Simulation Lab 1

Date: 10 February 2025

Q1 Sphere Sphere Intersection Test (Summative)

To check if two Spheres intersect you first need to calculate the vector between those two spheres. If the length of that vector is less that the sum of the radii of the two spheres those spheres are intersecting one another. Remember as getting the square root of a number is an expensive operation. Most vector classes include a function to calculate the length (or magnitude) squared so it is better to compare the length of the vector squared with the sum of the two radii squared.

```
@@ -0,0 +1,15 @@
     + #pragma once
 2
     + class Vector3 {
           public:
 3
 4
               float x, y, z;
 5
     +
              // Constructor
 6
               Vector3(float x = 0, float y = 0, float z = 0);
8
9
              // Vector subtraction
               Vector3 operator-(const Vector3& other) const;
10
11
              // Calculate length squared
12
     +
13
              float LengthSquared() const;
14 + };
15
       @@ -0,0 +1,16 @@
     + #include "pch.h"
1
2
    + #include "Vector3.h"
3
    + // Constructor
4
5
     + Vector3::Vector3(float x, float y, float z) : x(x), y(y), z(z) {}
6
    + // Vector subtraction
7
8
     + Vector3 Vector3::operator-(const Vector3& other) const {
9
           return Vector3(x - other.x, y - other.y, z - other.z);
10
     + }
11
12
    + // Calculate the squared length
13
    + float Vector3::LengthSquared() const {
14
    + return x * x + y * y + z * z;
15 + }
16
```

```
✓ Simulation Lab 1/Sphere.h □

            @@ -0,0 +1,17 @@
          + #pragma once
          + #include "Vector3.h"
     2
          + class Sphere {
          + public:
     6
                Vector3 center;
                float radius;
     9
     10
                Sphere(const Vector3& center, float radius);
     11
                // Method to check collision with another sphere
     12
                bool CollideWith(const Sphere& other) const;
     13
        + };
     14
     15
     16
```

```
@@ -0,0 +1,19 @@
1
     + #include "pch.h"
2
     + #include "Sphere.h"
4
     + Sphere::Sphere(const Vector3& center, float radius) : center(center), radius(radius)
6
     + // Check collision with another sphere
     + bool Sphere::CollideWith(const Sphere& other) const {
8
           // Calculate the squared distance between centers
9
           float distanceSquared = (center - other.center).LengthSquared();
10
11
12
           // Calculate the squared sum of radii
           float radiiSum = radius + other.radius;
13
           float radiiSumSquared = radiiSum * radiiSum;
14
15
16
           // Check if the squared distance is less than or equal to squared radii sum
           return distanceSquared <= radiiSumSquared;</pre>
18
     + }
19
```

```
Sample-Test1/test.cpp 📮
      + TEST(SphereSphereCollision, NoIntersectionCentreAtOrigin) {
            Sphere sphereA(Vector3(0, 0, 0), 1);
            Sphere sphereB(Vector3(5, 0, 0), 1);
            EXPECT_FALSE(sphereA.CollideWith(sphereB)) << "Spheres at (0,0,0) and (5,0,0) with radius 1 should not collide.";
 10
     + TEST(SphereSphereCollision, NoIntersectionOffsetCentre) {
 12
            Sphere sphereA(Vector3(3, 3, 3), 2);
            Sphere sphereB(Vector3(10, 10, 10), 2);
            EXPECT_FALSE(sphereA.CollideWith(sphereB)) << "Spheres at (3,3,3) and (10,10,10) with radius 2 should not collide.";
 14
 15
     + }
 16
 17
      + TEST(SphereSphereCollision, OverlappingCentreAtOrigin) {
            Sphere sphereA(Vector3(0, 0, 0), 2);
 19
            Sphere sphereB(Vector3(2, 0, 0), 2);
 20
            EXPECT TRUE(sphereA.CollideWith(sphereB)) << "Spheres at (0,0,0) and (2,0,0) with radius 2 should overlap.";
     + }
 21
22
     +
 23 + TEST(SphereSphereCollision, OverlappingOffsetCentre) {
            Sphere sphereA(Vector3(5, 5, 5), 3);
            Sphere sphereB(Vector3(8, 5, 5), 3);
            EXPECT_TRUE(sphereA.CollideWith(sphereB)) << "Spheres at (5,5,5) and (8,5,5) with radius 3 should overlap.";
     + }
 28
     + TEST(SphereSphereCollision, FullyContainedCentreAtOrigin) {
            Sphere sphereA(Vector3(0, 0, 0), 5);
            Sphere sphereB(Vector3(1, 0, 0), 1);
            EXPECT_TRUE(sphereA.CollideWith(sphereB)) << "A larger sphere fully containing a smaller one should collide.";</pre>
```

Q2 Closest Distance from a Point to a Line (Summative)

An infinite line can be expressed as a set of points using the parametric equation P_L + mD_L for all values of m, where P_L is a point on the line, and D_L is the direction of the line. This is typically a unit vector - although in the demo below P_L is not unit. The diagram

below shows an infinite red line, which is defined by the green point on the line (P_L) and the purple direction of the line (D_L). The orange dot represents a point on the line for a specific value of m.

Solution:

Vector.h

```
@@ -0,0 +1,15 @@
     + #pragma once
1
     + class Vector3 {
           public:
4
               float x, y, z;
               // Constructor
6
               Vector3(float x = 0, float y = 0, float z = 0);
8
9
               // Vector subtraction
               Vector3 operator-(const Vector3& other) const;
10
11
               // Calculate length squared
12
               float LengthSquared() const;
13
14
     + };
```

Vector.cpp

```
@@ -0,0 +1,16 @@
     + #include "pch.h"
2
     + #include "Vector3.h"
3
    + // Constructor
4
5
     + Vector3::Vector3(float x, float y, float z) : x(x), y(y), z(z) {}
6
    + // Vector subtraction
     + Vector3 Vector3::operator-(const Vector3& other) const {
8
9
           return Vector3(x - other.x, y - other.y, z - other.z);
10
     + }
11
    + // Calculate the squared length
12
13
     + float Vector3::LengthSquared() const {
         return x * x + y * y + z * z;
14
15
   + }
16 +
```

Line.h

Line.cpp

```
#include "pch.h"

// Constructor

Line::Line(const Vector3& point, const Vector3& direction)

// Compute shortest distance

// Compute shortest distanc
```

Test.cpp:

```
TEST(PointLineDistance, ClosestPoint) {
       Line line(Vector3(0, 0, 0), Vector3(1, 1, 1));
       Vector3 point(2, 3, 4);
      float expectedDistance = std::sqrt(2);
float actualDistance = line.closestDistance(point);
       std::cout << "Test: ClosestPoint\n";
std::cout << "Expected: " << expectedDistance << ", Actual: " << actualDistance << "\n";</pre>
       EXPECT_NEAR(line.closestDistance(point), expectedDistance, 0.01);
V TEST(PointLineDistance, PointOnLine) {
       Line line(Vector3(0, 0, 0), Vector3(1, 2, 3));
       Vector3 point(3, 6, 9);
       float expectedDistance = 0.0f:
       float actualDistance = line.closestDistance(point);
       std::cout << "Test: PointOnLine\n";</pre>
       std::cout << "Expected: " << expectedDistance << ", Actual: " << actualDistance << "\n";
       EXPECT_NEAR(line.closestDistance(point), 0.0f, 0.01);
 TEST(PointLineDistance, VerticalCase) {
   Line line(Vector3(2, 0, 0), Vector3(0, 1, 0));
       Vector3 point(4, 5, 3);
       float expectedDistance = 3.61;
       float actualDistance = line.closestDistance(point);
       std::cout << "Test: VerticalCase\n";
std::cout << "Expected: " << expectedDistance << ", Actual: " << actualDistance << "\n";</pre>
       EXPECT_NEAR(line.closestDistance(point), expectedDistance, 0.01);
```

Output:

Q3 Sphere Line Intersection Test (Summative)

Now that you have the closest distance to a point on a line you can create a Sphere Line intersection test. All you need to do is to find the shortest distance from the point at the centre of the sphere to the line, and then compare that distance to the radius of the sphere.

Sphere.h:

```
Simulation Lab 1/Sphere.h 📮 💠
             @@ -1,5 +1,6 @@
             #pragma once
             #include "Vector3.h"
           + #include "Line.h"
             class Sphere {
             public:
             @@ -10,7 +11,10 @@ class Sphere {
                 Sphere(const Vector3& center, float radius);
                 // Method to check collision with another sphere
13
                 bool CollideWith(const Sphere& other) const;
                 //bool CollideWith(const Sphere& other) const;
      14
      15
      16
                 bool intersects(const Line& line) const;
      17
             };
```

Sphere.cpp:

```
Simulation Lab 1/Sphere.cpp 🖰
           - // Check collision with another sphere
7
           - bool Sphere::CollideWith(const Sphere& other) const{
8
                  // Calculate the squared distance between centers
9
                  //float distanceSquared = (center - other.center).LengthSquared();
10
11
                  // Calculate the squared sum of radii
12
                  float distanceSquared = (other.center - center).lengthSquared();
13
                  float radiusSum = radius + other.radius;
14
15
                  // Check if the squared distance is less than or equal to squared ra
16
                  //return distanceSquared <= radiiSumSquared;</pre>
17
                  return distanceSquared <= (radiusSum * radiusSum);</pre>
18
           + bool Sphere::intersects(const Line& line) const
      8
           + {
      9
                  float distance = line.closestDistance(center);
                  return distance <= radius;;
      10
```

```
TEST(SphereLineIntersection, NoIntersection) {
            Line line(Vector3(5, 5, 5), Vector3(1, 0, 0));
            Sphere sphere(Vector3(0, 0, 0), 3);
            bool expected = false;
            bool actual = sphere.intersects(line);
            std::cout << "Test: NoIntersection\n";</pre>
            std::cout << "Expected: " << (expected ? "true" : "false")</pre>
                << ", Actual: " << (actual ? "true" : "false") << "\n";</pre>
            EXPECT_FALSE(sphere.intersects(line));
92
        {\color{red}{\textbf{TEST}(SphereLineIntersection, PassesThroughSphere)}} \ \{
            Line line(Vector3(10, 0, 0), Vector3(-1, 0, 0));
            Sphere sphere(Vector3(10, 0, 0), 5);
            bool expected = true;
            bool actual = sphere.intersects(line);
            std::cout << "Test: PassesThroughSphere\n";</pre>
            std::cout << "Expected: " << (expected ? "true" : "false")</pre>
                << ", Actual: " << (actual ? "true" : "false") << "\n";
            EXPECT_TRUE(sphere.intersects(line));
     TEST(SphereLineIntersection, LineStartsInsideSphere) {
            Line line(Vector3(3, 2, 2), Vector3(1, 0, 0));
            Sphere sphere(Vector3(2, 2, 2), 5);
            bool expected = true;
            bool actual = sphere.intersects(line);
            std::cout << "Test: LineStartsInsideSphere\n";</pre>
            std::cout << "Expected: " << (expected ? "true" : "false")</pre>
                << ", Actual: " << (actual ? "true" : "false") << "\n";
            EXPECT_TRUE(sphere.intersects(line));
        TEST(SphereLineIntersection, LinePassesThroughCenter) {
            Line line(Vector3(-5, 0, 0), Vector3(1, 0, 0));
            Sphere sphere(Vector3(0, 0, 0), 3);
            bool expected = true;
            bool actual = sphere.intersects(line);
```

```
Microsoft Visual Studio Debu
              Running 4 tests from 1 test case.
              Global test environment set-up.
              4 tests from SphereLineIntersection
             SphereLineIntersection.NoIntersection
Test: NoIntersection
Expected: false, Actual: false
[ OK ] SphereLineIntersection.NoIntersection (0 ms)
             SphereLineIntersection.PassesThroughSphere
[ HOW ] SphereEller
Expected: true, Actual: true
[ OK ] SphereLineIntersection.PassesThroughSphere (1 ms)
              SphereLineIntersection.LineStartsInsideSphere
Test: LineStartsInsideSphere
Expected: true, Actual: true
[ OK ] SphereLineIntersection.LineStartsInsideSphere (0 ms)
              SphereLineIntersection.LinePassesThroughCenter
Test: LinePassesThroughCenter
Expected: true, Actual: true
              SphereLineIntersection.LinePassesThroughCenter (0 ms)
        OK ]
              4 tests from SphereLineIntersection (3 ms total)
              Global test environment tear-down
              4 tests from 1 test case ran. (4 ms total)
            1 4 tests.
C:\Users\shruti\source\repos\Simulation Lab 1\x64\Debug\Sample-Test1.exe (process 25372) exited with code 0 (0x0).
To automatically close the console when debugging stops, enable Tools->Options->Debugging->Automatically close the conso
le when debugging stops
Press any key to close this window .
```

Q4. Closest Distance from a Point to a Plane (Summative)

You can define a plane as a point on the plane and the normal vector; the unit vector that is perpendicular to the plane. It can also be useful to store two other vectors that are on the plane.

In the diagram (and interactive demo) below the Plane is being defined by three points in the Plane. The green sphere, and the points at the end of the blue and red vectors. The green vector is the cross product of the red and blue vectors, and so is perpendicular to the red and blue vectors, and the plane. Note that the green vector is **not** a unit length vector.

In the interactive demo you can move the orange sphere around on the plane by using the sliders to adjust the values of S and T. This represents the number of blue vectors (S) and red vectors (T) to get to that point from the green point on the plane - so the points on the plane could be defined as $P_P + SP_B + TP_R$

```
class Vector3 {
   public:
       float x, y, z;
       // Constructor
       Vector3();
       Vector3(float x, float y, float z);
       float lengthSquared() const;
       // Vector subtraction
       Vector3 operator-(const Vector3& other) const;
       Vector3 operator+(const Vector3& other) const;
       Vector3 operator*(float scalar) const;
       float dot(const Vector3& other) const;
       float length() const;
       Vector3 normalize() const;
       // Print
       void print() const;
```

```
// Subtraction

Vector3 Vector3::operator-(const Vector3& other) const {
    return Vector3(x - other.x, y - other.y, z - other.z);
}

// Addition

Vector3 Vector3::operator+(const Vector3& other) const {
    return Vector3(x + other.x, y + other.y, z + other.z);
}

// Scalar multiplication

Vector3 Vector3::operator*(float scalar) const {
    return Vector3(x * scalar, y * scalar, z * scalar);
}

// Dot product

float Vector3::dot(const Vector3& other) const {
    return x * other.x + y * other.y + z * other.z;
}

// Length (magnitude)

float Vector3::length() const {
    return std::sqrt(xx: x * x + y * y + z * z);
}

// Normalize

Vector3 Vector3::normalize() const {
    float len = length();
    return (len > 0) ? *this * (1.0f / len) : Vector3(x:0, y:0, z:0);
}

// Print
```

```
Simulation Lab 1/Plane.h 📮
         @@ -0,0 +1,14 @@
       + #pragma once
       + #include "pch.h"
       + #include "Vector3.h"
  3
  4
  5
       + class Plane {
       + public:
             Vector3 point; // A point on the plane
  7
             Vector3 normal; // Normal vector of the plane
  8
  9
             Plane(const Vector3& point, const Vector3& normal);
  10
  11
             float closestDistance(const Vector3& P_G) const;
      + };
  12
  13
  Simulation Lab 1/Plane.cpp 📮
           @@ -0,0 +1,13 @@
    1
         + #include "pch.h"
         + #include "Plane.h"
    2
         + #include <cmath>
    3
    4
         + Plane::Plane(const Vector3& point, const Vector3& normal)
                : point(point), normal(normal.normalize()) {}
         + // Compute shortest distance from a point to the plane
         + float Plane::closestDistance(const Vector3& P_G) const {
    8
    9
                // Vector from plane point to general point
               Vector3 V = P_G - point;
    10
               // Perpendicular distance using dot product
    11
    12
               return std::fabs(V.dot(normal));
         + }
    13
```

```
** Sample-Test1
                                                     (Global Scope)
         Plane plane(Vector3(0, 0, 0), Vector3(0, 0, 1));
                Vector3 point(2, 3, 5);
                float expected = 5.0;
                float actual = plane.closestDistance(point);
                std::cout << "Test: PointAbovePlane\n";</pre>
                std::cout << "Expected: " << expected << ", Actual: " << actual << "\n";
   143
                EXPECT_NEAR(actual, expected, 0.01);
         TEST(PointPlaneDistance, PointBelowPlane) {
                Plane plane(Vector3(0, 0, 0), Vector3(0, 0, 1));
                Vector3 point(2, 3, -4);
                float expected = 4.0;
                float actual = plane.closestDistance(point);
                std::cout << "Test: PointBelowPlane\n";</pre>
                std::cout << "Expected: " << expected << ", Actual: " << actual << "\n";
                EXPECT_NEAR(actual, expected, 0.01);
         TEST(PointPlaneDistance, PointOnPlane) {
                Plane plane(Vector3(1, 1, 1), Vector3(1, 1, 1).normalize());
                Vector3 point(0, 2, 1);
                float expected = 0.0;
                float actual = plane.closestDistance(point);
                std::cout << "Test: PointOnPlane\n";</pre>
                std::cout << "Expected: " << expected << ", Actual: " << actual << "\n";
                EXPECT_NEAR(actual, expected, 0.01);
            int main(int argc, char** argv) {
                ::testing::InitGoogleTest(&argc, argv);
                return RUN_ALL_TESTS();
```

```
Microsoft Visual Studio Debuc X
                  Running 3 tests from 1 test case.
                 Global test environment set-up. 3 tests from PointPlaneDistance
                  PointPlaneDistance.PointAbovePlane
Test: PointAbovePlane
Expected: 5, Actual: 5
                  PointPlaneDistance.PointAbovePlane (1 ms)
                  PointPlaneDistance.PointBelowPlane
Test: PointBelowPlane
Expected: 4, Actual: 4
[ OK ] PointPlaneDistance.PointBelowPlane (0 ms)
                  PointPlaneDistance.PointOnPlane
Test: PointOnPlane
Expected: 0, Actual: 0

[ OK ] PointPlaneDistance.PointOnPlane (1 ms)

[-----] 3 tests from PointPlaneDistance (2 ms total)
                  Global test environment tear-down
               = 3 tests from 1 test case ran. (2 ms total) 3 tests.
C:\Users\shruti\source\repos\Simulation Lab 1\x64\Debug\Sample-Test1.exe (process 22232) exited with code 0 (0x0).
To automatically close the console when debugging stops, enable Tools->Options->Debugging->Automatically close the conso
le when debugging stops.
Press any key to close this window . . .
```

Q5. Sphere to Plane Collision (Summative)

Again once you can find the closest point to a plane finding out if a sphere and a plane are intersecting is simple. You just need to find out if the closest distance from the centre of the sphere to the plane is less that the radius.

You are encouraged to do your own research to find the distance from a point to a plane. One way is to project the Vector from the point on the plane to the general point onto the normal vector of the plane.

Sphere.h:

```
//to check if a line intersects with the sphere
//bool intersects(const Line& line) const;
bool planeIntersects(const Plane& plane) const;
```

```
v bool Sphere::planeIntersects(const Plane& plane) const
{
          float distance = plane.closestDistance(center);
          return distance <= radius;
}</pre>
```

```
TEST(SpherePlaneCollision, SphereAbovePlane_NoCollision) {
       Plane plane(Vector3(0, 0, 0), Vector3(0, 0, 1));
Sphere sphere(Vector3(0, 0, 5), 3);
       bool expected = false;
       bool actual = sphere.planeIntersects(plane);
       EXPECT_EQ(actual, expected);
v TEST(SpherePlaneCollision, SphereTouchesPlane) {
    Plane plane(Vector3(0, 0, 0), Vector3(0, 0, 1));
    Sphere sphere(Vector3(0, 0, 3), 3);
      bool expected = true;
      bool actual = sphere.planeIntersects(plane);
       std::cout << "Test: SphereTouchesPlane\n";</pre>
       EXPECT_EQ(actual, expected);
V TEST(SpherePlaneCollision, SphereIntersectsPlane) {
       Plane plane(Vector3(0, 0, 0), Vector3(0, 0, 1));
Sphere sphere(Vector3(0, 0, 2), 3);
       bool expected = true;
       bool actual = sphere.planeIntersects(plane);
       std::cout << "Test: SphereIntersectsPlane\n";</pre>
       std::cout << "Expected: " << (expected ? "true" : "false")
<< ", Actual: " << (actual ? "true" : "false") << "\n";
       EXPECT_EQ(actual, expected);
```