

Create a knowledge base consisting of first order logic statements and prove the given query using Resolution

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# resolution_prover.py

from copy import deepcopy

# -----
# Resolution helper: pair resolve
# -----

def resolve_pair(ci, cj):
    """
    Try to resolve two clauses (lists of literals).
    Returns a list of resolvent clauses.
    """
    resolvents = []
    for lit_i in ci:
        for lit_j in cj:
            # Case 1:  $\neg P$  vs  $P$ 
            if lit_i.startswith('¬') and lit_i[1:] == lit_j:
                new_clause = list(set(ci + cj))
                new_clause.remove(lit_i)
                new_clause.remove(lit_j)
                resolvents.append(new_clause)

            # Case 2:  $P$  vs  $\neg P$ 
            elif lit_j.startswith('¬') and lit_j[1:] == lit_i:
                new_clause = list(set(ci + cj))
                new_clause.remove(lit_j)
                new_clause.remove(lit_i)
                resolvents.append(new_clause)

    return resolvents
```

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# -----
# Resolution algorithm
# -----

def resolution(KB, query):
    """
    Apply the resolution method to  $KB \cup \{\neg \text{query}\}$ .
    KB is a list of clauses (each clause = list of literals).
    """
    clauses = deepcopy(KB)
    clauses.append(['¬' + query]) # Add negated query

    print("=== INITIAL CLAUSES ===")
    for c in clauses:
        print(c)

    new = set()

    while True:
        n = len(clauses)
        pairs = [(clauses[i], clauses[j]) for i in range(n) for j in range(i + 1, n)]

        for (ci, cj) in pairs:
            resolvents = resolve_pair(ci, cj)
            for res in resolvents:
                if not res:
                    print(f"\nResolved {ci} and {cj} -> []")
                    print("□ Empty clause derived ⇒ Query PROVED!")
                    return True
                new.add(tuple(sorted(res)))

    new_clauses = [list(x) for x in new if list(x) not in clauses]

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if not new_clauses:

    print("\nNo new clauses  $\Rightarrow$  Query cannot be proved.")

    return False


for c in new_clauses:

    clauses.append(c)

    print("Added new clause:", c)


# -----
# Knowledge Base (Grounded)
# -----

KB = [

    ['¬Food(Apple)', 'Likes(John,Apple)'],    # John likes Apple if Apple is Food
    ['¬Food(Vegetable)', 'Likes(John,Vegetable)'],# John likes Vegetable if it's Food
    ['¬Food(Peanut)', 'Likes(John,Peanut)'],    # John likes Peanut if it's Food
    ['Food(Apple)'],                            # Apple is Food
    ['Food(Vegetable)'],                        # Vegetable is Food
    ['Alive(Anil)'],                            # Anil is Alive
    ['¬Alive(Anil)', 'NotKilled(Anil)'],        #  $\text{Alive} \rightarrow \text{NotKilled}$ 
    ['¬NotKilled(Anil)', 'Alive(Anil)'],        #  $\text{NotKilled} \rightarrow \text{Alive}$ 
    ['Eats(Anil,Peanut)'],                      # Anil eats Peanut
    ['¬Eats(Anil,Peanut)', '¬NotKilled(Anil)', 'Food(Peanut)'] #  $\text{Eats} \ \& \ \text{NotKilled} \rightarrow \text{Food}$ 
]


query = 'Likes(John,Peanut)'


# -----
# Run Resolution
# -----

if __name__ == "__main__":

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print(f"Proving query: {query}\n")

result = resolution(KB, query)

print("\n=== RESULT ===")

if result:

    print("□ The query is PROVED using resolution.")

else:

    print("□ The query CANNOT be proved from the KB.")

```

OUTPUT:

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Initial Clauses:
['~Food(Apple)', 'Likes(John,Apple)']
['~Food(Vegetable)', 'Likes(John,Vegetable)']
['~Food(Peanut)', 'Likes(John,Peanut)']
['Food(Apple)']
['Food(Vegetable)']
['Alive(Anil)']
['~Alive(Anil)', 'NotKilled(Anil)']
['~NotKilled(Anil)', 'Alive(Anil)']
['Eats(Anil,Peanut)']
['~Eats(Anil,Peanut)', '~NotKilled(Anil)', 'Food(Peanut)']
['~Likes(John,Peanut)']

Resolved ['Alive(Anil)'] and ['Alive(Anil)', '~Alive(Anil)'] -> []
✅ Empty clause derived ⇒ Query PROVED!
True

```