

Roll No. 418271031

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CBA-255-T

M.C.A. First Semester

(End Semester)

Examination Dec., 2018

COMPUTER SCIENCE AND APPLICATIONS

Paper - CSA-CC-125

(Discrete Mathematics)

Time : Three Hours]

[Maximum Marks : 60

Note :- Attempt all sections A, B and C. Follow the instructions given in each section.

[P. T. O.

Section-A

(Objective Type Questions) $10 \times 1 = 10$

Note :- Attempt all question and in each question select the correct option.

1. (i) Range of a function is:

- (a) The maximal set of numbers for which function is defined
- (b) The maximal set of numbers which a function can take values
- (c) It is set of natural number for which a function is defined
- (d) None of the mentioned

(ii) In which of the following sets $A-B$ is equal to $B-A$

- (a) $A = \{1, 2, 3\}$, $B = \{2, 3, 4\}$
- (b) $A = \{1, 2, 3\}$, $B = \{1, 2, 3, 4\}$
- (c) $A = \{1, 2, 3\}$, $B = \{2, 3, 1\}$
- (d) $A = \{1, 2, 3, 4, 5, 6\}$, $B = \{2, 3, 4, 5, 1\}$

(iii) The set of all real numbers under the usual multiplication operation is not a group since

- (a) multiplication is not a binary operation
- (b) multiplication is not associative
- (c) identity element does not exist
- (d) zero has no inverse

(iv) The sum of the entries in the fourth row of Pascal's triangle is

- (a) 8
- (b) 4
- (c) 10
- (d) 16

(v) A polygon with 7 sides can be triangulated into

- (a) 7
- (b) 14
- (c) 5
- (d) 10

(vi) Hasse diagram are drawn

- (a) Partially ordered sets
- (b) Lattices
- (c) Boolean algebra
- (d) None of these

(vii) Let P: I am in Bangalore., Q: I loved cricket.; then

$q \rightarrow p$ (q implies p) is:

- (a) If I am in Bangalore then I love cricket
- (b) I am not in Bangalore
- (c) I Love cricket
- (d) If I love cricket then I am in Bangalore

(viii) A compound proposition that is neither a tautology nor a contradiction is called

- (a) Condition
- (b) Inference
- (c) Contingency
- (d) Equivalence

(ix) In any undirected graph the sum of degrees of all the nodes

- (a) Must be even
- (b) Are twice the number of edges
- (c) Must be odd
- (d) Need not be even

(x) A graph with n vertices will definitely have a parallel edge or self loop if the total number of edges are

- (a) greater than $n-1$
- (b) less than $n(n-1)$
- (c) greater than $n(n-1)/2$
- (d) less than $(n^3)/2$

Section 'B'

(Short Answer Type Questions) 4×5=20

Note :- Attempt all four questions. Each question carries five marks.

- ① Define Relation, Function and Recursive function with suitable example.
- ② Define Group and prove that the Set $S = \{1, -1, i, -i\}$ is a group under the operation multiplication.

[P. T. O.]

3. Consider the set $A = \{1, 2, 3, \dots, 400\}$. Find the number of integers in set A which are neither divisible by 3 nor by 7.

④ Define lattice and bounded lattice. Give the properties of lattice.

5. Establish the equivalence :

$$(p \Rightarrow q) \wedge (r \Rightarrow q) \equiv (p \Rightarrow q) \Rightarrow q$$

⑥ Define Graph, Bipartite Graph, Euler path and Hamiltonian path.
Vertex *2 vertex* *edge*

Section 'C'

(Long Answer Type Questions) $3 \times 10 = 30$

Note :- Attempt any three questions. Each question carries ten marks.

① Describe the method of mathematical induction. Show that $1^3 + 2^3 + \dots + n^3 = (1+2+\dots+n)^2$ using mathematical induction for $n \geq 1$.

2. What is recurrence relation? What you understand by solving recurrence relation? Solve the following recurrence relation.

$$g(n) = g(n-1) + 2n-1$$

$$g(0) = 0.$$

3. State and verify Absorption Laws. Reduce the following Boolean expression using K-Map: $F(U, V, W, Z) = \{(0, 1, 2, 4, 5, 14, 15)\}$

④ Write notes on the following:

(a) Tautology and Contradiction

(b) First Order Predicate

(c) Quantifiers *-V* *A*

(d) Inference theory

⑤ What are Binary Tree and Binary search Tree? Write code for in order, pre-order and post-order traversal of binary tree. Explain with an example the binary tree in order, pre-order and post-order.