

# Binary Tree Notes:

## 1 Level Order Traversal (BFS)

**Type:** Basic BFS / Level Order

**Problem Solved:** "Print all levels of a tree"

**Approach / Logic:**

1. Use queue → push root
2. Loop while queue not empty:
  - Record `size = queue.size()`
  - Loop over level size: pop node, push left & right children
3. For storing per level → vector inside vector

**Tricks / Observations:**

- Level-based problems → BFS
- $i==0$  → first node of level → Left View
- $i==size-1$  → last node → Right View

```
vector<vector<int>> levelOrder(TreeNode* root){  
    vector<vector<int>> ans;  
    if(!root) return ans;  
    queue<TreeNode*> q; q.push(root);  
  
    while(!q.empty()){  
        int size = q.size();  
        vector<int> level;  
        for(int i=0;i<size;i++){  
            TreeNode* node = q.front(); q.pop();  
            level.push_back(node->val);  
            if(node->left) q.push(node->left);  
            if(node->right) q.push(node->right);  
        }  
        ans.push_back(level);  
    }  
    return ans;  
}
```

```

    }
    ans.push_back(level);
}
return ans;
}

```

## 2 Zigzag Level Order

**Type:** BFS + Alternating Direction

**Problem Solved:** LeetCode Zigzag Level Order

**Approach / Logic:**

- BFS like normal
- Maintain level count → if  $\text{level} \% 2 == 0 \rightarrow \text{push\_back}$ , else → insert at begin
- Collect vector of vectors

**Tricks / Observations:**

- $\text{level} \% 2 \rightarrow \text{alternate order}$
- Queue still normal BFS

```

vector<vector<int>> zigzagLevelOrder(TreeNode* root){
    vector<vector<int>> ans;
    if(!root) return ans;
    queue<TreeNode*> q; q.push(root);
    int level=0;

    while(!q.empty()){
        int size = q.size();
        vector<int> levelAns;
        for(int i=0;i<size;i++){
            TreeNode* node = q.front(); q.pop();
            if(level%2==0) levelAns.push_back(node->val);
            else levelAns.insert(levelAns.begin(), node->val);
            if(node->left) q.push(node->left);
        }
        ans.push_back(levelAns);
        level++;
    }
    return ans;
}

```

```

        if(node->right) q.push(node->right);
    }
    ans.push_back(levelAns);
    level++;
}
return ans;
}

```

## 3 Height of Binary Tree

**Type:** DFS / Recursion

**Problem Solved:** Compute height

**Approach / Logic:**

- Base case: root==NULL → return 0
- Else: 1 + max(height(left), height(right))

**Trick:**

- Simple post-order DFS
- Height = number of edges (or nodes based on definition)

```

int height(TreeNode* root){
    if(!root) return 0;
    return 1 + max(height(root->left), height(root->right));
}

```

## 4 Diameter of Binary Tree

**Type:** DFS + Post-order

**Problem Solved:** Max distance between 2 nodes

**Approach / Logic:**

1. Use height function recursively

2. Diameter = max(diameter of left subtree, diameter of right subtree,  
leftHeight+rightHeight)

**Trick / Shortcut:**

- Post-order recursion → height calculation
- Combine left + right heights at each node → candidate diameter
- Use global variable to track max (more optimal)

```
int diameter(TreeNode* root, int &maxDia){  
    if(!root) return 0;  
    int lh = diameter(root->left, maxDia);  
    int rh = diameter(root->right, maxDia);  
    maxDia = max(maxDia, lh+rh);  
    return 1 + max(lh,rh);  
}  
  
int diameterOfBinaryTree(TreeNode* root){  
    int maxDia=0;  
    diameter(root,maxDia);  
    return maxDia;  
}
```

## 5 Maximum Path Sum

**Type:** DFS + Global variable

**Problem Solved:** Max sum of any path in BT

**Approach / Logic:**

- Recursive DFS → bottom-up
- For each node:
  - max path including left + node
  - max path including right + node
  - max path through node = left+node+right

- Update global max

### Tricks / Shortcut:

- Return max of (node + left) or (node + right) for recursion
- Keep global max for total

```
int maxPath(TreeNode* root, int &res){
    if(!root) return 0;
    int left = max(0, maxPath(root->left,res));
    int right = max(0, maxPath(root->right,res));
    res = max(res, left + right + root->val);
    return root->val + max(left,right);
}
```

```
int maxPathSum(TreeNode* root){
    int res = INT_MIN;
    maxPath(root,res);
    return res;
}
```

## 6 Left / Right View

**Type:** BFS + Level order

**Right View Logic:**  $i == \text{size}-1$

**Left View Logic:**  $i == 0$

**Code Snippet (Right View):**

```
if(i==size-1) ans.push_back(node->val);
```

**Code Snippet (Left View):**

```
if(i==0) ans.push_back(node->val);
```

**Memory Trick:**

- BFS skeleton same → only index condition changes

## 7 LCA (Lowest Common Ancestor)

**Type:** DFS / Bottom-up recursion

**Approach / Logic:**

- If root==p or q → return root
- left = dfs(left), right = dfs(right)
- Both left & right non-null → root is LCA
- Else return non-null

```
TreeNode* lowestCommonAncestor(TreeNode* root, TreeNode* p, TreeNode
*q){
    if(!root) return NULL;
    if(root==p || root==q) return root;
    TreeNode* left = lowestCommonAncestor(root->left,p,q);
    TreeNode* right = lowestCommonAncestor(root->right,p,q);
    if(left && right) return root;
    return left?left:right;
}
```

## 8 Top / Bottom View (High-level)

**Type:** BFS + Horizontal Distance

**Logic / Trick:**

- Top View → first node per HD
- Bottom View → last node per HD
- Map<int, val> → store nodes per HD

**Skeleton Code:**

```
queue<pair<TreeNode*, int>> q; // node, HD  
map<int,int> mp;
```