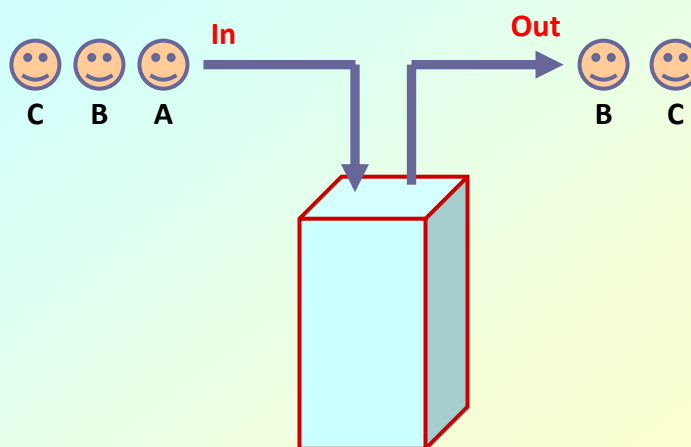


Stacks and Queues: Implementation

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Visualization of a Stack (Last In First Out)



2

Stack Implementation

- a) Using arrays
- b) Using linked list

3

Basic Idea

- In the array implementation, we would:
 - Declare an array of fixed size (which determines the maximum size of the stack).
 - Keep a variable **top** which always points to the “top” of the stack.
 - Contains the array index of the “top” element.
- In the linked list implementation, we would:
 - Maintain the stack as a linked list.
 - A pointer variable **top** points to the start of the list.
 - The first element of the linked list is considered as the stack top.

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Declaration

```
#define MAXSIZE 100

struct lifo
{
    int  st[MAXSIZE];
    int  top;
};

typedef struct lifo stack;
```

ARRAY

```
struct lifo
{
    int value;
    struct lifo *next;
};

typedef struct lifo stack;
```

LINKED LIST

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Stack Creation

```
void create (stack *s)
{
    (*s).top = -1;

    /* s.top points to
       last element
       pushed in;
       initially -1 */
}
```

ARRAY

```
void create (stack **top)
{
    *top = NULL;

    /* top points to NULL,
       indicating empty
       stack */
}
```

LINKED LIST

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Pushing an element into the stack

```
void push (stack *s, int element)
{
    if ((*s).top == (MAXSIZE-1))
    {
        printf ("\n Stack overflow");
        exit(-1);
    }
    else
    {
        (*s).top++;
        (*s).st[(*s).top] = element;
    }
}
```

ARRAY

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```
void push (stack **top, int element)
{
    stack *new;

    new = (stack *) malloc(sizeof(stack));
    if (new == NULL)
    {
        printf ("\n Stack is full");
        exit(-1);
    }

    new->value = element;
    new->next = *top;
    *top = new;
}
```

LINKED LIST

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Popping an element from the stack

```
int pop (stack *s)
{
    if ((*s).top == -1)
    {
        printf ("\n Stack underflow");
        exit(-1);
    }
    else
    {
        return ((*s).st[(*s).top--]);
    }
}
```

ARRAY

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```
int pop (stack **top)
{
    int t;
    stack *p;

    if (*top == NULL)
    {
        printf ("\n Stack is empty");
        exit(-1);
    }
    else
    {
        t = (*top)->value;
        p = *top;
        *top = (*top)->next;
        free (p);
        return t;
    }
}
```

LINKED LIST

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Checking for stack empty

```
int isempty (stack s)
{
    if (s.top == -1)
        return (1);
    else
        return (0);
}
```

ARRAY

```
int isempty (stack *top)
{
    if (top == NULL)
        return (1);
    else
        return (0);
}
```

LINKED LIST

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Checking for stack full

```
int isfull (stack s)
{
    if (s.top ==
        (MAXSIZE-1))
        return (1);
    else
        return (0);
}
```

ARRAY

- Not required for linked list implementation.
- In the `push()` function, we can check the return value of `malloc()`.
 - If -1, then memory cannot be allocated.

LINKED LIST

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Example main function :: array

```
#include <stdio.h>
#define MAXSIZE 100

struct lifo
{
    int st[MAXSIZE];
    int top;
};
typedef struct lifo stack;

main()
{
    stack A, B;
    create(&A); create(&B);
    push(&A,10);
    push(&A,20);
```

```
    push(&A,30);
    push(&B,100); push(&B,5);

    printf ("%d %d", pop(&A),
            pop(&B));

    push (&A, pop(&B));

    if (isempty(B))
        printf ("\nB is empty");
}
```

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Example main function :: linked list

```
#include <stdio.h>
struct lifo
{
    int value;
    struct lifo *next;
};
typedef struct lifo stack;

main()
{
    stack *A, *B;
    create(&A); create(&B);
    push(&A,10);
    push(&A,20);
```

```
    push(&A,30);
    push(&B,100); push(&B,5);

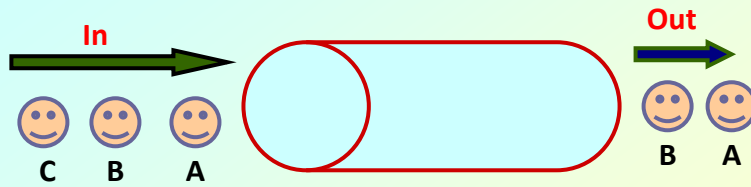
    printf ("%d %d",
            pop(&A), pop(&B));

    push (&A, pop(&B));

    if (isempty(B))
        printf ("\nB is empty");
}
```

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Visualization of a Queue (First In First Out)



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Queue Implementation using Linked List

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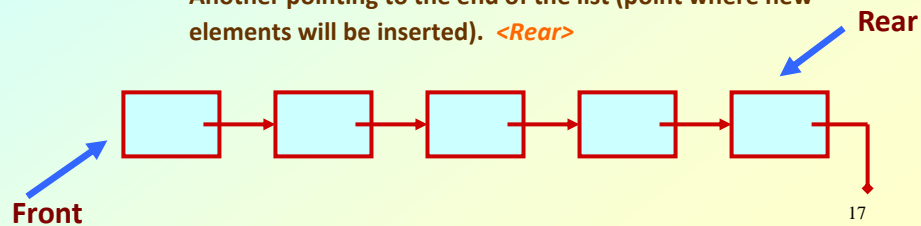
Basic Idea

- **Basic idea:**

- Create a linked list to which items would be added to one end and deleted from the other end.

- Two pointers will be maintained:

- One pointing to the beginning of the list (point from where elements will be deleted). *<Front>*
- Another pointing to the end of the list (point where new elements will be inserted). *<Rear>*



Declaration

```
struct fifo {
    int value;
    struct fifo *next;
};
typedef struct fifo queue;

queue *front, *rear;
```

Creating a queue

```
void createq (queue **front, queue **rear)
{
    *front = NULL;
    *rear  = NULL;
}
```

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Inserting an element in queue

```
void enqueue (queue **front, queue **rear, int x)
{
    queue *ptr;
    ptr = (queue *) malloc(sizeof(queue));

    if (*rear == NULL)    /* Queue is empty */
    {
        *front = ptr;
        *rear  = ptr;
        ptr->value = x;
        ptr->next = NULL;
    }
    else                  /* Queue is not empty */
    {
        (*rear)->next = ptr;
        *rear = ptr;
        ptr->value = x;
        ptr->next = NULL;
    }
}
```

Deleting an element from queue

```
int dequeue (queue **front, queue **rear)
{
    queue *old;    int k;

    if (*front == NULL)                /* Queue is empty */
        printf ("\n Queue is empty");
    else if (*front == *rear)          /* Single element */
    {
        k = (*front)->value;
        free (*front);    front = rear = NULL;
        return (k);
    }
    else
    {
        k = (*front)->value;    old = *front;
        *front = (*front)->next;
        free (old);
        return (k);
    }
}
```

Checking if empty

```
int isempty (queue *front)
{
    if (front == NULL)
        return (1);
    else
        return (0);
}
```

Example main function

```
#include <stdio.h>
struct fifo
{
    int value;
    struct fifo *next;
};
typedef struct fifo queue;
```

```
main()
{
    queue *Af, *Ar;
    createq (&Af, &Ar);
    enqueue (&Af, &Ar, 10);
    enqueue (&Af, &Ar, 20);
```

```
    enqueue (&Af, &Ar, 30);

    printf ("%d %d",
            dequeue (&Af, &Ar),
            dequeue (&Af, &Ar));

    if (isempty(Af))
        printf ("\n Q is empty");
}
```

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Some Applications of Stack

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Applications of Stack

- Evaluation of expressions
 - Polish postfix and prefix notations
- Convert infix to postfix
- Parenthesis matching

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Arithmetic Expressions Polish Notation

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What is Polish Notation?

- Conventionally, we use the operator symbol between its two operands in an arithmetic expression.

$A+B$ $C-D * E$ $A * (B+C)$

- We can use parentheses to change the precedence of the operators.
 - Operator precedence is pre-defined.
- This notation is called **INFIX notation**.
 - Parentheses can change the precedence of evaluation.
 - Multiple passes required for evaluation.

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Polish notation

- Named after Polish mathematician Jan Lukasiewicz.
- Polish POSTFIX notation

- Refers to the notation in which the operator symbol is placed after its two operands.

$AB+$ $CD*$ $AB * CD + /$

- Polish PREFIX notation

- Refers to the notation in which the operator symbol is placed before its two operands.

$+AB$ $*CD$ $/*AB-CD$

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How to convert an infix expression to Polish form?

- Write down the expression in fully parenthesized form.
Then convert stepwise.
- Example:

$A + (B * C) / D - (E * F) - G$

$(((A + (B * C) / D)) - (E * F)) - G$

- Polish Postfix form:

$A B C * D / + E F * - G -$

- Polish Prefix form:

– Try it out

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- Advantages:

- No concept of operator priority.
 - Simplifies the expression evaluation rule.
- No need of any parenthesis.
 - Hence no ambiguity in the order of evaluation.
- Evaluation can be carried out using a single scan over the expression string.
 - Using stack.

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Evaluation of a Polish Expression

- Can be done very conveniently using a stack.
 - We would use the Polish postfix notation as illustration.
 - Requires a single pass through the expression string from left to right.
 - Polish prefix evaluation would be similar, but the string needs to be scanned from right to left.

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```
while (not end of string) do
{
    a = get_next_token();
    if (a is an operand)
        push (a);
    if (a is an operator)
    {
        y = pop(); x = pop();
        push (x 'a' y);
    }
}
return (pop());
```

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Evaluate: 10 6 3 - * 7 4 + -

Scan string from left to right:

10:	push (10)	Stack: 10
6:	push (6)	Stack: 10 6
3:	push (3)	Stack: 10 6 3
-:	y = pop() = 3	Stack: 10 6
	x = pop() = 6	Stack: 10
	push (x-y)	Stack: 10 3
*:	y = pop() = 3	Stack: 10
	x = pop() = 10	Stack: EMPTY
	push (x*y)	Stack: 30
7:	push (7)	Stack: 30 7
4:	push (4)	Stack: 30 7 4
+:	y = pop() = 4	Stack: 30 7
	x = pop() = 7	Stack: 30
	push (x+y)	Stack: 30 11
-:	y = pop() = 11	Stack: 30
	x = pop() = 30	Stack: EMPTY
	push (x-y)	Stack: 19

**Final result
in stack**

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Converting an INFIX expression to POSTFIX

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Basic Idea

- Let Q denote an infix expression.
 - May contain left and right parentheses.
 - Operators are:
 - Highest priority: ^ (exponentiation)
 - Then: * (multiplication), / (division)
 - Then: + (addition), – (subtraction)
 - Operators at the same level are evaluated from left to right.
- In the algorithm to be presented:
 - We begin by pushing a '(' in the stack.
 - Also add a ')' at the end of Q.

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The Algorithm (Q:: given infix expression, P:: output postfix expression)

```

push '(';
Add ")" to the end of Q;
while (not end of string in Q do)
{
    a = get_next_token();
    if (a is an operand) add it to P;
    if (a is '(') push(a);
    if (a is an operator)
    {
        Repeatedly pop from stack and add to P each
        operator (on top of the stack) which has the
        same or higher precedence than "a";
        push(a);
    }
}

```

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```
if (a is '(')
{
    Repeatedly pop from stack and add to P each
    operator (on the top of the stack) until a
    left parenthesis is encountered;

    Remove the left parenthesis;
}
}
```

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Q: $A + (B * C - (D / E ^ F) * G) * H$

Q	STACK	Output Postfix String P
A	(A
+	(+	A
((+ (A
B	(+ (A B
*	(+ (*	A B
C	(+ (*	A B C
-	(+ (-	A B C *
((+ (- (A B C *
D	(+ (- (A B C * D
/	(+ (- (/	A B C * D
E	(+ (- (/	A B C * D E
^	(+ (- (/ ^	A B C * D E
F	(+ (- (/ ^	A B C * D E F
)	(+ (-	A B C * D E F ^ /

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Q	STACK	Output Postfix String P
*	(+ (- *	A B C * D E F ^ /
G	(+ (- *	A B C * D E F ^ / G
)	(+	A B C * D E F ^ / G * -
*	(+ *	A B C * D E F ^ / G * -
H	(+ *	A B C * D E F ^ / G * - H
)		A B C * D E F ^ / G * - H * +

Parenthesis Matching

The Basic Problem

- Given a parenthesized expression, to test whether the expression is properly parenthesized.
 - Whenever a left parenthesis is encountered, it is pushed in the stack.
 - Whenever a right parenthesis is encountered, pop from stack and check if the parentheses match.
 - Works for multiple types of parentheses

(), { }, []

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```
while (not end of string) do
{
    a = get_next_token();
    if (a is '(' or '{' or '[')
        push (a);
    if (a is ')' or '}' or ']')
    {
        if (isempty()) {
            printf ("Not well formed");
            exit();
        }
        x = pop();
        if (a and x do not match) {
            printf ("Not well formed");
            exit();
        }
    }
}
if (not isempty())
    printf ("Not well formed");
```

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Given expression: $(a + (b - c) * (d + e))$

Search string for parenthesis from left to right:

(:	push '('	Stack: (
(:	push '('	Stack: ((
):	x = pop() = (Stack: (MATCH
(:	push '('	Stack: ((
):	x = pop() = (Stack: (MATCH
):	x = pop() = (Stack: EMPTY	MATCH

Given expression: $(a + (b - c)) * d)$

Search string for parenthesis from left to right:

(:	push '('	Stack: (
(:	push '('	Stack: ((
):	x = pop() = (Stack: (MATCH
):	x = pop() = (Stack: EMPTY	MATCH
):	x = pop() = (Stack: ?	MISMATCH

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Some Other Applications

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Other applications

- Reversing a string of characters.
- Generating 3-address code from Polish postfix (or prefix) expressions.
- Handling function calls and return
- Handling recursion

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