

Advanced Database Systems

Spring 2024

Lecture #22:

Query Optimisation: Costing

R&G: Chapter 15

WHAT IS NEEDED FOR QUERY OPTIMISATION

Given: A closed set of operators

Relational operators (table in, table out)

Physical implementations (of those operators and a few more)

Plan space

Based on relational equivalences, different implementations

Cost estimation

Cost formula & size estimation for each physical operator

Search algorithm

To sift through the plan space and find lowest cost option!

2

COST ESTIMATION

For each plan considered, must estimate total cost:

Must estimate cost of each operation in plan tree

Depends on input cardinalities

Already discussed costs for various operators (sequential scan, index scan, joins, etc.)

Must estimate size of result for each operation in tree!

Because it determines downstream input cardinalities!

Use information about the input relations

For selections and joins, assume independence of predicates

In System R, cost boils down to a single number: #I/Os + CPU-factor * #tuples

Second term estimate the cost of tuple processing

STATISTICS AND CATALOGS

System catalogs store internal statistics about tables, attributes, and indexes Typically contain at least:

STATISTIC	MEANING
NTuples	# of tuples in a table (cardinality)
NPages	# of disk pages in a table or index
Low/High	min/max value in a column
NKeys	# of distinct values in a column
Height	the height of an index

Can also keep more detailed statistical information on data values (e.g., histograms)

Catalogs are updated periodically

Users can also manually refresh them (e.g,. ANALYZE in PostgreSQL)

Too expensive to do continuously. Lots of approximation anyway, so a little slop is OK

13 14

SIZE ESTIMATION AND SELECTIVITY

Max output cardinality = product of input cardinalities

Selectivity (sel) associated with each term

Reflects the impact of the term in reducing result size

Selectivity = |output| / |input|

Sometimes called "Reduction Factor" (RF)

Always between 0 and 1

Avoid confusion:

"highly selective" in common English is opposite of a high selectivity value (|output|/|input| high!)

SELECTION ESTIMATES

The **selectivity** (**sel**) of a predicate **P** is the fraction of tuples that qualify

Equality predicates on unique keys are easy to estimate

What about more complex predicates? What is their selectivity?

Formula depends on type of predicate

Equality, range, negation, conjunction, disjunction

SELECT * FROM Students
WHERE sid = 123

SELECT * FROM Students
WHERE age = 21

SELECT * FROM Students
WHERE age > 22
AND dept = 'CS'

15

SELECTIONS - COMPLEX PREDICATES

Assume attribute age in relation *Students* has five distinct values (20-24)

NKeys(age) = 5

Equality predicate

sel(A = constant) = 1 / NKeys(A)

Example: sel(age = 22) = 1/5

SELECT * FROM Students
WHERE age > 22

SELECT * FROM Students

WHERE age = 22

Range predicate

sel(A > a) = (High(A) - a) / (High(A) - Low(A) + 1) (when A is integer-valued column) sel(A > a) = (High(A) - a) / (High(A) - Low(A)) (when A is floating-valued column)

Example: sel(age > 22) = (24 - 22) / (24 - 20 + 1) = 2/5

SELECTIONS - COMPLEX PREDICATES

Equality predicate

 $sel(A = B) = 1 / max{NKeys(A), NKeys(B)}$

(handy for joins, too)

Why MAX?

Assume that A-values and B-values are independent

Let there be 2 distinct A-values { v1, v2 } and 10 distinct B-values { v1, ..., v10 }

What is the probability of matching values?

 $P(A = B) = \sum_{i} P(A = v_i, B = v_i) = \sum_{i} P(A = v_i) \cdot P(B = v_i)$ $= (1/2 \cdot 1/10) + (1/2 \cdot 1/10) + (0 \cdot 1/10) + ...$ $= 1/10 = 1 / max \{ 2, 10 \}$

17

18

SELECTIONS - COMPLEX PREDICATES

Negation query

sel(not P) = 1 - sel(P)

Example: sel(age != 22) = 1 - 1/5 = 4/5

Observation: selectivity ≈ probability

Conjunction

 $sel(P1 \land P2) = sel(P1) \cdot sel(P2)$

Assumes that the predicates are independent

Disjunction

 $sel(P1 \vee P2) = sel(P1) + sel(P2) - sel(P1 \wedge P2)$

Assumes that the predicates are independent

SELECT * FROM Students WHERE age != 22

SELECT * **FROM** Students WHERE age = 22 AND name LIKE 'A%'

SELECT * FROM Students WHERE age = 22OR name LIKE 'A%'

RESULT SIZE ESTIMATION FOR JOINS

How to estimate the size of a join between R and S?

Key-foreign key join

Since each value in S relation, will have one result in R Example: S has a foreign key referencing R relation due to foreign key constraints

The foreign key constraint guarantees $\pi_A(S) \subseteq \pi_A(R)$, thus $|R \bowtie S| = |S|$

Assumes non-null FK values (e.g., if A is part of a primary key in S); otherwise, $|R \bowtie S| \le |S|$

19

RESULT SIZE ESTIMATION FOR JOINS

General case: R join S on A which is not a key for either table

Recall algebraic equivalence: $R \bowtie_p S \equiv \sigma_p(R \times S)$

Hence join selectivity is "just" selectivity sel(p) over a big input $|R| \cdot |S|!$

Total rows: $sel(p) \cdot |R| \cdot |S|$

Equi-join on A

Match each **R**-tuple with **S**-tuple: $|R \bowtie S| \approx |R| \cdot |S|$ / NKeys(S.A)

Symmetrically, for S: $|R \bowtie S| \approx |S| \cdot |R| / NKeys(R.A)$

The final estimate is the smaller of the two estimates

Overall: $|R \bowtie S| \approx |R| \cdot |S| \cdot 1 / \max \{ NKeys(R.A), NKeys(S.A) \}$

sel(R.A = S.A)

20

MISSING STATISTICS? USE DEFAULT VALUES

```
/* default selectivity estimate for equalities such as "A = b" */
                                                         Postgres 13.0
#define DEFAULT_EQ_SEL 0.005
                                                         src/include/utils/selfuncs.h
/* default selectivity estimate for inequalities such as "A < b" */
```

/* default selectivity estimate for range inequalities "A > b AND A < c" */ #define DEFAULT_RANGE_INEQ_SEL 0.005

/* default selectivity estimate for multirange inequalities "A > b AND A < c" */ #define DEFAULT MULTIRANGE INEQ SEL 0.005

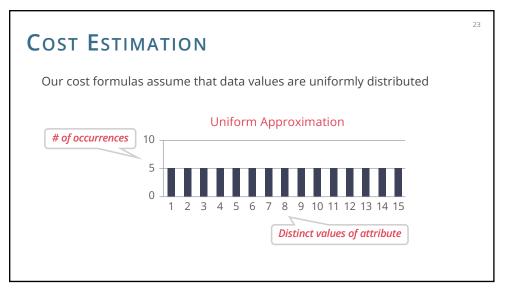
/* default selectivity estimate for pattern-match operators such as LIKE */ #define DEFAULT_MATCH_SEL 0.005

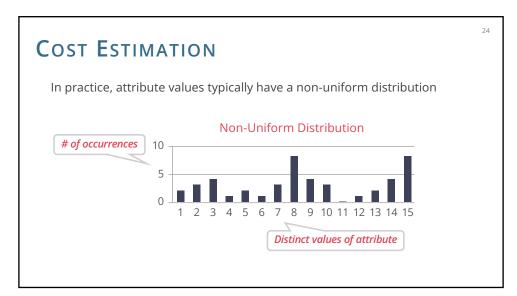
/* default selectivity estimate for other matching operators */

/* default number of distinct values in a table */ #define DEFAULT_NUM_DISTINCT 200

#define DEFAULT MATCHING SEL 0.010

22





23

HISTOGRAMS

To keep track of this non-uniformity for an attribute *A*, we can maintain a **histogram** to approximate the actual distribution

Divide the active domain of *A* into adjacent intervals

Collect statistical parameters for each interval (b_{i-1}, b_i), for example

of tuples r with $b_{i-1} < r.A \le b_i$

of distinct A values in interval (b_{i-1}, b_i]

The histogram intervals are also called buckets

Types of Histograms

Equi-width histograms

25

All buckets have the **same width w** or number of distinct values

I.e., boundary $b_{i+1} = b_i + w$ for some fixed width w

Equi-depth histograms

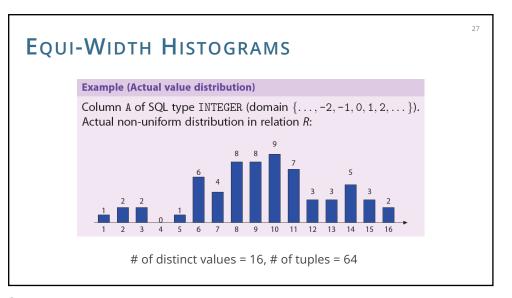
All buckets contain the same number of tuples (their width may vary)

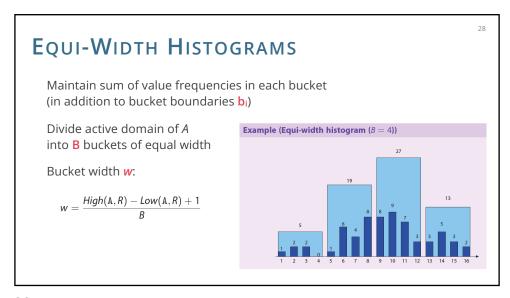
Able to adapt to data skew (high uniformity)

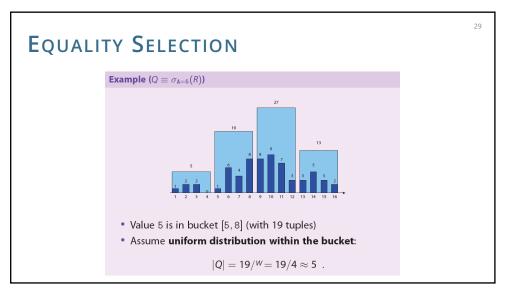
The number of buckets is the tuning knob that defines the trade-off between histogram resolution (estimation quality) and histogram size

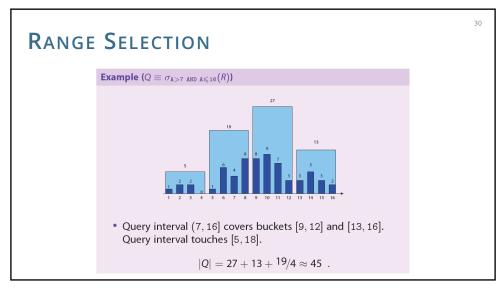
Catalog space is limited!

25









EQUI-DEPTH HISTOGRAMS

Divide active domain of attribute A into B buckets with *roughly* the same number of tuples in each bucket

Depth d of each bucket will be approximately |R|/B

Maintain depth d and bucket boundaries bi

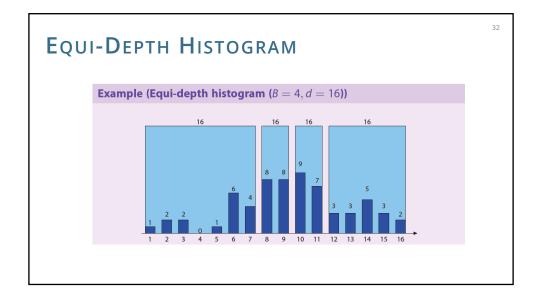
Intuition:

31

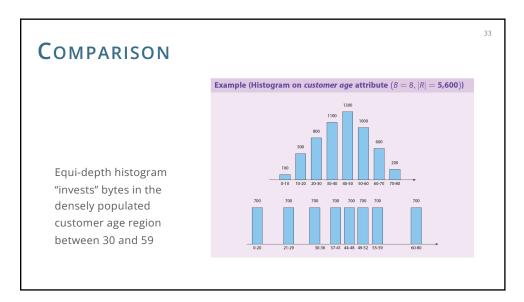
High-value frequencies are more important than low-value frequencies and put in smaller buckets

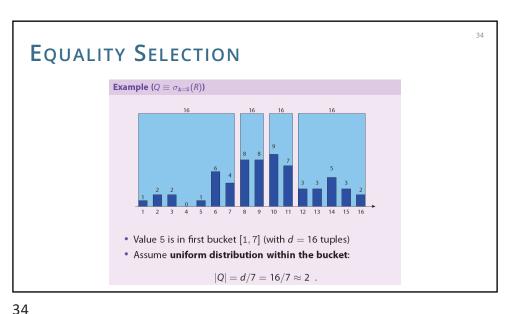
Equi-depth provides better estimates than equi-width for highly frequent values

Resolution of histogram adapts to skewed value distributions

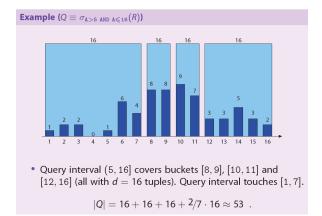


32









SUMMARY: SELECTIVITY ESTIMATION

We need a way to estimate the size of the intermediate tables

Output size = input size * operator selectivity

Assumption 1: Uniform distribution within histogram bins

Within a bin, fraction of range = fraction of count

Assumption 2: Independent predicates

Selectivity of AND = product of selectivities of predicates

Selectivity of OR = sum of selectivities of predicates – product of selectivities of predicates

Selectivity of NOT = 1 – selectivity of predicates

General joins

36

Simply compute the selectivity of all predicates And multiply by the product of the table sizes