No. of times loop is ownning by 
$$k$$

$$S_{K} = 1 + 3 + 6 + 10 + - - T_{K}$$

$$S_{K-1} = 1 + 3 + 6 + - - - T_{K-1}$$
Subtonacting both
$$S_{K} - S_{K-1} = 1 + 2 + 3 + 4 + - - - + (R-1)$$

$$T_{K} = \frac{(R-1)K}{2}$$

Curen that Rth term is n

$$\frac{T_{\kappa=n}}{\frac{k(k-1)}{2}-n} \rightarrow \frac{k^2-k}{2}-k=h$$

$$\Rightarrow k^2=h$$

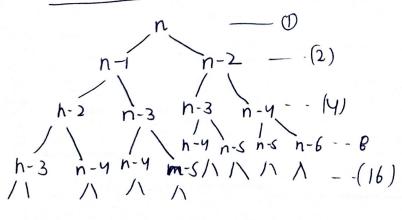
$$\Rightarrow k=\sqrt{n}$$

$$\Rightarrow \int T(n)=o(\sqrt{n})$$

Ignoring lower order terms & constants

2) 
$$T(n) = T(n-1) + T(n-2) + O(1)$$
  
For successive fiboracion

Recursion Toru:



No. of time function is ourning will be sum of the series:  $S = 1 + 2 + 4 + \cdots + 2^{n}$   $= 2^{n+1} - 1 = 2^{n+1} - 1$   $= 2^{-1} = 2^{n+1} - 1$ 

Time (ouplexity: 
$$T(n) = O(2^n)$$

From sucurion tow ] After pumo ning height of towe = n ] spare (omplexity = O(n))

```
3) (ode having time complexity:
    O(nlogn): foor (int i=1; i <= n; i++)
                        fog (int ] =1 ; j<n ; j=j+2)
                                pount[("Hello");
    o (n3): for (int i=0; i<n; i++)
               { ton (int j=0; j<n j j++)
                      fon (int k=0; R < n; R++)

pounts ("Hello");
                fog (int i=2; i<=n; i= pow (i,3))
 0 (log (log n)):
                     ¿ punt ('Hello');
     Here no can le vary positive integer
```

Ignoring lower order ferms:

$$T(n) = T\left(\frac{n}{4}\right) + \Gamma\left(\frac{n}{2}\right) + (n^{2})$$

Ignoring lower order ferms:

$$T(n) = \Gamma\left(\frac{n}{2}\right) + (h^{2})$$

Using master fluorum

$$a = 1 \quad b = 2 \quad f(n) = n^{2}$$

$$(= \log_{3} a = \log_{3} 1 = 0)$$

$$(= \log$$

6) Sequencing: 2,2k,(2r)k, (pr)k)k Generalising! 2k°, 2P', 2k², --- 2R2-) Assumption: let no, of ferme le 2 Given: last form is  $n = 2^{R^{\lambda-1}} = n$ R1-1 log 2 = log n  $R^{\lambda-1} = \log n$  [Ignoring constant (log 2)]  $(\lambda-1)\log k = \log n$ 12 = log(10gn) [ Ignosing constant fears] Time complexity: [T(n) = O (log (log n)) 8) a)  $\log 2 \log \lceil \log n \rceil \ge \log n \ge (\log n)^2 \le 5n \le n \le n (\log n)$   $\ge \log \lceil n \rceil \rceil \ge n^2 \le 2^n \ge 4^n \ge 2^n$ b)  $1 < \log(\log n) < \sqrt{\log n} < \log n < \log 2n < 2(\log n) < n < \log n$   $\log n < \log 2n < 2(\log n) < n^2 < n < 2^2$ 

c)  $96 < \log_8 n < \log_2 n < 5n < n (\log_6 n) < n (\log_2 n) < \log_6 (n!) < 8n^2 < 7n^3 < n! < 8^{2n}$