

Particle swarm optimization

Pseudo code:

Objective function:  $f(x) = x^2$

1. Initialise parameters:

- population size = 20
- num. generation = 50
- mutation rate = 0.1
- crossover rate = 0.7
- value range = (-10, 10)

2. Create population

- Create a population

Function initialise\_population(size, value\_range):  
return np.random.uniform(value\_range[0], value\_range[1], size)

3. - Evaluate fitness

Function evaluate\_fitness(population):  
return np.array([objective\_function(x)  
for x in population])

4. - Selection

Function selection(population, fitness):  
probabilities = fitness / fitness\_sum()  
return population[np.random.choice  
(len(population), size = 2, p = probabilities)]

5. - crossover

Function crossover(parent1, parent2):  
if np.random() < crossover\_rate:  
return (parent1 + parent2) / 2  
return parent1 if np.random() < 0.5  
else parent2



// mutation

```
function mutate(indiv, mut_rate, value_range)
    if np.random.rand() < mut_rate:
        return np.random.uniform(
            value_range[0], value_range[1])
    return individual
```

// genetic algo

```
function genetic_algo():
    pop = init_population(pop_size,
        value_range)
    best_sol = None
    best_fitness = -np.inf

    for gen in range(num_gen):
        fitness = eval_fit(population)
        current_best_i = np.argmax(fitness)
        if fitness[current_best_i] > best_fitness:
            best_fitness = fitness[current_best_i]
            best_sol = population[current_best_i]

        for i in range(pop_size):
            pair1, pair2 = selection(pop, fitness)
            offspring = crossover(pair1, pair2)
            offspring = mutate(offspring,
                mut_rate, value_range)
        pop = np.array(new_pop)
    return best_sol, best_fitness
```

24/10/24



Pseudocode:

## 1. Initialise swarm

- for each particle  $i$  in swarm:
  - initialise position ( $x_i$ ) randomly within problem bounds
  - initialise velocity ( $v_i$ ) randomly
  - set personal best position  $pbest_i = x_i$
  - set personal best value  $f(pbest_i)$

## 2. Set global best ( $gbest$ )

- set  $gbest$  = position of particle with best value  $f(pbest_i)$

## 3. for each iteration ( $t = 1$ to max-iteration)

### a. for each particle $i$ :

- Evaluate fitness  $f(x_i)$  at current position  $x_i$
- if  $f(x_i) < f(pbest_i)$ 
  - update  $pbest_i = x_i$
  - update  $f(pbest_i) = f(x_i)$
- if  $(f(pbest_i) < f(gbest))$ :
  - update  $gbest = pbest_i$

### b. for each particle $i$

- Update velocity  $v_i$  using the form  
$$v_i(t+1) = w * v_i(t) + c1 * r1 * (pbest_i - x_i) + c2 * r2 * (gbest - x_i)$$

where:

- $w$  = inertia weight (controls exploration vs exploitation)
- $c1, c2$  = cognitive and social learning factors



-  $r_1, r_2$  = random value between 0 and 1

-  $p_{best-i}$  = personal best position of particle  $i$

-  $g_{best}$  = global best position of the swarm

c. for each particle  $i$ :

- update position  $x_i$  using formula  

$$x_i(t+1) = x_i(t) + v_i(t+1)$$

- ensure that  $x_i$  stays within bounds (boundary handling)

d. Output global best position  $g_{best}$  and its corresponding value (if best)

~~Q. 10/24~~



# Ant colony optimization:

## Travelling Salesman Problem

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- 1) Initialise parameters:
  - $n$  cities,  $\alpha$ ,  $\beta$ ,  $\rho$ ,  $Q$ , iterations, ant count, initial-pheromone
- 2) generate cities with random coordinates
- 3) calculate distance matrix:  $\text{distance}[i][j] =$  Euclidean distance between cities  $i$  and  $j$
- 4) Initialise pheromone matrix:  $\text{pheromone}[i][j] =$  initial pheromone
- 5) define functions:
  - $\text{calc\_distance}(\text{city}_1, \text{city}_2)$ : Return Euclidean distance
  - $\text{choose\_next\_city}(\text{current\_visited}, \text{pheromone}, \text{distances})$ :
    - Compute probability for each unvisited city
    - Return city with highest probability
  - $\text{simulate\_ants}(\text{pheromone}, \text{distances})$ :
    - For each ant, construct a tour by selecting cities based on pheromone and distance
    - Calculate tour length and update best tour if shorter
    - Return best tour and best length
  - $\text{update\_pheromones}(\text{pheromone}, \text{all\_tours}, \text{best\_tour}, \text{best\_length}, Q, \rho)$ 
    - Evaporate pheromones:  $\text{pheromone} * (1 - \rho)$
    - Deposit pheromone on all tours based on tour quality
    - Reinforce pheromone on best tour



6. Main loop (ACO algorithm):
  - Initialise best\_tour and best\_length
  - For each iteration (1 to iterations):
    - Run simulate anneal() to get best tour and best\_length
    - update best solution if necessary
    - call update pheromones()
7. Return best\_tour, best\_length
8. Display best tour and plot path

→ Initialise parameters

$n\_cities = 10$

$a = 1.0$

$b = 5.0$

$\rho_0 = 0.5$

$Q = 100$

iterations = 100

ant\_c = 100

init\_pheromone = 1.0

$np.random.seed(42)$

$cities = np.random.rand(n\_cities, 2)$

→ function calc\_distance(city1, city2):

return  $np.sqrt((city1[0] - city2[0])^2 + (city1[1] - city2[1])^2)$

→ function choose\_next\_city(curr\_city, visited, pheromone, dist):



```
for i in range(len(count):
```

```
    visited = set()
```

```
    tour = [np.random.randint(0,
                                no_cities - 1)]
```

```
    visited.add(tour[0])
```

```
    while len(visited) < cities:
```

```
        cur_city = tour[-1]
```

```
        next_city = choose_next_city()
```

```
        tour.append(next_city)
```

```
        visited.add(next_city)
```

```
    if tour_len < best_len:
```

```
        best_len = tour_len
```

```
        best_tour = tour
```

```
def update_pheromone(pheromone, all_cities,
                    best_tour, best_len, alpha, rho)
```

```
    pheromone *= (1 - rho)
```

```
    for tour, len in all_tours:
```

```
        for i in range(len(tour) - 1):
```

```
            pheromone[tour[i]][tour[i+1]] +=
                alpha / len
```

```
            pheromone[tour[i+1]][best_tour[i]]
                = alpha / best_len
```

```
for i in range(len(best_tour) - 1):
```

```
    pheromone[best_tour[i]]
```

```
    [best_tour[i+1]] = alpha / best_len
```

```
    pheromone[best_tour[i+1]]
```

```
    [best_tour[i]] = alpha / best_len
```



```
def acc-top:
    for iteration in range(Iterations):
        best-tour, best-length, all-tours
        = simulate_ants(pheromone,
            distance)
        if best-length < best-overall-len:
            best-overall-len = best-len
            best-overall-tour = best-tour
            update-pheromone(pheromone,
                all-tours, best-tour, best-length,
                Q, rho)
    return best-overall-tour, best-overall-
        length
```

best-tour, best-length = acc-top()

*Ali*  
21/11/24



1. Initialise Parameters:
  - $n = 20$
  - $pa = 0.25$
  - $max\_l = 1000$
  - $bounds = [(-5, 5), (-5, 5)]$
2. Initialise Population (random nest positions):
  - for each nest, randomly initialise position within bounds -
  - $nest[i] = \text{random pos within bounds}(\text{bounds})$
3. Evaluate fitness
  - for each nest, evaluate its fitness:
  - $fitness[i] = \text{objective\_fn}(nests[i])$
- def cuckoo-search:
  4. Iterate until max-its or convergence
    - (a) - for each nest 'i' perform its levy flights
      - $step = \text{levy\_flight}()$
      - $\text{new\_nest}[i] = nests[i] + step * (nests[i] - \text{best\_nest})$
      - ensure the nest is within bounds:
      - $\text{new\_nest}[i] = \text{clip}(\text{new\_nest}[i], \text{bounds}[0], \text{bounds}[1])$
    - (b) Evaluate new solution (fitness):
      - Evaluate fitness for each nest:
      - $\text{fitness\_new}[i] = \text{objective\_function}(\text{new\_nests}[i])$
    - (c) update nests:
      - If new nest has better fitness: replace old nest
      - if  $\text{fitness\_new}[i] < \text{fitness}[i]$ , update  $\text{new\_nests}[i]$  and  $\text{fitness}$



## (d) Abandon worst nests

- Find worst nests based on fitness:  
 $\text{worst\_nests} = \text{sorted\_indices\_of\_worst\_fitness}()$

- For each worst nest, replace it with new random position:

- ~~new~~  $\text{nests}[\text{worst\_nests}[i]] =$   
 $\text{random\_pos\_within\_bounds}()$

-  $\text{fitness}[\text{worst\_nests}[i]] =$   
 $\text{objective\_fn}(\text{nests}[\text{worst\_nests}[i]])$

## (e) Track Better solution:

- If better solution found update best solution:

- if  $\text{fitness}[\text{min\_fitness\_index}] <$   
 $\text{best\_fitness}$ , update best nest  
 and best fitness

## f. Return Best solution

Output best solution and its fitness value

- return best nest, best fitness

## Go def levy-flight:

$s =$  Random sample from  
 Gaussian distribution:

$$s \sim N(0, 1)$$

$$\text{step} = \text{alpha} * s / |s|^{(1/2)}$$

$$\text{new\_nest}_i = \text{nest}_i + \text{step}$$

$$\text{return new\_nest}_i$$



# GREY WOLF OPTIMIZER

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1 objective function(x)

Input: Positive vector 'x'

Output: fitness value

fitness = np.sum(x\*\*2)

return fitness

2 initialise parameters (search space, num w, dimensions)

Input: search space (bounds), number of wolves, and dimensions

Output: matrix of initialised positions for wolves

→ extract bounds of search space

lower bound, upper bound = search space

→ generate random wolf position

wolves = np.random.uniform

(lower bound, upper bound, (num wolves, dimensions))

→ Return wolves

3 Update positions (wolves, alpha\_pos, beta\_pos, delta\_pos, a, search space)

~~compare~~

→ get search space bounds

→ for each wolf in wolves:

for each dimension in wolf:

- generate random coefficients:

r1, r2 = np.random.random(),

np.random.random()

- compute influence from alpha:

A1 = 2 \* a \* r1 - a

C1 = 2 \* r2

D\_alpha = abs(C1 \* alpha\_pos[d] - wolves[i, d])

x1 = alpha\_pos[d] - A1 \* D\_alpha



- Repeat for beta and delta values to compute  $x_2$  and  $x_3$
- Average contributions to update position:  
new position  $[i, d] = (x_1 + x_2 + x_3) / 3$

3. Ensure new position is within bounds:

new positions  $[i, :] = \text{np.clip}$   
 (new\_position  $[i, :]$ ,  
 lower bound, upper bound,  
 (axis=dimension))

4. Return updated positions

Function: grey-wolf-optimizer  
 (objective function, search space,  
 num wolves, dimension,  
 max iterations)

→ initialise wolves

→ compute initial fitness of wolves

wolves = initialise parameters

(search space, num wolves,  
 dimension)

→ fitness = np.apply\_along\_axis

(objective function, 1, wolves)

→ Identify alpha, beta, delta wolves

sorted\_indices = np.argsort(fitness)

alpha\_pos, alpha\_score =

wolves[sorted\_indices[0]]

fitness[sorted\_indices[0]]



beta\_pos, beta\_score = values

[sorted\_indices[1]], fitness[sorted\_indices[1]]

delta\_pos, delta\_score = values

[sorted\_indices[2]], fitness[sorted\_indices[2]]

→ for each iteration (t in range(max\_iteration)):

$\alpha = 2 - t * (2 / \text{max\_iterations})$

update wolves position

compute new fitness

update alpha, beta, delta

print progress

g. Return ~~alpha\_pos~~ and alpha\_score

0/7

Iteration 100/100, Best score: 1.98580855e-

Best solution found:

$[-4.383735e-17, -1.316635e-15,$

$-2.055024e-16, 1.098286e-17]$

Best score:

Q. This is the



Parallel Collision Algo

import numpy as np  
from multiprocessing import Pool

```
def obj_fn(x):  
    return np.sum(x**2)
```

```
def initialise_pop(grid_size, num_cell)  
    return [np.random.uniform(-5, 5, grid_size)  
            for _ in range(num_cell)]
```

```
def update_cell(idn, population, grid_size)  
    row, col = divmod(idn, int(np.sqrt(  
        len(population))))  
    neighbours = []
```

```
    if row > 0: neighbours.append(  
        population[(row-1)*grid_size+col])  
    if row < grid_size-1+col)
```

```
        if col > 0: neighbours.append(  
            population[(row+1)*grid_size+col-1])
```

```
        if col < grid_size-1: neighbours.append(  
            population[row*grid_size+col+1])
```

```
    new_state = population[idn] + 0 *  
        np.mean(neighbours, axis=0) +  
        np.random.uniform(-0.1, 0.1,  
            grid_size)  
    return new_state
```



```
def parallel-cellular-algo(grid-size,
    num-cells, num-iterations):
```

```
    popu = initialise-pop(grid-size, num-cells)
    best-sol, best-fit = None, float("inf")
```

```
    for i in range(num-iterations):
```

```
        fitness = (objective-function(cell))
```

```
        for cell in population:
```

```
            best_idx = np.argmin(fitness)
```

```
    if fitness[best_idx] < best-fitness:
```

```
        best-solution, best-fitness =
```

```
            population[best_idx],
```

```
            fitness[best_idx]
```

with Pool as pool:

```
    population = pool.starmap(update-cell,
```

```
        [(i, pop, grid-size) for i in
         range(num-cells)])
```

~~return best-solution, best-fitness~~

0/1 knapsack problem:

Iteration 1:

[1 0 0 1]

[1 0 1 0]

[1 0 0 1]

[0 1 0 1]

Iteration 2:

[0 0 0 0]

[0 0 0 0]

[0 0 0 0]

[0 0 0 0]



# GA Expression Algo

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```
def optimise_fun(x):  
    return np.sum(x**2)
```

```
def init_pop():  
    return np.random.uniform(  
        -10, 10, 50, 5)
```

```
def evaluate_fitness(pop):  
    fitness = np.array([optimise_fun(  
        ind) for ind in pop])  
    return fitness
```

```
def select_parents(pop, fitness):  
    inv_fitness = 1 / (fitness + 1e-6)  
    selected_prob = inv_fitness /  
        np.sum(inv_fitness)  
    selected_ind = np.random.choice(  
        np.arange(50), size=50,  
        p=selected_prob)  
    return pop[selected_ind]
```

```
def crossover(parents):  
    offspring = np.empty_like(parents)  
    for i in range(0, 50, 2):  
        p1, p2 = parents[i], parents[i+1]  
        if np.random.rand() <  
            CrossoverRate:  
            alpha = np.random.rand()  
            offspring[i] = alpha * p1 +  
                (1-alpha) * p2  
            offspring[i+1] = alpha * p2 +  
                (1-alpha) * p1  
        else:  
            offspring[i], offspring[i+1] =  
                p1, p2
```



```
def mutate(offsp):
    for i in range(50):
        if np.random.rand() < 0.1:
            mutation_point = np.random.
                rand_int(0, 100)
            offspring[i][mutation_point] =
                np.clip(offspring[i]
                    [mutation_point], -10, 10)
    return offspring
```

```
def gene_expression(genes):
    return genes
```

```
def gene_expression_algo():
    pop = init_pop()
    best_sol = None
    best_fitness = float('inf')
    for gene in range(50):
        fitness = evaluate_fitness(pop)
        current_best_idx = np.argmin
            if fitness[current_best_idx] < best_fitness:
                best_fitness = fitness[current_best_idx]
                best_sol = population[current_best
                    - idx]
        parents = select_parents(pop, fitness)
        offsp = crossover(parents)
        offsp = mutate(offsp)
        pop = gene_exp(offsp)
    return best_sol
```

Best soln: Chromosome [1, 3, '+', 2, 1, 4, '\*',  
'\*', 3], Fitness: 12592057

o/p -  
18/12/24