

# Week 9 Exercises

## Adversarial Search

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*PROF. LIM KWAN HUI*

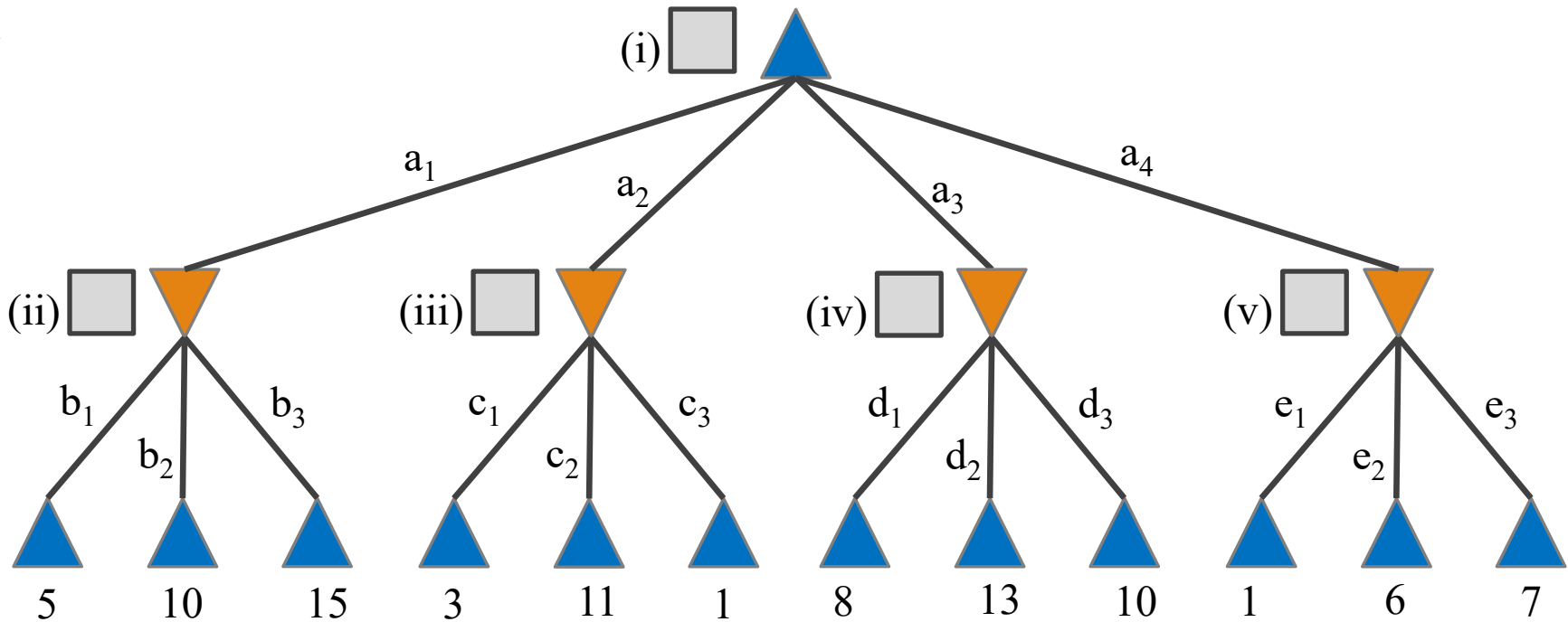
50.021 Artificial Intelligence

*The following notes are compiled from various sources such as textbooks, lecture materials, Web resources and are shared for academic purposes only, intended for use by students registered for a specific course. In the interest of brevity, every source is not cited. The compiler of these notes gratefully acknowledges all such sources.*

# Exercise: MiniMax

MAX

MIN

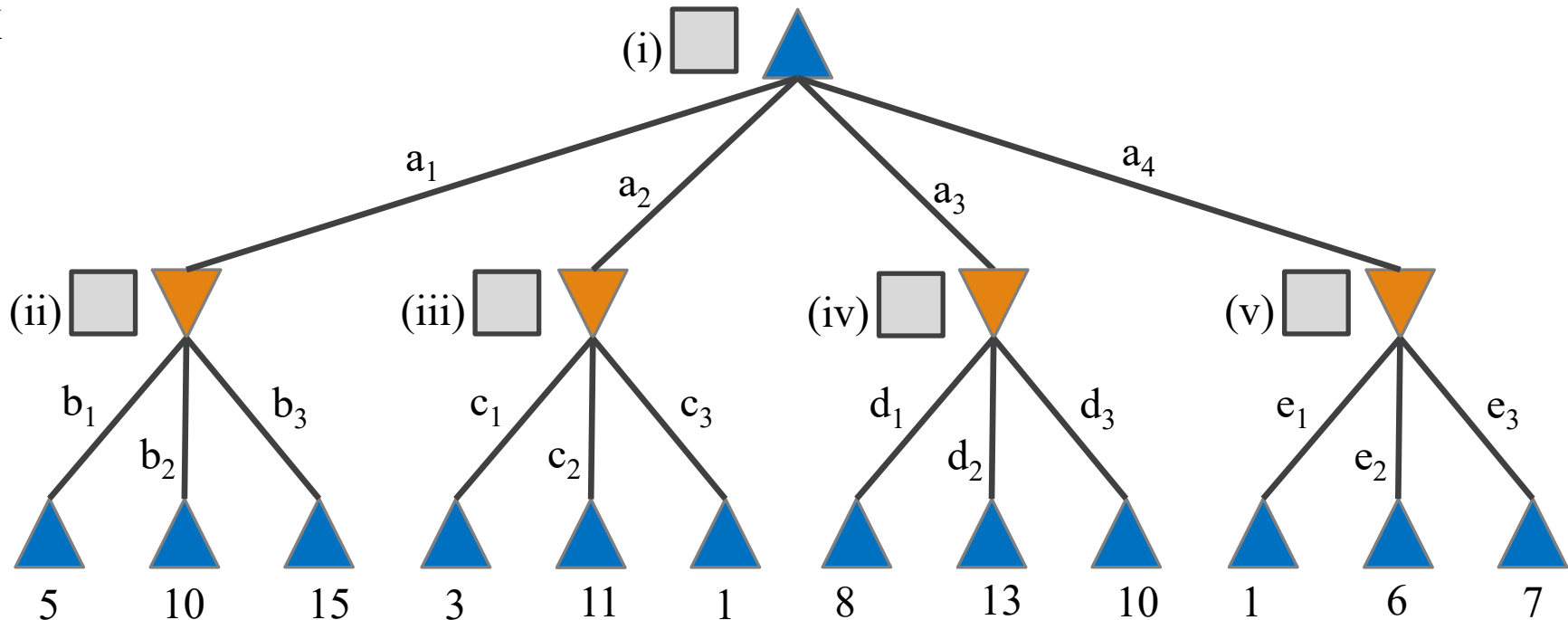


# Exercise: MiniMax

- Apply the **MiniMax algorithm** on this game tree. Assume that moves/actions are explored in lowest alphabetical order. List down the MiniMax values and state which move is chosen.

MAX

MIN



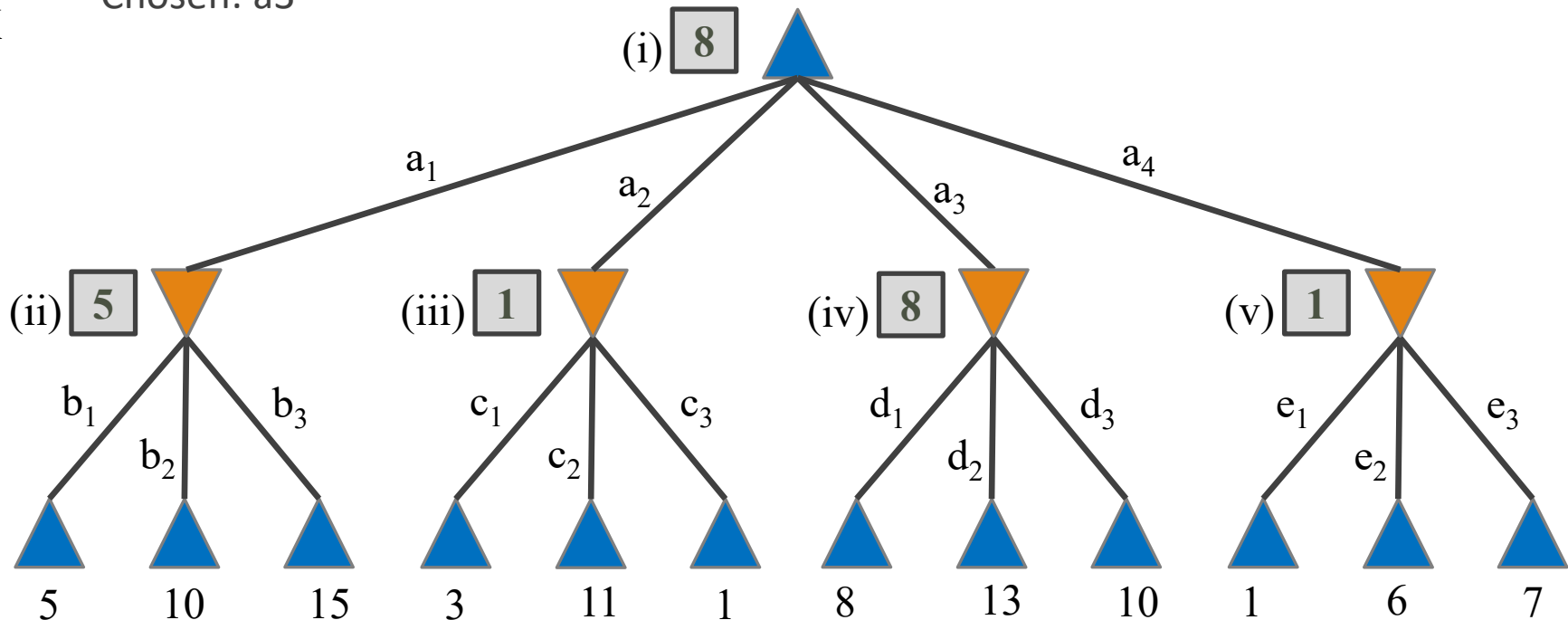
# Exercise: MiniMax

- Apply the **MiniMax algorithm** on this game tree. Assume that moves/actions are explored in lowest alphabetical order. List down the MiniMax values and state which move is chosen.

○ Chosen: a3

**MAX**

**MIN**

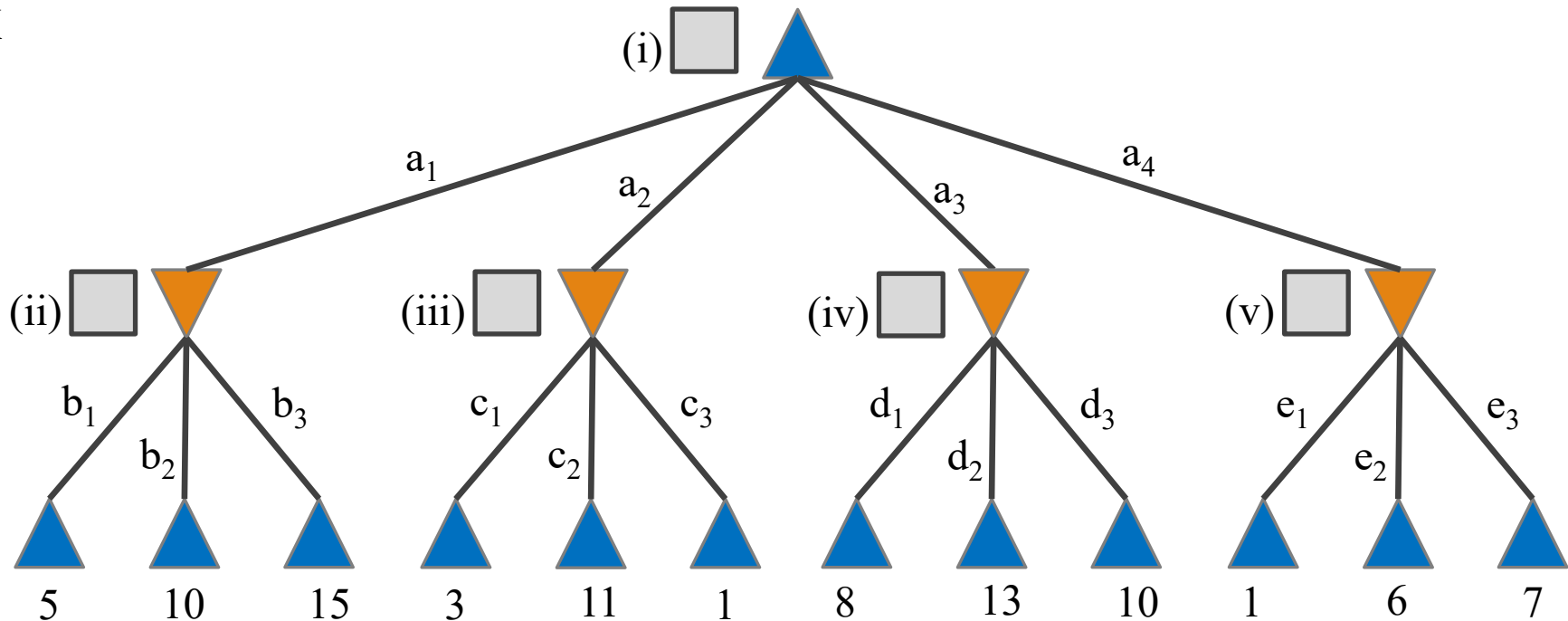


# Exercise: MiniMax with $\alpha$ - $\beta$

- Apply the **MiniMax algorithm with  $\alpha$ - $\beta$  pruning** on this game tree. Assume that moves/actions are explored in lowest alphabetical order. List down the moves/actions that were pruned (not explored at all), if any.

MAX

MIN



# Exercise: MiniMax with $\alpha$ - $\beta$

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## *Simple Intuitive Solution*

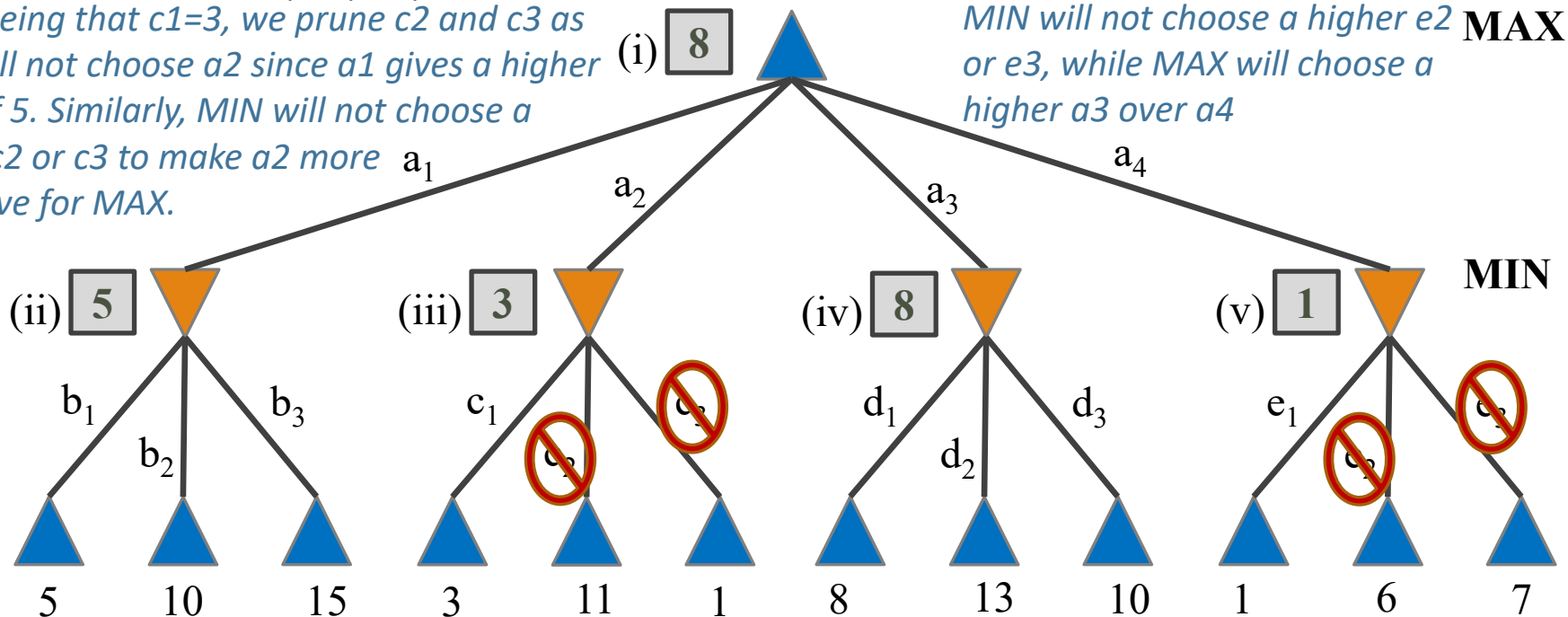
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- Pruned: c2, c3, e2, e3

After seeing that  $c_1=3$ , we prune  $c_2$  and  $c_3$  as MAX will not choose  $a_2$  since  $a_1$  gives a higher score of 5. Similarly, MIN will not choose a higher  $c_2$  or  $c_3$  to make  $a_2$  more attractive for MAX.

Similar reasoning for  $e_2$  and  $e_3$ . MIN will not choose a higher  $e_2$  or  $e_3$ , while MAX will choose a higher  $a_3$  over  $a_4$



# Exercise: MiniMax with $\alpha$ - $\beta$

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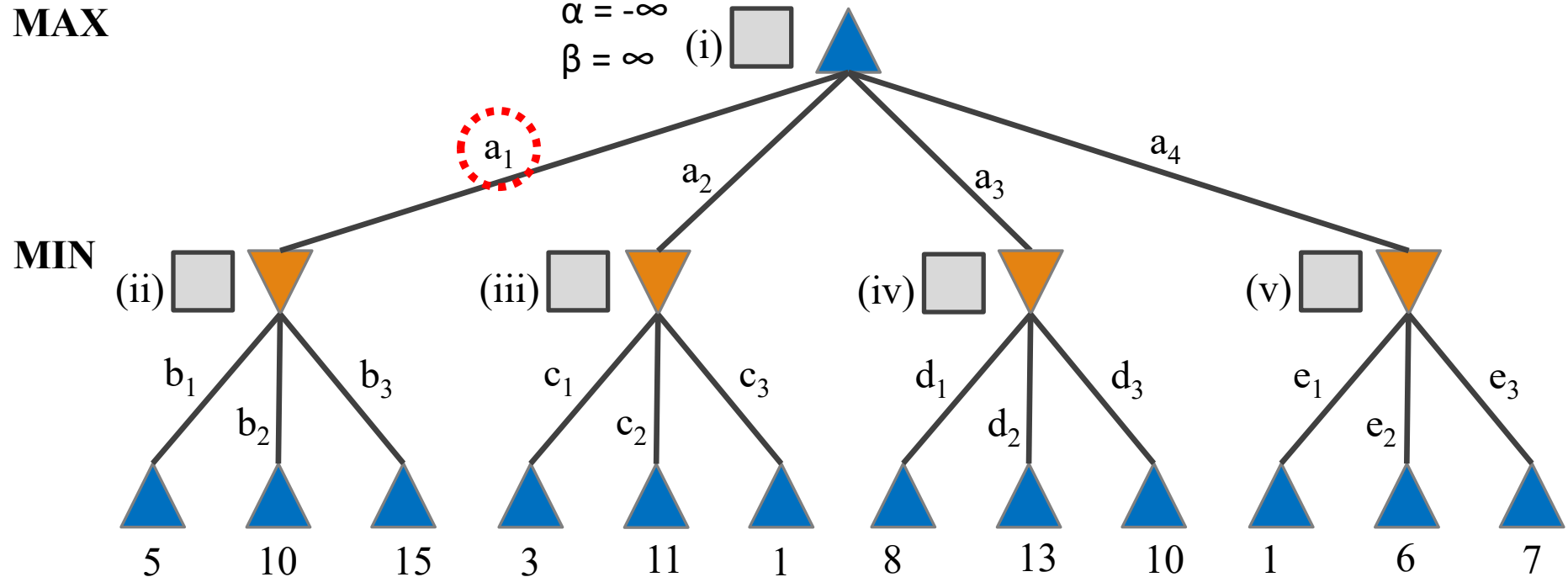
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## *Detailed Steps*



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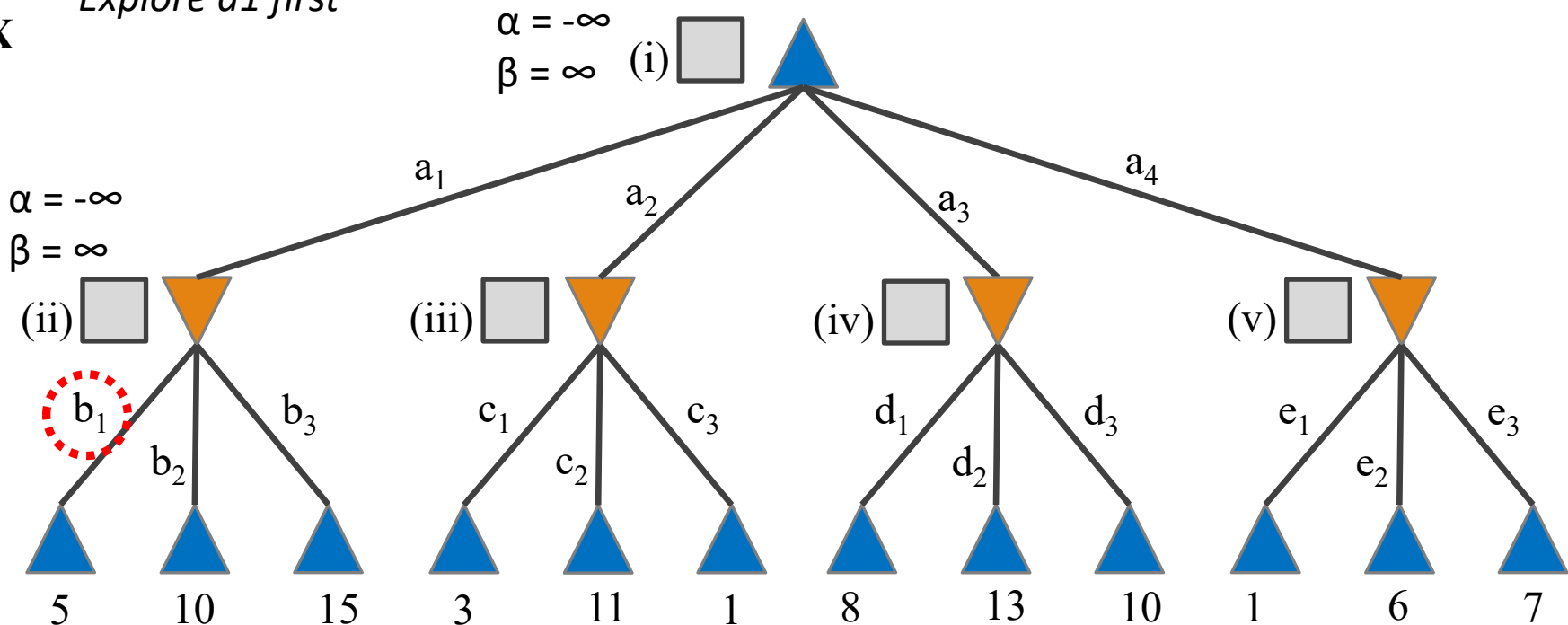
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*Explore  $a_1$  first*

**MAX**

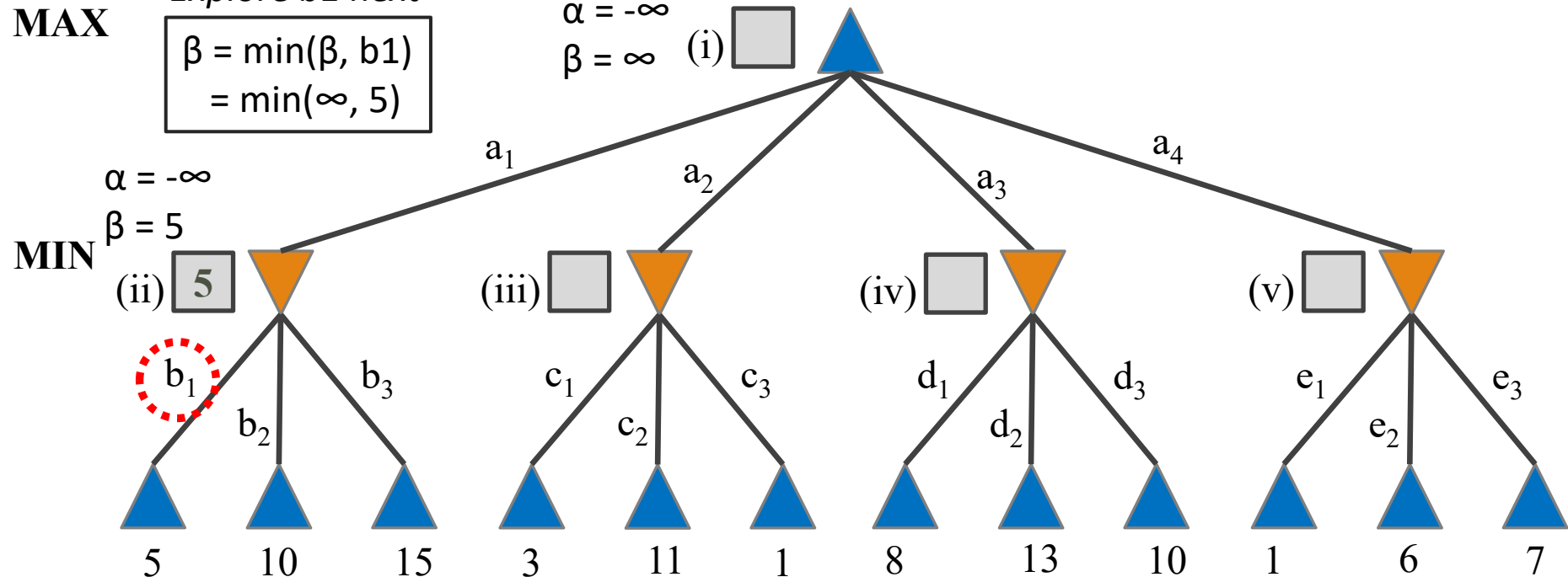
**MIN**



# Exercise: MiniMax with $\alpha$ - $\beta$

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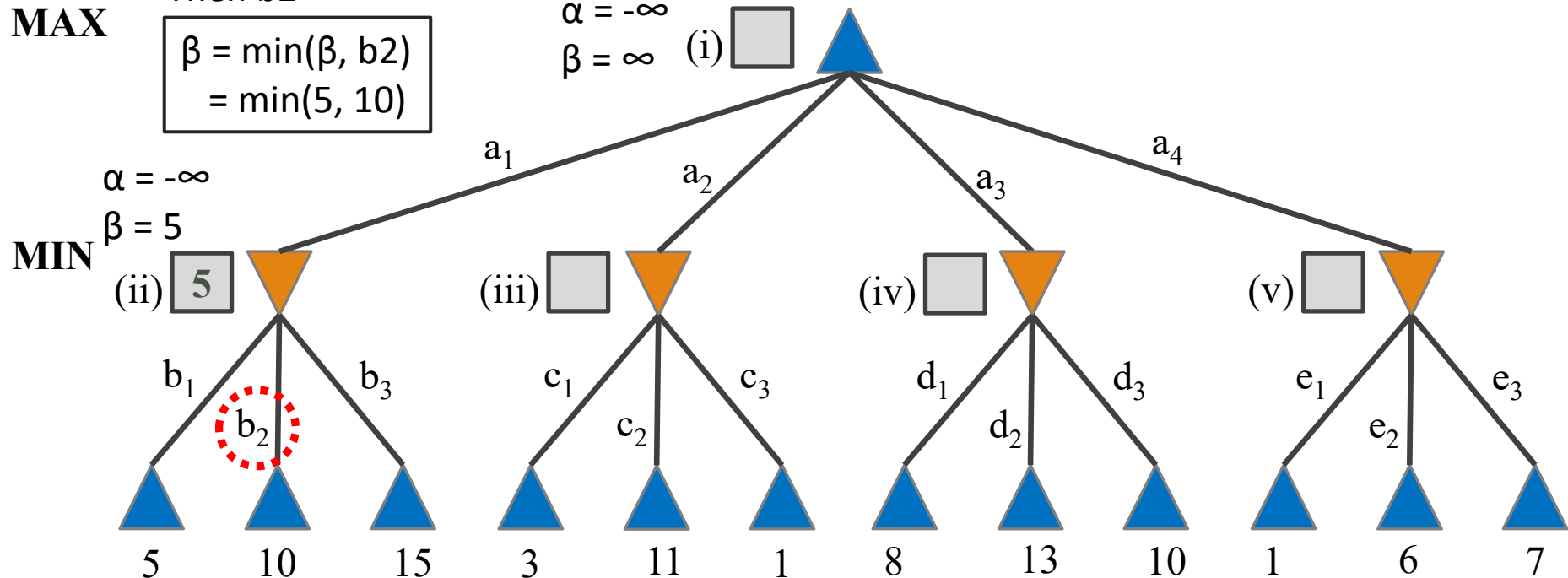
*Explore b1 next*



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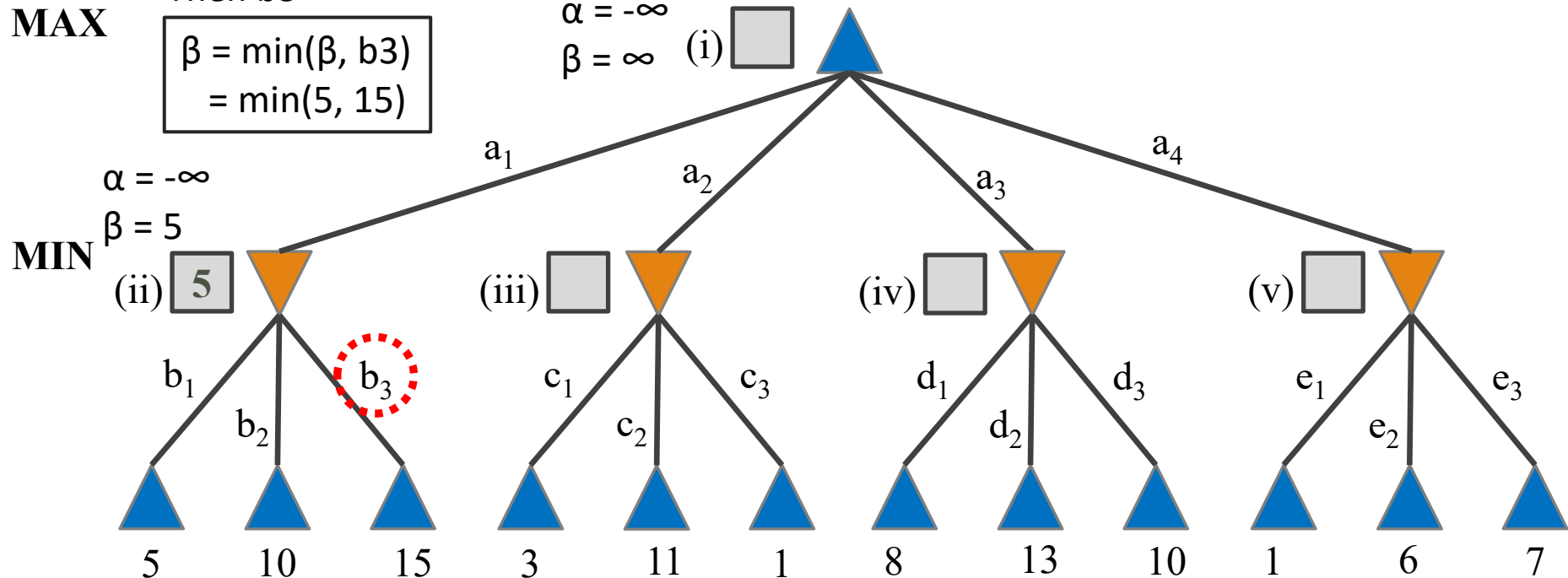
Then  $b_2$



# Exercise: MiniMax with $\alpha$ - $\beta$

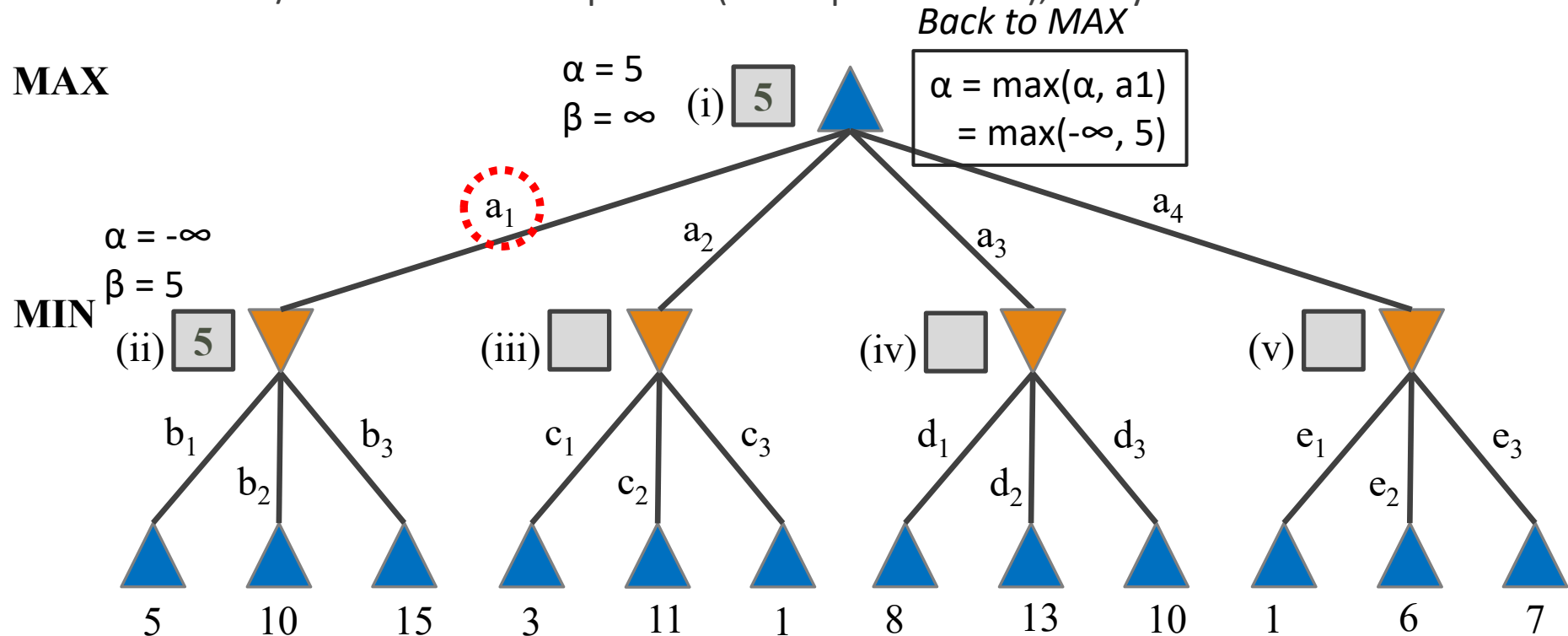
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Then  $b_3$



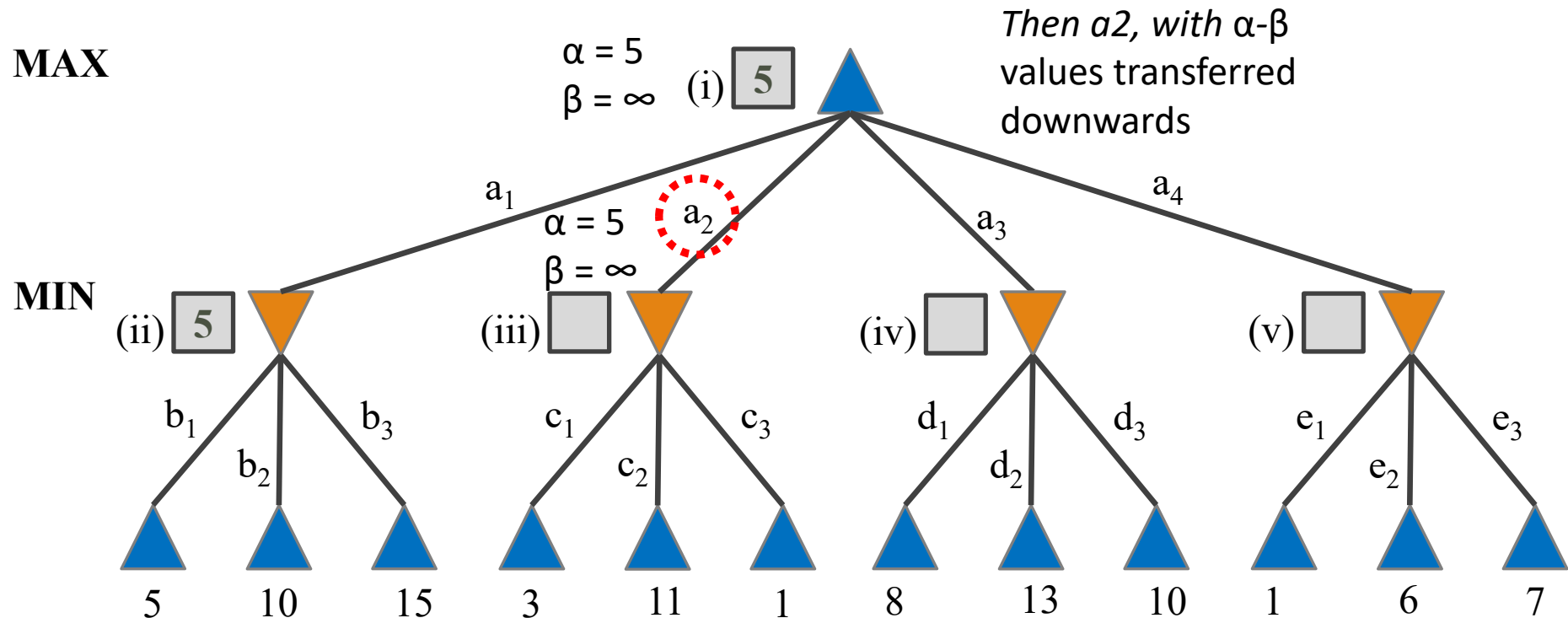
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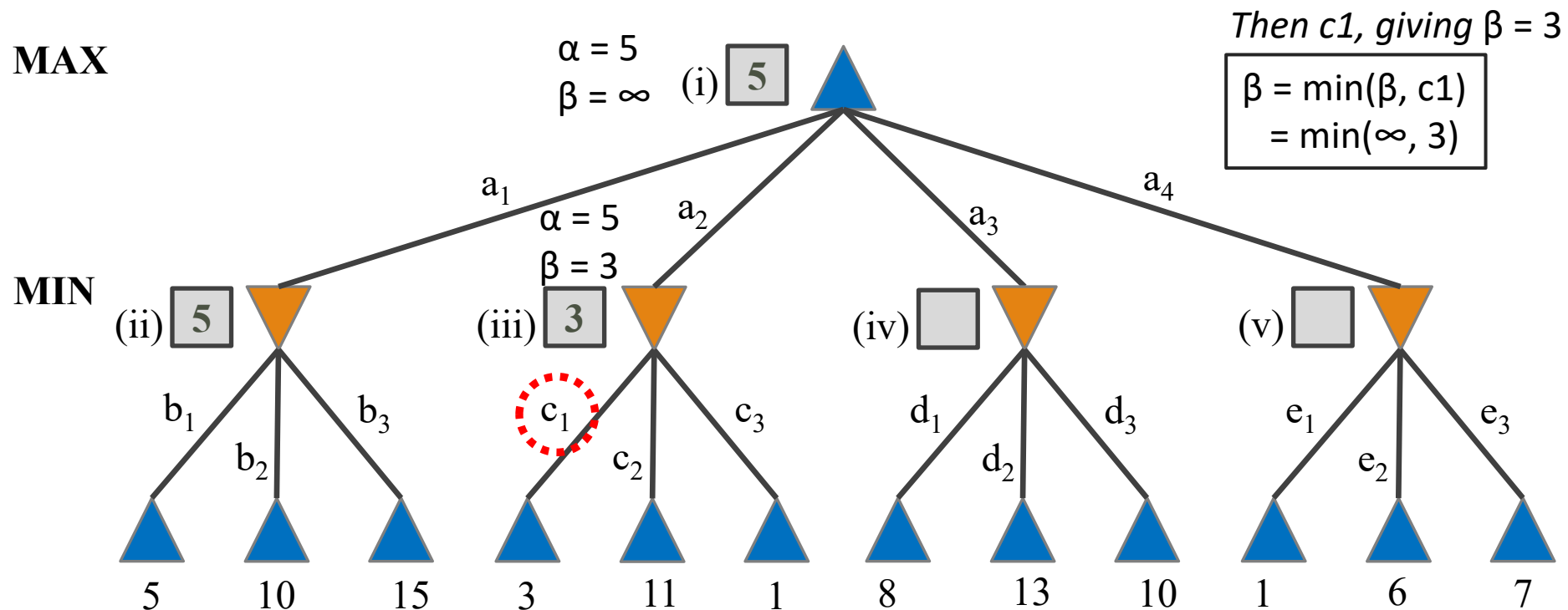
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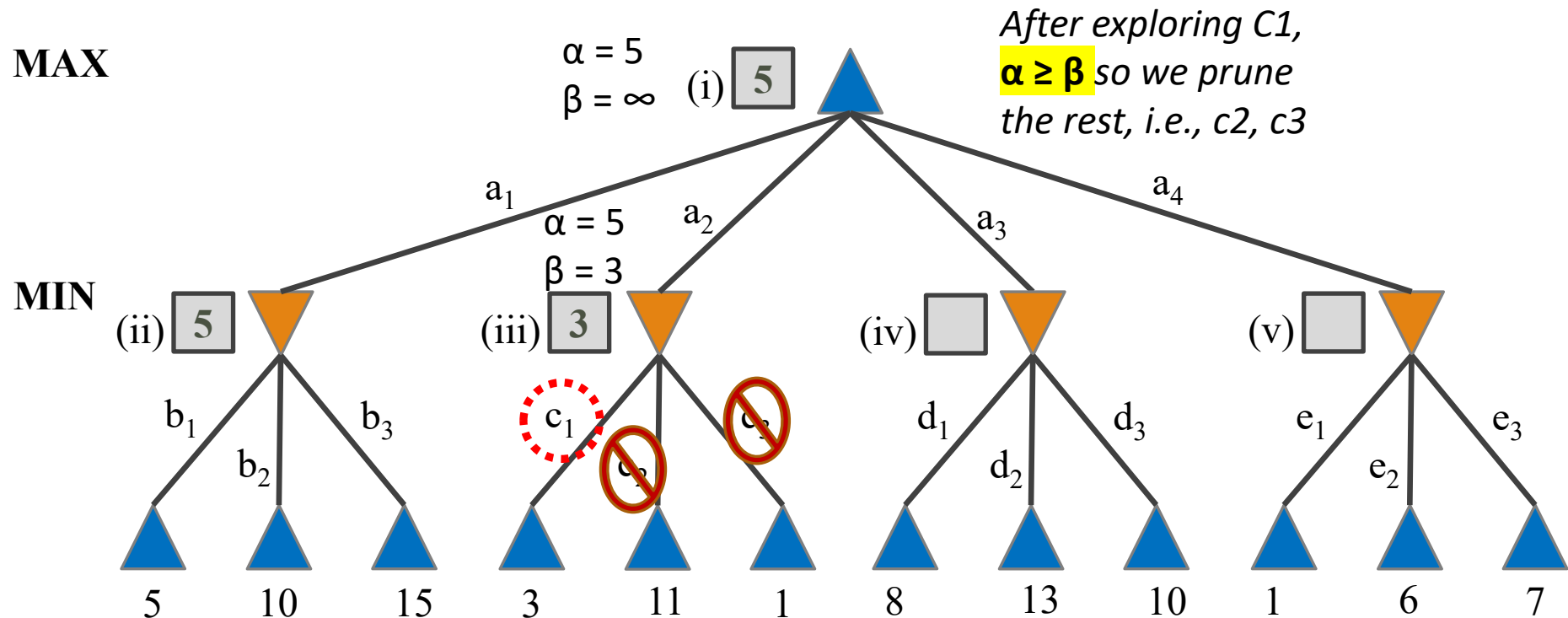
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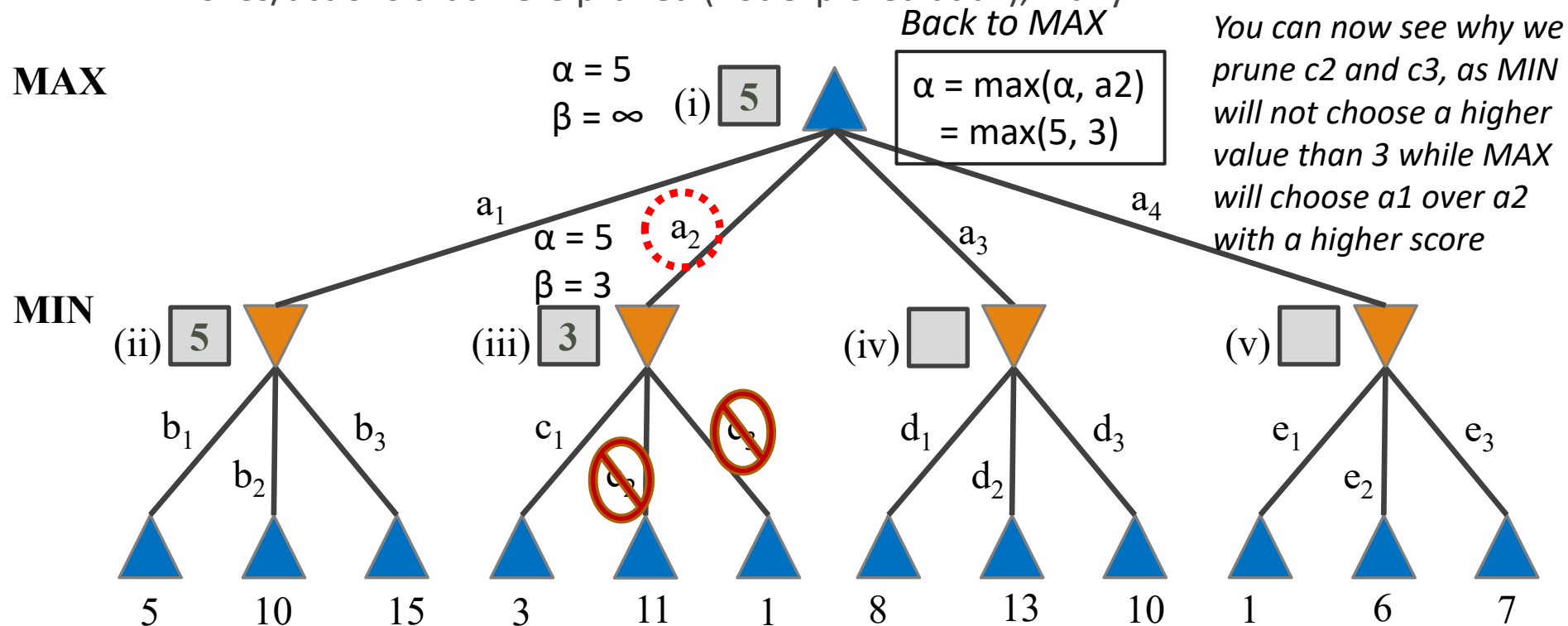
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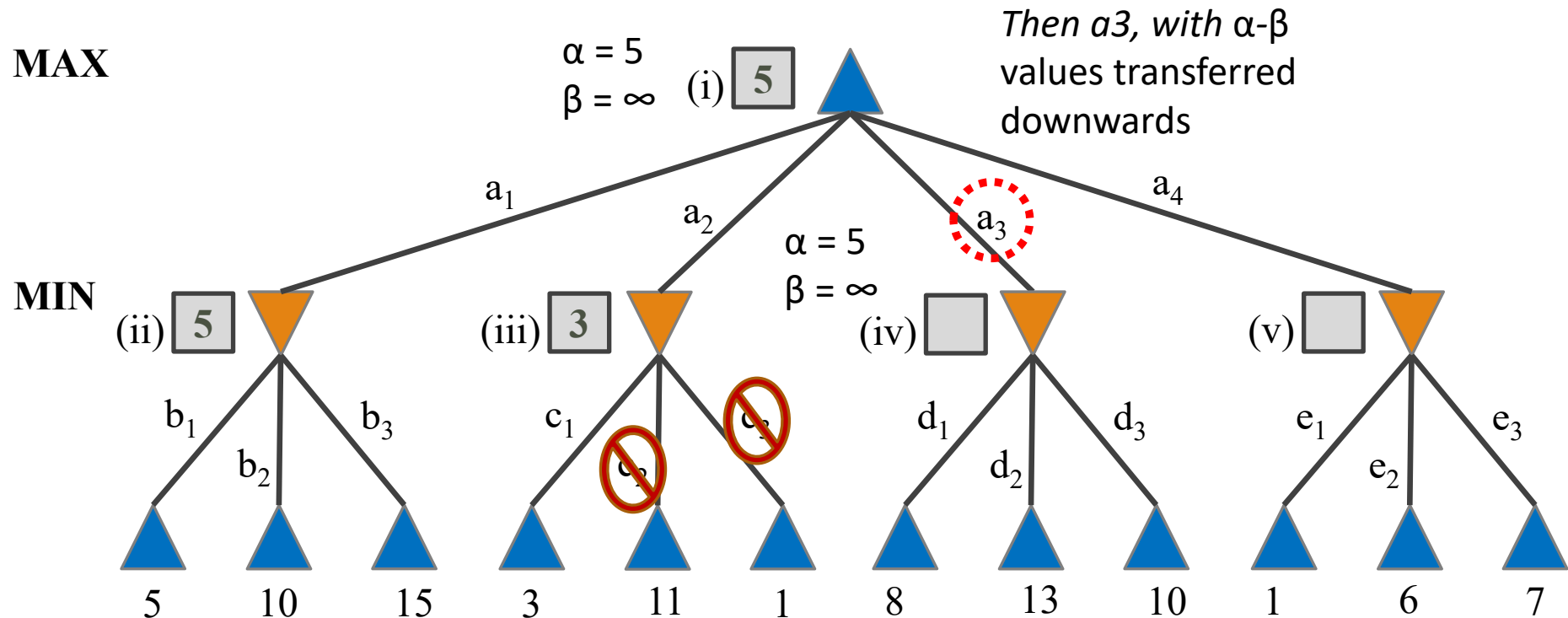
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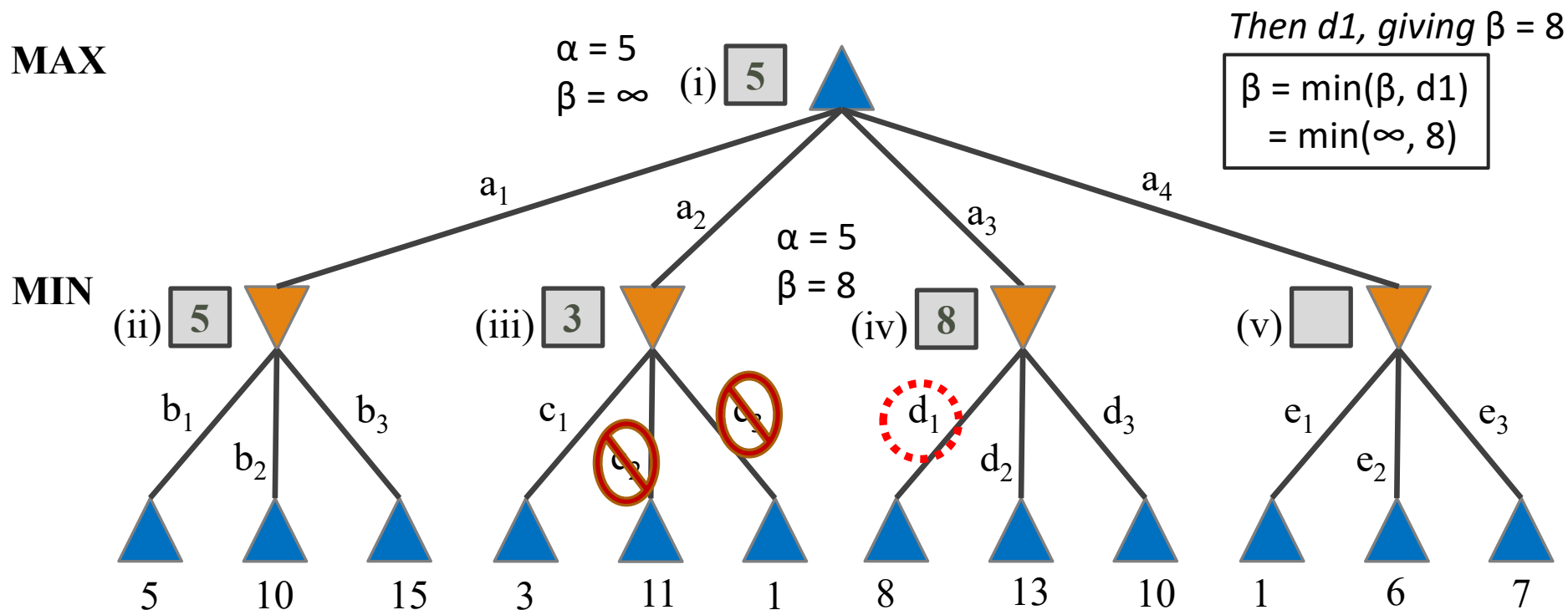
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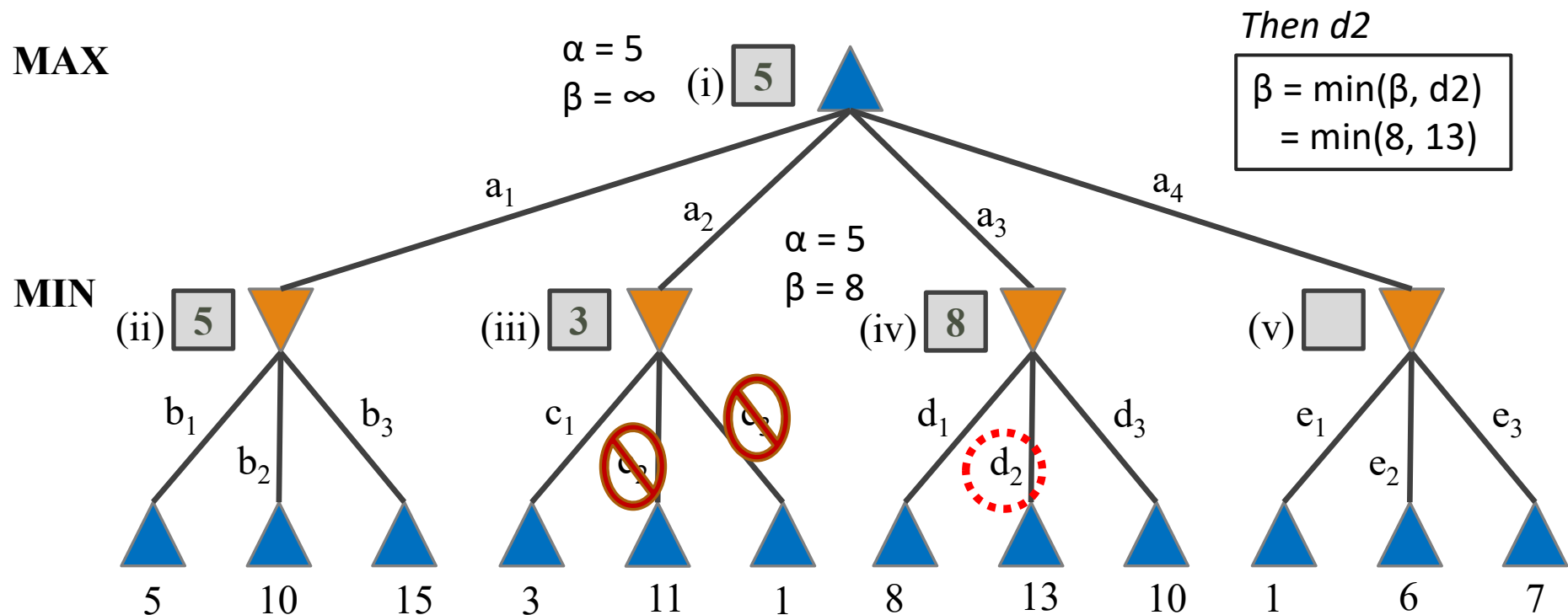
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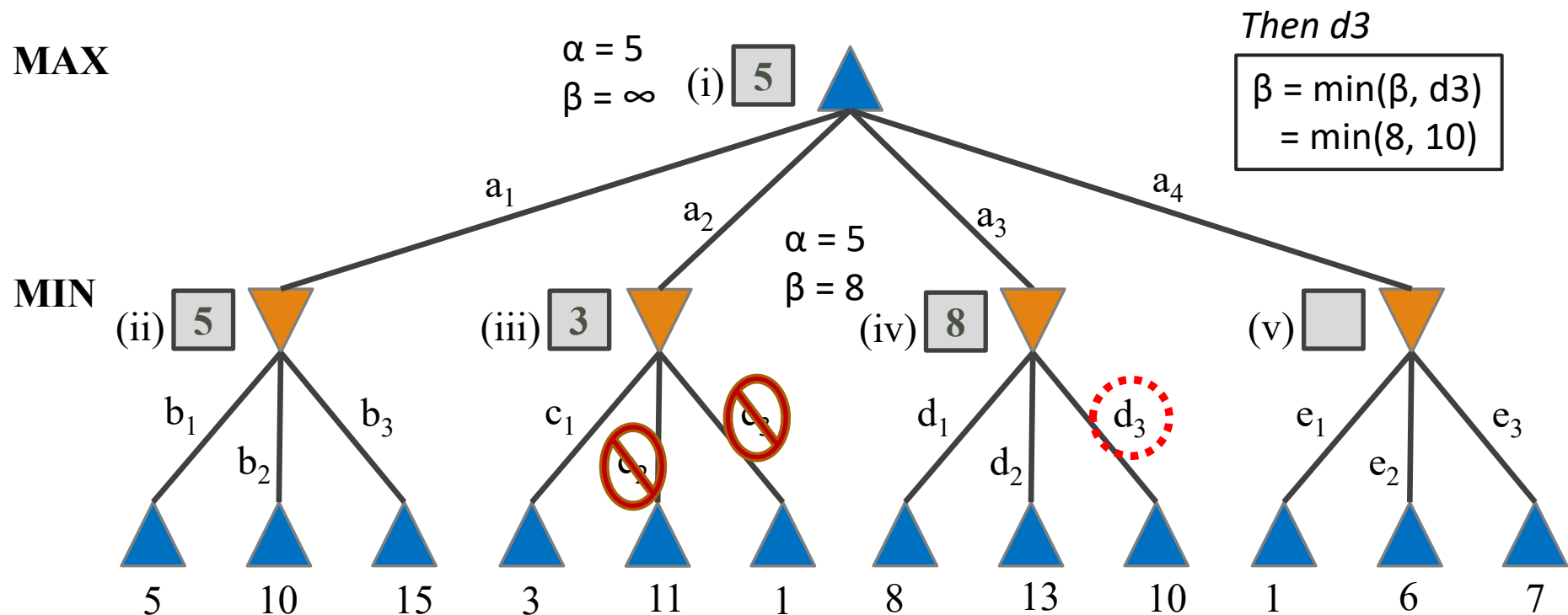
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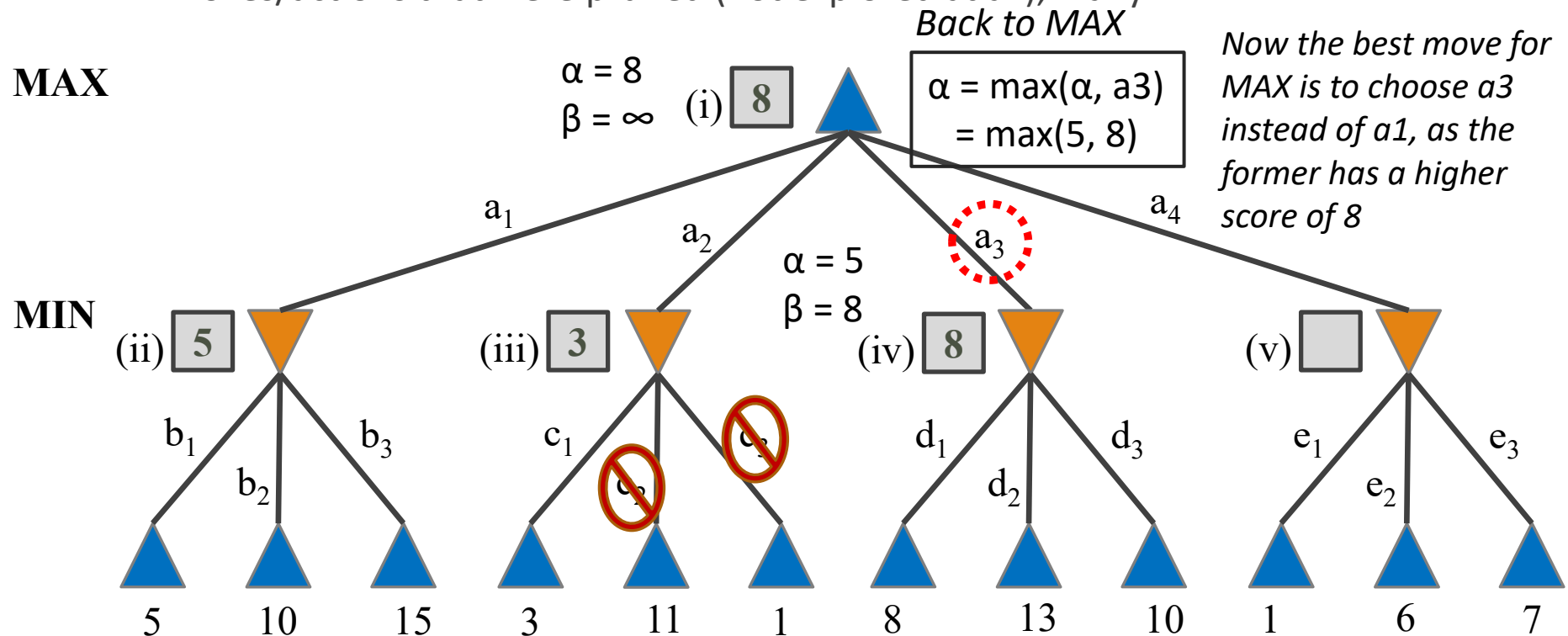
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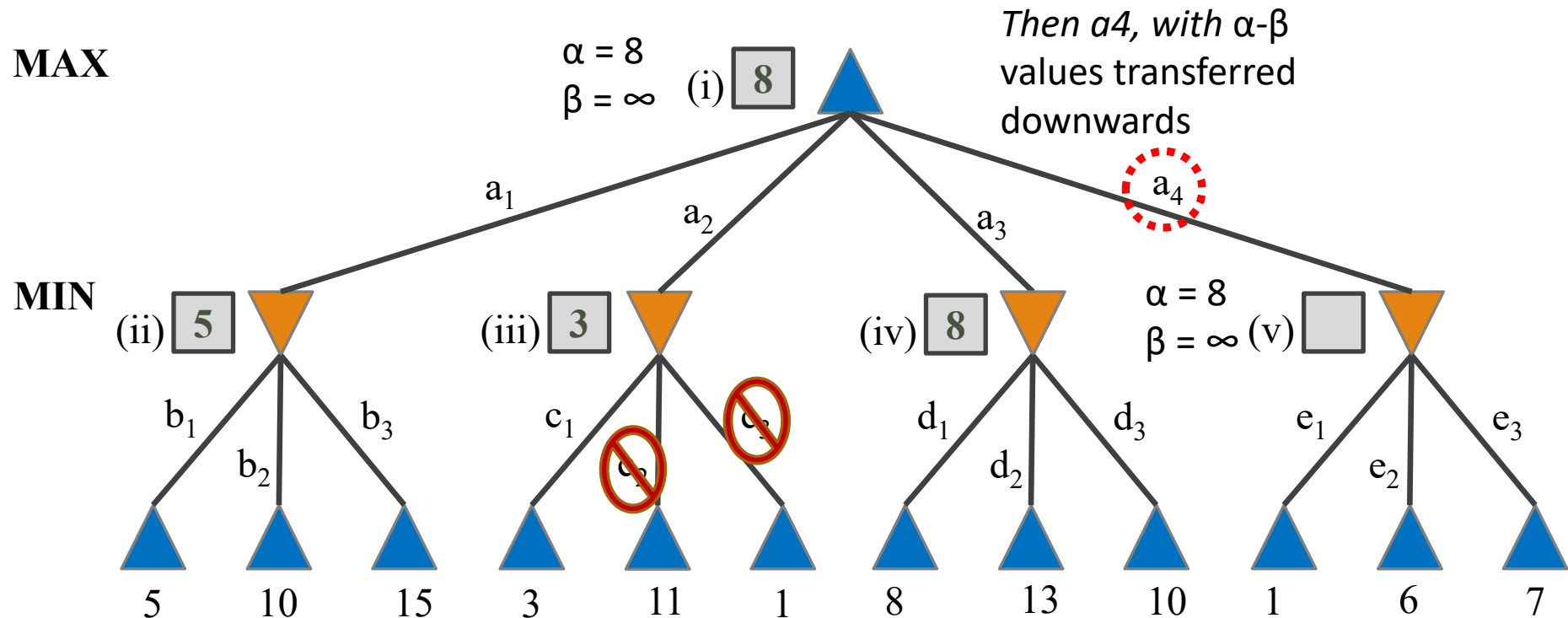
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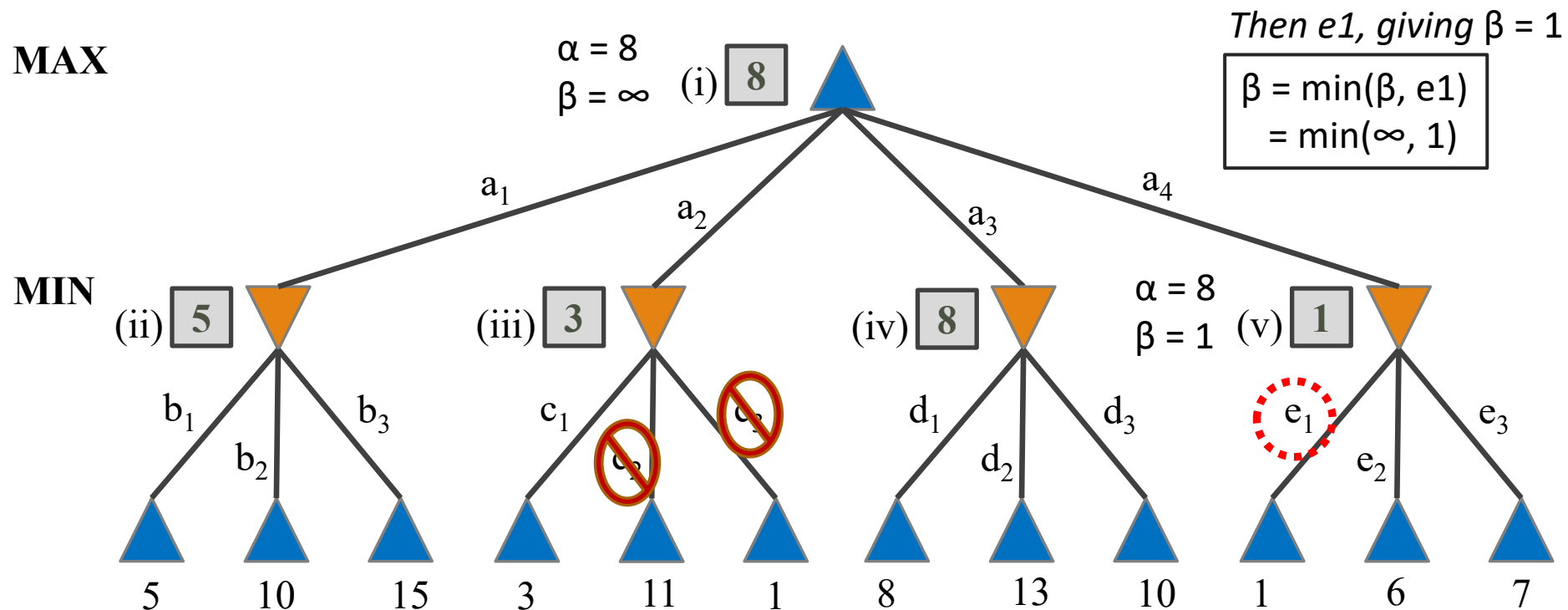
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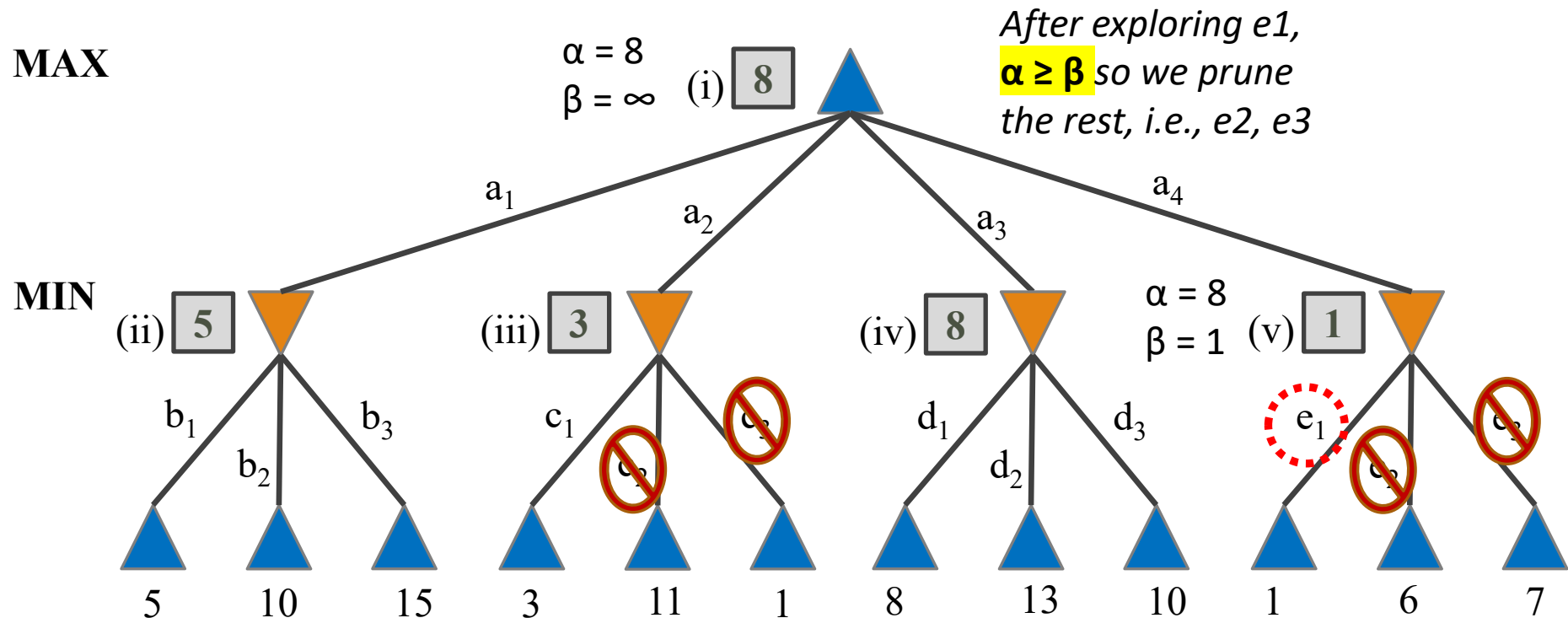
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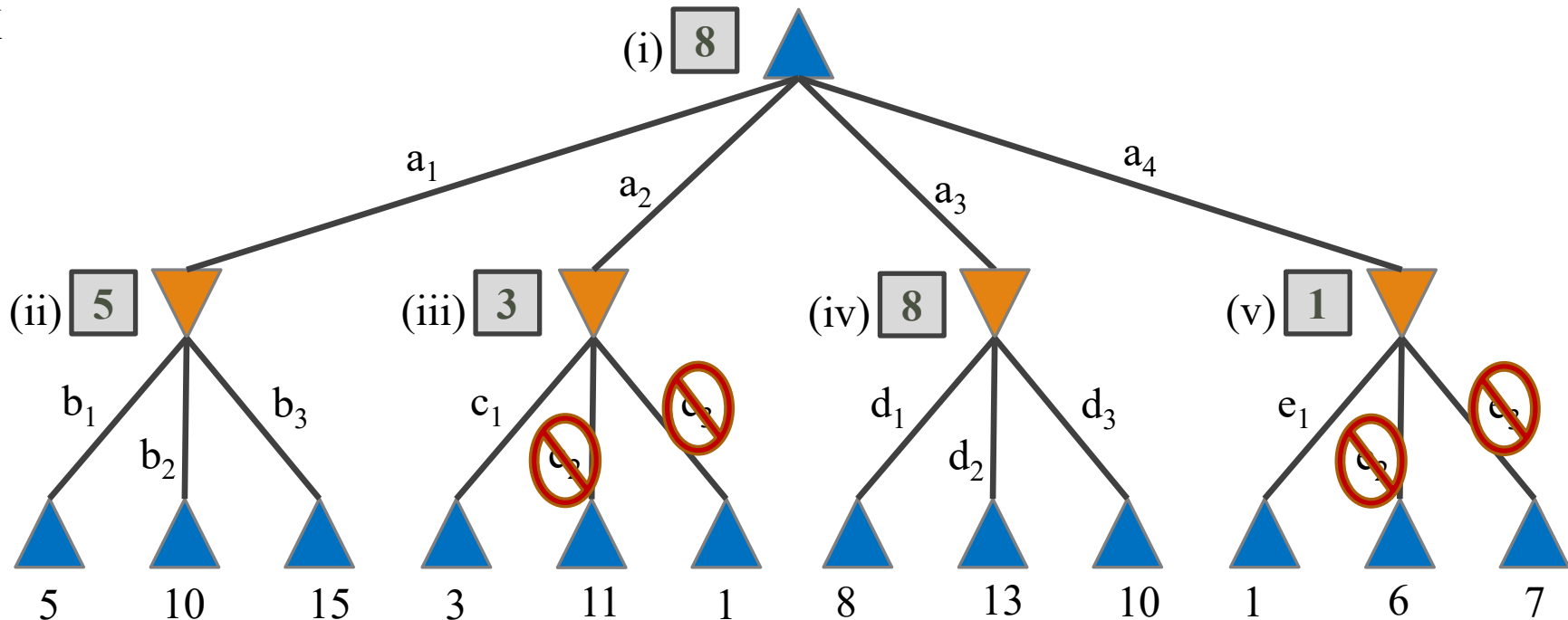


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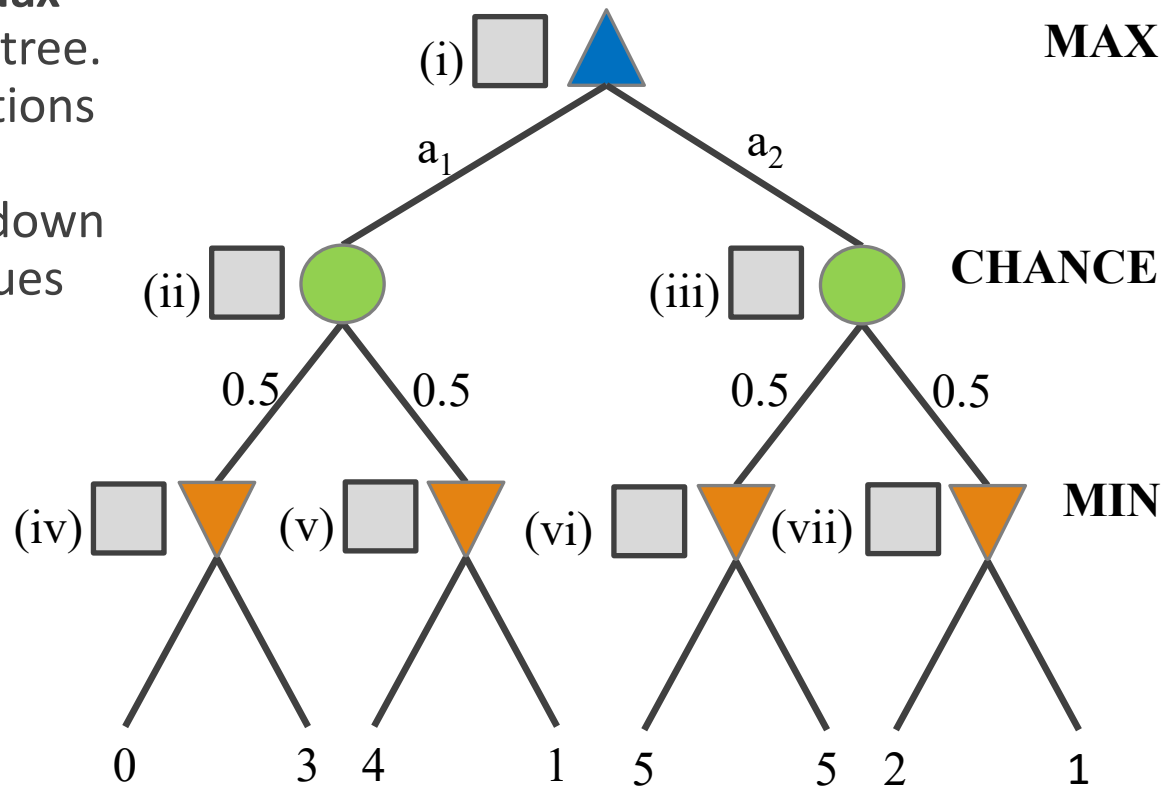
MAX

MIN



# Exercise: ExpectiMiniMax

- Apply the **ExpectiMiniMax algorithm** on this game tree. Assume that moves/ actions are explored in lowest alphabetical order. List down the ExpectiMiniMax values and state which move is chosen.



# Exercise: ExpectiMiniMax

- Apply the **ExpectiMiniMax algorithm** on this game tree. Assume that moves/ actions are explored in lowest alphabetical order. List down the ExpectiMiniMax values and state which move is chosen.
  - Solution: a2

