

SORTING

A file is **sorted** with respect to key k and ordering Θ , if for any two records r_1 and r_2 with r_1 preceding r_2 in the file, their corresponding keys are in Θ -order:

 $r_1 \Theta r_2 \Leftrightarrow r_1.k \Theta r_2.k$

A key may be a single attribute or an ordered list of attributes. In the latter case, the order is **lexicographical**

Consider key (A,B) and Θ is <

 $r_1 < r_2 \Leftrightarrow r_1.A < r_2.A \lor (r_1.A = r_2.A \land r_1.B < r_2.B)$

SORTING ALGORITHMS

If data **fits** in memory, then we can use a standard sorting algorithm like quick-sort

Problem: sort 100GB of data with 1GB of RAM

Why not virtual memory?

If data does not fit in memory, then we need to use a technique that is aware of the cost of writing data out to disk

EXTERNAL SORTING

How can we sort a file of records whose size exceeds the available main memory space (let alone the available buffer manager space) by far?

Idea: Divide and conquer

Sort chunks of data that fit in memory, then write back the sorted chunks to disk Combine sorted chunks into a single larger file

Approach the task in two phases:

- 1. Sorting a file of arbitrary size is possible using only three buffer pages
- 2. Refine this algorithm to make effective use of larger buffer sizes

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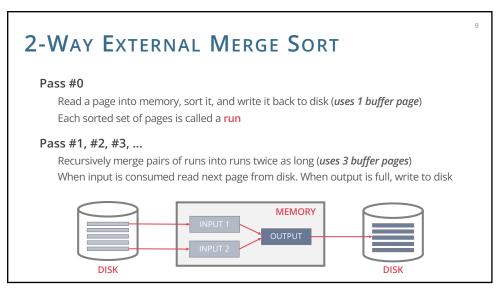
OVERVIEW

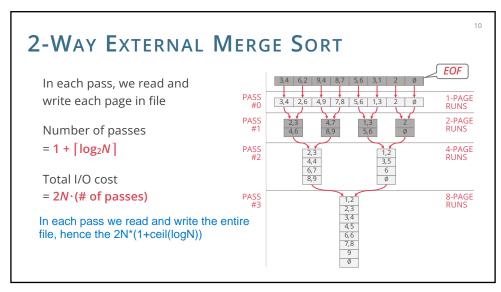
We will start with a simple example of a 2-way external merge sort

Files are broken up into **N** pages

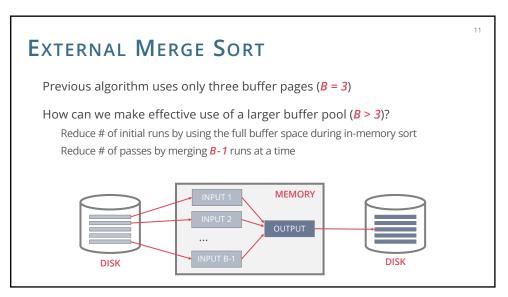
The DBMS has a finite number of **B** fixed-size buffer pages

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EXTERNAL MERGE SORT

Pass #0
Use B buffer pages
Produce [N/B] sorted runs of size B

Pass #1, #2, #3, ...
Merge B - 1 runs (i.e., multi-way merge)

Number of passes = 1 + [log<sub>B-1</sub>[N/B]]

Total I/O cost = 2N·(# of passes)
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EXAMPLE

Sort N = 108 page file with B = 5 buffer pages

Pass #0: [108/5] = 22 sorted runs of 5 pages each (last run is only 3 pages)

Pass #1: [22/4] = 6 sorted runs of 20 pages each (last run is only 8 pages)

Pass #2: [6/4] = 2 sorted runs of 80 pages and 28 pages

Pass #3: Sorted file of 108 pages

Number of passes = $1 + \lceil \log_{B-1} \lceil N / B \rceil \rceil = 1 + \lceil \log_4 22 \rceil = 1 + \lceil 2.229... \rceil$ = 4 passes

Total I/O cost = $2N \cdot (\# \text{ of passes}) = 2 \cdot 108 \cdot 4 = 864$

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USING B+ TREES FOR SORTING

If the table to be sorted has a B+ tree index on the sort attribute(s), we may be better off by accessing the index and avoid external sorting

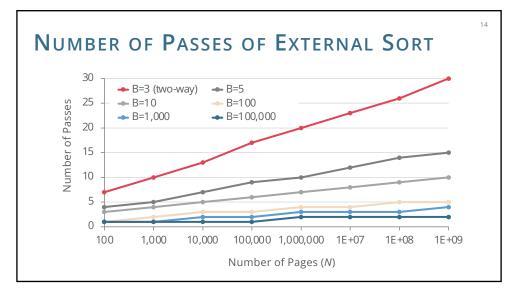
Retrieve sorted records by simply traversing the leaf pages of the tree

Cases to consider

Clustered B+ tree

Unclustered B+ tree

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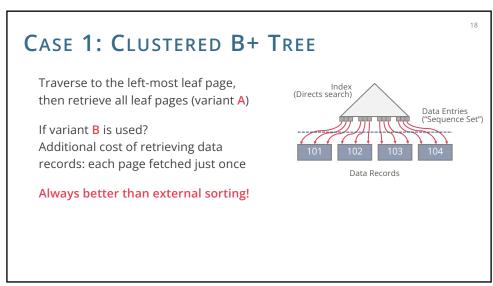


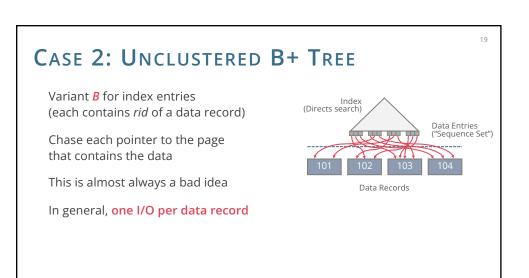
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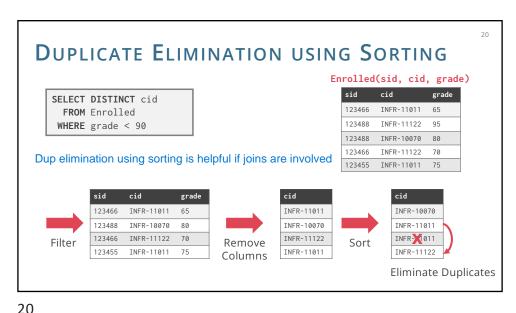
Variant A: Clustered B+ with index only scan

Variant B: Clustered B+ with non index only scan

Variant C: Unclustered B+ tree (better to not use the index in this case as the performance is poor)







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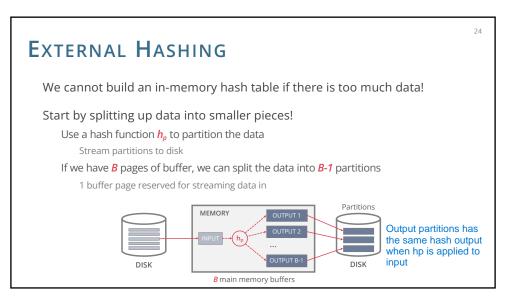


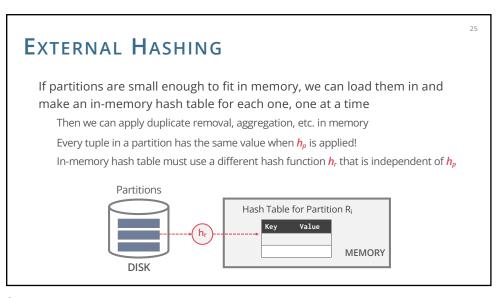
What if we do not need the data to be ordered?

Forming groups in **GROUP BY** (no ordering) Removing duplicates in **DISTINCT** (no ordering)

Hashing is a better alternative in this scenario
Only need to remove duplicates, no need for ordering

Can be computationally cheaper than sorting





AGGREGATIONS

Collapse multiple tuples into a single scalar value (SUM, MIN, MAX, ...)

Hashing aggregates:
Populate an ephemeral hash table as the DBMS scans the relation. For each record check whether there is already an entry in the hash table

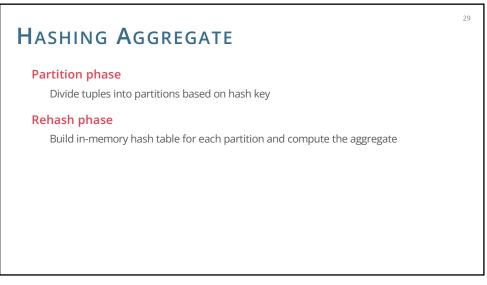
DISTINCT: Discard duplicate

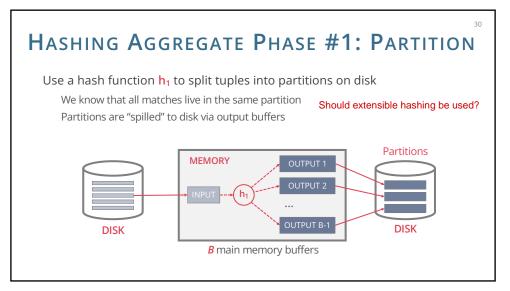
GROUP BY: Perform aggregate computation
If everything fits in memory, then it's easy
If we have to spill to disk, then we need to be smarter...

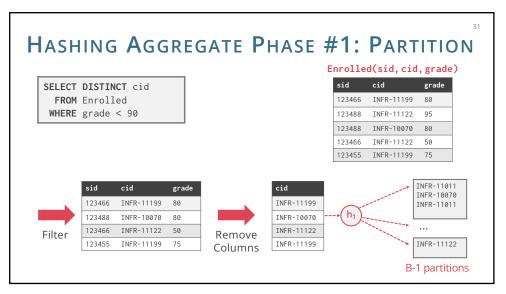
SELECT A, MAX(B) FROM R
GROUP BY A;

In hash table, key is A and value is max(B)

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HASHING AGGREGATE PHASE #2: REHASH

For each partition on disk:

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Read it into memory and build an in-memory hash table based on a second hash function $h_2 (\neq h_1)$

Then go through each bucket of this hash table to bring together matching tuples

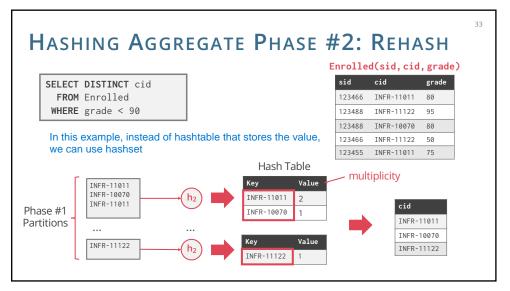
No need to load the entire partition at once in memory

Can load several pages at a time

But the hash table built for each partition must fit in memory

If not enough memory, repeat Phase #1 on each partition with a different hash function

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HASHING SUMMARISATION

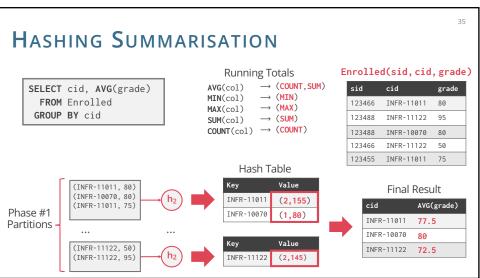
During the Rehash phase, store pairs of the form GroupKey → RunningValue

When we want to insert a new tuple into the hash table

If we find a matching **GroupKey**, just update the **RunningValue** appropriately

Else insert a new **GroupKey** → **RunningValue**

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CONCLUSION: SORTING VS. HASHING

External merge sort often finishes in 1-2 passes

Great if we need output to be sorted anyway Not sensitive to duplicates or "bad" hash functions

Duplicate elimination

Hashing preferred as it scales with # of distinct values

Delete duplicates in first pass while partitioning

Vs. sort which scales with # of values

Group-by aggregation

Typically computed via hashing

COST ANALYSIS Doubt?

How big of a table can we hash using this approach?

B-1 "spill partitions" in Phase #1

Each partition (i.e., its hash table) should be no more than **B** pages big

Answer: $B \cdot (B-1)$

A table of **N** pages needs about **sqrt(N)** buffer pages

Note: assumes hash distributes records evenly!

Use a "fudge factor" f > 1 to capture the (small) increase in size

between the partition and a hash table for that partition

Must be $B > f \cdot N / (B-1)$; thus, we need approx. $B > \operatorname{sqrt}(f \cdot N)$ buffer pages

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