Due: Aug 16, 2019

DS 211

Problem 1

- 1. The derivative $f'(x) = \frac{-12x}{(6x^2-1)^2}$.
- 2. $f(0.408) = \infty$ (denominator became 0) using 3-digit arithmetic and f(0.408) = 833.3using 4-digit arithmetic with rounding.
- 3. Horner's representation of the given polynomial is y = -0.35 + x(8 + x(-7 + x)). The value of y at x = 1.37 is 0.048 using 3-digit arithmetic rounding.
- 4. The value of y at x = 1.37 is 0.02 using direct substitution and 3-digit arithmetic rounding.
- 5. The value computed using Horner's rule is more accurate since it is closer the actual value without rounding which is 0.0431.

Problem 2

- 1. The RAM size necessary to store the given array is 49439 MB.
- 2. No. 32 GB is not sufficient to store the entire array in RAM alone. But swap space could be used to spill excess array to disk and still use the RAM.
- 3. No. It is not possible to use the workstation as this increase in resolution requires 111² more space than the previous array which amounts to roughly 600 TB.

Problem 3

- 1. The optimality condition is $f'(x) = (A + A^T)X + b = 0$. This optimum is for minimum since $f''(x) = A + A^T$ and ||f''(x)|| > 0 since $||A + A^T|| > 0$ for the given A.
- 2. The algorithm for gaussian elimination is as follows,

Algorithm 1: Gaussian Elimination (LU Decomposition)

```
U = A + AT; L = I
for k = 1 to m-1
       for j = k+1 to m
               l[j][k] = u[j][k] / u[k][k]
               u[j][k:m] = u[j][k:m] - l[j][k] * u[k][k:m]
Y = L^-1 * -b // Back Substitution
X = U^-1 * Y // Back Substitution
```

3. The above program is implemented in sgauss.m file.

- 4. There is no trouble for the current case. However, if the pivot element is 0 in any iteration, the algorithm breaks. Hence, Gaussian elimination with partial pivoting (interchange of rows) is required to overcome this problem.
- 5. The modified program with partial pivoting is implemented in sgausspivot.m file.

Problem 4

- 1. The functions have been implemented in scgs.m and smgs.m files.
- 2. Matrix generation function has been implemented in matgen.m file.
- 3. The script to run for different matrix sizes is written in exp.m file.
- 4. The plot for error is available below,

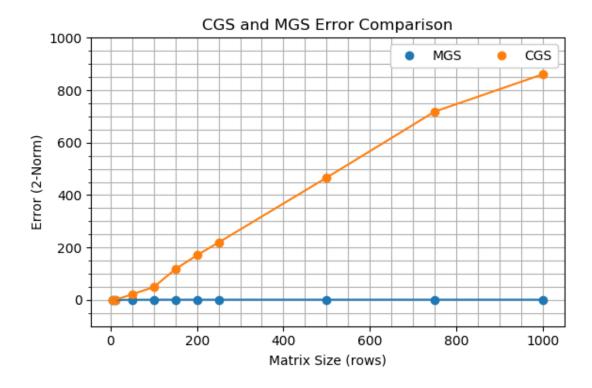


Figure 1: CGS and MGS Error Comparison

5. The modified Gram-Schmidt technique is more numerically stable than the classical version. Error remains low and constant for modified technique and increases linearly with respect to matrix size for classical version.

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Problem 5

The following contour plot was taken gridded dataset downloaded from [1]

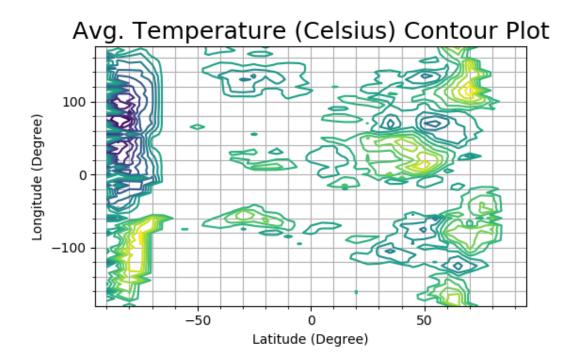


Figure 2: Average Temperature Contour Plot

References

1. http://berkeleyearth.lbl.gov/auto/Global/Gridded/Complete_TAVG_EqualArea.nc