $\neq \emptyset$ \leftarrow Not Enroll all the courses

T₁.sid = S₃ \Rightarrow {C₁, C₂, C₃} - {C₄} $\neq \emptyset$ \leftarrow Not Enroll all the courses

Select distinct sid

from Enroll T1

WHERE NOT EXISTS (select cid

from course

where Inst = KORTH

when
Inner Query is \emptyset
Then it will provide
True

we inner query have
some element then it
will provide false

due to
minus
Present

EXCEPT

Select cid

from Enroll T2

where T2.sid = T1.sid);

Ex ②

WorksFor (eid pid) project (pid pname)

Retrieve eid's who works for every project of project DB ✓

{means use division} ✓

801ⁿ

R.A

T1

work

(work for)

T2(pid)

/

T3 (project)

/

T4
pid

pname= db

S.Q.L Query ✓

Works

T1

	eid	pid

Project

pid	pname
P1	DB
P2	DB
P3	DB
P4	CN

T2 works

eid	pid

= \emptyset ✓

Retrieve T1.eid from WorksFor(T1)

If $\{ \text{all pid's of pname: DB} \} - \{ \text{pid's works by T1.eid} \} = \emptyset$

Select distinct $T_1.eid$

① from Works for T_1 If inner query $= \emptyset$ then it will give True Value.

③ Where Not Exists (Select pid from project where pname = DB) If It will select all pid which is belongs to project data base

It will do subtraction operations

Except

Select pid from Works for T_2 where $T_2.eid = T_1.eid$;

It will give all pid of (work for) for which we come here to calculate that, it is belonging to that eid which uses all DataBase Project or not.

SQL finish

Imp concept :-

- ① An SQL Query can contain having clause only if it has a group by clause.
- ② All attributes used in the group by clause need to appear in the select clause.

TRG { Tuple relational Query } ✓

- ⇒ Non-Procedural Query language.
- ⇒ Uses first order logic & predicate calculus formulas.
- ⇒ Basic formulas used in TRG :-

P, Q are predicates -

↳ [statements which can be True/false].

$$\{ P \vee Q \}$$

$$\{ P \wedge Q \}$$

$$\{ \neg P \}$$

$\neg P \rightarrow Q \Leftrightarrow$ If P then Q

$X \in \text{Rel}$ [x is a variable]

$$\{ \exists X \in R(P(x)) \}$$

for **Some** x which belongs to Relation
such that $P(x)$ must be TRUE.

$$\{ \forall X \in R(P(x)) \}$$

for **every** x which belongs to Relation
such that
 $P(x)$ must be True

Quantifiers

Format of TRG Query :-

T: Tuple Variable

$P(T)$: formula over tuple Variable T

Retrieves set of Tuples (T) those are satisfied $P(T)$

$$\{ T / P(T) \}$$

$P(T)$

$$\{ T / (T \in \text{stud} \wedge T.\text{age} > 20) \}$$

Retrieves students whose age more than 20.

$$* \{ T / P(T) \}$$

must be free variable

Tuple Variable

↳ Bounded Tuple Variable :- Variable Bounded by

Quantifiers [\exists, \forall]

Ex :- $\exists T, T \in \text{stud} (\dots)$

Bounded $\exists T, T \in \text{stud} (\dots)$

Free Variable :-

→ Not Bounded by Quantifier

→ Also called Universal Variable

Ex $T \in \text{stud}$.

↑ Not Bounded
Tuple Variable { free variable ✓ }

Ex :-
Suppliers (Sid , rating)
Parts (Pid , Pname, color)
Catalog (Sid , Pid , Cost)

Retrieve sid's of suppliers who supplied some red part.

sol^u

$\sigma_{\text{color}=\text{Red}} (\text{catalog} \times \text{Parts})$

$\exists T_1$

$\exists T_2$

$\pi_{\text{sid}} (\sigma_{\text{color}=\text{Red}} (\text{catalog} \times \text{Parts}))$

Catalog.Pid = Parts.Pid

$[T / \exists T_1 \in \text{catalog} \quad \exists T_2 \in \text{Parts}]$

some

$(T_1 . \text{Pid} = T_2 . \text{Pid} \wedge T_2 . \text{color} = \text{RED})$

Phle
T1 aur
To define Kiya
Kiya hain
wo

$\wedge T = T_1 . \text{Sid})]$

at last me kya dena
hai wo likha

$\sigma_p(R \times S)$

some / any / at least one

Express by using \exists existential Quantifiers.

~~Ques~~ Retrieve sids of suppliers who supplied at least two parts.

$$\begin{aligned}
 & \text{def}^{\text{def}} \text{Catalog}(\text{sid} \text{Pid}) = \text{Catalog}(\text{sid} \text{Pid}) \\
 & \quad \uparrow \qquad \qquad \qquad \uparrow \exists T_2 \\
 & \neg \text{sid} \left(\text{Catalog} \left(\begin{array}{c} \cancel{\text{sid}} \\ \text{sid} = s \\ \wedge \text{pid} \neq p \end{array} \right) \right) \wedge \text{f(Catalog)} \\
 & \quad \left[\rightarrow \left\{ \begin{array}{l} T_1 \mid \exists T_1 \in \text{catalog}, \exists T_2 \in \text{catalog} : \right. \\ \left. (T_1 \cdot \cancel{\text{sid}} = T_2 \cdot \text{sid}) \wedge \right. \\ \left. T_1 \cdot \text{Pid} \neq T_2 \cdot \text{Pid} \wedge \right. \\ \left. T = T_1, \text{sid} \right\} \right]
 \end{aligned}$$

• Some, any, at least one → ~~exist~~ Replace by \exists

Set operators :-

$$RUS = \{T \mid T \in R \vee T \in S\}$$

$$RNS = \{T \mid T \in R \wedge T \in S\}$$

AND.

$$R-S = \{T \mid T \in R \wedge T \notin S\}$$

$\{T \in R \wedge T \notin S\}$ but not ✓

or

$T \in R$
or
 $T \in S$

Ques Retrieve supplier id's whose rating maximum.

$$\text{Soln} \quad \pi_{sid}(\text{supplier}) - \pi_{sid}(\text{supplier}) \neq \text{rating} < R$$

$\rightarrow \underline{\text{TRC}}$

The best idea to write TRC Query firstly
write R.A Query then form it into TRC By
using its Basic Rule (T/F formula)

$$\{T \mid \exists T_1 \in \text{supplier} (T = T_1.sid) \wedge$$

$$\neg \exists T_1 \in \text{supplier} \exists T_2 \in \text{supplier}$$

$$(T_1.rating < T_2.rating \wedge T = T_1.sid)\}$$

(OR)

rating > Every rating

$$\{T \mid \exists T_1 \in \text{supplier} \forall T_2 \in \text{supplier}.$$

$$(T_1.rating > T_2.rating \wedge T = T_1.sid)\}$$

Select sid
from supplier
where rating
 $> All$ (select
 $T = All$ (select
rating
from supplier);

Conclusion :-

→ Unsafe TRG Query :-

↳ TRG Query with infinite records in result.

Ex:- $\{ T \mid \neg (T \in \text{supplier}) \} \rightarrow \text{unsafe TRG query}$

Infinite.

→ Expressive power :-

Basic RA Queries { $\{ U, \cap, \Delta, \times, \setminus, \exists, \forall, \dots \}$ }

Basic RA Queries :-

Queries which can express using :-

{ $\pi, \sigma, \times, \Delta, \setminus, \exists \pi, \exists \sigma, U, \cap, -, / \pi \div$ } operators.

safe TRG Queries
expressive power

Kyun KP dono ek doosare se derived
kyle ja skte hain ✓

Queries which are failed to express using :-

(Basic RA | safe TRG)

⇒ Count of records | Count of attributes Values

⇒ Sum of attribute Values

⇒ Avg of attribute Values.

Count x
Sum x
Avg x
Order x
Proof duplicate x

→ Ordering of Records.

→ Failed to prove duplicate Records Existence. etc