

# Planning IV

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#### 50.021 Artificial Intelligence

The following notes are compiled from various sources such as textbooks, lecture materials, Web resources and are shared for academic purposes only, intended for use by students registered for a specific course. In the interest of brevity, every source is not cited. The compiler of these notes gratefully acknowledges all such sources.



### Faster Heuristics: Overall Idea

Concise representation using facts (F) and actions (A)

$$^{\circ} F_0 = x_1, x_2$$

$$\circ$$
 A<sub>0</sub> = O<sub>1</sub>, O<sub>2</sub>

$$\circ$$
  $F_1 = X_1, X_2, X_3, X_4, X_5$ 

$$\circ$$
 A<sub>1</sub> = O<sub>3</sub>, O<sub>4</sub>

$$\circ$$
  $F_2 = x_1, x_2, x_3, x_4, x_5, x_6, x_7$ 

$$^{\circ}$$
 A<sub>2</sub> = o<sub>5</sub>

$$F_3 = X_1, X_2, X_3, X_4, X_5, X_6, X_7, X_8$$

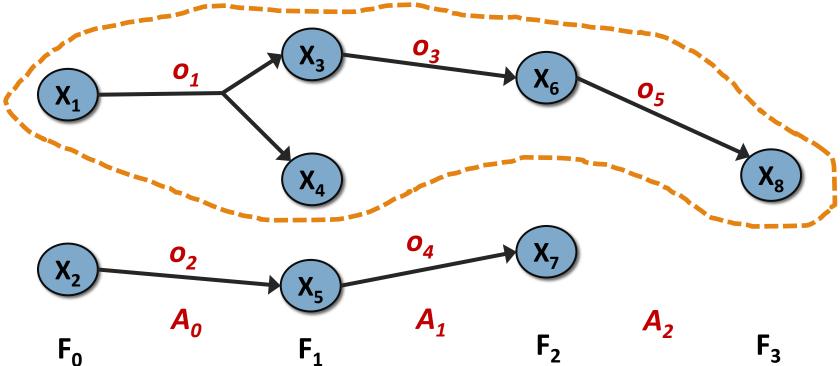
- Why do we care about the level/index of a fact?
  - It tells us the <u>number of actions (i.e., cost) required</u> to achieve that fact
  - This is useful as we examine the h<sub>max</sub>, h<sub>add</sub> heuristics



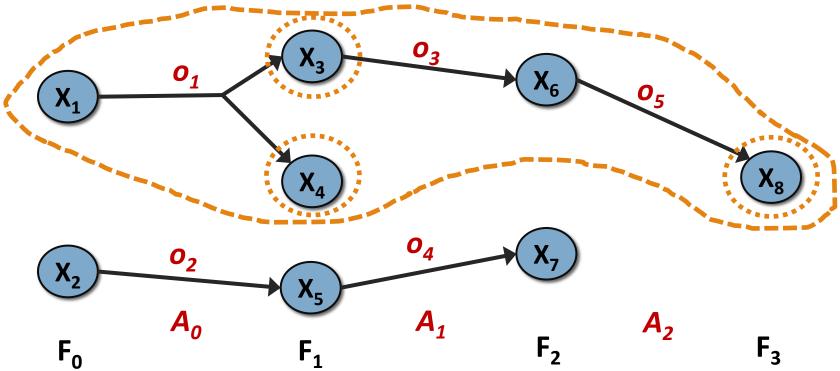
- h<sub>max</sub> is the cost of the single most costly goal fact (out of all goal facts)
  - i.e., the max number of actions needed for achieving one of the goal facts.



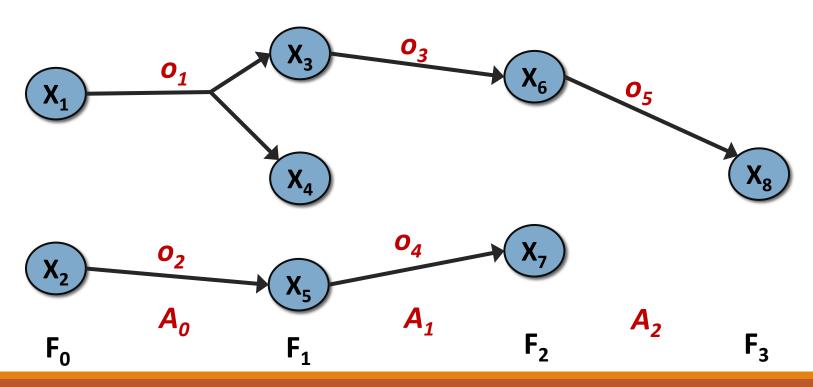
- h<sub>max</sub> is the cost of the single most costly goal fact (out of all goal facts)
  - Given goals  $x_3$ ,  $x_4$ ,  $x_8$ ,  $h_{max} = 3$



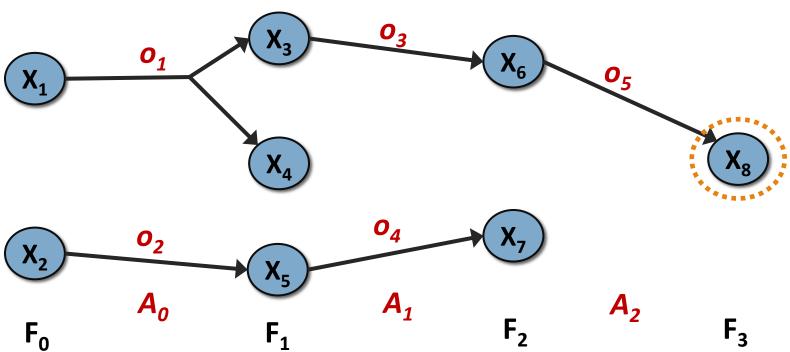
- An optimistic heuristic
  - Implicit assumption is that an action can set multiple facts to true



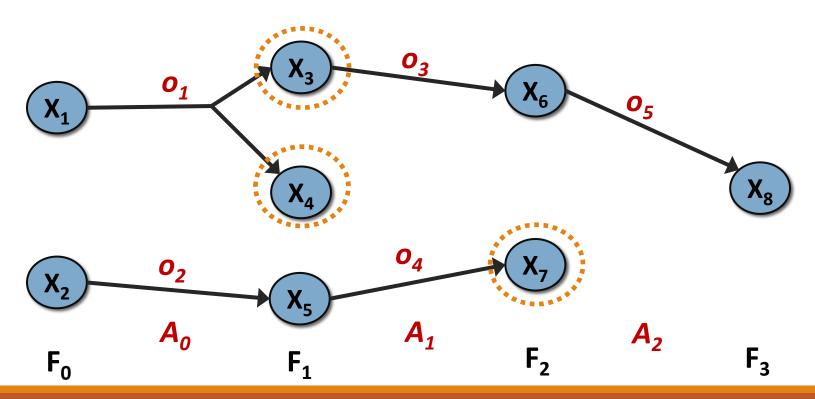
o Is h<sub>max</sub> admissible?



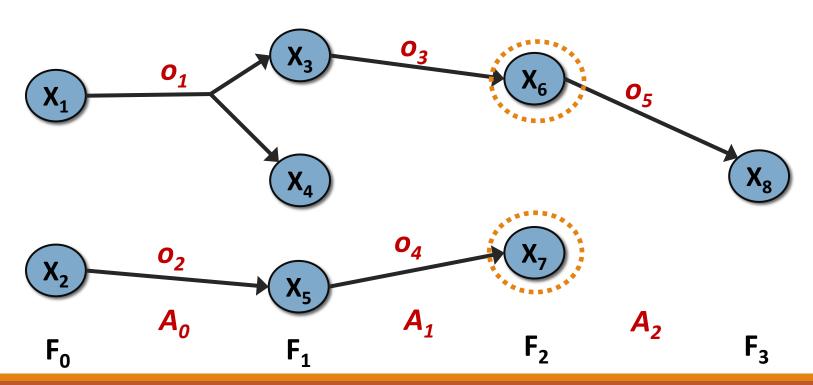
- o Is h<sub>max</sub> admissible? Yes
  - Given goals  $x_8$ ,  $h_{max} = h^*$



- Is h<sub>max</sub> admissible? Yes
  - Given goals  $x_3$ ,  $x_4$ ,  $x_7$ ,  $h_{max} < h^*$

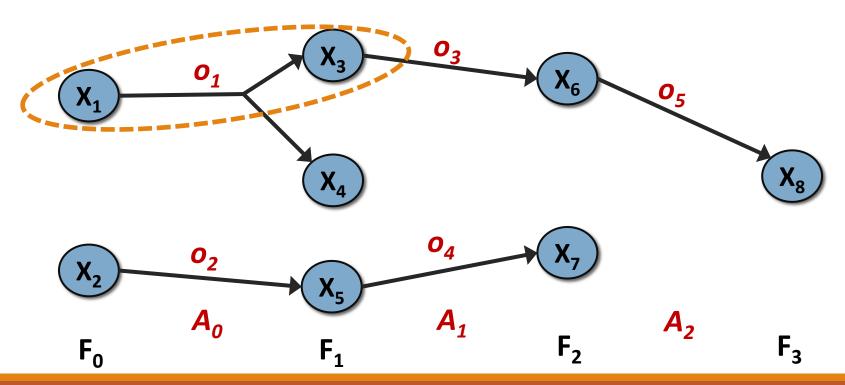


- However, h<sub>max</sub> could under-estimate the true cost (by a lot)
  - What if the goals were  $x_6$ ,  $x_7$ ?

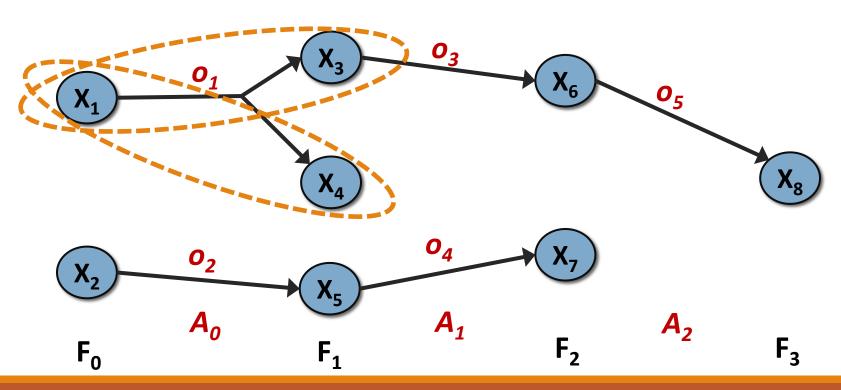


- h<sub>add</sub> is the summed cost of all goal facts
  - Adds up the number of actions needed to set a fact to true

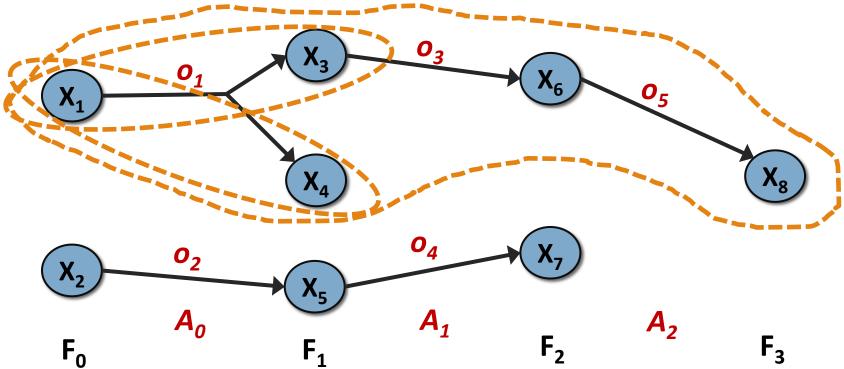
- h<sub>add</sub> is the summed cost of all goal facts
  - Given goals  $x_3$ ,  $x_4$ ,  $x_8$ ,  $h_{add} = 1$



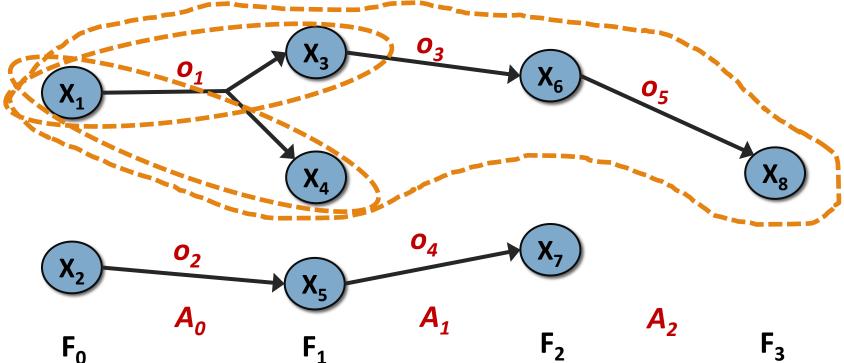
- h<sub>add</sub> is the summed cost of all goal facts
  - Given goals  $x_3$ ,  $x_4$ ,  $x_8$ ,  $h_{add} = 1 + 1$



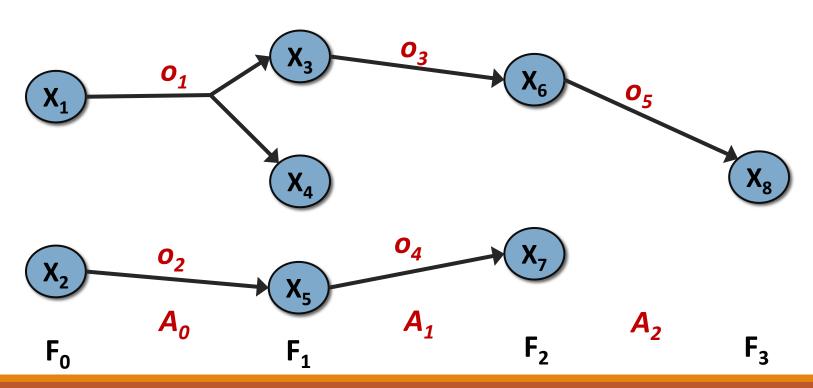
- h<sub>add</sub> is the summed cost of all goal facts
  - Given goals  $x_3$ ,  $x_4$ ,  $x_8$ ,  $h_{add} = 1 + 1 + 3 = 5$



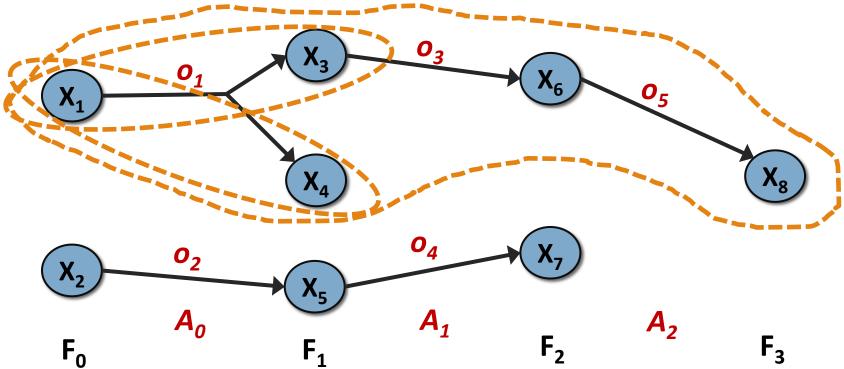
- A pessimistic heuristic
  - Implicit assumption is that an action can only set one fact to true, and vice versa



o Is h<sub>add</sub> admissible?

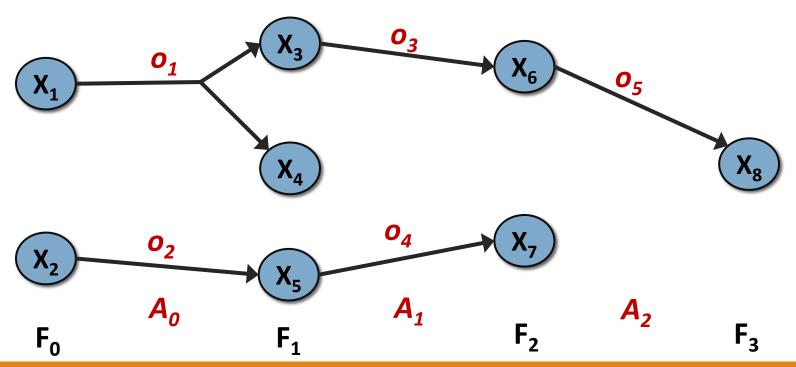


- o Is h<sub>add</sub> admissible? No
  - Given goals  $x_3$ ,  $x_4$ ,  $x_8$ ,  $h_{add} > h^*$



o Given goals  $x_3$ ,  $x_4$ ,  $x_7$ ,  $x_8$ , calculate  $h_{max}$  and  $h_{add}$ ?  $h \max = 3$  h add = 1+1+3+2=7

o Given goals  $x_6$ ,  $x_7$ , calculate  $h_{max}$  and  $h_{add}$ ?  $h_{max} = 2$  $h_{add} = 2+2=4$ 



- o Given goals  $x_3$ ,  $x_4$ ,  $x_7$ ,  $x_8$ , calculate  $h_{max}$  and  $h_{add}$ ?  $h_{max} = 3$ ,  $h_{add} = 7$
- o Given goals  $x_6$ ,  $x_7$ , calculate  $h_{max}$  and  $h_{add}$ ?
- Concise representation using facts (F) and actions (A)

$$^{\circ} F_0 = x_1, x_2$$

$$\circ$$
 A<sub>0</sub> = O<sub>1</sub>, O<sub>2</sub>

$$\circ$$
  $F_1 = x_1, x_2, x_3, x_4, x_5$ 

$$\circ$$
 A<sub>1</sub> = O<sub>3</sub>, O<sub>4</sub>

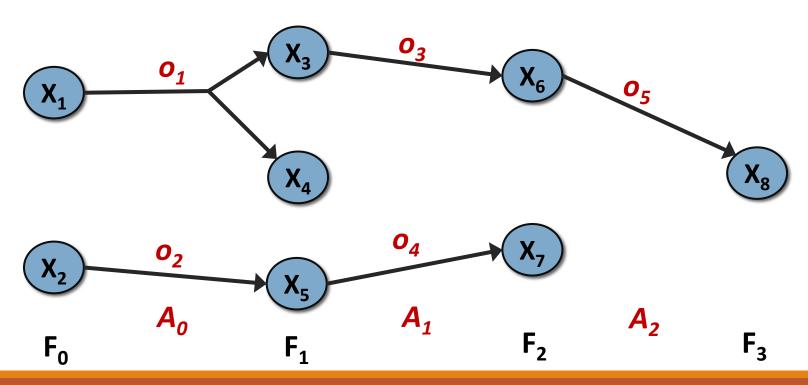
$$\circ$$
  $F_2 = x_1, x_2, x_3, x_4, x_5, x_6, x_7$ 

$$^{\circ}$$
 A<sub>2</sub> = o<sub>5</sub>

$$F_3 = X_1, X_2, X_3, X_4, X_5, X_6, X_7, X_8$$

- o Given goals  $x_3$ ,  $x_4$ ,  $x_7$ ,  $x_8$ , calculate  $h_{max}$  and  $h_{add}$ ?  $h_{max} = 3$ ,  $h_{add} = 7$

• Given goals  $x_6$ ,  $x_7$ , calculate  $h_{max}$  and  $h_{add}$ ?



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- o Given goals  $x_3$ ,  $x_4$ ,  $x_7$ ,  $x_8$ , calculate  $h_{max}$  and  $h_{add}$ ?  $h_{max} = 3$ ,  $h_{add} = 7$
- o Given goals  $x_6$ ,  $x_7$ , calculate  $h_{max}$  and  $h_{add}$ ?  $h_{max} = 2$ ,  $h_{add} = 4$
- Concise representation using facts (F) and actions (A)
  - $^{\circ} F_0 = x_1, x_2$
  - $\circ$  A<sub>0</sub> = O<sub>1</sub>, O<sub>2</sub>
  - $\circ$   $F_1 = X_1, X_2, X_3, X_4, X_5$
  - $^{\circ}$  A<sub>1</sub> = 0<sub>3</sub>, 0<sub>4</sub>
  - $\cdot F_2 = X_1, X_2, X_3, X_4, X_5, X_6, X_7$
  - $\circ$   $A_2 = o_5$
  - $\circ$   $F_3 = X_1, X_2, X_3, X_4, X_5, X_6, X_7, X_8$

## h<sub>max</sub> versus h<sub>add</sub>

- h<sub>max</sub> is too optimistic tends to underestimate true cost
  - Only considers the longest path of actions (assumes that all goals are on that path)
  - Ignores that there can be partially non-overlapping or independent paths of actions leading to multiple goals.
- h<sub>add</sub> is too pessimistic tends to overestimate true cost
  - Assumes that there are only independent paths leading to each goal
  - However, multiple goals or facts can exist on a single path of action
- In reality, paths of actions can be partially independent, and partially overlapping/shared



### Summary

- Discussed planning problem formulation using STRIPS
- Discussed a relaxation to the planning problem by removing negations
- Discussed various heuristics:
  - h+ is the optimal plan to a delete-relaxed problem
  - h<sub>max</sub> is admissible, but often too loose, too low.
  - h<sub>add</sub> is inadmissible, sometimes way too large compared to h+ which we want to approximate
  - h<sub>FF</sub> is inadmissible, but in practice useful



o Given this problem definition:

```
• Variables: x_1, x_2, x_3, x_4, x_5, x_6
```

Initial State: x<sub>1</sub>

• Goal:  $x_2, x_5, x_6$ 

• Actions:  $o_1$ : precond:  $x_1$ , postcond:  $x_2$ 

 $o_2$ : precond:  $x_2$ , postcond:  $x_1$ ,  $x_3$ 

 $o_3$ : precond:  $x_3$ , postcond:  $x_2$ ,  $x_1$ ,  $x_4$ 

 $o_4$ : precond:  $x_2$ ,  $x_4$ , postcond:  $x_5$ 

 $o_5$ : precond:  $x_1$ ,  $x_5$ , postcond:  $-x_5$ ,  $x_6$ 

- Task: Make this a delete-relaxed problem
- Task: Determine the level where all goal facts are achieved
- Task: Calculate the h<sub>max</sub> and h<sub>add</sub> heuristics



o Given this problem definition:

```
• Variables: x_1, x_2, x_3, x_4, x_5, x_6
```

Initial State: x<sub>1</sub>

• Goal:  $x_2, x_5, x_6$ 

• Actions:  $o_1$ : precond:  $x_1$ , postcond:  $x_2$ 

 $o_2$ : precond:  $x_2$ , postcond:  $-x_1$ ,  $x_3$ 

 $o_3$ : precond:  $x_3$ , postcond:  $-x_2$ ,  $x_1$ ,  $x_4$ 

 $o_4$ : precond:  $x_2$ ,  $x_4$ , postcond:  $x_5$ 

 $o_5$ : precond:  $x_1$ ,  $x_5$ , postcond:  $-x_5$ ,  $x_6$ 

Task: Make this a delete-relaxed problem



o Given this problem definition:

```
• Variables: x_1, x_2, x_3, x_4, x_5, x_6
```

Initial State: x<sub>1</sub>

• Goal:  $x_2, x_5, x_6$ 

• Actions:  $o_1$ : precond:  $x_1$ , postcond:  $x_2$ 

 $o_2$ : precond:  $x_2$ , postcond:  $-x_1$ ,  $x_3$ 

 $o_3$ : precond:  $x_3$ , postcond:  $-x_2$ ,  $x_1$ ,  $x_4$ 

 $o_4$ : precond:  $x_2$ ,  $x_4$ , postcond:  $x_5$ 

 $o_5$ : precond:  $x_1$ ,  $x_5$ , postcond:  $-x_5$ ,  $x_6$ 

Task: Determine the level where all goal facts are achieved

Concise representation using facts (F) and actions (A)

$$^{\circ}$$
  $F_0 = x_1$ 

$$^{\circ}$$
 A<sub>0</sub> = o<sub>1</sub>,

$$F_1 = X_1, X_2$$

$$\circ$$
 A<sub>1</sub> = O<sub>2</sub>

$$F_2 = X_1, X_2, X_3$$

$$^{\circ}$$
 A<sub>2</sub> = o<sub>3</sub>

$$F_3 = X_1, X_2, X_3, X_4$$

$$\circ$$
 A<sub>4</sub> = O<sub>4</sub>

$$F_4 = X_1, X_2, X_3, X_4, X_5$$

$$\circ$$
 A<sub>5</sub> = o<sub>5</sub>

$$\circ$$
  $F_5 = x_1, x_2, x_3, x_4, x_5, x_6$ 

```
Variables: x_1, x_2, x_3, x_4, x_5, x_6

Initial State: x_1

Goal: x_2, x_5, x_6

Actions: o_1: pre: x_1, post: x_2

o_2: pre: x_2, post: -x_1, x_3

o_3: pre: x_3, post: -x_2, x_1, x_4

o_4: pre: x_2, x_4, post: x_5

o_5: pre: x_1, x_2, post: -x_3, x_4
```

Concise representation using facts (F) and actions (A)

```
^{\circ} F_0 = x_1
```

$$^{\circ}$$
 A<sub>0</sub> = o<sub>1</sub>,

$$^{\circ} F_1 = x_1, x_2$$

$$\circ$$
 A<sub>1</sub> = O<sub>2</sub>

$$F_2 = X_1, X_2, X_3$$

$$\circ$$
  $A_2 = o_3$ 

$$F_3 = X_1, X_2, X_3, X_4$$

$$^{\circ}$$
 A<sub>4 3</sub> = O<sub>4</sub>

$$F_4 = X_1, X_2, X_3, X_4, X_5$$

$$\circ$$
 A<sub>54</sub> = o<sub>5</sub>

$$\circ$$
  $F_5 = x_1, x_2, x_3, x_4, x_5, x_6$ 

```
Variables: x_1, x_2, x_3, x_4, x_5, x_6

Initial State: x_1

Goal: x_2, x_5, x_6

Actions: o_1: pre: x_1, post: x_2

o_2: pre: x_2, post: -x_1, x_3

o_3: pre: x_3, post: -x_2, x_1, x_4

o_4: pre: x_2, x_4, post: x_5

o_5: pre: x_1, x_5, post: -x_5, x_6
```

Task: Calculate the  $h_{max}$  and  $h_{add}$  heuristics

#### Concise representation using facts (F) and actions (A)

$$_{0}$$
  $F_{0}$  =  $x_{1}$ 

$$^{\circ}$$
 A<sub>0</sub> = o<sub>1</sub>,

$$F_1 = X_1, X_2$$

$$^{\circ}$$
 A<sub>1</sub> = 0<sub>2</sub>

$$F_2 = X_1, X_2, X_3$$

$$^{\circ}$$
 A<sub>2</sub> = o<sub>3</sub>

$$\circ$$
  $F_3 = X_1, X_2, X_3, X_4$ 

$$\circ$$
 A<sub>4</sub> = O<sub>4</sub>

$$F_4 = X_1, X_2, X_3, X_4, X_5$$

$$^{\circ}$$
 A<sub>5</sub> = o<sub>5</sub>

$$\circ$$
 F<sub>5</sub> = x<sub>1</sub>, x<sub>2</sub>, x<sub>3</sub>, x<sub>4</sub>, x<sub>5</sub>, x<sub>6</sub>

Variables: 
$$x_1, x_2, x_3, x_4, x_5, x_6$$
  
Initial State:  $x_1$   
Goal:  $x_2, x_5, x_6$   
Actions:  $o_1$ : pre:  $o_1$ : pre:  $o_2$ : pre:  $o_2$ : pre:  $o_3$ 

#### Task: Calculate the $h_{max}$ and $h_{add}$ heuristics

• 
$$h_{max} = max(1, 4, 5) = 5$$

• 
$$h_{add} = 1 + 4 + 5 = 10$$



### Overall Summary

- Able to describe planning problems in a simple formalism that is finding a sequence of actions.
- Able to formulate a planning problem as a STRIPS instance
- Understand the PDDL planning language
- Develop relaxed versions of planning problems and understand the various heuristics that can be used