

Heaps Notes:-

1 Kth Largest Element in a Stream (LeetCode)

Problem:

- Stream me naya number aata hai → return **current k-th largest** element

Heap type: Min Heap (size = k) → top() = kth largest

Approach:

1. Use **min heap**
2. Push all initial numbers → maintain size $\leq k$
3. Add function → push new val → if size $> k$ → pop → return top

```
class KthLargest {  
    int k;  
    priority_queue<int, vector<int>, greater<int>> pq;  
public:  
    KthLargest(int k, vector<int>& nums) {  
        this->k = k;  
        for (int num : nums) {  
            pq.push(num);  
            if (pq.size() > k) pq.pop();  
        }  
    }  
    int add(int val) {  
        pq.push(val);  
        if (pq.size() > k) pq.pop();  
        return pq.top();  
    }  
};
```

Dry Run:

- $k = 3$, $\text{nums} = [4, 5, 8, 2]$

- Initial heap = [4,5,8] → top = 4
- Add 3 → heap = [4,5,8] → top = 4
- Add 5 → heap = [5,5,8] → top = 5

Time Complexity: $O(\log k)$ per add

Space Complexity: $O(k)$

Pattern / Template:

| Min Heap, size = k, top = kth largest

2 Merge K Sorted Lists (LeetCode)

Problem:

- k sorted linked lists → merge into one sorted list

Heap type: Min Heap (size ≤ k) → top = smallest current node

Approach:

1. Push **first node of each list** into min heap
2. Pop top → add to result
3. If node→next exists → push next into heap
4. Repeat until heap empty

```
class Solution {
public:
    ListNode* mergeKLists(vector<ListNode*>& lists) {
        priority_queue<pair<int,ListNode*>, vector<pair<int,ListNode*>>, greater
<pair<int,ListNode*>>> pq;
        for (auto node : lists) if (node) pq.push({node->val, node});
        ListNode* dummy = new ListNode(0);
        ListNode* tail = dummy;
        while (!pq.empty()) {
            auto top = pq.top(); pq.pop();
            tail->next = top.second; tail = tail->next;
            if (top.second->next) pq.push({top.second->next->val, top.second->ne
```

```

        xt});
    }
    return dummy→next;
}
};

```

Dry Run:

- Lists: [1→4→5, 1→3→4, 2→6]
- Heap initial: [1(L1),1(L2),2(L3)]
- Pop 1(L1) → push 4(L1) → Pop 1(L2) → push 3(L2) ... → final merged list = 1→1->2→3→4→4→5→6

Time Complexity: O(N log k)

Space Complexity: O(k)

Pattern / Template:

| Min Heap, store {value,node pointer}, size ≤ k, push next nodes

3 Merge K Sorted Arrays

Problem:

- k sorted arrays → merge into one sorted array

Heap type: Min Heap (size ≤ k) → top = smallest current element

Approach:

1. Push first element of each array into heap → store {value, array_idx, element_idx}
2. Pop top → push value into result
3. If element_idx+1 exists → push next element into heap
4. Repeat until heap empty

```

vector<int> mergeKSortedArrays(vector<vector<int>>& arrays) {
    priority_queue<tuple<int,int,int>, vector<tuple<int,int,int>>, greater<tuple<i

```

```

nt,int,int>>> pq;
vector<int> result;
for (int i=0;i<arrays.size();i++)
    if (!arrays[i].empty()) pq.push({arrays[i][0],i,0});
while (!pq.empty()) {
    auto [val,arrIdx,elemIdx] = pq.top(); pq.pop();
    result.push_back(val);
    if (elemIdx+1 < arrays[arrIdx].size())
        pq.push({arrays[arrIdx][elemIdx+1],arrIdx,elemIdx+1});
}
return result;
}

```

Dry Run:

- arrays = [[1,4,5],[1,3,4],[2,6]]
- Initial heap: [(1,0,0),(1,1,0),(2,2,0)] → pop 1, push next 4 → ... → final = [1,1,2,3,4,4,5,6]

Time Complexity: O(N log k)

Space Complexity: O(k)

Pattern / Template:

| Min Heap, store {value, array_idx, element_idx}, push next element

4 Task Scheduler (LeetCode)

Problem:

- Tasks = [A,A,A,B,B,B], cooling interval n
- Min total time to execute all tasks

Heap type: Max Heap (size ≤ 26) → top = most frequent task

Approach:

1. Count frequency of tasks
2. Push all frequencies into max heap

3. While heap not empty:

- Loop $i=0..n$ (cooling interval)
- Pop top \rightarrow execute \rightarrow decrement frequency \rightarrow if >0 store in temp
- Increment time (idle if needed)
- Push temp back into heap

```
int leastInterval(vector<char>& tasks, int n) {  
    unordered_map<char,int> freq;  
    for (char t: tasks) freq[t]++;  
    priority_queue<int> pq;  
    for (auto it: freq) pq.push(it.second);  
    int time=0;  
    while(!pq.empty()) {  
        vector<int> temp;  
        int i=0;  
        for(;i<=n;i++) {  
            if(!pq.empty()) {  
                int f=pq.top(); pq.pop(); f--;  
                if(f>0) temp.push_back(f);  
            }  
            time++;  
            if(pq.empty() && temp.empty()) break;  
        }  
        for(int f: temp) pq.push(f);  
    }  
    return time;  
}
```

Dry Run:

- tasks = [A,A,A,B,B,B], n=2
- freq: A=3, B=3 \rightarrow heap: [3,3]
- Interval 1: pop A,B \rightarrow push back [2,2] \rightarrow time += 3 (idle included)

- Interval 2: pop A,B → push back [1,1] → time += 3
- Interval 3: pop A,B → heap empty → time +=2
- Total time = 8

Time Complexity: O(N)

Space Complexity: O(26)

Pattern / Template:

| Max Heap → top = most frequent task, loop n+1 units, push remaining back