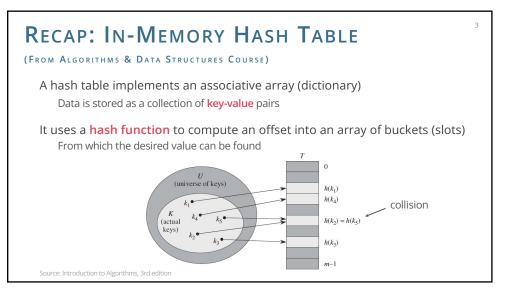
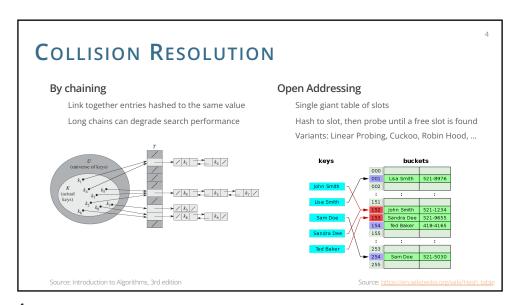


**Hash-Based Indexing** 

R&G: Chapter 11

# RECAP: FILE ORGANISATIONS Method of arranging a file of records on secondary storage Heap Files SQL Client Store records in no particular order Sorted Files Files & Index Management Store records in sorted order, based on search key fields Index Files Store records to enable fast lookup and modifications Database Tree-based & hash-based indexes





# HASHING IN DATABASES

We want to be able to group together tuples with the same key value

Partition the data with hash function(s) applied on the key

All tuples with a certain key will be in the same partition

#### Useful for:

Removing duplicates (all duplicates will be grouped together)

Grouping data (for GROUP BY)

Looking up data using hash indexes

OVERVIEW

Static and dynamic hashing techniques exist

Trade-offs similar to ISAM vs. B+ trees

Static hashing schemes

Chained hashing

Dynamic hashing schemes

Extendible hashing Linear hashing

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# HASH-BASED INDEXING

Suitable for equality-based predicates

SELECT \* FROM Customer WHERE A = constant

**Cannot** support range queries

Other query operations internally generate a flood of equality tests

E.g.: nested loop join, where hash index can make a real difference

Support in commercial DBMSs

Tree-structured indexes preferred since they cover the more general range predicates But hash-based indexes are used for (index) nested loop joins

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# STATIC CHAINED HASHING

Hash index is a collection of buckets

Build static hash index on column A

Allocate a fixed area of N (successive) pages, the so-called primary buckets

In each bucket, install a pointer to a chain of overflow pages (initially set to null)

Define a **hash function** *h* with range [0, ..., N-1]

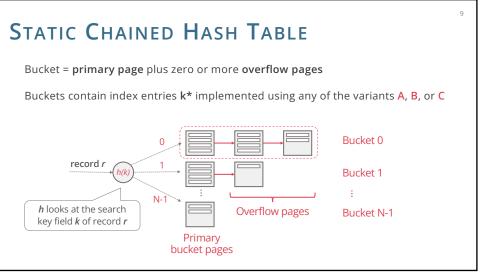
The domain of **h** is the type of A

e.g., h: INTEGER  $\rightarrow$  [0, ..., N-1], if A is of type INTEGER

The hash function determines the bucket where the desired value can be found

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STATIC CHAINED HASH TABLE MANAGEMENT

Operations: search, insert, delete

Compute h(k) on the search key field k of record r

Access the primary bucket page with number h(k)

Search for/insert/delete record on this page or, if needed, access the overflow pages

If overflow chain access is avoidable

**search** requires a single I/O operation

insert and delete require two I/O operations

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# HASH COLLISIONS AND OVERFLOW CHAINS

#### Hash collisions are unavoidable

For search keys k and k', can happen h(k) = h(k')

Search keys may not be unique (e.g., student age)

Even if unique, the search key space is much larger than # of buckets

Having as many primary bucket pages as different search keys in database ⇒ waste of space

#### Long overflow chains can degrade performance

Operation costs become non-uniform and unpredictable for a query optimiser

To reduce this problem, *h* needs to scatter search keys evenly across [0, ..., N-1]

Large # of entries can still cause long chains (dynamic hashing to fix this)

## HASH FUNCTIONS

How to map a large key space into a smaller domain

Real distributions of search key values are often non-uniform (skewed)

Trade-off between being fast vs. collision rate

We want a lightweight (non-cryptographic) hash function with a low collision rate

Simple hash function:  $h(k) = k \mod N$ 

Guarantees the range of *h(k)* to be [0, N-1]

Choosing  $N = 2^d$  for some d effectively considers the least d bits of k only

Prime numbers work best for N

Better hash functions used in practice

xxHash (+ benchmark), MurmurHash, Google CitvHash, Google FarmHash, CLHash

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# STATIC HASHING AND DYNAMIC FILES

If the data file grows,

the development of overflow chains spoils the index I/O behaviour (1–2 I/O operations)

If the data file shrinks,

a significant fraction of primary buckets may be (almost) empty – a waste of space

We may **periodically rehash** the data file to restore the ideal situation (20% free space, no overflow chains)

Expensive – the index not usable while rehashing is in progress

As for ISAM, static hashing has advantages with concurrent access

Only need to lock one bucket page to store a new entry or extend the overflow chain

EXTENDIBLE HASHING

Situation: Bucket (primary page) is full and we want to insert. Why not reorganize the index by doubling # of buckets?

Reading and writing all pages is expensive!

Idea: Use directory of pointers to buckets, double # of buckets by doubling the directory, splitting just the bucket that overflowed

Directory much smaller than file, so doubling it is much cheaper

Only one page of data entries is split

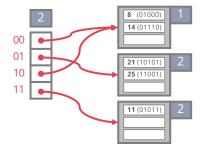
No overflow pages!

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# EXTENDIBLE HASHING



Note: we depict as index entries h(k) instead of  $k^*$ 

Why not separate local bucket for 10?

# GLOBAL AND LOCAL DEPTH

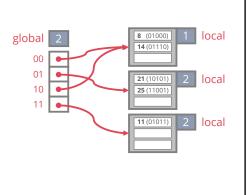
# Global depth (n at directory)

Use the least *n* bits of *h(k)* to find a bucket pointer in the directory

The directory size is  $2^n$ 

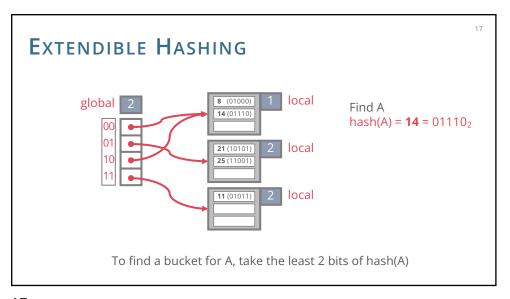
### **Local depth** (*d* at individual buckets)

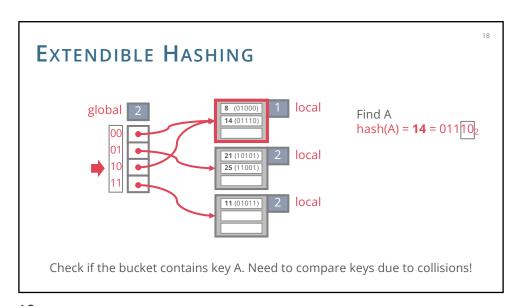
The hash values h(k) of all entries in this bucket agree on their least d bits

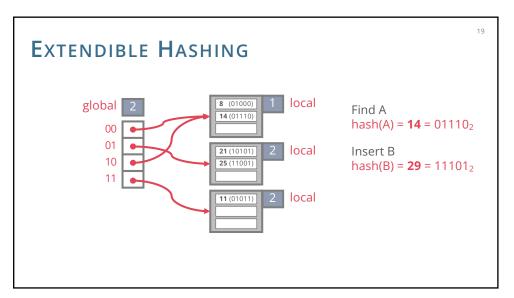


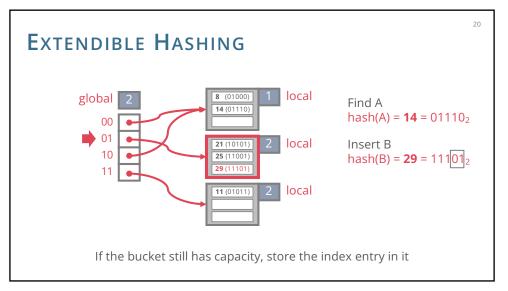
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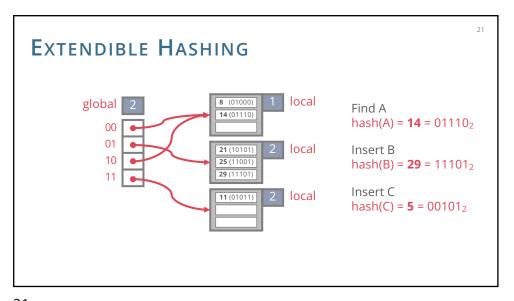
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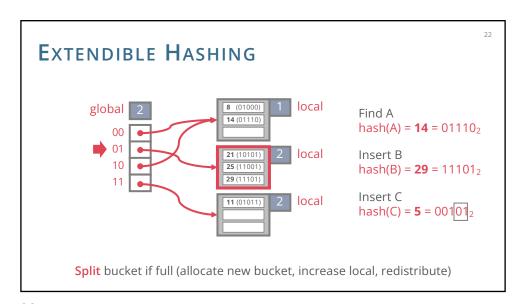


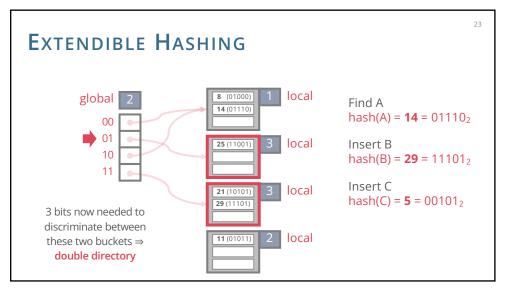


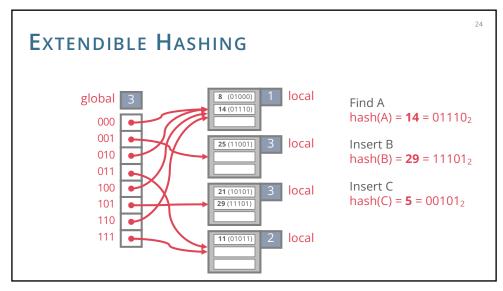


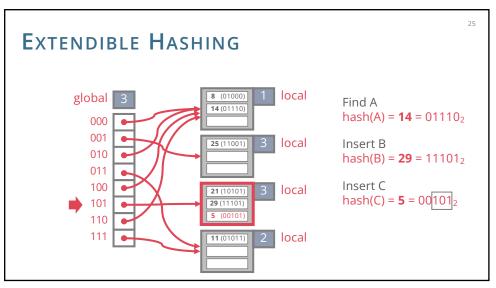












DIRECTORY DOUBLING

Double directory by **copying** its original pointers and "fixing" pointer to split bucket

Use of least significant bits enables efficient doubling via copying!

Splitting a bucket does not always require doubling the directory

Buckets with local depth < global depth have multiple pointers to them

Splitting such buckets does not require doubling

Modifying one or more bucket pointers in directory is sufficient

Directory can also shrink when buckets become empty

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## Not examinable

## LINEAR HASHING

Linear hashing adapts its data structure to record insertions and deletions

Handles the problem of long overflow chains without using a directory

Idea: Use a family of hash functions  $h_0$ ,  $h_1$ ,  $h_2$ , ...

The subscript is called the hash function's level

 $\emph{h}_{\textit{level+1}}$  doubles the range of  $\emph{h}_{\textit{level}}$ 

Split buckets in rounds

One by one from the first to the last bucket

In round *level*, use  $h_{level}$  for unsplit buckets and  $h_{level+1}$  for split buckets

## HASH FUNCTION FAMILY

Given an initial hash function h and an initial hash table with N buckets Range of h is <u>not</u> 0 to N - 1

Define a family of hash functions  $h_0$ ,  $h_1$ ,  $h_2$ , ...

 $h_{level}(k) = h(k) \mod (2^{level} \cdot N)$  (level = 0, 1, 2, ...)

Example:

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Initial hash function h(k) = k

N = 4 initial buckets

 $h_0(k) = k \mod 4$   $h_1(k) = k \mod 8$   $h_2(k) = k \mod 16$  ...

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# LINEAR HASHING Maintains a pointer that tracks the next bucket to split When any bucket overflows, split the bucket at the pointer location This may not be the bucket that triggered the split! Split criterion is left up to the implementation Space utilization of a bucket beyond some % capacity, or Average length of overflow chains longer than p pages

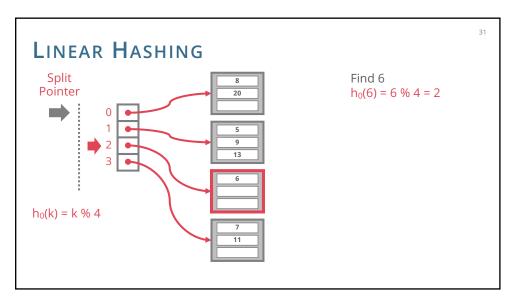
LINEAR HASHING

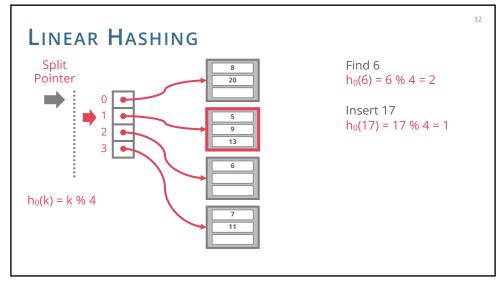
Split
Pointer

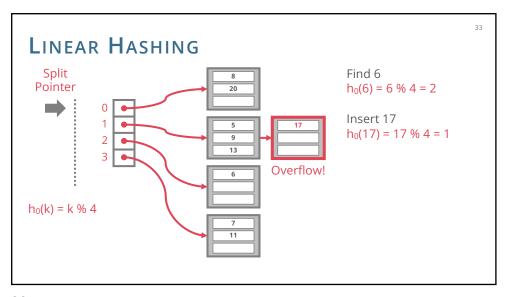
Use  $h_0$  for all buckets

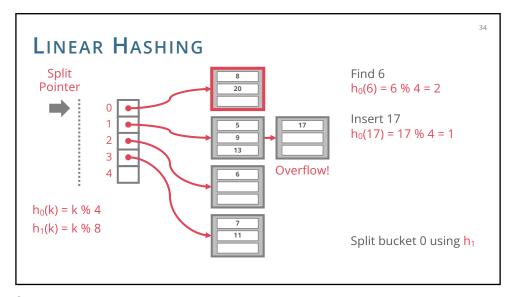
Note: the directory is shown here for presentation purpose, not needed in practice

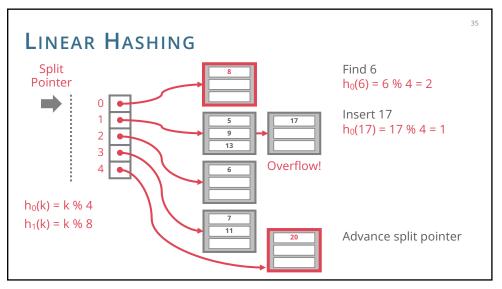
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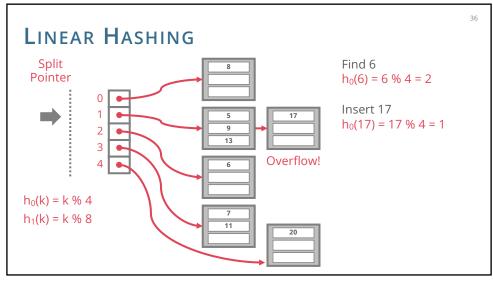


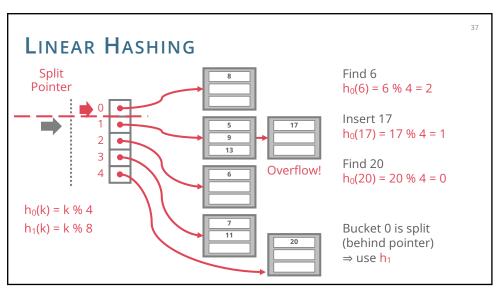


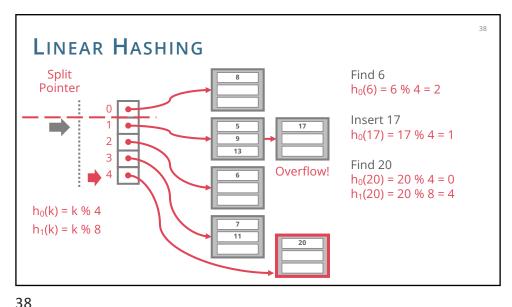












# LINEAR HASHING

Since buckets are split round-robin, long overflow chains don't develop!

After splitting the last bucket, start a new round: delete the first hash function, increase level, and move back to beginning

The pointer can also move backwards when buckets are empty

Doubling of directory in Extendible Hashing is similar Linear hashing doubles the directory gradually

Primary bucket pages are **created in order**. If they are allocated in sequence too (so that finding i-th is easy), we don't need a directory!

**SUMMARY** 

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Hash-based indexes

Best for equality searches, cannot support range searches

Static hashing

Can lead to long overflow chains

Extendible hashing

Avoids overflow chains by splitting a full bucket when a new entry is to be added to it

Linear hashing

Avoids directory by splitting buckets round-robin and using overflow pages

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