BAN 602: Quantitative Fundamentals

Spring, 2020 Online Lecture Slides – Week 1



Agenda

- Set up R and R Studio
- Basics of R
- Data Structures in R
- Computing Summary Statistics using R
- Contingency Tables using R
- Data Visualization using R



Setup R and R-Studio

- To install R on your laptop/MacBook:
 - Go to http://www.r-project.org/ from your browser
 - Follow the download link on the page
 - Choose a CRAN location and follow the instructions for installation of the latest version for your laptop/MacBook
- Once R is properly installed, next install R-Studio:
 - Open https://rstudio.com/products/rstudio/ on your browser
 - Click on the button to download RStudio Desktop, Open Source Edition
 - Choose the latest version recommended for your laptop/MacBook and follow the instructions



Environment

- The "workspace" in R is called the global environment.
- This is where variables are stored
- The objects in the global environment can be listed using command ls()
- Objects can be removed using command rm()
- Set working directory using command setwd("Working_Directory_Path"). In this location you should keep the data files you want to load in R.



What is R?

- R is both a computing environment and a programming language
- Born 26 years ago, rapid recent growth in popularity
- Enormous number of user-developed packages implementing multitudes of statistical methods
- Defacto language for academic research
- Rapidly becoming the language to use for industrial "data science"
- Formally, R language is:
 - functional (like Lisp)
 - interpreted (like Python)



Interacting with R

- You can use R interactively through its command line interface (CLI) or console:
 - enter a command
 - R executes the command
 - get a printed response
 - repeat
- You can use R in batch mode:
 - give R a script: a list of commands
 - R executes the commands
 - get result(s) displayed on screen or stored in files: text, tables, graphics, and more



R as a Calculator

```
      7 + 10

      ## [1] 17

      67.1 * 11

      ## [1] 738.1

      5/7

      ## [1] 0.7142857
```

- R doesn't mind spaces
- Spaces can go wherever you like, just not in the middle of numbers or names



R works with vectors

$$c(5, 8, 100) + c(3, 1,7)$$

$$c(5,7,10) * c(2,4,3)$$

```
## [1] 10 28 30
```

- c() is a function that concatenates scalars into a vector.
- Use c() to create a vector from individual values



R has built-in functions and constants

```
1 / sqrt(2*pi) * exp(-2)

## [1] 0.05399097

dnorm(0)

## [1] 0.3989423
```

- sqrt() computes the square root
- exp() computes e^x
- dnorm() computes the standard normal density function



R has built-in help

```
help(dnorm)
help.search('normal distribution')
```

```
?dnorm
??'normal distribution'
```

- Text has to be enclosed between:
 - Two single quotes
 - Two double quotes



Scripts

- Most data analyses involve:
 - more than one command
 - mistakes
 - changes
- Don't enter commands one-by-one into the console
- Write your commands in a script:
 - plain text file containing your commands
 - easy to go back and make fixes/changes
 - easy to share
 - easy to add human-readable comments



Objects and Variables

- Objects are the "things" that we manipulate in R
- Conceptually, there are two kinds of objects:
 - data things like 7, "seven", 7.00, the vector [7 7 7]
 - functions things like log, sin, +
- R considers both to be objects
- Variables
 - A variable is a storage location and an associated name that contains some object
 - Variables allow us to
 - abstract the data in our computations
 - generalize computations to different data
 - reuse data in different computations



Functions

- A function is a defined rule for turning
 - input objects (arguments) into an
 - output object (return value),
 - possibly with side effects
- Examples of side effects
 - plotting
 - saving a file
 - posting a Tweet
- Basic usage: f(arg_1, arg_2, ..., arg_n)

```
log(10)

## [1] 2.302585

10 + 5

## [1] 15
```



Variable Names and Assignment

- R variable names must obey rules:
 - Mix of alphabetical, digits, and periods
 - Cannot start with a number
- Pro tips:
 - avoid single character names
 - use underscores _ in place of spaces in names
- Variable assignment:
 - R uses the <- operator to an object to a variable
 - Pro tip: Avoid using = for assignment in R

```
name <- "Vince"
height <- 66
```

```
height <- 66
feet <- height %/% 12 # integer division
inches <- height %% 12 # modulus</pre>
```



Data type: Double

- R defines several primitive data types
- The four most common:
 - double
 - integer
 - logical
 - character
- These are the atoms of more complex data structures
- Double:
 - Default way of representing numbers in R
 - More specifically double-precision floating point numbers
 - Subject to rounding error, e.g. $1/3 \approx 0.33333$





Data types: Integer and Logical

• Integer:

- Whole numbers, represented internally (by the computer) as a binary sequence (bits)
- Most modern computers use 64-bits to represent integers
 - 2⁶⁴ possible numbers

Largest: $2^{63} - 1$ Smallest: $-(2^{63})$

• Often useful for counting or indexing things

• Logical:

• Boolean TRUE or FALSE — binary values

```
10 < 15

## [1] TRUE

10 > 15

## [1] FALSE
```



Data types: Character

• Character:

- Also known as text or character string or string
- Internally represented by the computer as a sequence of integers and a predefined map between integers and symbols
- Created by enclosing with single or double quotation marks



Data structure: Vectors

- Group related data values into one object: a data structure
- Most important data structures in R:
 - Atomic vector
 - List
 - Matrix
 - Data frame array
- Vectors:
 - Vectors come in two flavors in R:
 - Atomic vector
 - List
 - Two important properties (queried by functions):
 - length() how many elements the vector contains
 - typeof() what type of data it contains
 - Can create vectors with c() function



Atomic Vectors

- A homogeneous sequence of values, i.e. all of the same type
- Sometimes referred to generically as a vector
- Examples:
 - Double vector [1.1, 5, 7.3]
 - Integer vector [4L, 5L, 6L, 7L]
 - Character vector [bob, alice, john]
 - Logical vector [TRUE, FALSE, TRUE]
- Note: R does not have a scalar type. So the scalar in R is actually an atomic vector of length 1





Example of character vector

```
x <- c('apples', 'oranges', 'bananas')
print(x)

## [1] "apples" "oranges" "bananas"

length(x)

## [1] 3

typeof(x)

## [1] "character"</pre>
```



Sequence

- Sequences of numbers are used frequently, so there are built- in functions to make sequences:
 - a:b construct an integer sequence from a to b (note: a can be larger than b)
 - seq() function to create arbitrary sequences

```
i <- 1:10
print(i)
```

```
## [1] 1 2 3 4 5 6 7 8 9 10
```

```
j <- seq(1, 10, 2)
print(j)</pre>
```

```
## [1] 1 3 5 7 9
```



Indexing

- Elements of a vector are accessed via indexing
- Examples:
 - x[1] first element
 - x[2] second element
 - x[length(x)] last element
- Negative indices are allowed too:
 - x[-1] all but first element
 - x[-5] all but 5th element

Example of Indexing

```
x <- c('lions', 'tigers', 'bears', 'oh my!')
x[1]

## [1] "lions"

x[length(x)]

## [1] "oh my!"

x[-2]

## [1] "lions" "bears" "oh my!"</pre>
```



Indexing by Vectors

• Vectors can be indexed by vectors

```
x <- c('lions', 'tigers', 'bears', 'oh my!')
x[1:2]

## [1] "lions" "tigers"

x[c(1,3)]

## [1] "lions" "bears"

x[-(1:2)]

## [1] "bears" "oh my!"</pre>
```



Type Coercion

```
x <- c(57, 'columbus', 1.56)
is.vector(x)

## [1] TRUE

x <- c(57, 'columbus', 1.56)
typeof(x)

## [1] "character"</pre>
```

- c() coerces its arguments to be of the same type
- Here double got converted into character



Missing Values

- Real data sets often has missing values, for example:
 - survey questions not answered
 - measurements unknown/unrecorded
- R has a fundamental representation for missing values: NA

```
x <- c(5, 10, NA, 13)
print(x)
```

```
## [1] 5 10 NA 13
```

```
is.na(x)
```

```
## [1] FALSE FALSE TRUE FALSE
```



Operators

- Operators are functions, but with special syntax
- They are of two types:
 - Unary e.g. negation, ! Boolean negation
 - Binary e.g. + addition, subtraction, < less-than
- How they operate depends on their arguments
- **Arithmetic Operators:** Operators defined on numbers
 - Take numbers as input and return a number as output
 - Examples:
 - - negation
 - +, -, *, / add, subtract, multiply, divide
 - %% modulus
- **Logical Operators:** Operators that return a logical
 - Most often used as conditions involving other data types
 - Examples:
 - <, <= less than, less than or equal to
 - >, >= greater than, greater than or equal to
 - == is equal to



Boolean Indexing

- A vector can be indexed by a logical vector of the same length
- Useful for getting subsets of data, when combined with boolean operations

```
x <- c(1, 5, 7)
x[c(TRUE, FALSE, TRUE)]
```

```
## [1] 1 7
```

```
student <- c('bob', 'alice', 'john', 'mary')
gender <- c('M', 'F', 'M', 'F')
student[gender == 'M']</pre>
```

```
## [1] "bob" "john"
```



Another Example of Boolean Indexing

```
fruits <- c('apple', 'orange', 'banana', 'cherry')
vegetables <- c('broccoli', 'carrot', 'asparagus', 'onion')
refrigerator <- c('apple', 'carrot', 'cheese')
refrigerator %in% fruits</pre>
```

```
## [1] TRUE FALSE FALSE
```

```
refrigerator[refrigerator %in% fruits]
```

```
## [1] "apple"
```



Function Names and Defaults

- R allows function arguments to have names and default values
- This makes functions easier to use as you can refer to arguments by name. There is no need to memorize argument positions.
- Learn function names and defaults using help command
- For example: function rnorm() has 3 arguments: n number of samples to generate (no default), mean of the Normal distribution (default = 0), sd of the Normal distribution (default = 1)

```
rnorm(n = 10, sd = 10)

## [1] -6.9568004 -9.8547346 -6.0635654 1.2393049 -18.2644090
## [6] -12.8456064 -1.0497898 1.4678847 -2.8156671 -0.5414748
```



Data Structure: Matrix

- A matrix is like an atomic vector:
 - Collection of elements all of the same type
 - but with 2 dimensions
- Construct with matrix()
- Subset with []

```
x <- matrix(1:9, nrow = 3, ncol = 3)
print(x)

## [,1] [,2] [,3]
## [1,] 1 4 7
## [2,] 2 5 8
## [3,] 3 6 9

x[2, 3]

## [1] 8

x[3, ]

## [1] 3 6 9</pre>
```



Array

- An array is a higher-dimensional generalization of a matrix:
 - Collection of elements all of the same type
 - Any fixed number of dimensions
- Construct with array()
- Subset with []



Data Structure: List

- A vector, not necessarily all of the same type
- Elements can have names
- Create with list() function

```
my_distribution <- list('normal', 0, FALSE)
print(my_distribution)</pre>
```

```
## [[1]]
## [1] "normal"
##
## [[2]]
## [1] 0
##
## [[3]]
## [1] FALSE
```



List Index

- x[i] is a list containing the elements in x corresponding to i
- [] always returns a list

```
my_distribution[1:2]

## [[1]]
## [1] "normal"
##
## [[2]]
## [1] 0

my_distribution[2]

## [[1]]
## [1]]
```



Content of a List

• [[]] returns a single value content of a list

```
typeof(my_distribution[2])

## [1] "list"

typeof(my_distribution[[2]])

## [1] "double"
```

"If list x is a train carrying objects, then x[[5]] is the object in car 5; x[4:6] is a train of cars 4-6."

— @RLangTip

```
my_distribution[[2]] + 10

## [1] 10
```



Naming the List Elements

```
names(my_distribution) <- c('family', 'mean', 'is.symmetric')</pre>
names(my_distribution)
## [1] "family"
                      "mean"
                                      "is.symmetric"
print(my_distribution)
## $family
## [1] "normal"
##
## $mean
## [1] 0
##
## $is.symmetric
## [1] FALSE
```



Using Names to Access List Elements

```
# 3 ways:
my_distribution[[2]]
## [1] 0
my_distribution[["mean"]]
## [1] 0
my_distribution$mean # short-hand for [[]]
## [1] 0
```



Assigning Names during List Creation

```
## $family
## [1] "gaussian"
##
## $mean
## [1] 7
##
## $sd
## [1] 1
##
## $is.symmetric
## [1] TRUE
```



Properties of List

- Lists give us a way to store and look up data by name
- They are like key-value pairs/associative array/dictionary in other languages
- If all our distributions have a component named family, then we can look it up by name without caring about its location.

another_distribution\$family

[1] "gaussian"



Data Structure: Data Frames

- A data frame is a classic data table, organized with
 - n rows (observations)
 - p columns (variables)
- Most statistical functions in R work with data frames
- A data frame is a list that
 - has atomic vector components all of the same length
 - can also be indexed like a matrix
- Construct with data.frame()

```
## student score
## 1 bob 70
## 2 alice 90
## 3 john 85
## 4 mary 100
```



Properties of Data Frames

These functions are helpful to know the properties of data-frames:

- nrow() returns number of rows in a data-frame
- ncol() returns number of columns in a data-frame
- dim() returns dimension of a data-frame i.e. number of rows and columns as a vector of length 2
- names() inherited from lists
- rownames() optional names for each row

```
nrow(df)

## [1] 4

ncol(df)

## [1] 2

dim(df)

## [1] 4 2
```



Data Frame Indexing

• Data frames can be index like a matrix or a list

```
df[1,]

## student score
## 1 bob 70

df[,1]

## [1] bob alice john mary
## Levels: alice bob john mary

df$score

## [1] 70 90 85 100
```



Attributes

- names is an example of an attribute
- R allows objects to have optional attributes

```
## $names
## [1] "family" "mean" "is.symmetric"
```

- All vectors can have names
- Note: attributes() returns a list of the object's attributes



Vector Indexing by Name

- Vectors (atomic vectors and lists) can have an optional names attribute
- Vectors can be indexed by name

```
x <- c(john = 10, bob = 3, alice = 7)
x['bob']

## bob
## 3

x[c('john', 'alice')]

## john alice
## 10 7</pre>
```



Matrix Indexing by Name

- Matrices and data frames can have optional rownames and colnames attributes
 - but for data frames, colnames is a synonym for names
- They can be indexed by name

```
x <- matrix(1:12, nrow=4,ncol=3)
rownames(x) <- c('john', 'bob', 'alice', 'mike')
colnames(x) <- c('homework', 'exam', 'final')
x['john', ]</pre>
```

```
## homework exam final
## 1 5 9
```

```
x['alice', 'final']
```

```
## [1] 11
```



Functions to Inspect Objects

- These functions are very helpful:
 - str() returns the structure of an object
 - head() returns the head (first few entries) of an object
 - tail() returns the tail (last few entries) of an object



Reading Dataset

- There are a number of functions in R to read dataset. The name of the file to be read must be specified as an argument.
 - read.table() reads data from a flat file. If the first row of the dataset contains column headers, pass an argument "header=T"
 - Can read data directly from an url: read.table(URL, header=T)
 - read.csv(), or read.csv2() reads comma separated value files directly.
 - read.delim(), or read.delim2() reads delimited text files
 - read.xlsx(), or read.xlsx2() reads excel files

• Example: To read the Babies.csv file from your working directory, execute the command: babies <- read.csv(file="Babies.csv", header = TRUE)



Descriptive Statistics: Statistical Summary

- summary() this generic function summarizes an object
- For data frames, summary() provides a 6 number summary of each column: minimum, first quartile, median (i.e. second quartile), mean, third quartile, maximum.

```
summary(babies)
```

```
##
         bwt
                      gestation
                                         parity
                                                            age
    Min.
           : 55.0
                    Min.
                            :148.0
                                     Min.
                                             :0.0000
                                                       Min.
                                                              :15.00
    1st Qu.:108.8
                    1st Qu.:272.0
                                    1st Qu.:0.0000
                                                       1st Qu.:23.00
    Median :120.0
                    Median :280.0
                                     Median :0.0000
                                                       Median :26.00
           :119.6
                            :286.9
                                             :0.2549
                                                              :27.37
    Mean
                     Mean
                                     Mean
                                                       Mean
    3rd Ou.:131.0
                     3rd Ou.:288.0
                                     3rd Ou.:1.0000
                                                       3rd Ou.:31.00
           :176.0
                            :999.0
                                             :1.0000
                                                              :99.00
    Max.
                    Max.
                                     Max.
                                                       Max.
        height
                        weight
                                       smoke
    Min.
           :53.00
                            : 87
                                           :0.0000
                    Min.
                                   Min.
   1st Qu.:62.00
                    1st Qu.:115
                                   1st Qu.:0.0000
    Median :64.00
                    Median :126
                                   Median :0.0000
    Mean
           :64.67
                     Mean
                            :154
                                   Mean
                                          :0.4644
    3rd Qu.:66.00
                     3rd Qu.:140
                                   3rd Qu.:1.0000
    Max.
           :99.00
                            :999
                                          :9.0000
                    Max.
                                   Max.
```



Simple Summary Statistics

- To calculate simple summary statistics of an object x use the following functions:
 - mean(x) returns the mean of x values
 - sd(x) returns the sample standard deviation of x values
 - var(x) returns the sample variance of x values
 - median(x) returns the median of x values
 - quantile(x) returns 0th, 25th, 50th, 75th, 100th percentile of x values
 - range(x) returns the range (minimum and maximum) of x values
- Practice: Calculate mean, standard deviation, variance, median, first and third quartiles, range of the weight variable from the babies dataset.



Covariance and Correlation

- The cov(x, y) function is used to compute covariance between two variables x and y.
- The cor(x, y) function computes correlation between two variables x and y.
- How the covariance or correlation should be computed in presence of missing values can be mentioned through 'use' argument.

• Practice: Find out the covariance and correlation between the weight and height variables from the babies dataset. Use the following R commands:

cov(babies\$height, babies\$weight)
cor(babies\$height, babies\$weight)



Transforming a Data frame

- The function transform(dataframe, ...)
 - Copies input data frame,
 - Evaluates the remaining arguments, and
 - Either replaces matching columns or appends new columns
- Convenient because ... arguments are evaluated within the data frame
- Example: To add two new columns (with values calculated based on existing columns) to the babies dataset BMI of the mothers and whether or not a baby was born preterm:



Missing Values in a Data frame

- In the babies dataset there are missing values. They are coded differently in different columns.
- For example, missing values in 'smoke' column is denoted by number 9. 0 in this column means the mother doesn't smoke, and 1 means she does.
- To clean up the missing values from 'smoke' column:
 - Select entries whose values are the missing (i.e. of value 9)
 - Assign NA to those entries

```
babies$smoke[babies$smoke == 9] <- NA

# Convert smoking status into a logical
babies$smoke <- as.logical(babies$smoke)</pre>
```

• This code snippet would mark the missing values as NA, and convert the smoke variable into logical (true/false) type.



Crosstabulation: Contingency Table

- The function table() builds a contingency table of the counts of at each combination of factor levels of its input arguments
- Converts each argument into a factor (categorical data type)
- Counts each combination of factor levels (categories)

```
# Contingency table
x <- table(babies$smoke, babies$preterm)
print(x)</pre>
```

```
##
## FALSE TRUE
## FALSE 677 56
## TRUE 439 41
```

• However the contingency table is not properly labeled here since the levels these two variables smoke and preterm could take have not been defined before.



Contingency Table with Factors Relabeled

• Now the contingency table looks meaningful:

```
# Contingency table
x <- table(babies$smoke, babies$preterm)
print(x)

##
## normal preterm
## non-smoking 677 56
## smoking 439 41</pre>
```



Marginal Table and Relative Frequency

- To compute the margins of a table i.e. the sum across each rows or each columns of a table, the *margin.table()* function is used:
 - To compute **row-wise** sum: use *margin.table(table name, 1)* command
 - To compute **column-wise** sum: use *margin.table(table name, 2)* command
- Practice: Execute the R command:
 - margin.table(x, 2) where x is the table from last slide.
- To compute relative frequency **row-wise** and **column-wise**, use the function *prop.table(table_name, 1)* and *prop.table(table_name, 2)* respectively.

```
##
## normal preterm
## smoking 0.92360164 0.07639836
## smoking 0.91458333 0.08541667

prop.table(x, 2)

##
## normal preterm
## non-smoking 0.6066308 0.5773196
## smoking 0.3933692 0.4226804
```



Histogram

- The hist(x) function can be used to plot a histogram of object x values.
- You can get approximately n bars in the histogram by specifying the argument breaks=n
- Exact location of the breaks can be specified using a vector for the 'breaks' argument.
- Use the 'xlab' and 'ylab' arguments to label the x-axis and y-axis respectively.
- Use 'main' argument to add a title to the histogram
- Practice: Execute the R command:

hist(babies\$bwt, breaks = c(40, 70, 100, 130, 160, 190), xlab = "Birth Weight", main = "Histogram of Birth Weight")

and check the histogram plotted.



Boxplot

- The boxplot(x) function can be used to draw a Box and Whiskers plot of object x values.
- Use the 'xlab' and 'ylab' arguments to label the x-axis and y-axis respectively.
- Use 'main' argument to add a title to the boxplot
- Adding the argument horizontal=T changes the orientation of the boxplot to horizontal
- Practice: Execute the R command:

boxplot(babies\$height, horizontal = T, main="Boxplot", xlab="Height")

and check the boxplot generated.



Bar Chart

- The barplot(x) function can be used to draw a bar chart of vector or matrix x.
- The bars created are stacked bars by default.
- If the bars are to stay side-by-side instead, use the argument 'beside=T'.
- If the bars are to be drawn horizontally, use the argument 'horiz=T'.
- The 'col' and 'border' arguments can be used to color the bars and their borders
- As usual xlab, ylab, and main can be used to add labels to the x-axis, y-axis and title of the chart
- Practice: Execute the R command:

```
barplot(x, beside=T)
```

and check the bar chart generated.



Pie Chart

- The pie(x) function can be used to draw a bar chart of vector or matrix x.
- The color of the slices can be mentioned in argument 'col'.
- The labels for each slice can be specified by argument 'labels'.
- The title can be specified through the 'main' argument.
- Practice: Execute the R command:

```
pie(x, labels = c("Normal-Non-smoking", "Normal-Smoking", "Preterm-Non-Smoking", "Preterm-Smoking"), <math>col=c("red", "green", "blue", "yellow"), main="Pie Chart")
```

and check the pie chart generated.



Scatter Plot

- The plot(x, y) function can be used to draw a scatter plot between two variables x and y.
- The title can be specified through the 'main' argument.
- The x-axis and y-axis can be labeled through xlab and ylab arguments
- Practice: Draw the scatter plot between baby weight and gestation period from the babies dataset:

```
plot(babies$bwt, babies$gestation, xlab = "Baby Weight", ylab="Gestation Period",
main="Scatter Plot")
```

