



# LMT

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# Notes

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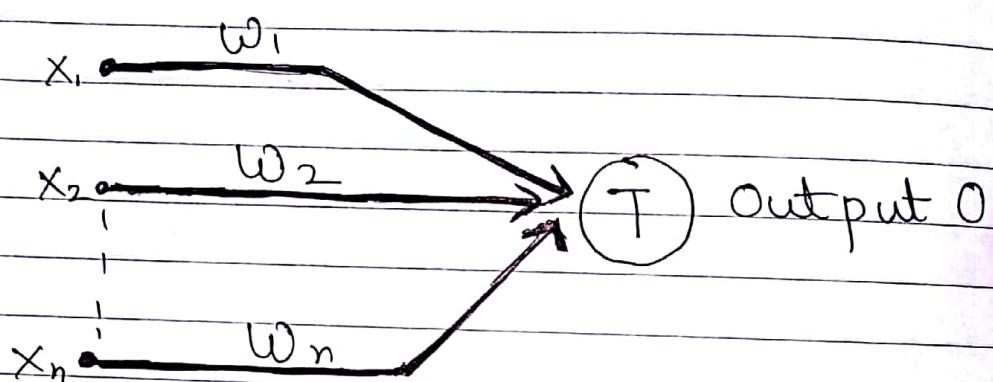
# Soft Computing

Page No.

Date:

## MP Neuron

- 1) This Neuron is known as McCulloch Pitts Neuron
- 2) The Model of this Neuron is as follow :-



$x \rightarrow$  input

$w \rightarrow$  Weights

$O \rightarrow$  Output

- 3) Their are 'n' inputs, having values '0' and '1'.

- 4) The weights may be excitatory

Or inhibitory ( $w = -1$ ) ( $w = +1$ )

5) There is a threshold for each neuron if net input is greater than threshold, then neuron fires

Agar input threshold se jyada hain, then output ayeega.

$$o^{k+1} = \begin{cases} 1 & \text{if } \sum_{i=1}^n w_i x_i \geq T \\ 0 & \text{if } \sum_{i=1}^n w_i x_i < T \end{cases}$$

7) This Neuron can perform basic logic operations such as AND, OR, NOT, etc

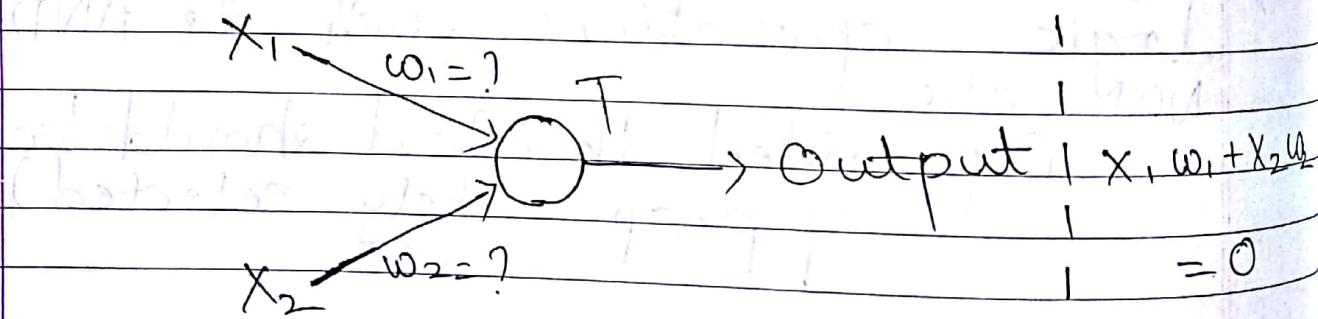
(provided threshold should be appropriately selected)

a) Design two input AND logic using M.P Neuron Model.

→ b) The truth table for AND is given by

	$x_1$	$x_2$	o	Here $x_1, x_2$ are 2 input and o is output
T	0	0	0	
T	0	1	0	
T	1	0	0	
T	1	1	1	

2) The diagram will be as follow



3) Drawing the four cases

a)  $x_1 = 0, x_2 = 0 \Rightarrow y = 0$  (inhibitory)

$$0 < T$$

b)  $x_1 = 1, x_2 = 0 \Rightarrow y = 0$  (inhibitory)

$$\therefore w_1 < T$$

c)  $x_1 = 0 \wedge x_2 = 1 \Rightarrow y = 0$  (inhibitory)

d)  $x_1 = 1 \wedge x_2 = 1 \Rightarrow y = 1$  (Firing)

$$x_1 w_1 + x_2 w_2 > T$$

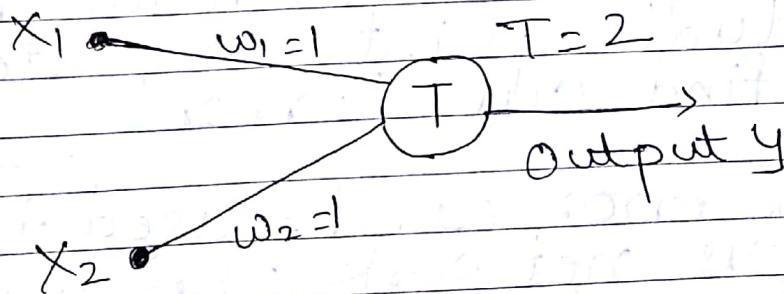
$$\therefore w_1 + w_2 > T$$

//  $w_1$  and  $w_2$  can take value only  
+1 or -1.

∴ Assuming  $w_1 = 1$  and  $w_2 = 1$

We get,  $T = 2$

Hence,



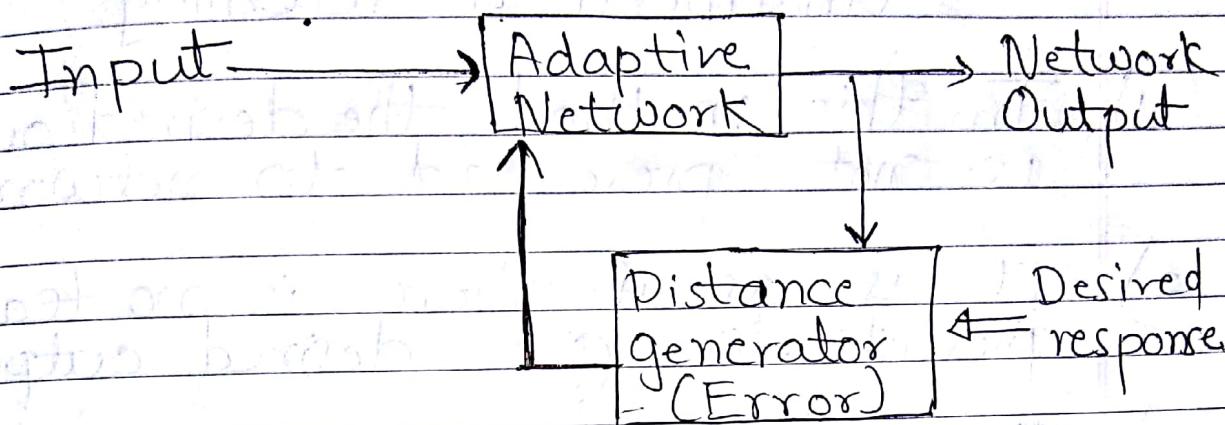
Agar Output is 0 or -1

then  $x_1 w_1 + x_2 w_2 < T$

Or Agar Output is 1 or +1.  
then  $x_1 w_1 + x_2 w_2 > T$

## Learning Method

- 1) Learning is relative permanent change in behaviour brought about by experience.
- 2) Learning in network is response to specific input.
- 3) Learning in network are of three types:-
  - a) Supervised Learning
    - i) Each input has a corresponding output associated with it, which is the target.
    - ii) A comparison is made between the actual point and desired output to find out error.
    - iii) These error can be used to adjust various network parameters like performance of Network.
    - iv) This training is done until the network is able to produce the desired response.
    - v) Weights are adjusted to improve Network performance.



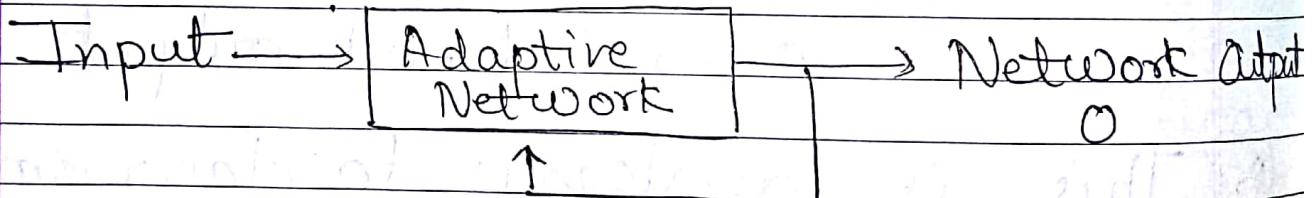
Here,  $p[d, 0]$  is distance function  
where  
 $d \rightarrow$  desired output

$0 \rightarrow$  Network output

- vii) This is analogous to classroom learning with Teacher.

## Unsupervised learning

- 1) In this method, the desired output is not presented to network.
- 2) It is as if there is no teacher is present to give desired output.
- 3) This system learns on its own by discovering features present in input pattern.



- 4) Here No information is available so as to correct the Network.

## Reinforced learning

- Here, a teacher is available, but it does present that whether computed output is correct or incorrect.
- It does not present the desired output.
- A reward is given for correct answer and penalty is given for wrong answer.
- It is used when knowledge required for supervised learning is not available.
- However, it is better method than supervised and unsupervised learning.
- Here system knows output is correct or not, but does not know correct output.

## Linear Separability

- 1) A classification problem, where if input pattern is member of class then desired output is 'Yes' or 'No'
- 2) A 'Yes' represent output signal '1' and 'No' represent output signal '-1' [Bipolar Signal]
- 3) Net input is compared with  

$$\text{net} = b + \sum_{i=1}^n x_i w_i$$
- 4) The boundary between region where  $\text{net} > 0$  and region where  $\text{net} < 0$

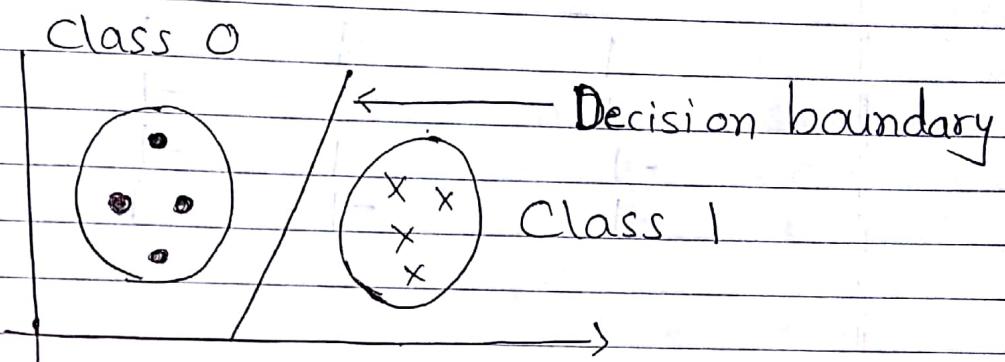
$\text{net} = 0$  — (Line of Separability)

$$\therefore b + \sum_{i=1}^n x_i w_i = 0 // b \rightarrow \underline{\text{bias}}$$

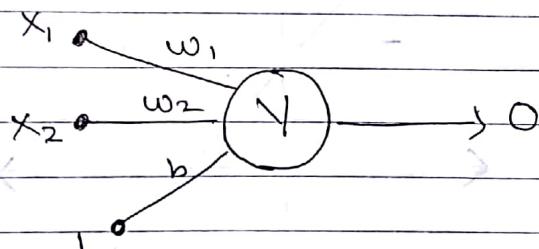
This is also called decision boundary.

- 5) Depending on the no of inputs, the equation can be line or hyperplane.

6) If there exist weights such that all training input  $+1$  lie on one side and  $-1$  lie on other side of boundary, then problem is linearly Separable.



7) Network Can be shown as



Considering two inputs and 2 weights and one bias,

$$\text{net} = x_1 w_1 + x_2 w_2 + b$$

Here, net = 0 — Decision boundary

$$\therefore b + w_1 x_1 + w_2 x_2 = 0$$

$$\therefore \boxed{x_2 = \frac{-w_1}{w_2} x_1 - \frac{b}{w_2}}$$

8)

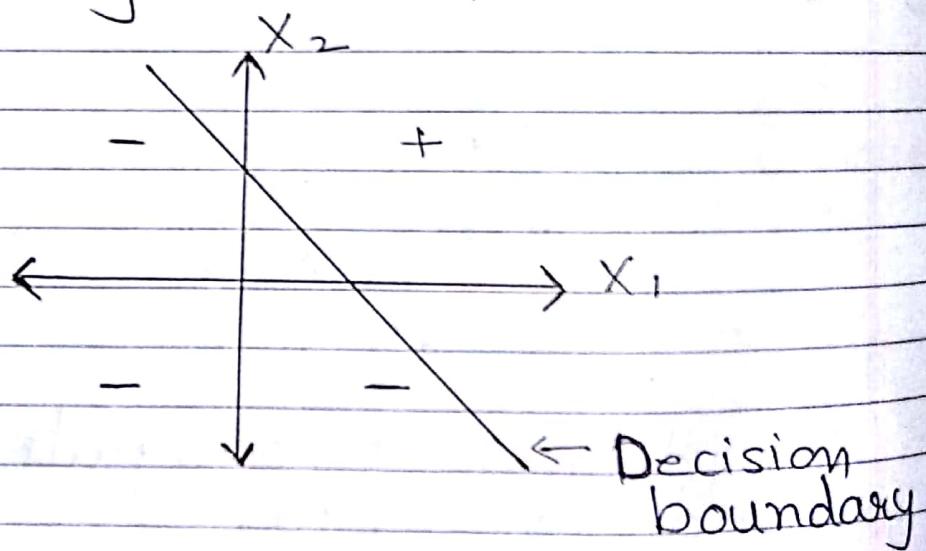
Considering AND function for linear separability

$x_1$ ,  $x_2$  y (Output)

1	1	1
-1	1	-1
-1	-1	-1

9)

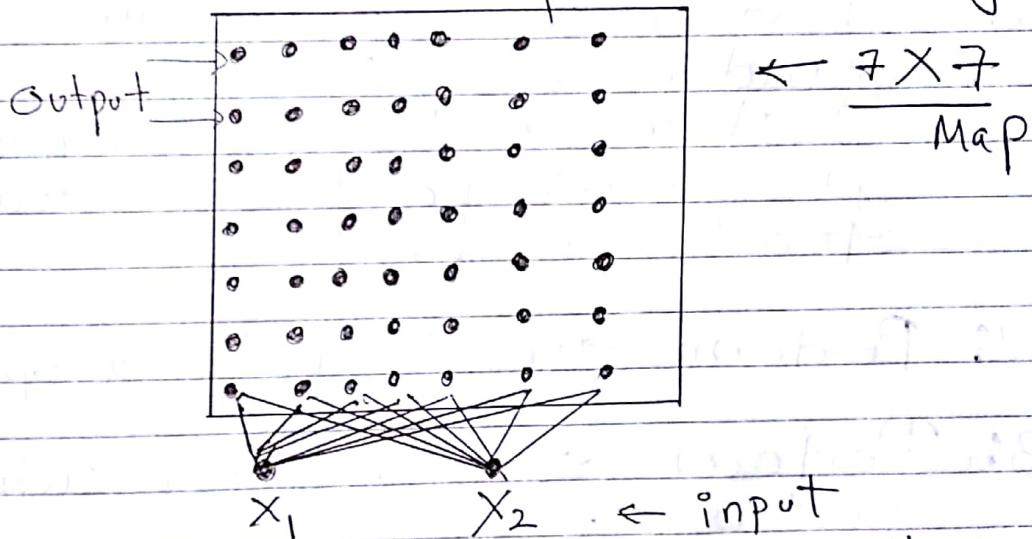
Graphically it can draw as



If the problem could not be solved by single line decision boundary, then the problem is linearly non-separable \*

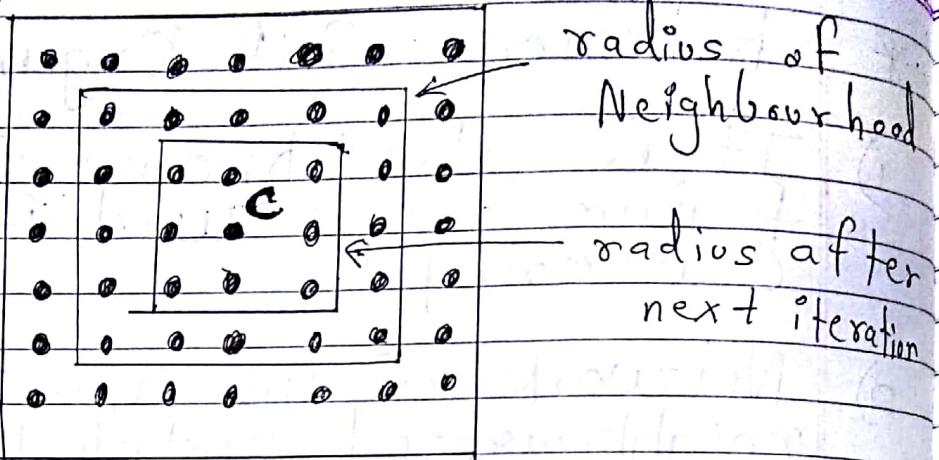
## \* Kohonen's Self Organizing Network

- 1) It is also known as Kohonens feature maps, used for Data Clustering
- 2) Network of this type impose a neighbourhood constraint on output such unit, such that certain property is reflected in output units weight.



- 3) The learning process is similar to that of competitive learning network.
- 4) Here, we update not only winning units' weight but also weight of neighbourhood around winning unit.
- 5) The neighbourhood size decreases with each iteration.

•  $c \rightarrow \text{center}$



## Algorithm

Step1: Initialize the weights at some Random values.

Initialize the learning rate ' $\lambda$ '.  
It should be slow decreasing function of time.

Step2: Perform steps 3-9 till stopping cond.

Step3: Perform steps 4-6 for each input vector  $x$ .

Step4: Compute the square of Euclidean distance

$$D(j) = \sum_{i=1}^n \sum_{j=1}^m (x_i - w_{ij})^2$$

// Distance to make neighbourhood less as per the iterations.

Step 5: Find winning unit index  $J$ ,  $s_0(j)$   
So  $D(j)$  is minimum.

Step 6: For all unit 'j', calculate new  
weights

$$w_{ij} = w_{ij} (\text{old}) + \alpha [x_i - w_{ij} (\text{old})]$$

// This are the neighbours

Step 7: Update learning rate using formula

$$\alpha(t+1) = 0.5(t)$$

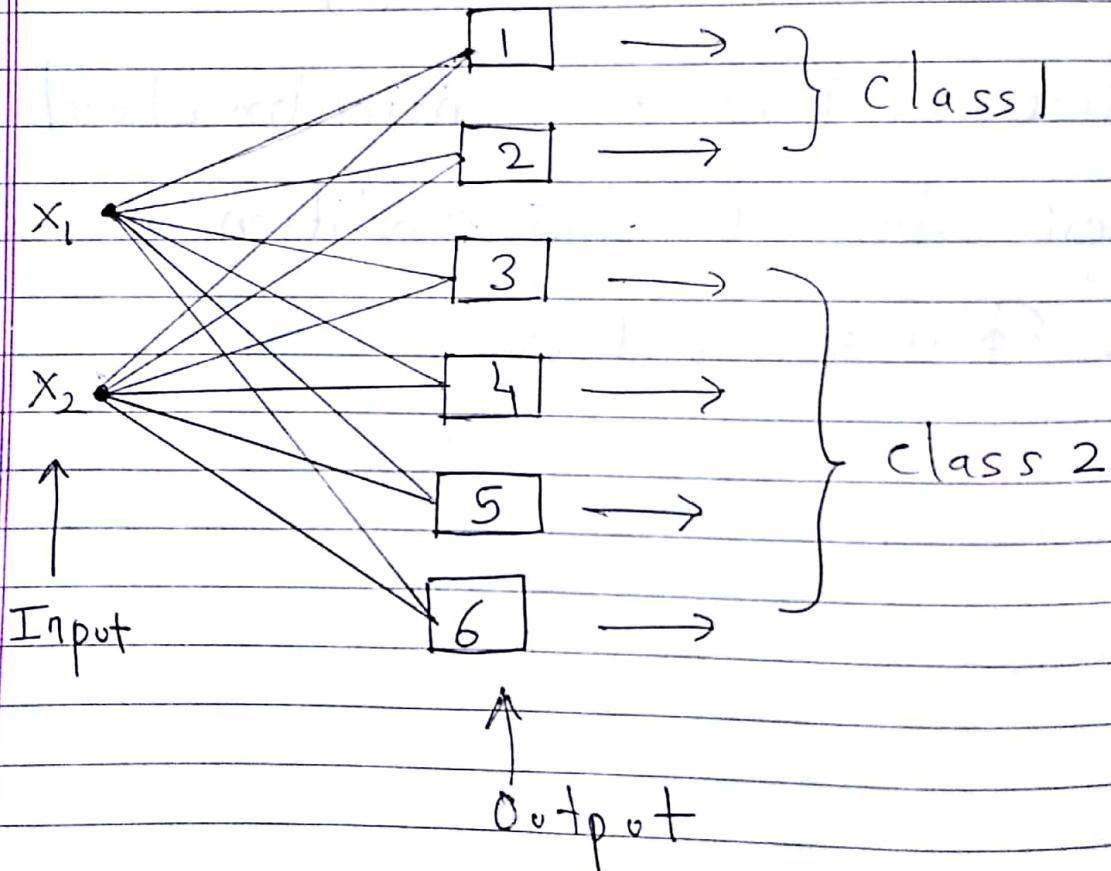
Step 8: Reduce Radius of neighbourhood

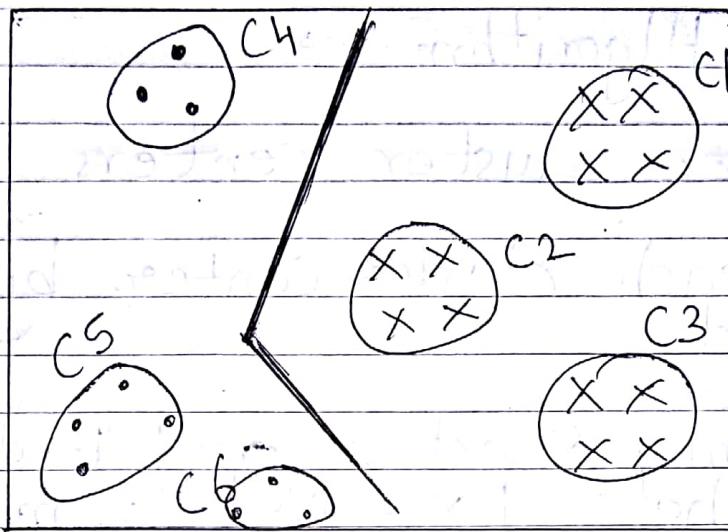
Step 9: Test for stopping condition

Refer Video

# Linear Vector Quantization

- \* LVQ is an adaptive classification method. It is based training data with desired class information.
- \* LVQ employs unsupervised data clustering technique.
- \* LVQ network architecture closely resembles competitive learning technique network.





Here input space is divided into 6 cluster and 2 dimensions.

\* Steps involved in LVQ

Step 1: Locate several cluster centers without using class information.

Step 2: Use class information and fine tune cluster to avoid the misclassification

## LVQ Algorithm :-

- 1) Initialize cluster centers
- 2) Label each cluster center by voting method.
- 3) Randomly select  $X$  and find  $k$  such that  $|X - w_k|$  is minimum.
- 4) If  $X$  and  $w_k$  belong to same class then update  $w_k$  as

$$\Delta w_k = n(X - w_k)$$

$$\Delta w_k = -n(X - w_k)$$

Where,  $X \rightarrow$  input vector

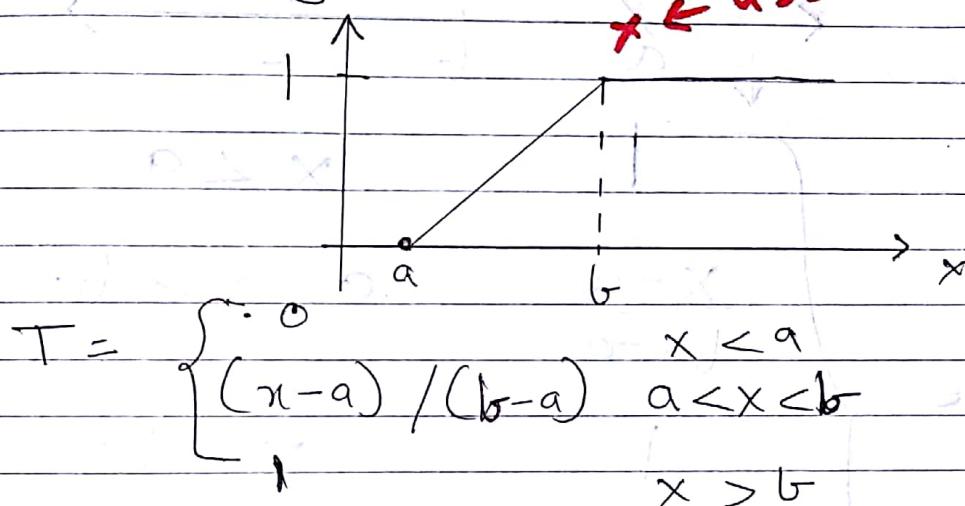
$w \rightarrow$  weight vector

$n \rightarrow$  learning rate

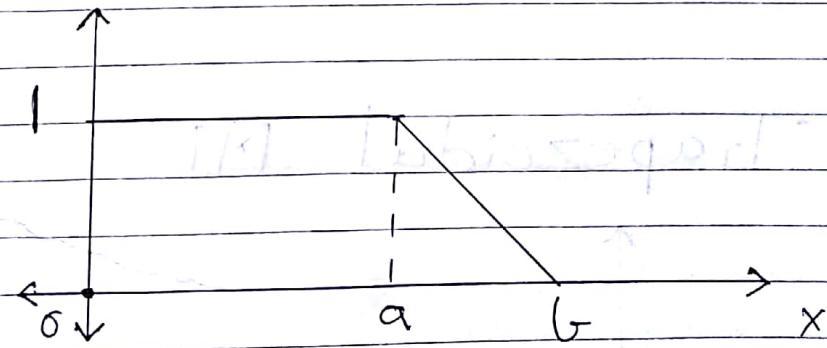
# Fuzzy Set Theory

## Different Membership function (M.F.)

### 1) Increasing M.F



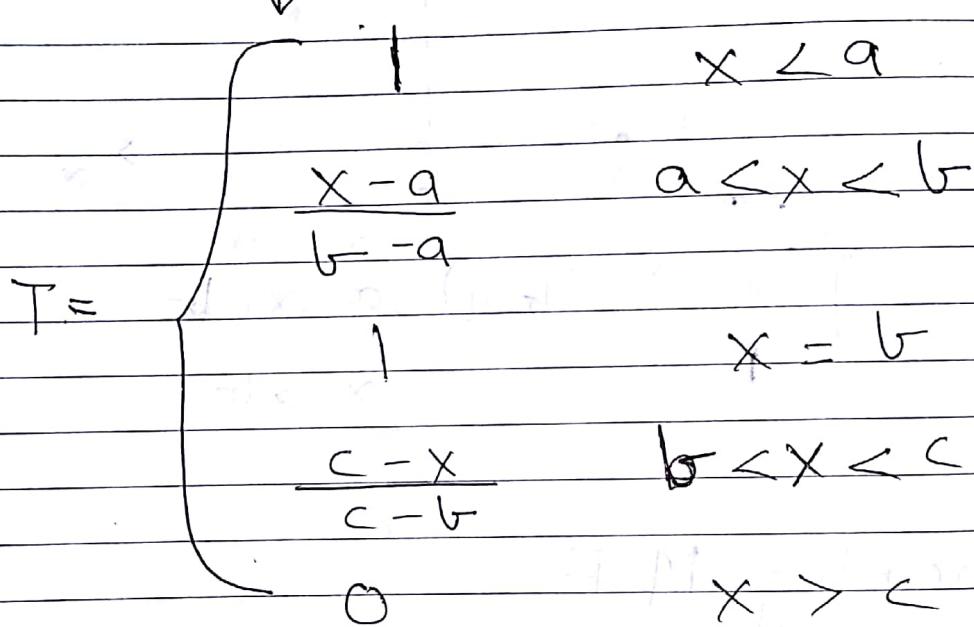
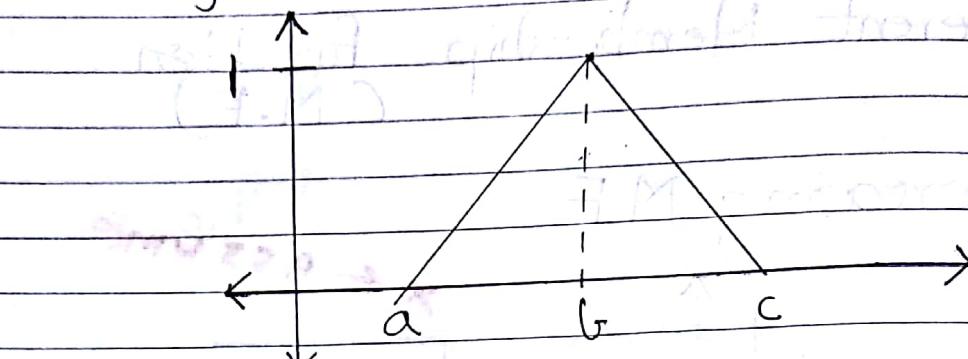
### 2) Decreasing M.F



$$\mu_T(x) = \begin{cases} 1 & x < a \\ (b-x)/(b-a) & a \leq x < b \\ 0 & x > b \end{cases}$$

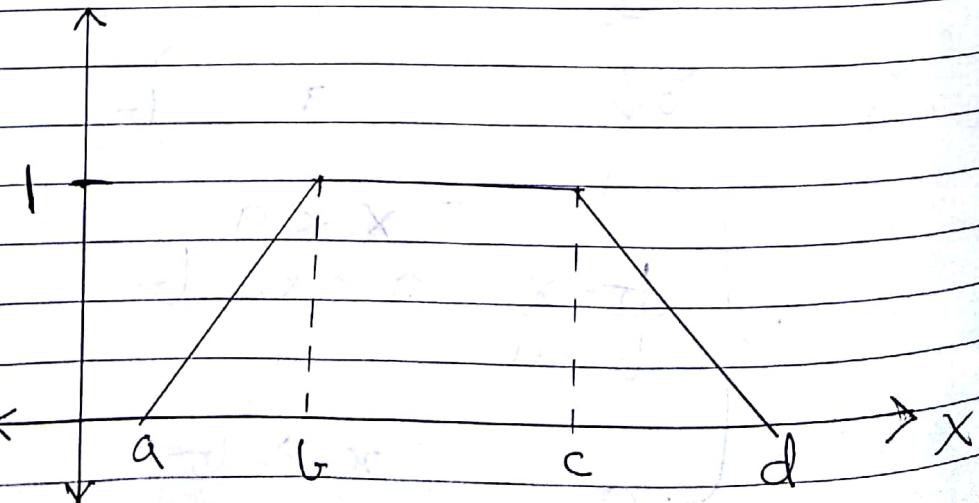
3)

Triangular M.F

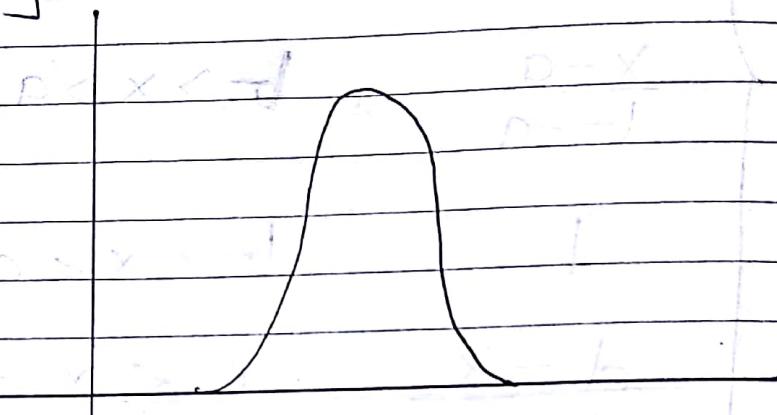


4)

Trapezoidal M.F



6) Cauchy M.F

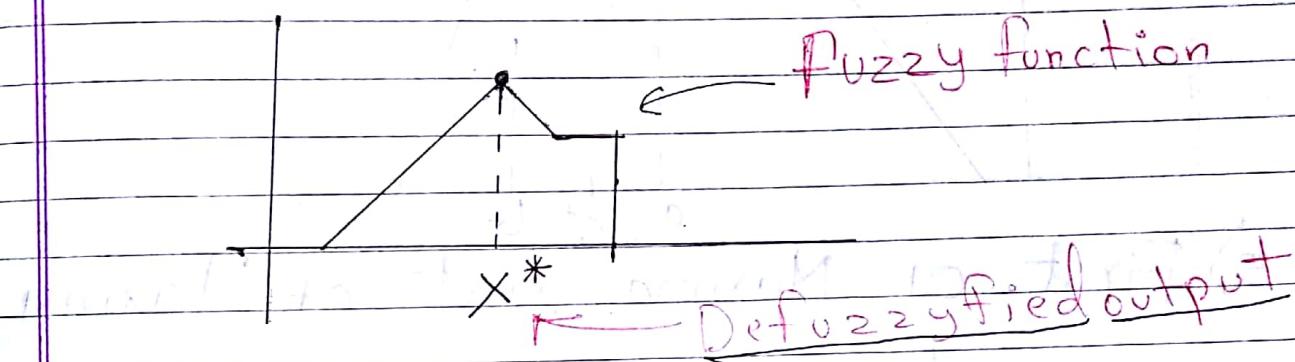


$$C = \frac{1}{1 + \left| \frac{x-c}{a} \right|^{2b}}$$

Defuzzification :- ~~cm = min M~~

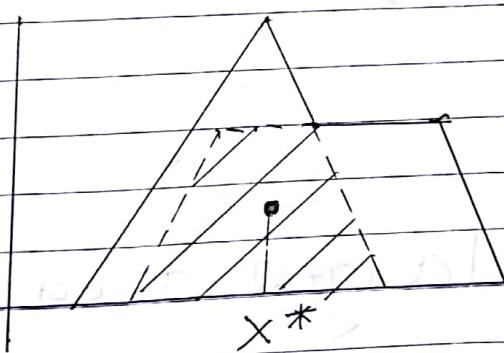
There are total 7 Defuzzification Methods

1) Max Membership Method

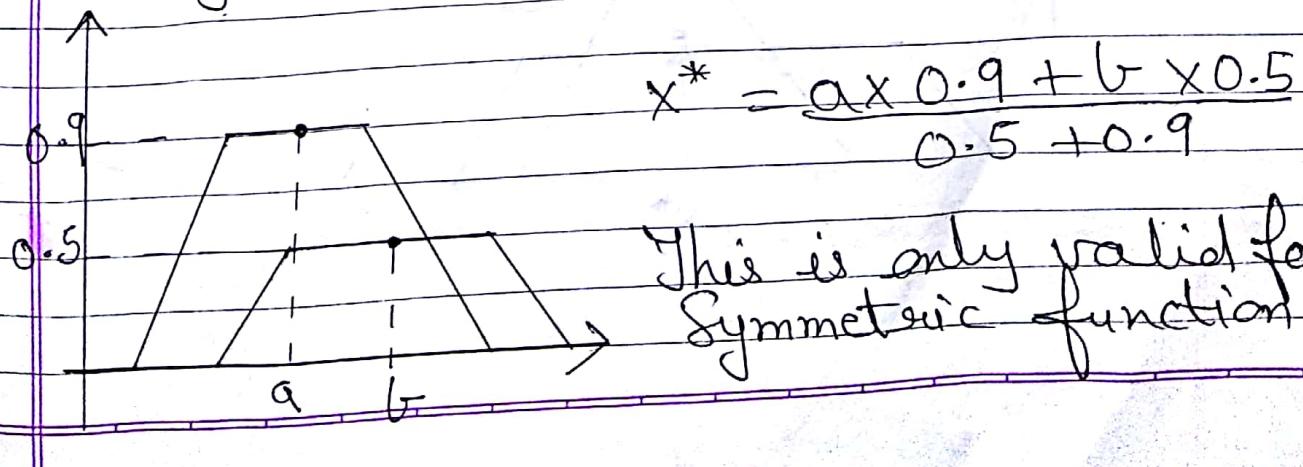


2) Center of Area

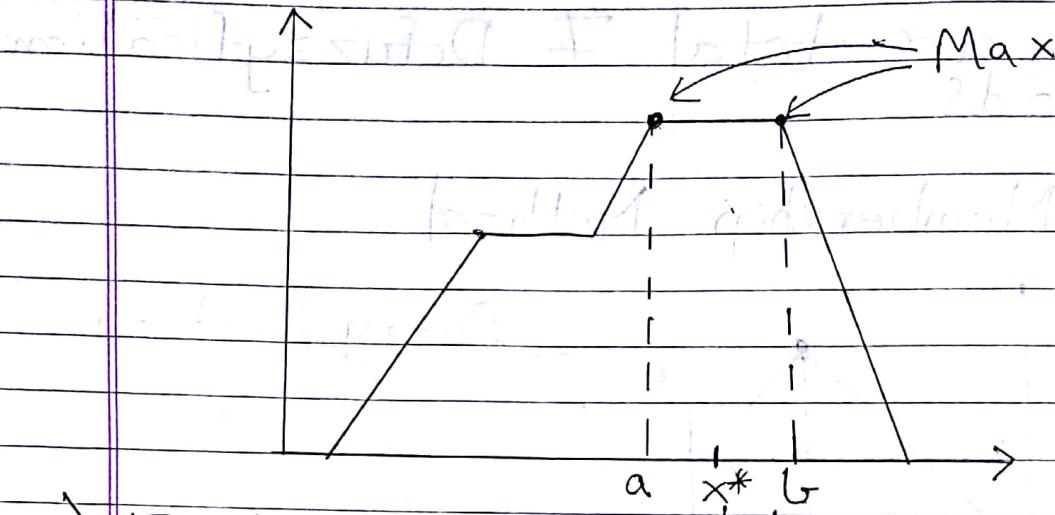
[Area ka Center]



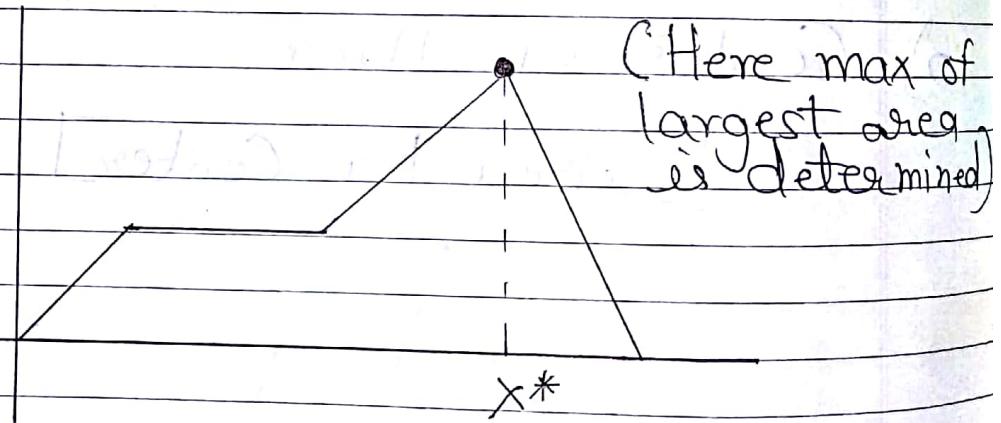
3) Weighted Average Method



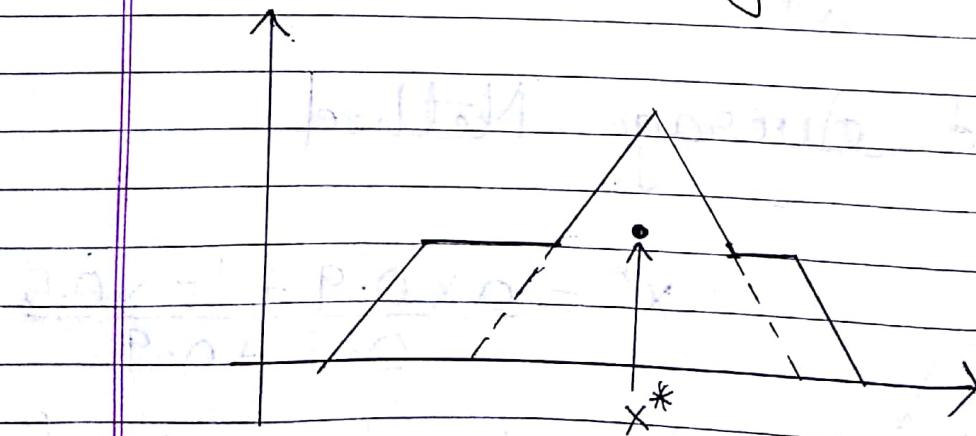
#### 4) Mean - Max Membership



#### 5) First of Maxima / Last of Maxima



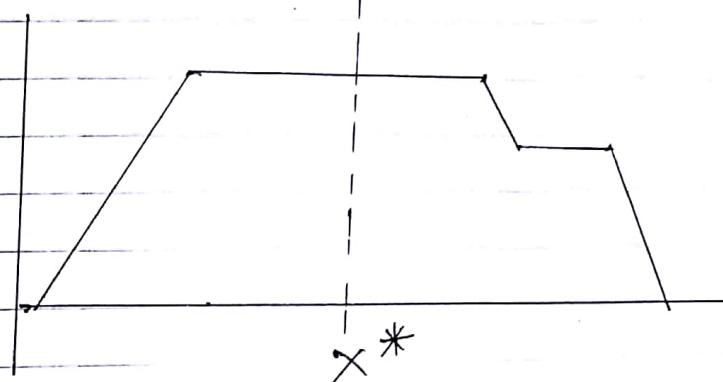
#### 6) Center of largest area



## 7) Bisection Method

Bisection

Bisection of  
function is the  
Defuzzyfied  
Output  
( $x^*$ )



Q)

## Optimization technique

- 1) Optimization techniques are classified as
  - i) Derivative based optimization
  - ii) Derivative free optimization
- 2) Derivative based optimization exploit the derivative value of objective function
- 3) The first order derivative is called as gradient and second is known as hessian matrix.
- 4) These methods cannot be applied to functions which are discontinuous or discrete.
- 5) Examples of Derivative based Optimization
  - i) Descent Method
  - ii) Steepest Descent Method
  - iii) Newton's Method
- 6) Another problem is that this method converge at locally optimal point.

## 7) Steepest Descent Method

$$\theta_{\text{next}} = \theta_{\text{now}} + n d$$

$n \rightarrow$  step size

$d \rightarrow$  direction

$\theta_{\text{next}} \rightarrow$  Next point

$\theta_{\text{now}} \rightarrow$  Current point

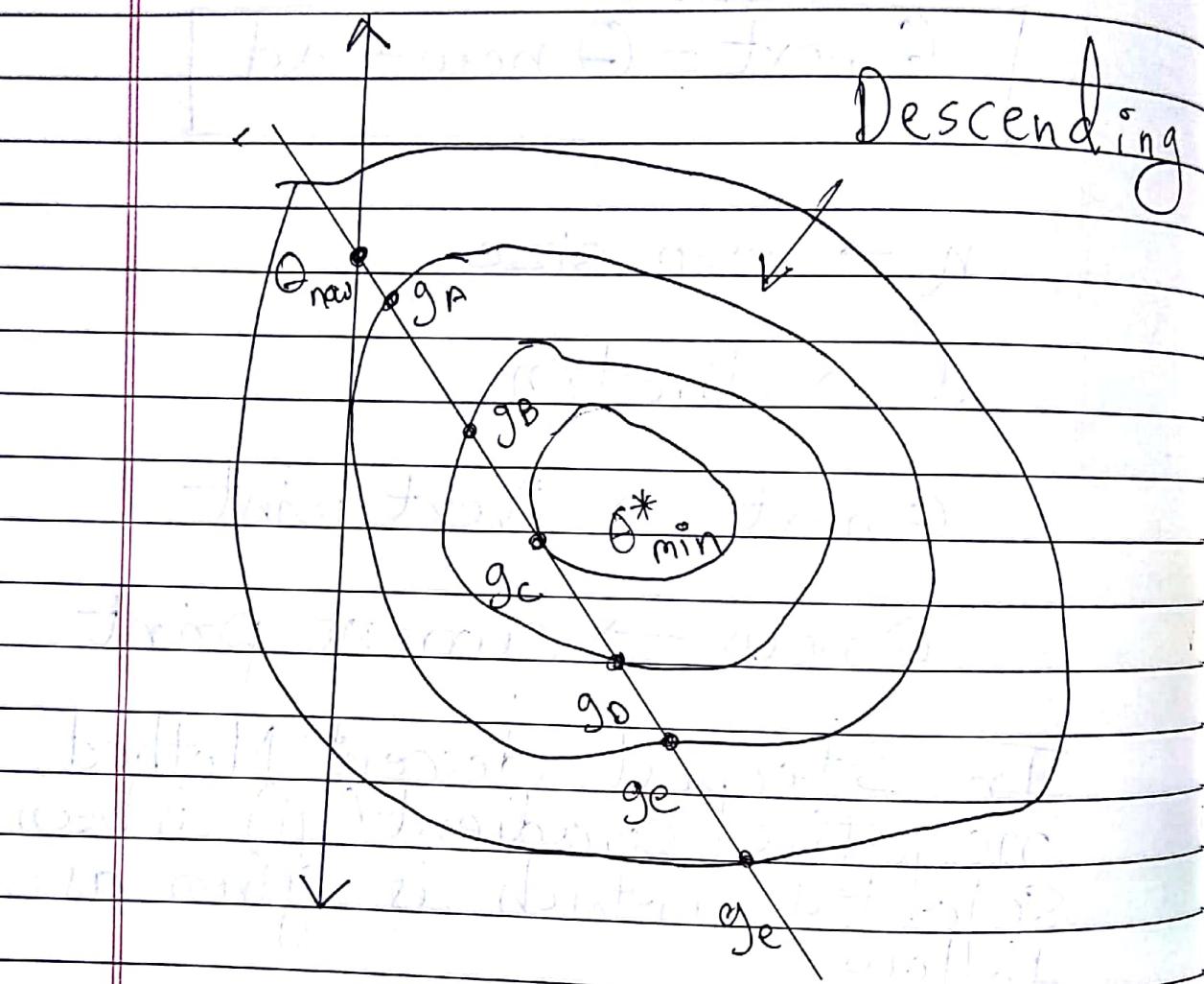
In Steepest descent Method, negative gradient ( $y_i$ ) is been selected, which is given as follow

$$d_i = -g_i$$

$$\therefore \theta_{i+1} = \theta_i - n g_i$$

$$\therefore \phi'(n) = \frac{d}{dn} (\theta_i - n g_i)$$

Testing  $\theta_{i+1}$  for optimality, if optimal then stop, else start again with new iteration



\* Newton's Method :-

Here descent direction by  
second derivative of Activation Function

$$\theta = \theta_{\text{now}} + n_d$$

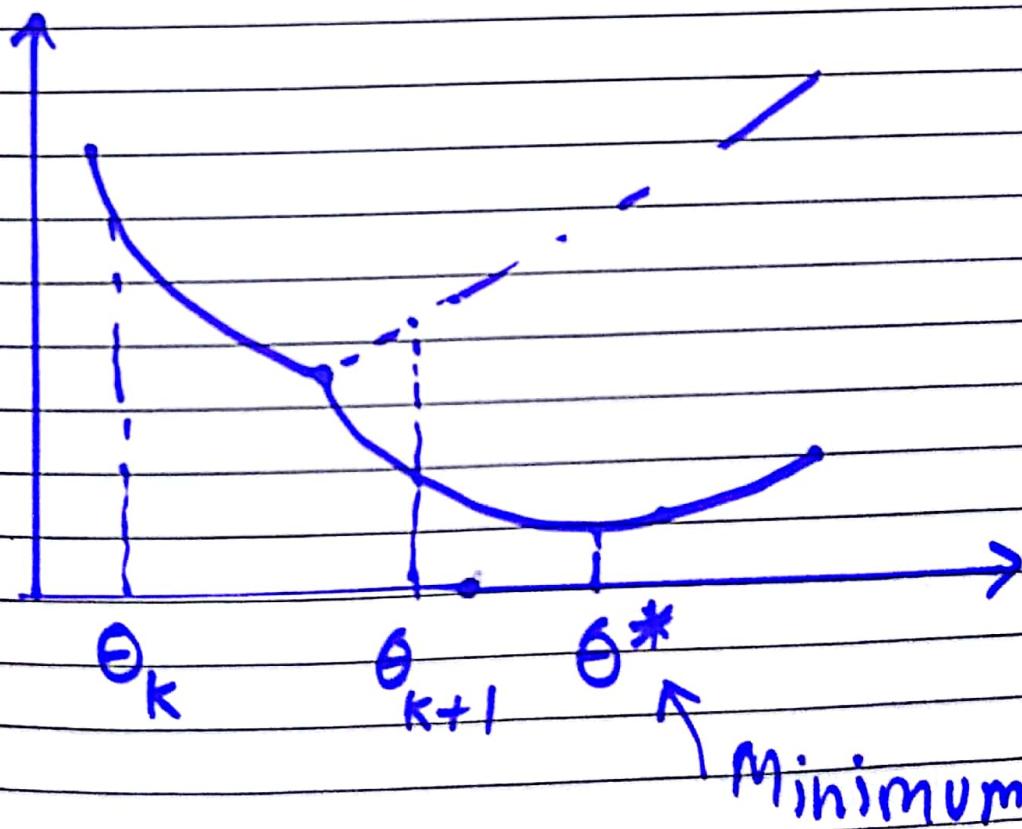
$$\therefore E(\theta) = E(\theta_{\text{now}} + n_d)$$

$$\hat{\theta} = \theta_{\text{now}} - H^{-1}g$$

$-H^{-1}g \rightarrow \text{Newton's step}$

When minimum point  $\hat{\theta}$  of approximated quadratic function is chosen as next point  $\theta_{\text{now}}$ , we call it Newton's Method

when  $n=1$  and  $G=H^{-1}$



Design a controller to determine the wash time of a domestic washing machine. Assume the input is dirt & grease on cloths. Use three descriptors for input variables and five descriptor for output variable. Derive the set of rules for controller action and defuzzification. The design should be supported by figure wherever possible. Show that if the clothes are solid to a larger degree the wash time will be more and vice versa.

## Steps to Solve

- step 1) Identify input and output variables and decide descriptor for the same
- step 2) Define membership functions for each of input and output variables
- step 3) Form a rule base
- step 4) Rule Evaluation
- step 5) Defuzzification

Step 1) Identify input & output variable and decide descriptor

- Here inputs are 'dirt' and 'grease'. Assume they % =
- Output is 'washing' measured in minutes

#### Descriptor for INPUT Variable

DIRT

SD - small dirt

MD - medium dirt

LD - Large dirt

{ SD, MD, LD }

Grease { NG, MG, LG }

NG - NO Grease

MG - Medium Grease

LG - Large Grease

#### Descriptor for Output Variable

Wash time { VS, S, M, L, VL }

VS - { Very short }

S - Short

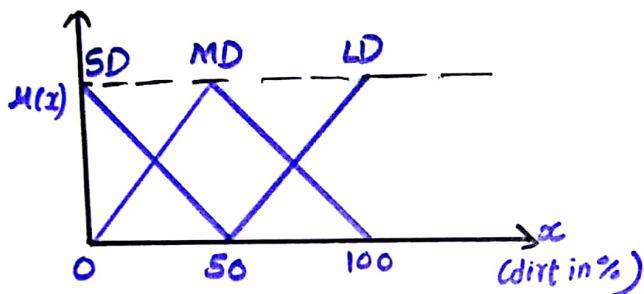
M - Medium

L - Large

VL - Very Large

Step 2) Define membership function for each of the input and Output variable. We use triangular MFs

(1) Membership Function for dirt:

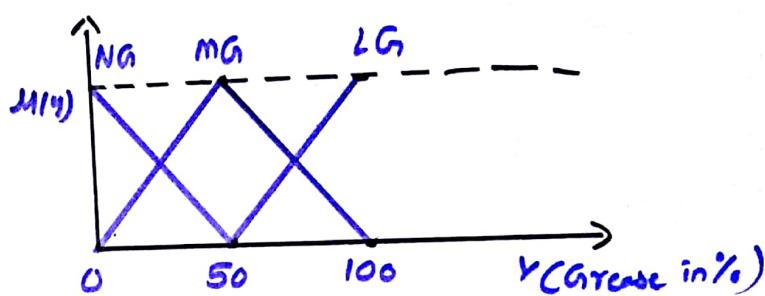


$$\mu_{SD}(x) = \frac{50-x}{50}, \quad 0 \leq x \leq 50$$

$$\mu_{MD}(x) = \begin{cases} \frac{x}{50}, & 0 \leq x \leq 50 \\ \frac{100-x}{50}, & 50 \leq x \leq 100 \end{cases}$$

$$\mu_{LD}(x) = \frac{x-50}{50}, \quad 50 \leq x \leq 100$$

(2) Membership Function for grease:

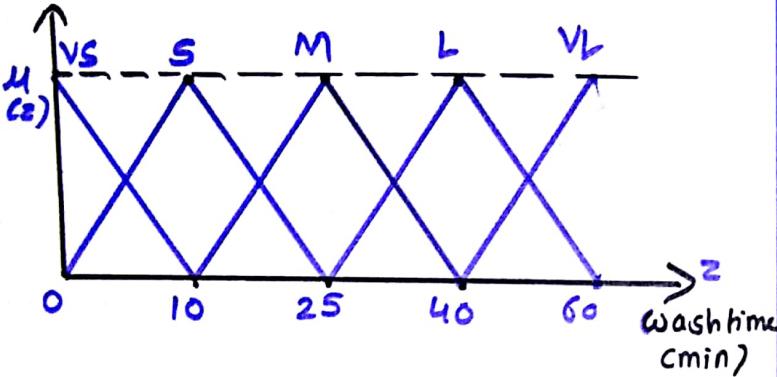


$$\mu_{NG}(y) = \frac{50-y}{50}, \quad 0 \leq y \leq 50$$

$$\mu_{MG}(y) = \begin{cases} \frac{y}{50}, & 0 \leq y \leq 50 \\ \frac{100-y}{50}, & 50 \leq y \leq 100 \end{cases}$$

$$\mu_{LG}(y) = \frac{y-50}{50}, \quad 50 \leq y \leq 100$$

3) Membership function for wash time



$$\mu_{VS}(z) = \frac{10-z}{10}, 0 \leq z \leq 10$$

$$\mu_S(z) = \begin{cases} \frac{z}{10}, & 0 \leq z \leq 10 \\ \frac{25-z}{15}, & 10 \leq z \leq 25 \end{cases}$$

$$\mu_M(z) = \begin{cases} \frac{z-10}{15}, & 10 \leq z \leq 25 \\ \frac{40-z}{15}, & 25 \leq z \leq 40 \end{cases}$$

$$\mu_L(z) = \begin{cases} \frac{z-25}{15}, & 25 \leq z \leq 40 \\ \frac{60-z}{20}, & 40 \leq z \leq 60 \end{cases}$$

$$\mu_{VL}(z) = \frac{z-40}{20}, 40 \leq z \leq 60$$

Step 3 : Form a Rule base

$x \setminus y$	NG	MG	LG
SD	VS	M	L
MD	S	M	L
LD	M	L	VL

#### Step 4) Rule Evaluation

Assume Dirt = 60%, Grease = 70%

Dirt = 60% maps two MFs of dirt ✓

$$\mu_{M0}(x) = \frac{100-x}{50} \quad | \quad \mu_{L0}(x) = \frac{x-50}{50}$$

simly Grease = 70% maps 2 MFs

$$\mu_{Mg}(y) = \frac{100-y}{50} \quad | \quad \mu_{Lg}(y) = \frac{y-50}{50}$$

Evaluate  $\mu_{M0}(x)$  and  $\mu_{L0}(x)$   
for  $x = 60$ , we get

$$\mu_{M0}(x) = \frac{100-60}{50} = \frac{4}{5}$$

$$\mu_{L0}(x) = \frac{60-50}{50} = \frac{1}{5}$$

Evaluate  $\mu_{Mg}(y)$  &  $\mu_{Lg}(y)$   
For  $y = 70$ , we get

$$\mu_{Mg}(70) = \frac{100-70}{50} = \frac{3}{5}$$

$$\mu_{Lg}(70) = \frac{70-50}{50} = \frac{2}{5}$$

The above four equation leads to 4 rules  
we need evaluate

- 1) dirt is Medium and Grease is Medium
- 2) dirt is Medium and Grease is Large
- 3) dirt is Large and Grease is Medium
- 4) dirt is large and Grease is Large

Since the antecedent part of each of the above rule is connected by **and** operator we use **min** operator to evaluate strength of each rule

Strength of rule 1 DMGM

$$S_1 = \min(\mu_{MD}(60), \mu_{MG}(70)) \\ = \min(4/5, 3/5) \\ = 3/5$$

Strength of rule 2 DMGL

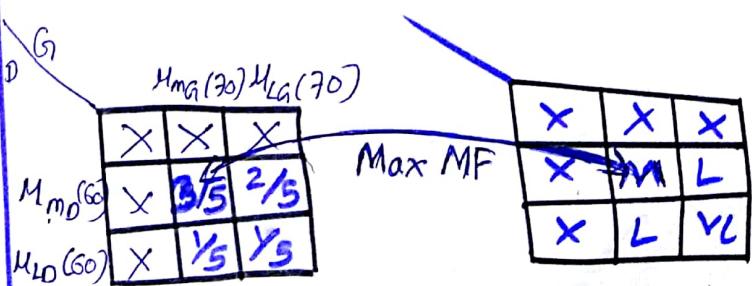
$$S_2 = \min(\mu_{MD}(60), \mu_{LG}(70)) \\ = \min(4/5, 2/5) \\ = 2/5$$

Strength of rule 3 DLGM

$$S_3 = \min(\mu_{LD}(60), \mu_{MG}(70)) \\ = \min(1/5, 3/5) = 1/5$$

Strength of rule 4 DLG L

$$S_4 = \min(\mu_{LD}(60), \mu_{LG}(70)) \\ = \min(1/5, 2/5) \\ = 1/5$$



## Step 5) Defuzzification

Since we use "Mean of max" defuzzification technique maximum strength

$$= \max(S_1, S_2, S_3, S_4)$$

$$= \max(3/5, 2/5, 1/5, 1/5) \\ = 3/5$$

This correspond to rule 1

rule 1 - Dirt is medium and Grease is medium has maximum strength (3/5)

To find out the final defuzzified value, we now take average (mean) of  $\mu_m(z)$

$$\mu_m(z) = \frac{z-10}{15} \text{ and } \mu_m(z) = \frac{40-z}{15}$$

$$3/5 = \frac{z-10}{15}$$

$$\therefore z = 19$$

$$3/5 = \frac{40-z}{15}$$

$$z = 31$$

$$\therefore z^* = \frac{19+31}{2} = 25 \text{ min}$$

//



Thank you so much 😊  
videos and notes dekhne ko

if you have any doubt  
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Strongly suggest to see  
*Sandeep maheshwari*  
videos



To  
change  
your  
life