### HW3

#### February 17, 2024

```
import pandas as pd
import numpy as np
import matplotlib.pyplot as plt
%matplotlib inline
from sklearn.metrics import accuracy_score, confusion_matrix
from sklearn.tree import DecisionTreeClassifier
from sklearn.ensemble import AdaBoostClassifier
import sklearn
pd.set_option('use_inf_as_na', True)
from collections import Counter
from functools import partial
import _pickle as cPickle

from tqdm import tqdm # to measure progress of for loops
```

/var/folders/sp/wlr6xm297918vx6kjh2z1dk00000gn/T/ipykernel\_15151/3896996703.py:9 : FutureWarning: use\_inf\_as\_na option is deprecated and will be removed in a future version. Convert inf values to NaN before operating instead. pd.set\_option('use\_inf\_as\_na', True)

```
[2]: raw_data = pd.read_pickle(r'dataset.pkl')
data = raw_data[raw_data['market_cap'] > 1000.0]
data = data.copy()
data.fillna(0.0,inplace=True)
```

```
[3]: def f(x):
    if x > 0.01:
        return 1
    elif x < -0.025:
        return -1
    else:
        return 0</pre>
```

```
[4]: data['rel_performance'] = data['pred_rel_return'].apply(f)
data.reset_index(inplace=True)
data.set_index('date',inplace=True)
```

```
[5]: from sklearn.preprocessing import MinMaxScaler,StandardScaler scaler = StandardScaler()
```

## Long term performance with AdaBoostClassifier and Finding Optimal Hyperparameters

```
[6]: start_dates = [pd.to_datetime('2001-01-01') + pd.DateOffset(months = 3*i) for i

in range(57)]
end_dates = [d + pd.DateOffset(months = 36) for d in start_dates]
```

#### [8]: training\_frames[0]

[8]:		ticker		actq	apq	а	ıtq	ceqq	cheq	\
	date									
	2001-01-04	FD0	76	32.484	356.469	1285.3	371	831.212	0.207	
	2001-01-04	FUJIY	1162	25.204	1406.343	20778.2	250	14726.288	6193.500	
	2001-01-04	NRG	67	72.658	263.108	5978.9	92	1462.088	107.378	
	2001-01-04	UBS		0.000	233964.000	585134.0	000	21388.937	43090.067	
	2001-01-05	THC	352	29.000	696.000	13121.0	000	4584.000	187.000	
	•••	•••			•••	•••		•••		
	2003-12-23	MITSY	3346	32.887	14015.209	58080.0	35	8214.489	6844.386	
	2003-12-23	SVU	196	32.064	1256.227	6117.3	881	2142.161	52.274	
	2003-12-24	CBK	12	22.502	4.599	200.8	342	175.700	72.022	
	2003-12-24	MU	236	39.100	435.800	7552.1	.00	5429.100	1172.000	
	2003-12-30	GFI	39	92.700	93.900	2466.9	00	1450.000	133.600	
		со	cogsq		q cshfdq	cshiq	•••	sector_cod	e_817.0 \	
	date						•••			
	2001-01-04	535.	734	171.2910	172.062	183.752	•••		0	
	2001-01-04	3621.	778	514.6260	514.626	514.626	•••		0	
	2001-01-04	523.	676	165.8610	182.030	180.001	•••		0	
	2001-01-04	2701.	902	395.0820	407.438	431.698	•••		0	
	2001-01-05	2409.	000	313.7930	325.726	320.250	•••		0	
		•••		•••		•••		•••		
	2003-12-23	50523.	573	79.096	79.114	79.184	•••		0	
	2003-12-23	4024.	789	133.8083	3 135.862	150.670	•••		0	
	2003-12-24	62.	210	37.712	38.705	42.204	•••		0	
	2003-12-24	526.	700	614.7000	636.600	609.100			0	
	2003-12-30	295.	300	471.8140	495.211	472.365	•••		0	

```
date
2001-01-04
                              0
                                                   0
                                                                        0
                                                                        0
2001-01-04
                              0
                                                   0
                              0
                                                                        0
2001-01-04
                                                   0
2001-01-04
                              0
                                                                        0
                                                   1
2001-01-05
                              0
                                                                        0
                                                   0
2003-12-23
                              0
                                                   0
                                                                        0
                                                                        0
2003-12-23
                              0
                                                   0
2003-12-24
                              0
                                                   0
                                                                        0
2003-12-24
                              0
                                                   0
                                                                        0
2003-12-30
                              0
                                                   0
                                                                        0
             sector_code_830.0 sector_code_835.0 sector_code_840.0 \
date
2001-01-04
                              0
                                                   0
                                                                        0
2001-01-04
                              0
                                                   0
                                                                        0
2001-01-04
                              0
                                                   0
                                                                        0
                              0
2001-01-04
                                                   0
                                                                        0
2001-01-05
                              0
                                                   0
                                                                        0
2003-12-23
                              0
                                                   0
                                                                        0
2003-12-23
                              0
                                                   0
                                                                        0
                                                                        0
2003-12-24
                              0
                                                   0
2003-12-24
                              0
                                                   0
                                                                        0
                              0
2003-12-30
                                                   0
             sector_code_845.0 sector_code_850.0 rel_performance
date
2001-01-04
                              0
                                                   0
                                                                      1
2001-01-04
                              0
                                                   0
                                                                      1
2001-01-04
                              0
                                                   0
                                                                      1
2001-01-04
                              0
                                                   0
                                                                      0
2001-01-05
                              0
                                                   0
                                                                      1
2003-12-23
                              0
                                                   0
                                                                      0
2003-12-23
                              0
                                                   0
                                                                      1
2003-12-24
                              0
                                                   0
                                                                      1
2003-12-24
                              0
                                                   0
                                                                      1
2003-12-30
                                                   0
                                                                     -1
```

[10831 rows x 733 columns]

```
'rel_performance','pred_rel_return',
                                        'return', 'cum_ret', 'spy_cum_ret'],axis=1)__

¬for d in training frames]
[10]: valid_data = [d.reset_index().drop
                                       (['ticker','date',
                                         'next_period_return',
                                         'spy_next_period_return',
                                         'rel_performance', 'pred_rel_return',
                                        'return', 'cum_ret', 'spy_cum_ret'],axis=1)__
       ofor d in valid frames]
[11]: test_data = [d.reset_index().drop(['ticker', 'date',
                                         'next_period_return',
                                         'spy_next_period_return',
                                         'rel_performance', 'pred_rel_return',
                                        'return', 'cum_ret', 'spy_cum_ret'],axis=1)__
       →for d in test_frames]
[12]: training labels = [d['rel performance'].values for d in training frames]
      valid_labels = [d['rel_performance'].values for d in valid_frames]
[13]: for i in range(len(start_dates)-1):
          float_vars = [x for x in training_data[i].columns if data[x].dtype ==_u
       scaler = StandardScaler()
          training_data[i] = training_data[i].copy()
          valid data[i] = valid data[i].copy()
          test_data[i] = test_data[i].copy()
          training_data[i][float_vars] = scaler.

fit_transform(training_data[i][float_vars])
          valid_data[i][float_vars] = scaler.transform(valid_data[i][float_vars])
          test_data[i][float_vars] = scaler.transform(test_data[i][float_vars])
[14]: import optuna
      from optuna.trial import Trial
      optuna.logging.set_verbosity(optuna.logging.FATAL)
      import warnings
      warnings.filterwarnings("ignore")
     Define two different objective functions (one for accuracy and one for max drawdown).
[15]: def objective_accuracy(trial:
       →Trial,train=None,labels=None,val=None,val labels=None,val rets=None):
          ada_m_depth = trial.suggest_int('max_depth',1,3,step=1)
          ada_n_estimators = trial.suggest_int('n_estimators', 10,100,step=10)
```

```
ada_learning_rate = trial.suggest_float('learning_rate',0.1,0.5, step=0.1)
          ada_clf = AdaBoostClassifier(DecisionTreeClassifier(max_depth=ada_m_depth),
                                        n_estimators=ada_n_estimators,
                                        learning_rate=ada_learning_rate,
                                        algorithm="SAMME.R")
          ada clf.fit(train,labels)
          preds = ada_clf.predict(val)
          accuracy = ada_clf.score(val,val_labels)
          return accuracy
[16]: def max_drawdown(returns):
              local_max = [n for n in range(len(returns)-1) if ((n==0) and___
       ⇒(returns[0] > returns[1])) or
                 ((n > 0) \text{ and } (returns[n-1] < returns[n]) \text{ and}_{n-1}
       ⇔(returns[n+1]<returns[n]))]
              local min = [n for n in range(1,len(returns)) if ((n == len(returns)-1)__
       →and (returns[-1] < returns[-2])) or</pre>
                       (returns[n-1]>returns[n]) and (returns[n+1]>returns[n])]
              def next local min(n):
                  if [m for m in local min if m > n]:
                      return [m for m in local min if m > n][0]
                  else: return None
              drawdowns = [(n,next_local_min(n)) for n in local_max]
              drawdown_values = [returns[n] - returns[m] for (n,m) in drawdowns if m !
       ⇒= Nonel
              if drawdown values:
                  return np.max(drawdown_values)
              else: return 0.0
[17]: def objective_max_drawdown(trial:
       Trial, train=None, labels=None, val=None, val_labels=None, val_rets=None):
          ada_m_depth = trial.suggest_int('max_depth',1,3,step=1)
          ada_n_estimators = trial.suggest_int('n_estimators', 10,100,step=10)
          ada_learning_rate = trial.suggest_float('learning_rate',0.1,0.5, step=0.1)
          ada_clf = AdaBoostClassifier(DecisionTreeClassifier(max_depth=ada_m_depth),
                                        n estimators=ada n estimators,
```

learning\_rate=ada\_learning\_rate,

```
algorithm="SAMME.R")

ada_clf.fit(train,labels)
preds = ada_clf.predict(val)

predicted_rets = preds * val_rets
profit = predicted_rets.sum()

max_draw = max_drawdown(predicted_rets)

return max_draw
```

Find the optimal hyperparameters using each objective

```
[18]: optimal_hyperparameters_accuracy = {}
study_1 = optuna.create_study(direction="maximize")

optimal_hyperparameters_drawdown = {}
study_2 = optuna.create_study(direction="minimize")
```

Find the optimal hyper parameters during the first training period 2001-01-01 to 2004-01-01

{'max\_depth': 3, 'n\_estimators': 50, 'learning\_rate': 0.4} CPU times: user 14min 6s, sys: 8.38 s, total: 14min 14s Wall time: 1min 49s

```
CPU times: user 11min 57s, sys: 6.7 s, total: 12min 4s
     Wall time: 1min 52s
     Open and read the 3 sets of optimal features over the holding period 2003 - 2018
[21]: with open(r'Data for HW 3/shap_features_ada.pkl','rb') as f:
          shap 1 = cPickle.load(f)
      with open(r'Data for HW 3/shap_features_ada_01.pkl','rb') as f:
          shap 2 = cPickle.load(f)
      with open(r'Data for HW 3/shap_features_ada_02.pkl','rb') as f:
          shap_3 = cPickle.load(f)
     0.0.1 For each combination of optimal features and hyperparameters, instantiate the
            AdaBoostClassifier with the features and compute the max drawdown for each
           of them.
     1: Optimal Hyperparameters 1 (Accuracy Objective)
[22]: optimal_hyperparameters_accuracy
[22]: {'max_depth': 3, 'n_estimators': 50, 'learning_rate': 0.4}
[23]: ada_clf_objective =
       -AdaBoostClassifier(DecisionTreeClassifier(max_depth=optimal_hyperparameters_accuracy['max_d
       →n_estimators=optimal_hyperparameters_accuracy['n_estimators'],
       →learning_rate=optimal_hyperparameters_accuracy['learning_rate'])
[24]: classifiers_shap_1 = [ada_clf_objective for i in range(len(start_dates) - 1)]
      classifiers_shap_2 = [ada_clf_objective for i in range(len(start_dates) - 1)]
      classifiers_shap_3 = [ada_clf_objective for i in range(len(start_dates) - 1)]
[25]: def train_classifiers(classifiers, shap_feats):
          scalers = [StandardScaler() for i in range(len(start_dates)-1)]
          opt_training_data = [pd.DataFrame(scalers[i].

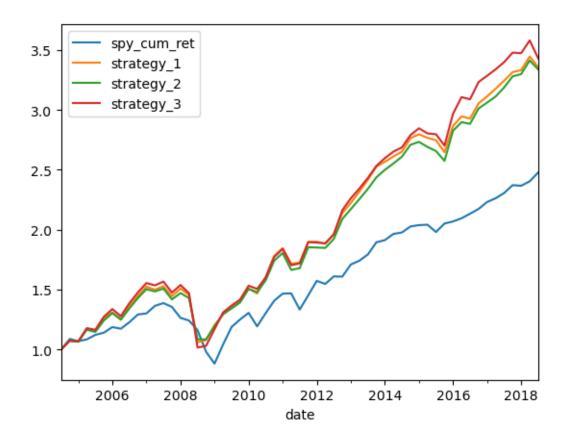
→fit_transform(training_frames[i][shap_feats[i]].
       avalues),columns=shap_feats[i]) for i in range(len(start_dates)-1)]
          opt_valid_data = [pd.DataFrame(scalers[i].

→fit_transform(training_frames[i][shap_feats[i]].
       ovalues),columns=shap_feats[i]) for i in range(len(start_dates)-1)]
          opt_test_data = [pd.DataFrame(scalers[i].
       otransform(test_frames[i][shap_feats[i]].values),columns=shap_feats[i]) for i⊔
       →in range(len(start_dates)-1)]
```

{'max\_depth': 3, 'n\_estimators': 50, 'learning\_rate': 0.2}

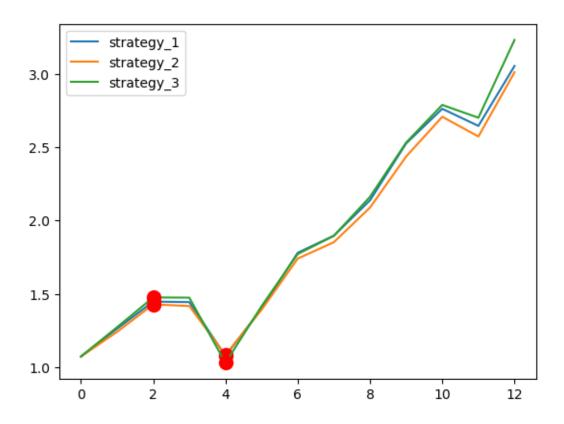
x = [1]ret = []

```
for i in tqdm(range(len(start_dates)-1)):
                  classifiers[i].fit(opt_training_data[i],training_labels[i])
                  preds = classifiers[i].predict(opt_test_data[i])
                  profit_i = (preds*test_frames[i]['next_period_return']).sum()
                  ret.append(profit_i)
                  num_names = len(opt_test_data[i])
                  x.append(x[i] + (x[i]/num_names)*profit_i)
          return x, ret
[26]: # Shap Features Set 1
      x_1, ret_1 = train_classifiers(classifiers_shap_1, shap_1)
     100%|
                                 | 56/56 [19:12<00:00, 20.57s/it]
[27]: # Shap Features Set 2
      x_2, ret_2 = train_classifiers(classifiers_shap_2, shap_2)
     100%|
                                  | 56/56 [17:59<00:00, 19.28s/it]
[28]: # Shap Features Set 3
      x_3, ret_3 = train_classifiers(classifiers_shap_3, shap_3)
     100%|
                                  | 56/56 [03:26<00:00, 3.68s/it]
[29]: # Import and read the SPY dataset
      SPY = pd.read_pickle(r'SPY_cum_ret.pkl')
      SPY = SPY.loc['2004-09-01':'2018-09-30']
      SPY = SPY.resample('Q').ffill()
      SPY['spy_cum_ret'] = (SPY['spy_cum_ret'] - SPY['spy_cum_ret'][0] + 1)
[30]: SPY['strategy_1'] = x_1
      SPY['strategy_2'] = x_2
      SPY['strategy_3'] = x_3
[31]: \# SPY = SPY.iloc[1:].resample('A').bfill()
      SPY.plot();
```



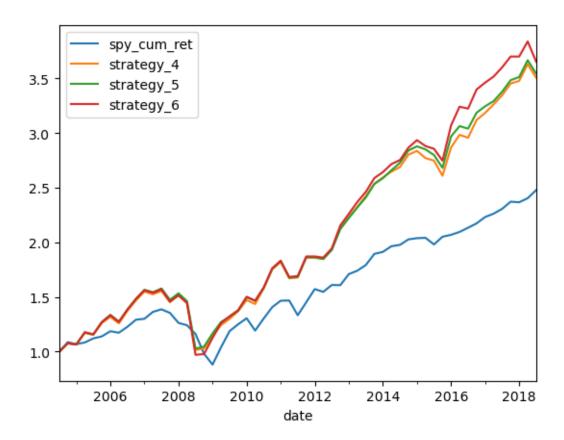
```
[33]: SPY = SPY.iloc[1:].resample('A').bfill()
max_dd_strats(['strategy_1', 'strategy_2', 'strategy_3'])
```

The max drawdown for strategy\_1 is 0.37011133168960764 The max drawdown for strategy\_2 is 0.34521343912984115 The max drawdown for strategy\_3 is 0.4469098856398048



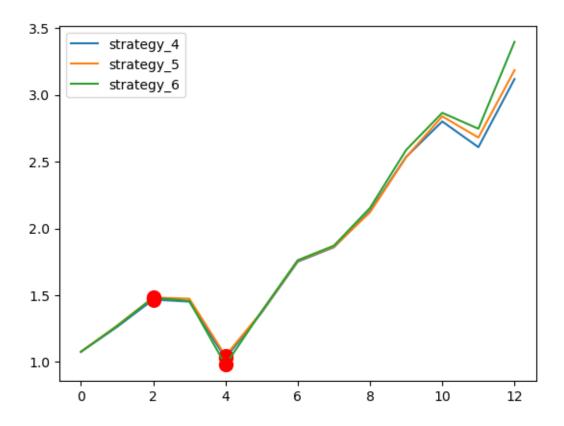
```
[34]: def sharpe_ratio_strats(strat_labels):
         for strat in strat_labels:
              strategy_mean_ret = (SPY[strat] - 1).diff().mean()
              strategy_std = (SPY[strat] - 1).diff().std()
              strategy_sr = strategy_mean_ret/strategy_std
              print(f'The Sharpe Ratio for {strat} is: {strategy_sr}')
[35]: SPY = SPY.resample('Y').ffill()
      sharpe_ratio_strats(['strategy_1', 'strategy_2', 'strategy_3'])
     The Sharpe Ratio for strategy_1 is: 0.7755875462339834
     The Sharpe Ratio for strategy_2 is: 0.7844852507777246
     The Sharpe Ratio for strategy_3 is: 0.7400953034232775
     2: Optimal Hyperparameters 2 (Max Drawdown Objective)
[36]: optimal_hyperparameters_drawdown
[36]: {'max_depth': 3, 'n_estimators': 50, 'learning_rate': 0.2}
[37]: ada_clf_objective =
       -AdaBoostClassifier(DecisionTreeClassifier(max_depth=optimal_hyperparameters_drawdown['max_d
```

```
n_estimators=optimal_hyperparameters_drawdown['n_estimators'],
       →learning_rate=optimal_hyperparameters_drawdown['learning_rate'])
[38]: classifiers_shap_1 = [ada_clf_objective for i in range(len(start_dates) - 1)]
      classifiers_shap_2 = [ada_clf_objective for i in range(len(start_dates) - 1)]
      classifiers_shap_3 = [ada_clf_objective for i in range(len(start_dates) - 1)]
[39]: # Shap Features Set 1
      x_4, ret_4 = train_classifiers(classifiers_shap_1, shap_1)
     100%|
                                 | 56/56 [19:09<00:00, 20.52s/it]
[40]: # Shap Features Set 2
      x_5, ret_5 = train_classifiers(classifiers_shap_2, shap_2)
     100%|
                                 | 56/56 [14:36<00:00, 15.65s/it]
[41]: # Shap Features Set 3
      x_6, ret_6 = train_classifiers(classifiers_shap_3, shap_3)
                                 | 56/56 [02:36<00:00, 2.79s/it]
     100%|
[42]: # Import and read the SPY dataset
      SPY = pd.read_pickle(r'SPY_cum_ret.pkl')
      SPY = SPY.loc['2004-09-01':'2018-09-30']
      SPY = SPY.resample('Q').ffill()
      SPY['spy_cum_ret'] = (SPY['spy_cum_ret'] - SPY['spy_cum_ret'][0] + 1)
[43]: SPY['strategy_4'] = x_4
      SPY['strategy_5'] = x_5
      SPY['strategy_6'] = x_6
[44]: SPY.plot();
```



```
[45]: SPY = SPY.iloc[1:].resample('A').bfill()
max_dd_strats(['strategy_4', 'strategy_5', 'strategy_6'])
```

The max drawdown for strategy\_4 is 0.438210267409908 The max drawdown for strategy\_5 is 0.4370627807089724 The max drawdown for strategy\_6 is 0.5030831108135541



```
[46]: SPY = SPY.resample('Y').ffill()
sharpe_ratio_strats(['strategy_4', 'strategy_5', 'strategy_6'])
```

The Sharpe Ratio for strategy\_4 is: 0.7026551977035782 The Sharpe Ratio for strategy\_5 is: 0.7242743678519502 The Sharpe Ratio for strategy\_6 is: 0.706931084267567

# 0.1 Now we choose the optimal features and optuna objective from the above that gives us a good Sharpe ratio and small max drawdown.

From the performances above we can conclude that strategy 3 (i.e. Shap feature set 3 and hyper parameters optained using the accuracy for the Optuna objective) gives the desired values.

As in previous homeworks, we can change the labels to see if we can improve our strategy:

We insert a column in the dataset where entries are:

- 2 if the stock return is more than 5% higher than the SPY return
- 1 if it is between 1% and 5% higher than the SPY return
- 0 if it is between -2.5% and +1% relative to the SPY return
- -1 if it is below -2.5% relative to the SPY return

```
[47]: # function to return appropriate values based on performance as detailed above def f_2(x):
```

```
if x > 0.05:
             return 2
         elif x > 0.01:
             return 1
         elif x > -0.025:
             return 0
         else:
             return -1
     Import data, make labels, split into training, validation, and test frames.
[48]: raw_data = pd.read_pickle(r'dataset.pkl')
     data = raw_data[raw_data['market_cap'] > 1000.0]
     data = data.copy()
     data.fillna(0.0,inplace=True)
[49]: data['rel performance'] = data['pred rel return'].apply(f 2)
     data.reset_index(inplace=True)
     data.set_index('date',inplace=True)
[50]: start_dates = [pd.to_datetime('2001-01-01') + pd.DateOffset(months = 3*i) for i
      \rightarrowin range(57)]
     end_dates = [d + pd.DateOffset(months = 36) for d in start_dates]
[51]: training_frames = [data.loc[d:d+pd.DateOffset(months = 36)] for d in_
      ⇔start_dates]
     valid_frames = [data.loc[d+pd.DateOffset(months = 3):d+pd.DateOffset(months = __
      →6)] for d in end_dates]
     →12)] for d in end_dates]
[52]: training_data = [d.reset_index().drop
                                     (['ticker','date',
                                       'next_period_return',
                                       'spy_next_period_return',
                                       'rel performance', 'pred rel return',
                                      'return', 'cum_ret', 'spy_cum_ret'],axis=1)__

¬for d in training_frames]

[53]: valid_data = [d.reset_index().drop
                                     (['ticker','date',
```

¬for d in valid\_frames]

'next\_period\_return',
'spy\_next\_period\_return',

'rel\_performance','pred\_rel\_return',

'return', 'cum\_ret', 'spy\_cum\_ret'],axis=1)\_\_

```
[54]: test_data = [d.reset_index().drop(['ticker','date',
                                         'next_period_return',
                                         'spy_next_period_return',
                                         'rel_performance', 'pred_rel_return',
                                        'return', 'cum_ret', 'spy_cum_ret'],axis=1)__
       ⇔for d in test_frames]
[55]: training_labels = [d['rel_performance'].values for d in training_frames]
      valid labels = [d['rel performance'].values for d in valid frames]
[56]: for i in range(len(start_dates)-1):
          float_vars = [x for x in training_data[i].columns if data[x].dtype ==_
       scaler = StandardScaler()
          training_data[i] = training_data[i].copy()
          valid_data[i] = valid_data[i].copy()
          test_data[i] = test_data[i].copy()
          training_data[i][float_vars] = scaler.

→fit_transform(training_data[i][float_vars])
          valid_data[i][float_vars] = scaler.transform(valid_data[i][float_vars])
          test_data[i][float_vars] = scaler.transform(test_data[i][float_vars])
     Train the classifiers using the selected shap feature set and optimal hyperparameters.
[57]: optimal_hyperparameters_accuracy
[57]: {'max_depth': 3, 'n_estimators': 50, 'learning_rate': 0.4}
[58]: shap_2[-1]
[58]: Index(['prccq', 'gpmq', 'txpdy', 'bmq', 'oepsxy', 'evmq', 'debt_ebitdaq',
             'invt_actq', 'efftaxq', 'at_turnq',
             'sic_3678', 'ibcy', 'oepf12', 'fqtr_3', 'cshiq', 'dvpspq', 'rect_turnq',
             'int_totdebtq', 'cogsq', 'dvy'],
            dtype='object', length=133)
[59]: ada_clf_objective =
       -AdaBoostClassifier(DecisionTreeClassifier(max depth=optimal hyperparameters accuracy['max d

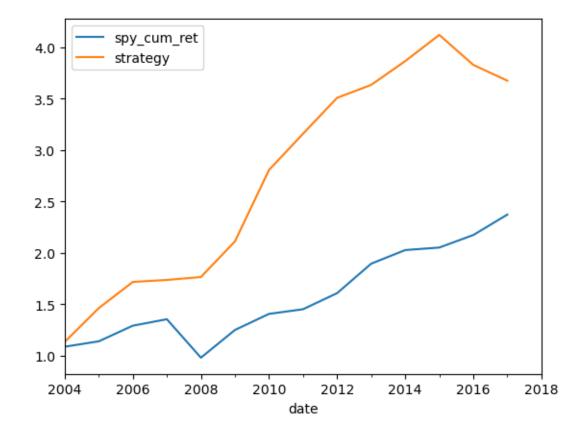
¬n_estimators=optimal_hyperparameters_accuracy['n_estimators'],

       →learning_rate=optimal_hyperparameters_accuracy['learning_rate'])
[60]: classifiers_ada = [ada_clf_objective for i in range(len(start_dates) - 1)]
[61]: x, ret = train_classifiers(classifiers_ada, shap_2)
```

#### Evaluate its performance over the holding period 2004 - 2018

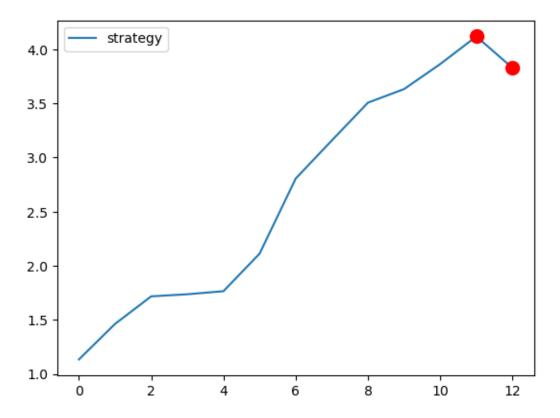
```
[62]: # Import and read the SPY dataset
SPY = pd.read_pickle(r'SPY_cum_ret.pkl')
SPY = SPY.loc['2004-09-01':'2018-09-30']
SPY = SPY.resample('Q').ffill()
SPY['spy_cum_ret'] = (SPY['spy_cum_ret'] - SPY['spy_cum_ret'][0] + 1)
```

/var/folders/sp/wlr6xm297918vx6kjh2z1dk00000gn/T/ipykernel\_15515/1499170714.py:5 : FutureWarning: Series.\_\_getitem\_\_ treating keys as positions is deprecated. In a future version, integer keys will always be treated as labels (consistent with DataFrame behavior). To access a value by position, use `ser.iloc[pos]` SPY['spy\_cum\_ret'] = (SPY['spy\_cum\_ret'] - SPY['spy\_cum\_ret'][0] + 1)

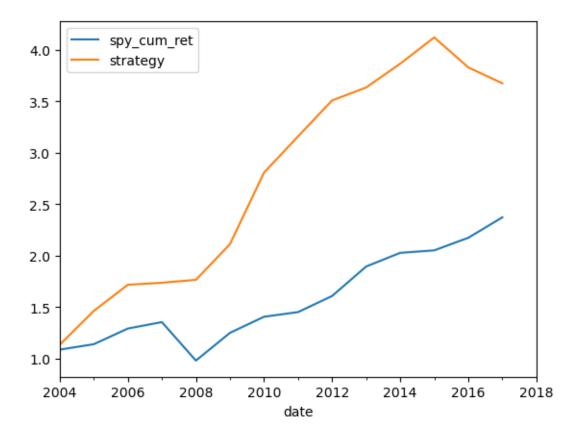


```
[65]: max_dd_strats(['strategy'])
```

The max drawdown for strategy is 0.2915385241818056



```
[66]: SPY = SPY.resample('Y').ffill()
SPY.plot();
```



[67]: sharpe\_ratio\_strats(['strategy'])

The Sharpe Ratio for strategy is: 0.7716614875830043

#### 0.1.1 Conclusion

In conclusion, we had 3 sets of possible features (computed using Shapley values), and 2 different measures for the objective function to find optimal hyperparameters (accuracy and drawdown).

After training and evaluating the models on the 6 possible combinations, we chose the ones that gave us the desired properties. Then we adjusted the labels as in previous homeworks to improve our strategy and finally:

We have found a strategy using an AdaBoostClassifier that has both: - a good Sharpe ratio that is close to 1 ( $\sim$ 0.772), which is a good measure of returns after adjusting for risk - and a small max drawdown ( $\sim$ 0.292) which can help ease investors