

Problem 1

(i) The given grammar is not LL(1) because

Left Recursion

Type \rightarrow Type *

Common Prefix

ArgList \rightarrow Type id, ArgList
ArgList \rightarrow Type id

(ii) We transform the grammar by removing left recursion and common prefix

Function \rightarrow Type id (Arguments)

Type \rightarrow id Type'

Type' \rightarrow * Type' ~~↓~~

~~Arguments~~

Type' \rightarrow ϵ

Arguments \rightarrow ArgList

Arguments \rightarrow ϵ

ArgList \rightarrow Type id ArgList'

ArgList' \rightarrow , ArgList

ArgList' \rightarrow ϵ

(iii)

FIRST (Function)	=	{id}
FIRST (Type)	=	{id}
FIRST (Type')	=	{ε, *}
FIRST (Arguments)	=	{ε, id}
FIRST (ArgList)	=	{id}
FIRST (ArgList')	=	{, , ε}

FOLLOW (Function)	=	{\$}
FOLLOW (Type)	=	{id}
FOLLOW (Type')	=	{id}
FOLLOW (Arguments)	=	{)}
FOLLOW (ArgList)	=	{)}
FOLLOW (ArgList')	=	{)}

(iv)

FIRST^+ (Function → Type id Arguments)	=	{id}
FIRST^+ (Type → id Type')	=	{id}
FIRST^+ (Type' → * Type')	=	{*}
FIRST^+ (Type' → ε)	=	{id}
FIRST^+ (Arguments → ArgList)	=	{id}
FIRST^+ (Arguments → ε)	=	{)}
FIRST^+ (ArgList → Type id ArgList')	=	{id}
FIRST^+ (ArgList' → , ArgList)	=	{, }
FIRST^+ (ArgList' → ε)	=	{)}

Columns for other terminals (\$ are empty) / /

Nonterminal	id)	*	,
Function	Function \rightarrow Type id (Arguments)			
Type	Type \rightarrow id Type'			
Type'	Type' \rightarrow ε		Type' \rightarrow Type'	
Arguments	Arguments \rightarrow ArgList	Arguments \rightarrow ε		
ArgList	ArgList \rightarrow Type id ArgList'			
ArgList'		ArgList' \rightarrow ε		ArgList' \rightarrow , ArgList

Problem 2

~~8~~

$$S' \rightarrow S$$

$$S \rightarrow LM - ①$$

$$S \rightarrow LP - ②$$

$$S \rightarrow qLr - ③$$

$$S \rightarrow sr - ④$$

$$S \rightarrow qsp - ⑤$$

$$L \rightarrow aMb - ⑥$$

$$L \rightarrow s - ⑦$$

$$L \rightarrow t - ⑧$$

$$M \rightarrow t - ⑨$$

LR(0) Canonical collection

$$\{ S' \rightarrow \cdot S,$$

$$S \rightarrow \cdot LM$$

$$S \rightarrow \cdot LP$$

$$S \rightarrow \cdot qLr$$

$$S \rightarrow \cdot sr$$

$$S \rightarrow \cdot qsp$$

$$L \rightarrow \cdot aMb$$

$$L \rightarrow \cdot s$$

$$L \rightarrow \cdot t$$

}

$$I_1 = \text{Goto}(I_0, L)$$

$$\{ S \rightarrow L \cdot M$$

$$S \rightarrow L \cdot p$$

$$M \rightarrow \cdot t$$

}

$$I_2 = \text{Goto}(I_0, \bullet S)$$

$$\{ S' \rightarrow S \cdot \}$$

$$I_4 = \text{Goto}(I_0, s)$$

$$= \{ S \rightarrow S \cdot r$$

$$L \rightarrow s \cdot$$

$$I_3 = \text{Goto}(I_0, q)$$

$$\{ S \rightarrow q \cdot Lr$$

$$L \rightarrow \cdot aMb$$

$$L \rightarrow \cdot s$$

$$L \rightarrow \cdot t$$

$$\{ S \rightarrow q \cdot sp$$

}

$$I_5 = \text{Goto}(I_0, a)$$

$$\{ L \rightarrow a \cdot Mb$$

$$M \rightarrow \cdot t \}$$

$$I_6 = \text{Goto}(I_1, t)$$

$$\{ L \rightarrow t \cdot \}$$

$$I_7 = \text{Goto}(I_2, M)$$

$$\{ S \rightarrow LM \cdot \}$$

$$I_8 = \text{Goto}(I_2, p)$$

$$\{ S \rightarrow LP \cdot \}$$

$$I_9 = \text{Goto}(I_2, t)$$

$$\{ M \rightarrow t \cdot \}$$

$$I_{10} = \text{Goto}(I_3, L)$$
$$\{ S \rightarrow q_L \cdot \gamma \}$$

$$I_{11} = \text{Goto}(I_3, S)$$
$$\{ \begin{array}{l} S \rightarrow q_S \cdot p \\ L \rightarrow s. \end{array} \}$$

~~$$I_{12}$$~~
$$\text{Goto}(I_3, a) = I_5$$

~~$$I_{12}$$~~
$$\text{Goto}(I_3, t) = I_6$$

$$I_{12} = \text{Goto}(I_4, \gamma) \Rightarrow$$
$$\{ S \rightarrow s \gamma \cdot \}$$

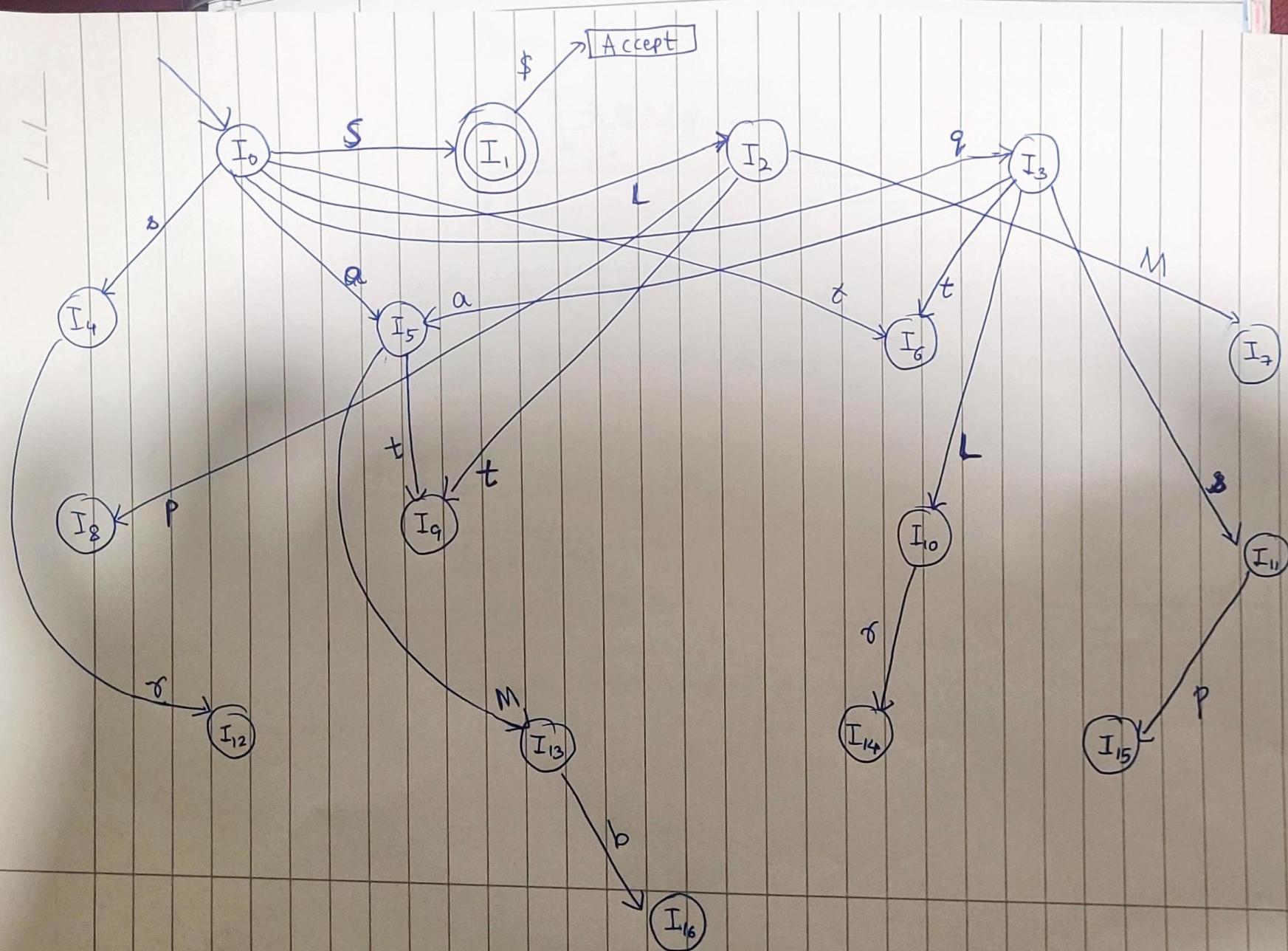
$$I_{13} = \text{Goto}(I_5, M)$$
$$\{ L \rightarrow aM \cdot b \}$$

$$I_{14} = \text{Goto}(I_{10}, \gamma)$$
$$\{ S \rightarrow q_L \gamma \cdot \}$$

$$\text{Goto}(I_5, t) = I_9$$

$$I_{15} = \text{Goto}(I_{11}, p)$$
$$\{ S \rightarrow q_S p \cdot \}$$

$$I_{16} = \text{Goto}(I_{13}, b)$$
$$\{ L \rightarrow aM b \cdot \}$$



SLR parsing table

State	ACTION							GOTO			
	p	q	r	s	t	a	b	\$	S	L	M
0		s3		s4	s6	s5			1	2	
1									[acc]		
2	s8				s9						7
3				s11	s6	s5					10
4	r7		(s12 r7)		r7						
5					s9						13
6	r8		r8		r8						
7							r1				
8							r2				
9							r9 r9				
10											
11	(s15 r7)		s14		r7						
12							r4				
13							s16				
14							r3				
15							r5				
16	r6		r6		r6						

There are 2 shift-reduce conflicts.

Hence the grammar is NOT SLR(1)

LR(1) collection

$$I_0 = \{ S' \rightarrow \cdot S, \$ \\ S \rightarrow \cdot LM, \$ \\ S \rightarrow \cdot LP, \$ \\ S \rightarrow \cdot q L\alpha, \$ \\ S \rightarrow \cdot Sr, \$ \\ S \rightarrow \cdot qsp, \$ \\ L \rightarrow \cdot aMb, t/p \\ L \rightarrow \cdot s, t/p \\ L \rightarrow \cdot t, t/p \}$$

$$I_1 = \text{Goto}(I_0, S) \\ = \{ S' \rightarrow S \cdot, \$ \}$$

$$I_2 = \text{Goto}(I_0, L) \\ = \{ S \rightarrow L \cdot M, \$, \\ S \rightarrow L \cdot p, \$ \\ M \rightarrow \cdot t, \$ \}$$

$$I_3 = \text{Goto}(I_0, q) \\ = \{ S \rightarrow q \cdot L\alpha, \$ \\ S \rightarrow q \cdot sp, \$ \\ L \rightarrow \cdot aMb, r \\ L \rightarrow \cdot s, r \\ L \rightarrow \cdot t, r \}$$

$$I_4 = \text{Goto}(I_0, s)$$

$$= \{ S \rightarrow s \cdot \sigma, \$$$

$$L \rightarrow s \cdot , t/p$$

$$\}$$

$$I_5 = \text{Goto}(I_0, a)$$

$$= \{ L \rightarrow a \cdot Mb, t/p$$

$$M \rightarrow \cdot t , b$$

$$\}$$

$$I_6 = \text{Goto}(I_0, t)$$

$$= \{ L \rightarrow t \cdot , t/p \}$$

$$I_7 = \text{Goto}(I_2, M)$$

$$S \rightarrow LM \cdot , \$ \}$$

$$I_8 = \text{Goto}(I_2, p)$$

$$= \{ S \rightarrow Lp \cdot , \$ \}$$

$$I_9 = \text{Goto}(I_2, t)$$

$$= \{ M \rightarrow t \cdot , \$ \}$$

$$I_{10} = \text{Goto}(I_3, L)$$

$$= \{ S \rightarrow qL \cdot \sigma , \$ \}$$

$$I_{11} = \text{Goto}(I_3, s)$$

$$= \{ S \rightarrow qS \cdot p , \$$$

$$L \rightarrow S \cdot , \sigma$$

$$\}$$

$$I_{12} = \text{Goto}(I_3, a)$$

$$= \{ L \rightarrow a \cdot Mb , \sigma$$

$$M \rightarrow \cdot t , b$$

$$\}$$

$$I_{13} = \text{Goto}(I_3, t) = \{ L \rightarrow t., \gamma \}$$

$$I_{14} = \text{Goto}(I_4, \gamma) = \{ S \rightarrow sr., \$ \}$$

$$I_{15} = \text{Goto}(I_5, M) = \{ L \rightarrow aM.b, t \}$$

$$I_{16} = \text{Goto}(I_5, t) = \{ M \rightarrow t., b \}$$

$$I_{17} = \text{Goto}(I_{10}, \gamma) = \{ S \rightarrow qLr., \$ \}$$

$$I_{18} = \text{Goto}(I_{11}, p) = \{ S \rightarrow qsp., \$ \}$$

$$I_{19} = \text{Goto}(I_{12}, M) = \{ L \rightarrow aM.b, \gamma \}$$

$$\text{Goto}(I_{12}, t) = I_{16}$$

$$I_{20} = \text{Goto}(I_{15}, b) = \{ L \rightarrow aMb., t \}$$

$$I_{21} = \text{Goto}(I_{19}, b) = \{ L \rightarrow aMb., \gamma \}$$

Matching cores

1) I_5, I_{12}

2) I_6, I_{13}

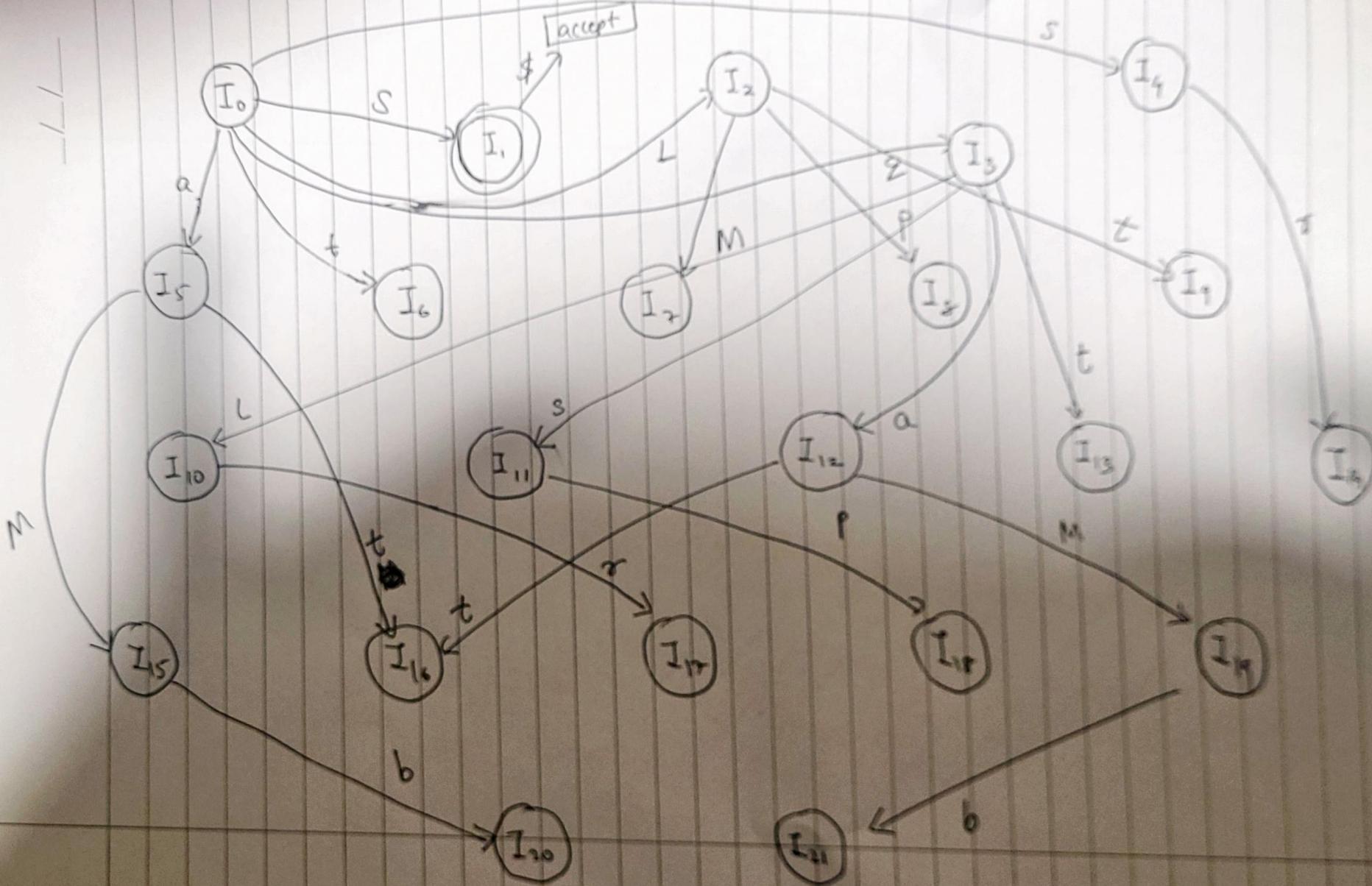
3) I_9, I_{16}

4) I_{15}, I_{19}

5) I_{20}, I_{21}

$$\begin{aligned}\text{FIRST}(S') &= \{a, s, a, t\} \\ \text{FIRST}(S) &= \{q, s, a, t\} \\ \text{FIRST}(L) &= \{a, s, t\} \\ \text{FIRST}(M) &= \{t\}\end{aligned}$$

$$\begin{aligned}\text{FOLLOW}(S') &= \{\$\} \\ \text{FOLLOW}(S) &= \{\$\} \\ \text{FOLLOW}(L) &= \{\cancel{b}, \$, p, o\} \{p, r, t\} \\ \text{FOLLOW}(M) &= \{b, \$\}\end{aligned}$$



LALR collection

$$I_0 = \{ S' \rightarrow \cdot S, \$ \\ S \rightarrow \cdot LM, \$ \\ S \rightarrow \cdot Lp, \$ \\ S \rightarrow \cdot q Lr, \$ \\ S \rightarrow \cdot sr, \$ \\ S \rightarrow \cdot q sp, \$ \\ L \rightarrow \cdot a Mb, t/p \\ L \rightarrow \cdot s, t/p \\ L \rightarrow \cdot t, t/p \}$$

$$I_1 = \text{Goto}(I_0, S) = \{ S' \rightarrow S \cdot, \$ \}$$

$$I_2 = \text{Goto}(I_0, L) = \{ S \rightarrow L \cdot M, \$ \\ S \rightarrow L \cdot p, \$ \\ M \rightarrow \cdot t, \$ \}$$

$$I_3 = \text{Goto}(I_0, q) = \{ S \rightarrow q \cdot Lr, \$ \\ S \rightarrow q \cdot sp, \$ \\ L \rightarrow \cdot a Mb, r \\ L \rightarrow \cdot s, r \\ L \rightarrow \cdot t, r \}$$

$$I_4 = \text{Goto}(I_0, s) = \{ S \rightarrow s \cdot r, \$ \\ L \rightarrow s \cdot, t/p \}$$

$$I_{5,12} = \{ L \rightarrow a \cdot Mb, t/p/r \\ M \rightarrow \cdot t, b \}$$

$$I_{6,13} = \{ L \rightarrow t \cdot, t/p/r \}$$

$I_7 = \{ S \rightarrow LM\cdot, \$ \}$

$I_8 = \{ S \rightarrow Lp\cdot, \$ \}$

$I_{9,16} = \{ M \rightarrow t\cdot, \$/b \}$

$I_{10} = \{ S \rightarrow qL\cdot r, \$ \}$

$I_{11} = \{ S \rightarrow qs.p, \$ \\ L \rightarrow s\cdot, r \}$

$I_{14} = \{ S \rightarrow sr\cdot, \$ \}$

$I_{15,19} = \{ L \rightarrow aM.b, t/p/r \}$

$I_{17} = \{ S \rightarrow qLr\cdot, \$ \}$

$I_{18} = \{ S \rightarrow qsp\cdot, \$ \}$

$I_{20,21} = \{ L \rightarrow aMb\cdot, t/p/r \}$

LALR parsing table

	ACTION							GO TO			
	p	q	r	s	t	a	b	\$	s	l	m
0		S3		S4		S6,13		S5,12		1	2
1									acc		
2	S8					S9,16				6	7
3				S11		S6,13		S5,12			10
4	r7		S14			r7					
5,12					S16,9						15,19
6,13	r8			r8		r8					
7									r1		
8									r2		
9,16								r9	r9		
10			S7								
11	S18		r7								
14								r4			
15,19								S20,21			
17								r3			
18								r5			
20,21	r6			r6		r6					

Problem 3:

Instructions to run the code

1. Paste the input text in the file `input.txt`
2. Go to directory problem3 and execute the following command
`./run.sh`