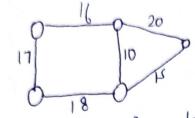
Tutorial - 6

1) Minimum Spanning Tout:

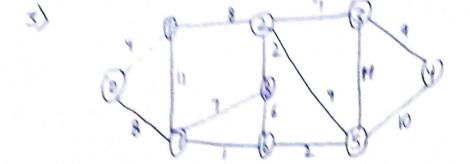
A spanning true of an undirected graph is a subgraph that is a done of joined by all vertices. One of those tree which has minimum total cost would be its minimum spanning tou.



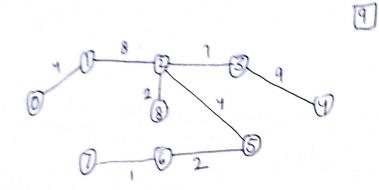
Minimum rost spanning tree

- 9t has direct applications in the design of networks including computer networks, telecommunication networks, tenansportation networks et Bellman

networks or		n langithm	pijkstora	Bellman
(Ams 2)	1903MI) TIGO TO	Kruukal's Algorithm O (Elog V)	Algo O (N+Elogy)	Bellman Fonds Algo O(VE)
TC	0 (V ²)	O (IEI+IVI)	0 (12)	0(Y ²)
SC	0 (V+E)			



Prism's Algo



Min Weight = 31

Parent: -1 0 1 2 3 2 5 62

Komskal's Algo

V V V

7 6 1 V

6 5 2 V

2 8 2 V V

2 9 4 V V

8 6 6 X

7 8 7 X

2 3 7 V

1 2 8 X

2 9 X

3 4 9 X

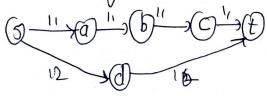
5 7 11 X

u) i) of 10 unik is added to each edge, the overall weight of the path may change.

Eg: 3 9 6

Spo Shortest path is $8 \rightarrow a \rightarrow b \rightarrow c \rightarrow t$ weight = |t|+|t|=4

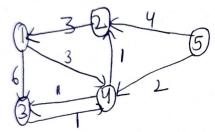
now if 10 units weight is added to each edge.



Shorter path changed to $s \rightarrow d \rightarrow t$ wight = 28

U) Multiplying the wight of each edge by 10 mill have no impact on the shortest path.

6) All pair shortest path algorithm - Floyd Warshall



$$R = \frac{1}{2} \begin{bmatrix} 0 & \infty & 6 & 3 & \infty \\ 0 & \infty & 6 & 3 & \infty \\ 2 & 3 & 0 & \infty & \infty & \infty \\ 3 & \infty & \infty & 0 & 2 & \infty \\ 3 & \infty & \infty & 0 & 0 & \infty \\ 4 & \infty & 4 & \infty & 2 & 0 \end{bmatrix}$$

$$A' = 1 \begin{bmatrix} 0 & \infty & 6 & 3 & \infty \\ 0 & \infty & 6 & 3 & \infty \\ 2 & 3 & 0 & 9 & 6 & \infty \\ 2 & \infty & 0 & 2 & \infty \\ 3 & \infty & 0 & 2 & \infty \\ 3 & \infty & 1 & 0 & \infty \\ 5 & \infty & 9 & 0 & 2 & 0 \end{bmatrix}$$

$$A^{\circ}[2,3]=\infty$$
 $A^{\circ}[2,1]+A^{\circ}[1,3]=3+\delta=9$
 $q<\infty$

$$A^{\circ}[2,1] + A^{\circ}[1,4] = 3+3=6$$

$$\Rightarrow 6 < \infty$$

$$A^{\circ}[2,5] = \infty$$
 $A^{\circ}[2,1] + A^{\circ}[1,5] = 3 + \infty$

$$A^{2} = \begin{bmatrix} 1 & 2 & 3 & 4 & S \\ 0 & \infty & 6 & 3 & \infty \\ 2 & 3 & 0 & 9 & 6 & \infty \\ 3 & \infty & \infty & 0 & 2 & \infty \\ 4 & \infty & 1 & 1 & 0 & \infty \\ 5 & 7 & 4 & 13 & 2 & 0 \end{bmatrix}$$

$$A'[1,3]=6$$
 $A'[1,2]+A'[2+3]=\infty+9$
 $6 < \infty+9$

$$A^{3} = 1 \begin{bmatrix} 0 & \infty & 6 & 3 & \alpha \\ 2 & 3 & 0 & 9 & 6 & \infty \\ 3 & \alpha & \infty & 0 & 2 & \infty \\ 4 & \infty & 1 & 1 & 0 & \infty \\ 5 & 7 & 4 & 13 & 2 & 0 \end{bmatrix}$$

$$A' = 1 \begin{cases} 0 & 4 & 4 & 3 & \infty \\ 2 & 3 & 0 & 7 & 6 & \infty \\ 3 & \infty & 3 & 0 & 2 & \infty \\ 4 & 0 & 1 & 1 & 0 & \infty \\ 5 & 7 & 3 & 3 & 2 & 0 \end{cases}$$

$$A = 1 \begin{cases} 0 & 4 & 4 & 3 & \infty \\ 2 & 3 & 0 & 7 & 6 & \infty \\ 3 & 0 & 3 & 0 & 2 & \infty \\ 4 & 0 & 1 & 1 & 0 & \infty \\ 5 & 7 & 3 & 3 & 2 & 0 \end{cases}$$