

1. Which one of the following gives the tightest bound on the time complexity of the following code: `<code>for (j = 1; j <= n; j++) { for (i = 1; i <= n; i++) { if (i % j == 0) { // do something } } }</code>`

- Correct**
- ☐ $O(n)$
- ☐ $O(n \cdot \log n)$
- ☐ $O(n^2)$
- ☐ $O(n^2 \cdot \log n)$

2. The recurrence equation $T(n) = 2T(n/2) + 1$, $n \geq 2$ evaluates to **Correct**

- ☐ $2^n(n-1) + 1$
- ☒ $2^n n - 1$
- ☐ $2^n(n+1) - 1$
- ☐ $2^n n - n$

3. The running time of an algorithm is represented by the following recurrence relation: $T(n) = n$ if $n \leq 3$ then $T(n) = T(n/3) + cn$. Which one of the following gives the tightest bound on the time complexity of the algorithm? **Correct**

- ☒ $O(n)$
- ☐ $O(n \log n)$
- ☐ $O(n^2)$
- ☐ $O(n^2 \log n)$

4. Let $a(n)$ be the number of n -bit strings that do NOT contain two consecutive 1s. Which one of the following is the recurrence relation for $a(n)$? **Correct**

- ☐ $a(n) = a(n-1) + 2a(n-2)$
- ☒ $a(n) = a(n-1) + a(n-2)$
- ☐ $a(n) = 2a(n-1) + a(n-2)$
- ☐ $a(n) = 2a(n-1) + 2a(n-2)$

5. Let the minimum number of comparisons to find the minimum of 150 numbers be x and the minimum number of comparisons to find the maximum of 150 numbers be y . Then which of the following is greater than $x+y$? **Correct**

- ☐ 290
- ☐ 295
- ☒ 300
- ☐ 310
- ☐ None

6. In the following function, let $m \geq n$. `gcd(n, m) { if (n % m == 0) return m; else return gcd(m, n); }` Which is the tightest bound on the time complexity for `gcd(n, m)`? **Correct**

- ☒ $O(\log(m))$
- ☐ $O(m)$
- ☐ $O(\log(\log(m)))$
- ☐ $O(\log(\log(n)))$

7. The worst case occurs in following linear search algorithm when `linearSearch(arr, int, int, int) { if (arr[i] == int) return true; else return false; }` Which is the tightest bound on the time complexity for `linearSearch(arr, int, int, int)`? **Correct**

- ☐ Item is in the middle of the array
- ☒ Item is the last element of the array
- ☒ Item is not present in the array
- ☐ Item is the first element of the array

8. What is the worst case time complexity of inserting a node in a doubly linked list? **Correct**

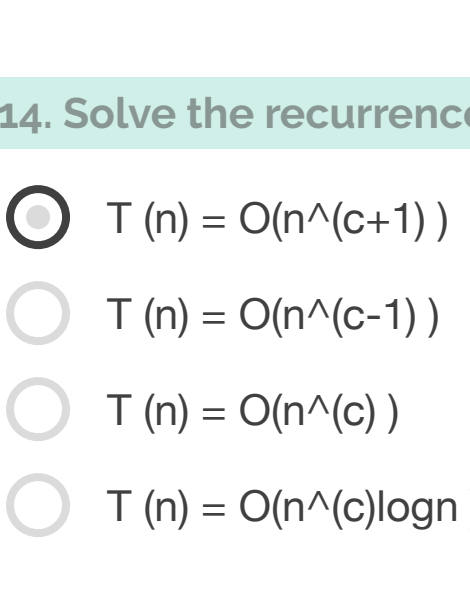
- ☐ $O(n \log n)$
- ☐ $O(\log n)$
- ☐ $O(n)$
- ☒ $O(1)$

9. Consider the following doubly linked list: (1, 2, 3, 4, 5). What will be the 3rd element in the list after performing the given sequence of operations: `insert(6, head, head), delete(1, head, head)`? **Correct**

- ☒ 0
- ☐ 1
- ☐ 2
- ☐ 3
- ☐ 4
- ☐ 5
- ☐ 6

10. Figure below is a perfectly balanced binary tree. If a node is inserted as a right child of the node R, how many nodes will become unbalanced? **Correct**

- ☐ 2
- ☒ 1
- ☐ 3
- ☐ 0
- ☐ 4
- ☐ 5



11. Suppose we define an almost balanced binary search tree to have at most $gn/10$ many nodes in either the left or right subtree. Then the tightest upper bound on the height of the tree is **Correct**

- ☐ $\log_{9/10} n$
- ☒ $\log_{10/9} n$
- ☐ $\log_2 10n/9$
- ☐ $\log_2 9/10n$

12. For an internal node x of a BST, $g(x)$ is defined as $\min(\text{no. of leaf-nodes in left-subtree of } x, \text{no. of leaf-nodes in right-subtree of } x)$. A program takes as input a binary search tree with n nodes and computes the value $g(x)$ for each internal node x . The tightest time complexity of the program is **Correct**

- ☐ $O(\log n)$
- ☐ $O(n \log n)$
- ☐ $O(n^2)$
- ☒ $O(n)$

13. The tightest bound on the worst case running time to search for an element in a perfectly balanced binary search tree with n^{2^n} elements is **Correct**

- ☐ $O(n \log n)$
- ☐ $O(n^{2^n})$
- ☒ $O(n)$
- ☐ $O(\log n)$

14. Solve the recurrence relation $T(n) = T(n-1) + n^c$, where, $c > 1$ is a constant. **Correct**

- ☒ $T(n) = O(n^{c+1})$
- ☐ $T(n) = O(n^c(c-1))$
- ☐ $T(n) = O(n^c(c))$
- ☐ $T(n) = O(n^c(c \log n))$

15. Which of the following algorithms is NOT a divide & conquer algorithm by nature? **Correct**

- ☐ Merge Sort
- ☐ Quick Sort
- ☒ Insertion Sort
- ☐ Binary Search
- ☒ Selection Sort

16. Consider the polynomial $p(x) = a_0 + a_1x + a_2x^2 + a_3x^3$, where $a_i \neq 0$, for all i . The minimum number of multiplications needed to evaluate p on an input x is: **Correct**

- ☐ 2
- ☒ 3
- ☐ 4
- ☐ 5
- ☐ 6
- ☐ 7
- ☐ 8
- ☐ 9

17. Consider a situation where you don't have a function to calculate power (`pow()` function in C) and you need to calculate x^n where x can be any number and n is a positive integer. What can be the best possible time complexity of your power function? **Correct**

- ☐ $O(n)$
- ☐ $O(n \log n)$
- ☐ $O(\log \log n)$
- ☒ $O(\log n)$

18. An array $[a_1, a_2, \dots, a_n]$ is said to be rotated by k if it becomes of the form $[a_{k+1}, \dots, a_n, a_1, \dots, a_k]$. Consider the problem of searching an element x in an array of size n . The problem can be solved in $O(\log n)$ time if **Correct**

- ☒ the Array is sorted
- ☒ the Array is sorted and rotated by k , k is given to you and $k \leq n$
- ☒ the Array is sorted and rotated by k , k is NOT given to you and $k \leq n$
- ☐ the Array is not sorted

19. What is the time complexity of the following code: `for (i = 0; i < N; i++) { for (j = 0; j < M; j++) { if (a[i] == b[j]) { // do something } } }` **Correct**

- ☐ $O(N \cdot \log M)$
- ☐ $O(\log N + M)$
- ☒ $O(N + \log M)$
- ☐ $O(\log N + \log M)$

20. What is the time complexity of following code: `for (i = 0; i < N; i++) { for (j = 0; j < N; j++) { if (a[i] == b[j]) { // do something } } }` **Correct**

- ☐ $O(N)$
- ☐ $O(N \log N)$
- ☐ $O(N \cdot \sqrt{N})$
- ☒ $O(N^2)$

21. What does it mean when we say that an algorithm X is asymptotically more efficient than algorithm Y ? **Correct**

- ☐ X will always be a better choice for small inputs
- ☒ X will always be a better choice for large inputs
- ☐ Y will always be a better choice for small inputs
- ☐ X will always be a better choice for all inputs

22. What is the time complexity of following code: `for (i = 0; i < N; i++) { for (j = 0; j < N; j++) { if (a[i] == b[j]) { // do something } } }` **Correct**

- ☐ $O(N^{1/4})$
- ☐ $O(\sqrt{N})$
- ☐ $O(N/4)$
- ☒ $O(\log N)$
- ☐ $O(N)$

23. Which one of the following is an application of Stack Data Structure? **Correct**

- ☒ Managing function calls
- ☐ Binary search
- ☒ Arithmetic expression evaluation
- ☐ Managing a Telephone directory

24. If an arithmetic expression (without parenthesis) has n operands and m operators then the maximum height of the operand stack (N -stack) and operator stack (O -stack) respectively are **Correct**

- ☐ m and n
- ☐ n and m
- ☒ $m+n$ and m
- ☐ $2n$ and m

25. What is the worst case time complexity for search, insert and delete operations in a general Binary Search Tree? **Correct**

- ☒ $O(n)$ for all
- ☐ $O(\log n)$ for all
- ☐ $O(\log n)$ for search, and $O(n)$ for delete
- ☐ $O(\log n)$ for search, and $O(n)$ for insert and delete

26. We are given a set of n distinct elements and an unlabeled binary tree with n nodes. In how many ways can we populate the tree with the given set so that it becomes a binary search tree? **Correct**

- ☐ 0
- ☒ 1
- ☐ $n!$
- ☐ $(1/(n+1)) \cdot 2n C n$

27. How many distinct binary search trees can be created out of 4 distinct keys? **Correct**

- ☐ 4
- ☒ 14
- ☐ 1
- ☐ 42

28. Consider the following two statements about a binary search tree: I. If u is a child of a parent of v , then u and v must be the same. II. If u is a parent of a child of v , then u and v must be the same. Which one of the above statements are true? **Correct**

- ☐ Both I and II are true
- ☐ I is true and II is false
- ☒ I is false and II is true
- ☐ Both I and II are false

29. Suppose we evaluate the following arithmetic expression using the algorithm discussed in class: $8/2^3 \cdot 2^3 \cdot 5^{-1}$. The element at the top of the operand stack (N -stack) when the $/$ operator is popped out is **Correct**

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30. Following is C like pseudo code of a function that takes a number as an argument, and uses a stack S to do processing. `void fun(int n) { Stack S; // Say it creates an empty stack S while (n > 0) { // This line pushes the value of n%2 to stack S push(S, n%2); n = n/2; } // Run while Stack S is not empty while (!isEmpty(S)) { // This line pops the value of n%2 from stack S pop(S); // What does the above function do in general? } }` **Correct**

- ☐ Prints binary representation of n in reverse order
- ☒ Prints binary representation of n
- ☐ Prints the value of $\log n$
- ☐ Prints the value of $\log n$ in reverse order

31. Consider the following C program: `int main() { int x, y, m, n; scanf("%d %d", &x, &y); if (x > 0 and y > 0) { m = x; n = y; } while (m != 1) { if (m > n) m = m - n; else n = n - m; printf("%d ", m); } }` What does the program compute? **Correct**

- ☐ $x + y$ using repeated subtraction
- ☐ $x \cdot y$ using repeated subtraction
- ☐ the greatest common divisor of x and y
- ☒ the least common multiple of x and y

32. State whether the following statement is true or false. $n! = O(2^n)$ **Correct**

- ☒ True
- ☐ False

33. State whether the following statement is true or false. $n^3 = O(n^4 \log n)$ **Correct**

- ☒ True
- ☐ False

34. State whether the following statement is true or false. $n^3 = O(n^2)$ **Correct**

- ☐ True
- ☒ False

35. State whether the following statement is true or false. $n! = O(3^n)$ **Correct**

- ☐ True
- ☒ False

36. State whether the following statement is true or false. $2^n = O(2^{n+c})$, for any constant $c > 0$. **Correct**

- ☐ True
- ☒ False

37. Consider the above algorithm for determining whether a sequence of parentheses is balanced. `bool isBalanced(string s) { CreateEmptyStack(); int i = 0; while (i < s.length()) { if (s[i] == '(') PushStack(s[i]); else if (s[i] == ')') { if (isEmptyStack()) return false; PopStack(); } } return !isEmptyStack(); }` What is the maximum number of parentheses that appear on the stack AT ANY TIME when the algorithm analyzes: `((()()()))`? **Correct**

- ☐ 1
- ☐ 2
- ☒ 3
- ☐ 4 or More