

Control Systems

G V V Sharma*

CONTENTS

1	Transfer function	1
1.1	Bode Plot	1

Abstract—The objective of this manual is to introduce control system design at an elementary level.

Download python codes using

```
svn co https://github.com/gadepall/school/trunk/
control/ketan/codes
```

1 TRANSFER FUNCTION

1.1 Bode Plot

1.1.1. Given set of points are:

Freq(rad/sec)	Mag(dB)
0.1	34
0.2	28
0.3	24.6
0.7	14.2
1.0	8
1.5	1.5
2.0	-3.5
2.5	-7.2
4.0	-10
5.0	-10
6.0	-14.7
9.0	-16.0
20	-17.5
35	-17.5
50	-18
100	-18.5

TABLE 1.1.1

Solution: The following code generates the plot for the given data.

```
codes/ee18btech11006/ee18btech11006_1.py
```

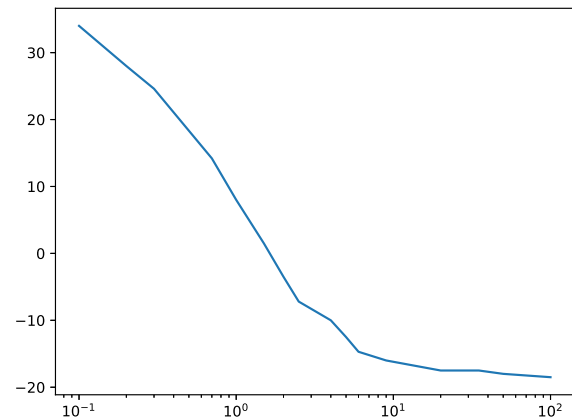


Fig. 1.1.1: 1

Consider the Transfer function

$$H(s) = \frac{k(s + z_1)(s + z_2)}{(s + p_1)(s + p_2)} \quad (1.1.1.1)$$

Let's draw the magnitude bode plot.

$$20\log_{10}|H(s)| = 20\log_{10}|s + z_1| + 20\log_{10}|s + z_2| - 20\log_{10}|s + p_1| - 20\log_{10}|s + p_2| + 20\log_{10}k \quad (1.1.1.2)$$

Now, for the given set of points finding slopes corresponding to every two points and identifying the points at which the slope change occurs by 20dB would give us the poles and zeros respectively. The slope initially is -20dB/decade i.e. pole at 0.1 We can observe that the slope decreases approximately by 20dB/dec at the point 0.7 and increases further by 20dB/dec at 2.5 and 6 giving a slope of almost 0 later on.

$$\text{Poles} = 0.1, 0.7 \quad (1.1.1.3)$$

$$\text{Zeros} = 2.5, 6 \quad (1.1.1.4)$$

*The author is with the Department of Electrical Engineering, Indian Institute of Technology, Hyderabad 502285 India e-mail: gadepall@iith.ac.in. All content in this manual is released under GNU GPL. Free and open source.

Lets plot the magnitude bode plot considering these poles and zeros.

The following code generates the plot for the transfer function

$$H(s) = \frac{(s + 2.5)(s + 6)}{(s + 0.1)(s + 0.7)} \quad (1.1.1.5)$$

```
codes/ee18btech11006/ee18btech11006_2.py
```

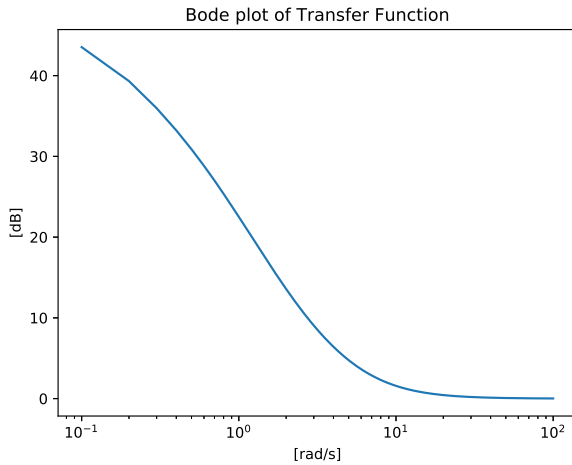


Fig. 1.1.1: 2

Now the gain,

$$K = \frac{H(\omega) (given)}{H(\omega) (calculated)} \quad (1.1.1.6)$$

This value would vary for different frequencies. Considering the average value, $K = 0.1778$. The following code generates the plot for the transfer function

$$H(s) = \frac{0.1778 (s + 2.5)(s + 6)}{(s + 0.1)(s + 0.7)} \quad (1.1.1.7)$$

```
codes/ee18btech11006/ee18btech11006_3.py
```

Thus, our Transfer function is

$$H(s) = \frac{0.1778 (s + 2.5)(s + 6)}{(s + 0.1)(s + 0.7)} \quad (1.1.1.8)$$

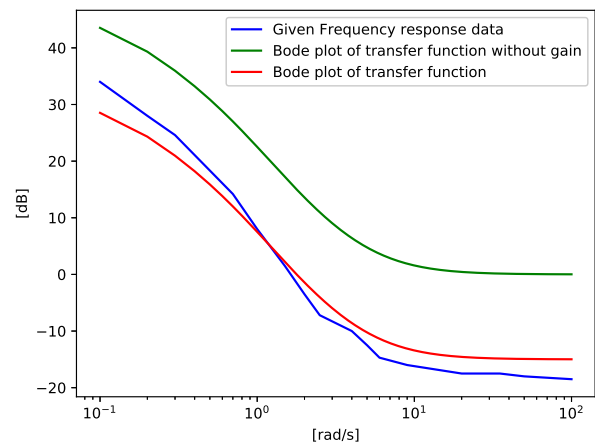


Fig. 1.1.1: 3