

JOIN OPERATOR **SELECT** R.id, S.city For a tuple $r \in R$ and a tuple $s \in S$ that FROM R, S match on join attributes, concatenate WHERE R.id = S.id r and s together into a new tuple AND S.value > 100 Subsequent operators in the query plan π R.id, S.city never need to go back to the base tables to get more data \bowtie R. id = S. id $\sigma_{\text{value}>100}$

JOINS: OVERVIEW

Joins are among the most expensive operations

of joins often used as a measure of query complexity Join of 10s of tables common in enterprise apps

Naïve implementation: $R \bowtie_c S \equiv \sigma_c(R \times S)$

Enumerate the cross product, then filter using the join condition Inefficient because the cross product is large

Three classes of join algorithms:

Nested loops

Sort-merge Hash

No particular algorithm works well in all scenarios I/O COST ANALYSIS

Assume:

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Table R has M pages and m tuples in total Table **S** has **N** pages and **n** tuples in total

Cost Metric: # of I/Os to compute join

Ignore output costs (same for all join algorithms) Ignore CPU costs

FROM R, S WHERE R.id = S.id

SELECT R.id, S.city

AND S.value > 100

SIMPLE NESTED LOOPS JOIN



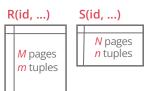
```
foreach tuple r \in R: Outer table foreach tuple s \in S: Inner table emit if r and s match
```

Why is this algorithm bad?

For every tuple in R, it scans S once

Terrible if S does not fit in memory

Cost: $M + (m \cdot N)$



SIMPLE NESTED LOOPS JOIN



Example database:

```
M = 1000, m = 100,000
N = 500, n = 40,000
```

Cost analysis:

```
M + (m \cdot N) = 1000 + (100,000 \cdot 500) = 50,001,000 \text{ I/Os}
At 0.1ms per I/O, total time \approx 1.4 \text{ hours}
```

What if smaller table (S) is used as the outer table?

```
N + (n \cdot M) = 500 + (40,000 \cdot 1000) = 40,000,500 \text{ I/Os}
At 0.1ms per I/O, total time \approx 1.1 hours
```

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SIMPLE NESTED LOOPS JOIN



SNLJ (but with page fetches written out explicitly)

Can we do better?

We scan S for every tuple in R,

... but we had to load an entire page of *R* into memory to get that tuple! Instead of finding the tuples in *S* that match a tuple in *R*,

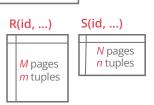
... do the check for all tuples in a page in **R** at once

PAGE NESTED LOOPS JOIN

```
\begin{array}{l} \text{for each page } p_R \in R: \\ \text{for each page } p_S \in S: \\ \text{for each tuple } r \in p_R: \\ \text{for each tuple } s \in p_S: \\ \text{emit if } r \text{ and } s \text{ match} \end{array}
```

This algorithm makes fewer disk accesses For every page in R, it scans S once

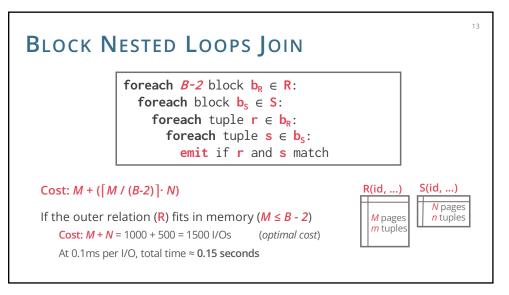
Cost: $M + (M \cdot N)$



PAGE NESTED LOOPS JOIN Example database: M = 1000, m = 100,000 N = 500, n = 40,000Which one should be the outer table? The smaller table in terms of # of pages Cost analysis: $N + (M \cdot N) = 500 + (1000 \cdot 500) = 500,500 \text{ I/Os}$ At 0.1ms per I/O, total time ≈ 50 seconds How many memory buffers are needed? Just 3: one for each input, one for output

```
BLOCK NESTED LOOPS JOIN
                 foreach B-2 block b_R \in R:
                   foreach block b_s \in S:
                      foreach tuple r \in b_{p}:
                        foreach tuple s \in b_s:
                           emit if r and s match
                                                                  S(id, ...)
                                                     R(id, ...)
  What if we have B buffers available?
     B-2 buffers for scanning the outer table
                                                                     N pages
                                                                    n tuples
     1 buffer for scanning the inner table
                                                       M pages
                                                       m tuples
      1 buffer for storing the output
```

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INDEX NESTED LOOPS JOIN

Why do simple nested loops joins suck?

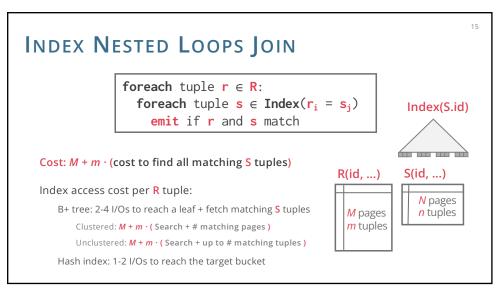
For each tuple in the outer table, we have to do a sequential scan to check for a match in the inner table

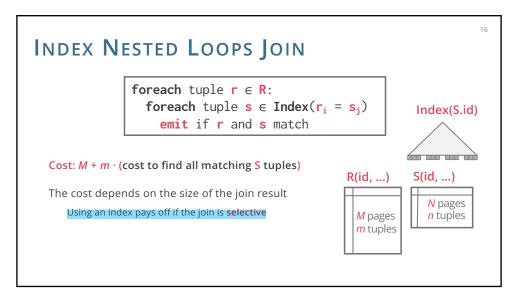
Can we accelerate the join using an index?

Use an index to find inner tuple matches

We could use an existing index or even build one on the fly

The index must match the join condition





RECAP: NESTED LOOPS JOINS

Pick the smaller table as the outer table

Buffer as much of the outer table in memory as possible

Loop over the inner table

Allows arbitrary join conditions Arbitrary join condition such as A.val>B.val+2

Or use an index over the inner table

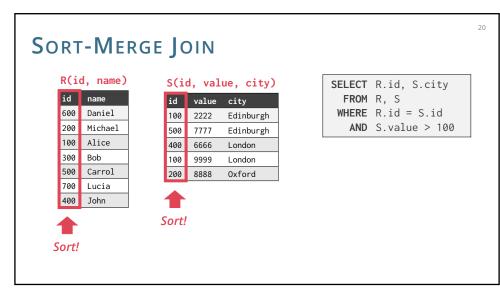
Only if matches the join condition

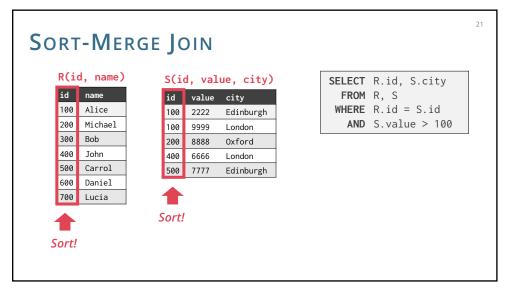
Requires equality predicate
Equi-joins & natural joins

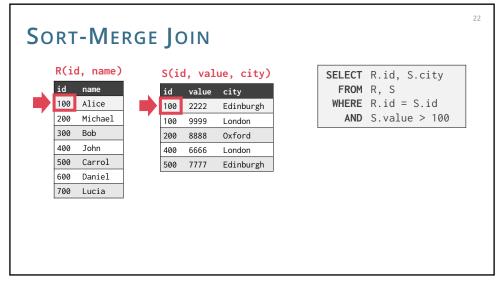
Phase #1: Sort
Sort both tables on the join key(s)
E.g. by using the external merge sort
Input might already be sorted... why?

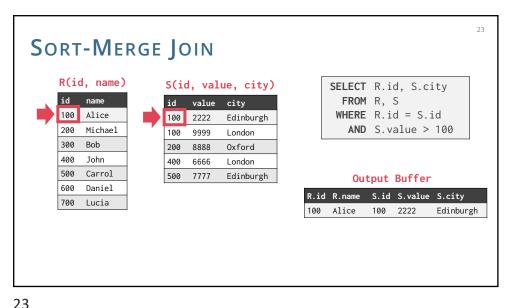
Phase #2: Merge
Scan the two sorted tables in parallel and emit matching tuples

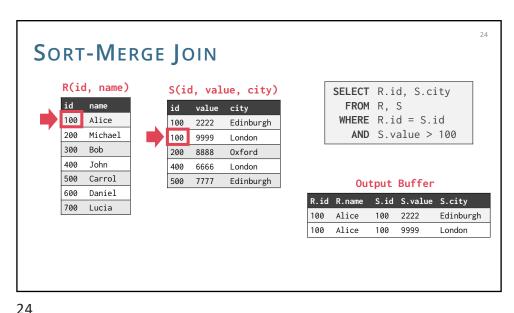
```
SORT-MERGE JOIN
           sort R,S on join key A
           r ← position of first tuple in R<sub>sorted</sub>
           s ← position of first tuple in S<sub>sorted</sub>
           while r \neq EOF and s \neq EOF:
             if r.A > s.A:
                advance s
             else if r.A < s.A:
                                         Extra bookkeeping if there
                                         are duplicates in R (tutorial question)
                advance r
             else if r.A = s.A:
                                             assumes no duplicates in R
                emit (r,s)
                                             (the merge phase could be easily
                                             extended to support duplicates)
                advance s
```

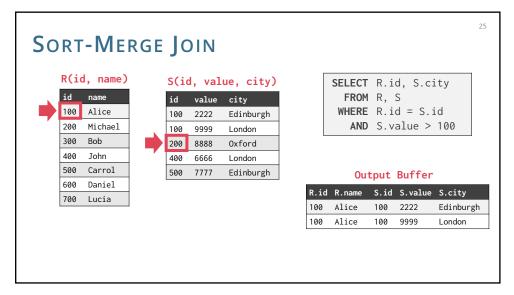


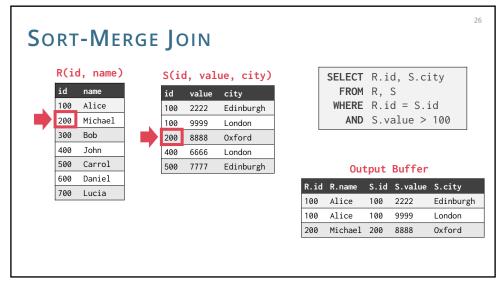


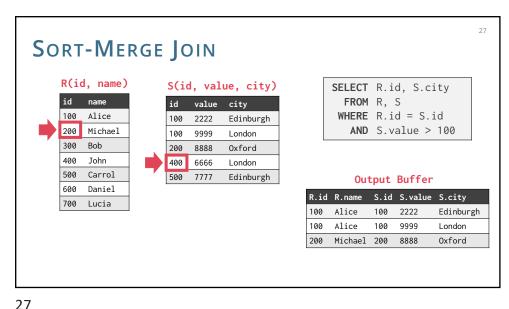


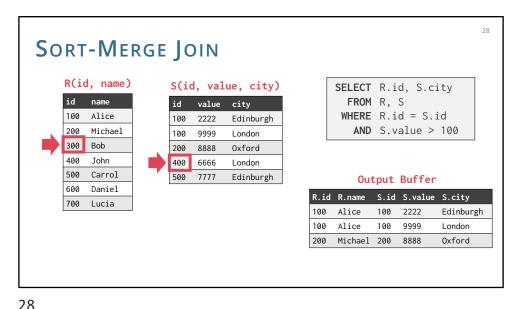




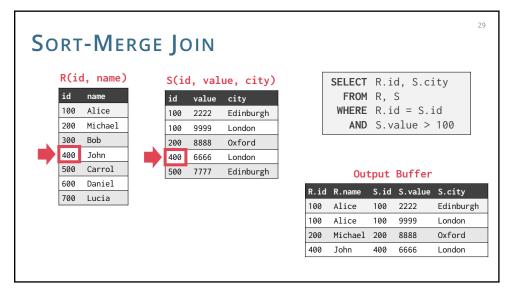


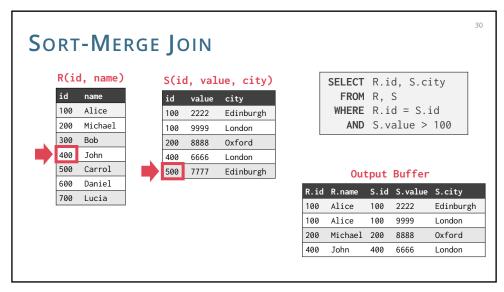


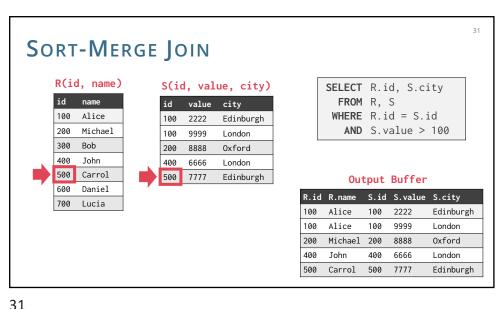


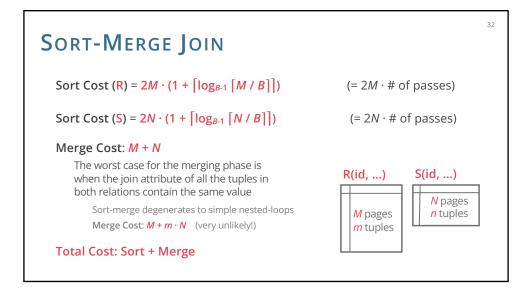


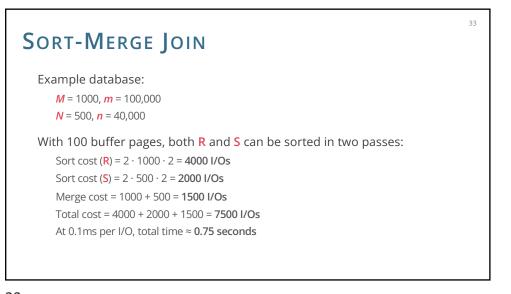
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34 SORT-MERGE JOIN REFINEMENT Combine the last pass of merge-sort with the merge phase of join Possible when the sum of # of runs in R and S in the penultimate (second-to-last) merge pass of sorting is at most B - 1 Example for 2-pass sort-merge join Read R and write out sorted runs (pass 0) Read S and write out sorted runs (pass 0) Merge R-runs and S-runs, while finding R ⋈ S matches Total cost = 2M + 2N + (M + N) = 2000 + 1000 + 1500 = 4500 I/OsEliminates one full read and write of R and S

WHEN IS SORT-MERGE JOIN USEFUL?

One or both tables are already sorted on the join key if previous operation used sort to remove duplicates

Output must be sorted on join key (e.g., ORDER BY clause)

Typically used for equi-joins only

Achieves highly sequential access

Weapon of choice for very large datasets

BASIC IN-MEMORY HASH JOIN

Requires equality predicate

Phase #1: Build

Scan the outer relation and build a hash table using a hash function **h** on join attributes

Key: the attribute(s) that the query is joining the tables on

Value: full tuple or tuple identifier (used in column stores)

Phase #2: Probe

Scan the inner relation and use **h** on each tuple to jump to a location in the hash table

Find matching tuples there

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BASIC IN-MEMORY HASH JOIN build hash table HT_R for R foreach tuple s ∈ S emit if h(s) ∈ HT_R Hash Table HT_R N pages

HASH JOIN

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What if both relations cannot fit in memory?

Idea: Decompose into smaller "partial joins"

If tuple $r \in R$ and tuple $s \in S$ satisfy the equi-join condition, then they have the same value for the join attributes

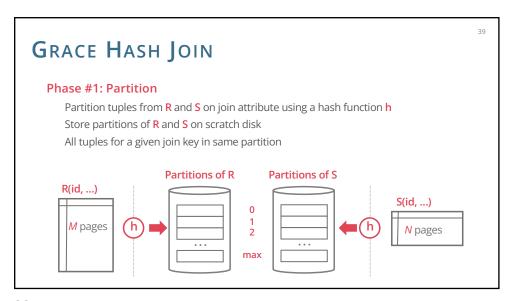
If that value is hashed to some value i, tuple r has to be in partition R_i and tuple s in partition S_i

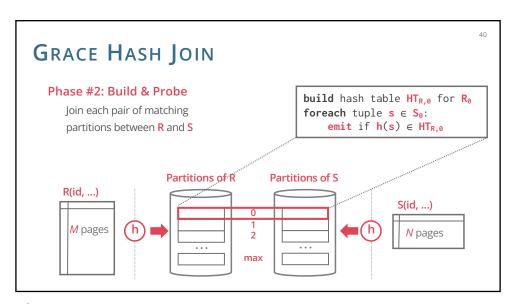
Thus, R-tuples in R_i need only to be compared with S-tuples in S_i

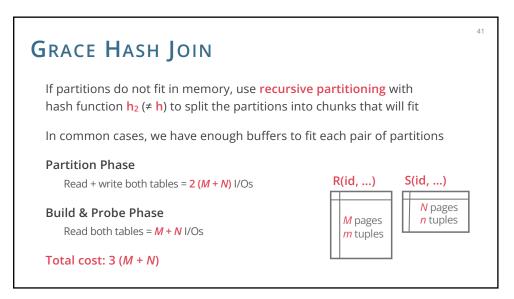
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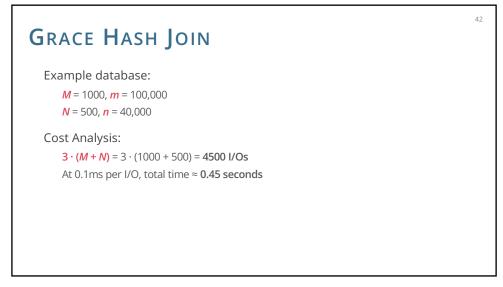
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HASH JOIN VS. SORT-MERGE JOIN

Sorting pros:

Good if input already sorted, or need output sorted Not sensitive to data skew or bad hash functions

Hashing pros:

For join: # of passes depends on size of smaller relation

E.g. if smaller relation is < **B**, basic in-memory hashing is great

Good if input already hashed, or need output hashed

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SUMMARY

Nested Loops

Works for arbitrary join condition

Make sure to utilize memory in blocks

Use the smaller table as the outer table

Index Nested Loops

When you already have an index on one side

For equi-joins mostly

For inequality joins needs a (clustered) B+-tree index

Sort/Hash

For equi-joins only, no index required

Hashing better if one relation is much smaller than other

Sorting better on non-uniform data & when results need to be sorted

No clear winners - may want to implement them all

Be sure you know the cost model for each. You will need it for query optimization!

JOIN ALGORITHMS: SUMMARY

JOIN ALGORITHM	I/O COST	TOTAL TIME
Simple Nested Loops Join	$M + (m \cdot N)$	1.4 hours
Page Nested Loops Join (using 2 input and 1 output buffer)	$M + (M \cdot N)$	50 seconds
Block Nested Loops Join (using B memory buffers)	$M + (\lceil M / (B-2) \rceil \cdot N)$	varies
Index Nested Loops Join	$M + (m \cdot \text{access cost})$	varies
Sort-Merge Join	M + N + (sort cost)	0.75 seconds
Hash Join	3 (M + N)	0.45 seconds
Nested Loops or Hash Join (one relation fits in memory)	M + N	0.15 seconds

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