

TOPIC 1: Introduction to Data Structures

1) Discuss the difference between

(1) Primitive Data Types

- i) Basic data types directly operated by machine instruct.
- ii) Cannot be NULL
- iii) Size depends on type of data structure (it is fixed)
- iv) Eg, integer, float, character, boolean, etc

Non-Primitive Data Types

- i) Group of homogeneous or heterogeneous primitive data types
- ii) Can have NULL values
- iii) Size is not fixed
- iv) Eg, Array, String, Linked List, Stack, etc

(2) Linear Data Structures

- i) Have data elements arranged in sequential manner
- ii) Each element is connected to its previous and next element.
- iii) Elements present in single level and can be traversed in single run.
- iv) Eg, Array, Stack, Queue, etc

Non-Linear Data Structures

- i) Have no set sequence of connecting all its elements
- ii) Each element can have multiple paths to connect to other elements
- iii) Elements present in multi-level and often can't be traversed in single run
- iv) Eg, Trees, Graphs, etc

(3) Space complexity

i) The amount of computer memory that is required from start of its execution to its completion wrt input size.

- ii) It is calculated as sum of :
 - Fixed Component
 - Variable Component

Time Complexity

i) The amount of time taken by an algorithm to run wrt input size.

ii) It is calculated by counting the number of elementary operations performed (Considering that each elementary operation takes a fixed amount of time to perform).

(4) Big Oh (O):

- Express upper bound of algorithm's running time.
- Measures the worst case time complexity.
- Maximum amount of time algorithm can take.

Omega (Ω):

- Express lower bound of algorithm's running time.
- Measures the best case time complexity.
- Minimum amount of time an algorithm can take to complete.

Theta (Θ):

- It measures the average case time complexity.

TOPIC 6 : Trees

- 1) Algorithm for evaluating an expression using tree

STEP 1 - START

STEP 2 - IF root is NULL return 0

STEP 3 - IF both Left and Right child of root are NULL return value of root as an integer

STEP 4 - DECLARE LeftVal and RightVal

STEP 5 - Call FUNCTION evaluateExpression for Left child of root and assign its value to LeftVal

STEP 6 - Call FUNCTION evaluateExpression for Right child of root and assign its value to RightVal

STEP 7 - IF root's value is +, return LeftVal + RightVal

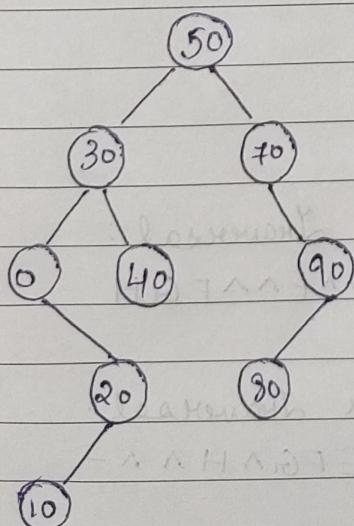
STEP 8 - IF root's value is -, return LeftVal - RightVal

STEP 9 - IF root's value is *, return LeftVal * RightVal

STEP 10 - IF root's value is /, return LeftVal / RightVal

- 2) Draw Binary Search Trees and Traverse \rightarrow In-order, Pre-order and Post-order

(i) 50, 30, 0, 20, 40, 90, 80, 10, 40



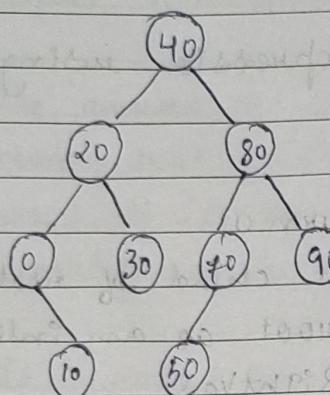
Traversal:

In-Order: 0, 10, 20, 30, 40, 50, 70, 80, 90

Pre-Order: 50, 30, 0, 20, 10, 70, 90, 80

Post-Order: 10, 20, 0, 40, 30, 80, 90, 70, 50

(2) 40, 20, 0, 30, 80, 90, 70, 10, 50



Traversal:

In-Order: 0, 10, 20, 30, 40, 50, 70, 80, 90

Pre-Order: 40, 20, 0, 10, 30, 80, 70, 50, 90

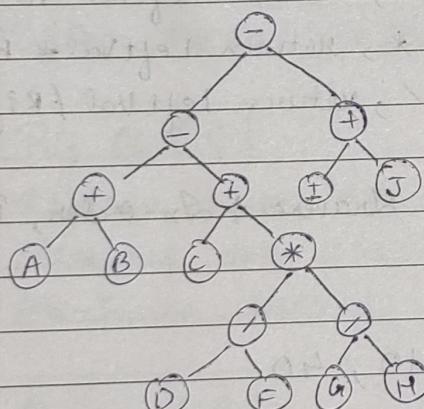
Post-Order: 10, 0, 30, 20, 50, 40, 90, 80, 40

(3)

3) Draw expression trees and give Traversals:

Pre-order and Post-order.

(1) A + B - C + D / F * G / H - I + J



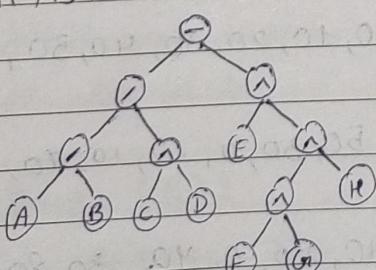
Pre-Order Traversal:

- + + A B - C + D / F * G / H - I J

Post-Order Traversal:

A B + C D F / G H / * + - I J + -

(2) A / B / C ^ D - E ^ (F ^ G) ^ H



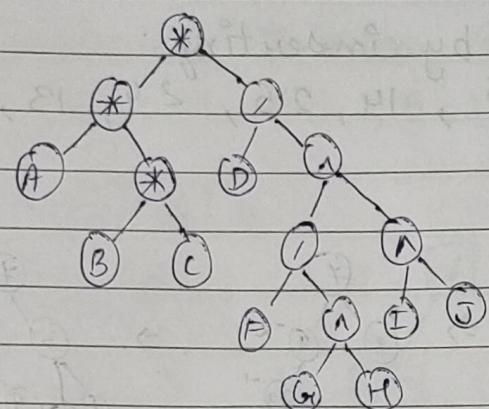
Pre-Order Traversal:

- / / A B / C ^ D - E ^ (F ^ G) ^ H

Post-Order Traversal:

A B / C D ^ / E F G ^ H ^ -

(3) $A * (B * C) * D / (F / G \wedge H) \wedge I \wedge J$



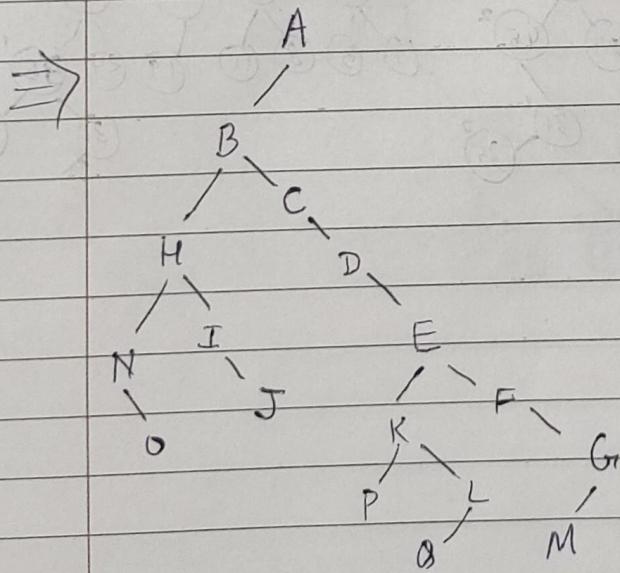
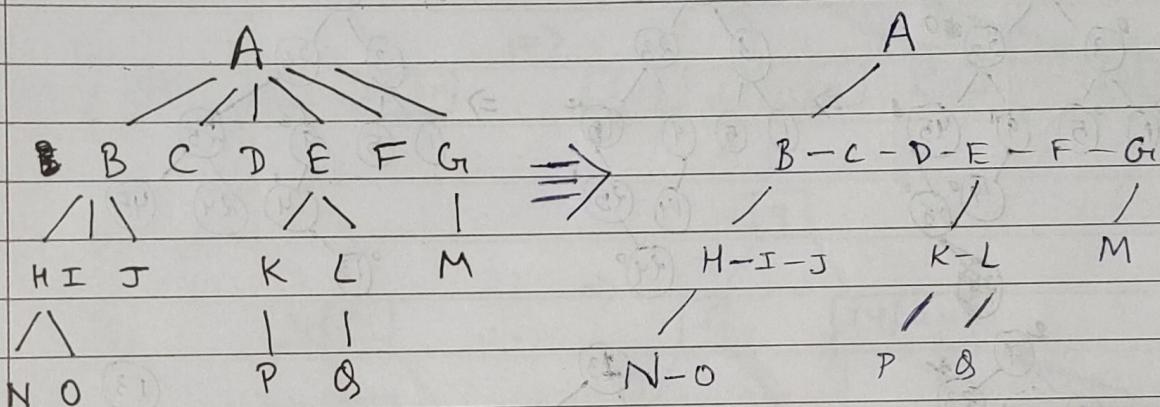
Pre-Order Traversal:

* * A * B C / D / F ^ G H ^ I J

Post-Order Traversal:

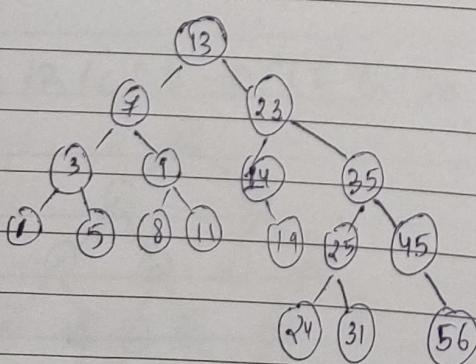
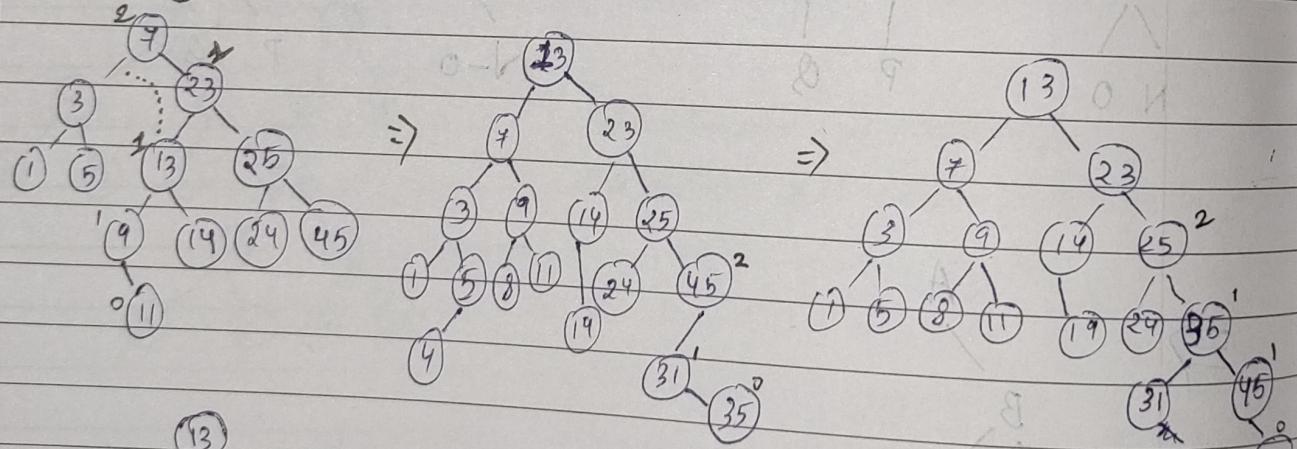
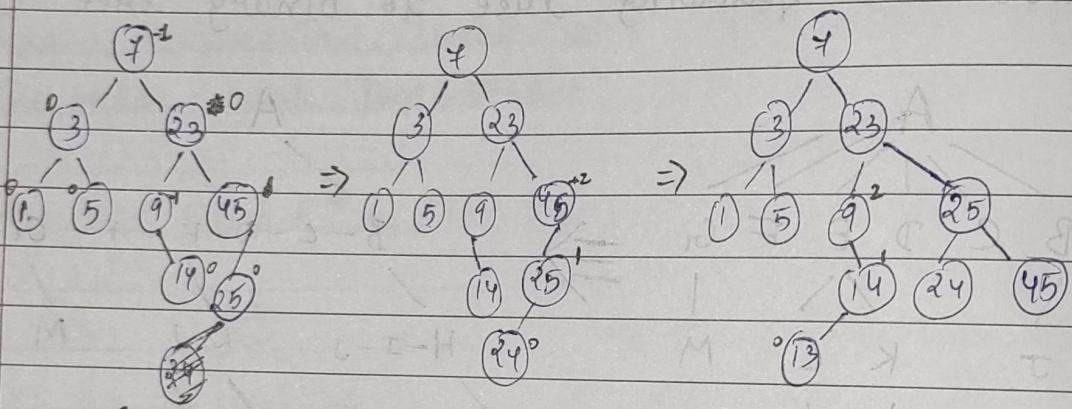
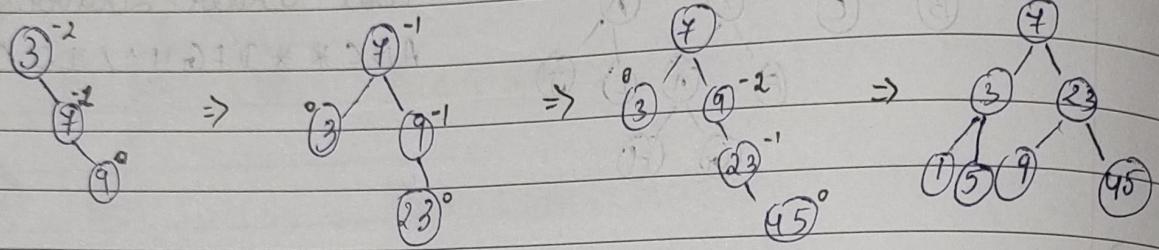
A B C * * D F G H ^ / I J . ^ ^ / *

4) Convert the following tree to binary tree:



TOPIC 6.1 : Balanced Trees and More

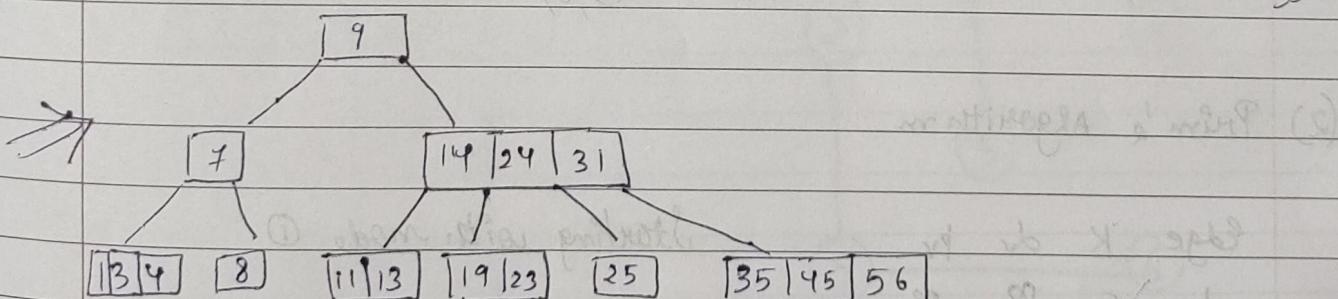
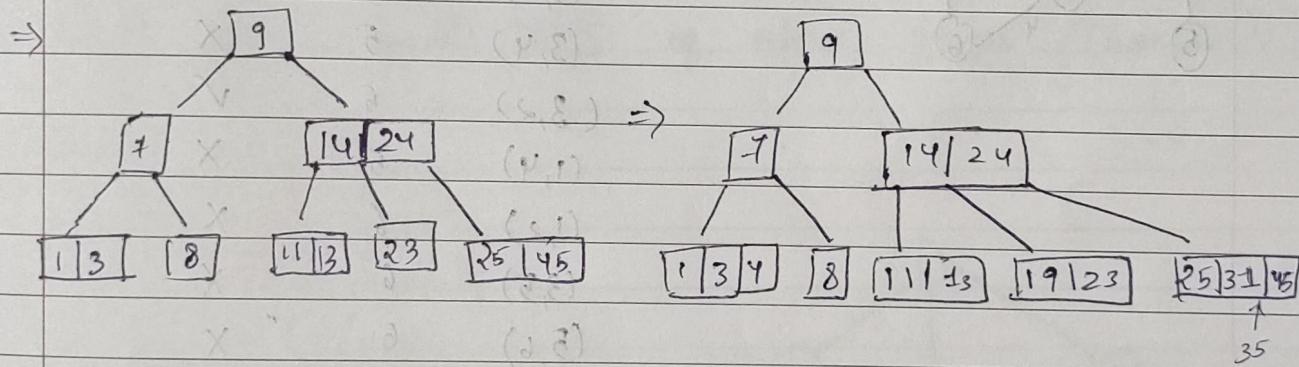
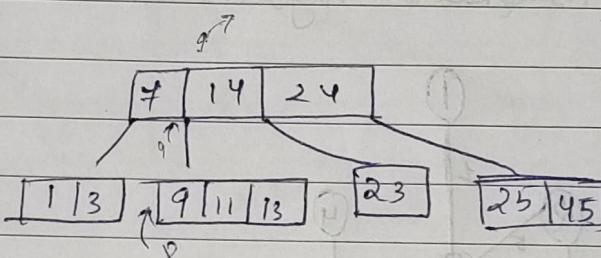
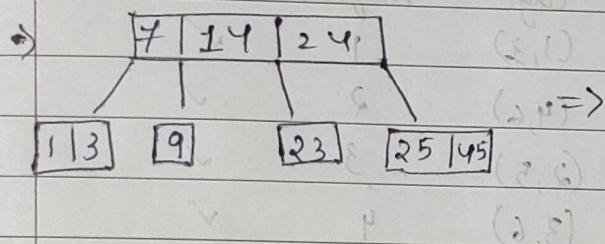
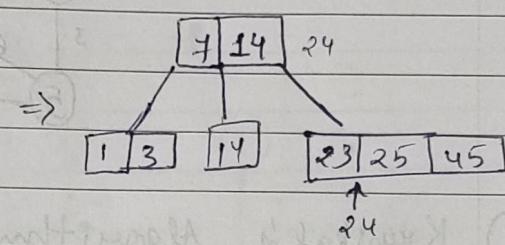
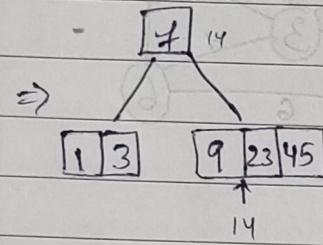
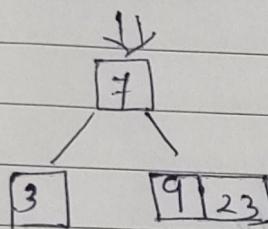
1) Construct AVL Tree by inserting:
3, 7, 9, 23, 45, 1, 5, 14, 25, 24, 13, 11,
8, 19, 4, 31, 35, 56



$$(3) A^*(B^*C)^*D / (F/G^*H)^*I^*J$$

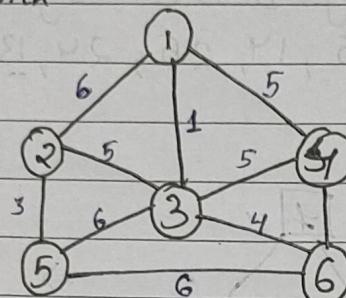
2) Construct B 4-way B-Tree by inserting
 $3, 7, 9, 23, 45, 1, 5, 14, 25, 24, 13, 11, 8, 19, 4, 31, 35, 56$

$\boxed{3 \mid 7 \mid 9} \quad 23$

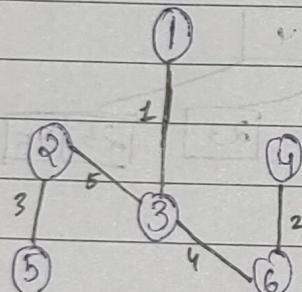


TOPIC 7 : Graph

1) Find MST with



(1) Kruskal's Algorithm



Edge Weight

(1,3)

(4,6)

(2,5)

(3,6)

(3,4)

(3,2)

(1,4)

(1,2)

(3,5)

(5,6)

(2) Prim's Algorithm

Edge K dv pr

1 F ∞ ∞

2 F ∞ ∞

3 F ∞ ∞

4 F ∞ ∞

5 F ∞ ∞

6 F ∞ ∞

Starting with node ①

E K dv pr

1 T 0 -

2 6 1

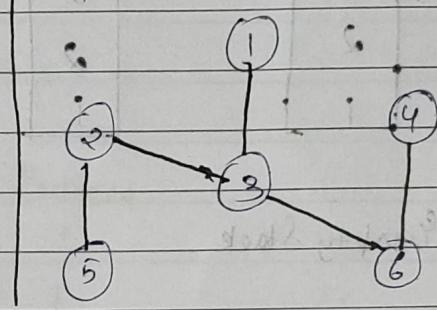
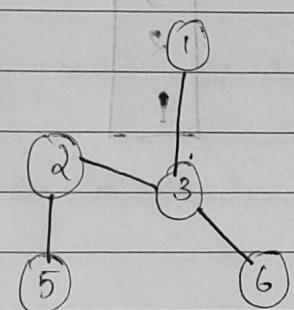
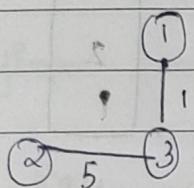
3 T 1 1

4 5 1

5

6

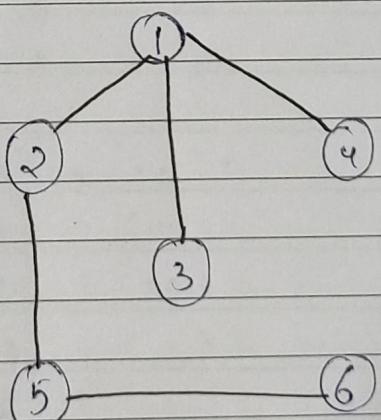
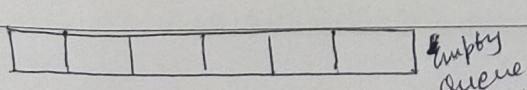
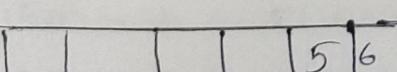
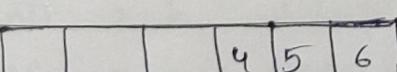
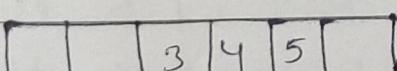
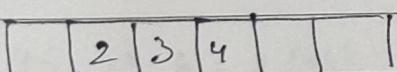
| E | K | dv | pv | E | K | dv | pv | E | K | dv | pv |
|---|---|----|----|---|---|----|----|---|---|----|----|
| 1 | T | 0 | - | 1 | T | 0 | - | 1 | T | 0 | - |
| 2 | T | 5 | 7 | 2 | T | 5 | 3 | 2 | T | 5 | 3 |
| 3 | T | 1 | 1 | 3 | T | 1 | 1 | 3 | T | 1 | 1 |
| 4 | | | | 4 | | | | 4 | T | 2 | 6 |
| 5 | | 3 | 2 | 5 | T | 3 | 2 | 5 | T | 3 | 2 |
| 6 | | | | 6 | | 4 | 3 | 6 | | - | - |



MST : 15

2) Find BFS and DFS of above graph (choose ①)

(1) BFS

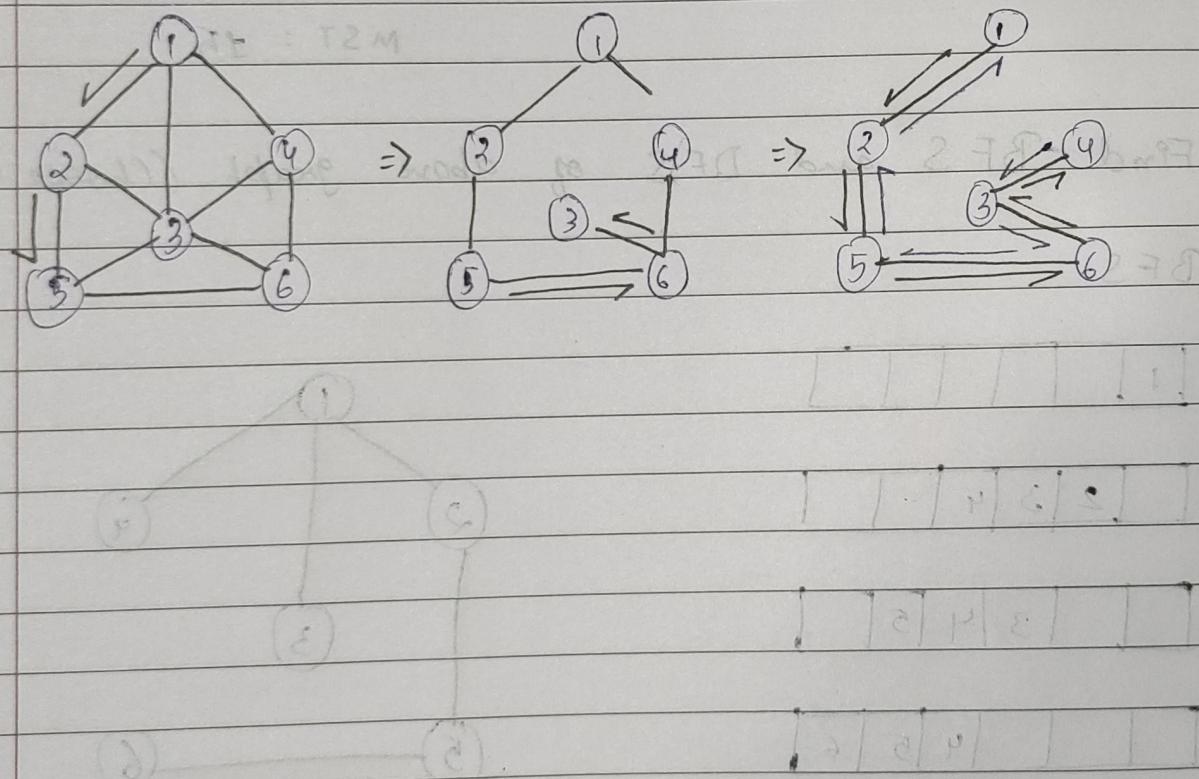


(2) DFS

Stack

| (i) | | (ii) | | (iii) | | (iv) | | (v) | | (vi) | |
|-----|--|------|---|-------|---|------|---|-----|---|------|--|
| | | | 3 | | | | 6 | | | | |
| 5 | | 6 | 5 | | 6 | | 5 | | | | |
| 2 | | 2 | 2 | | 2 | | 2 | | 1 | 2 | |
| 1 | | 1 | 1 | | 1 | | 1 | | 1 | 1 | |

(vii) Empty Stack



TOPIC 8 : Hashing

- 1) Insert following keys by creating hash-table of size $m = 15$ and write the no. of probes for each key.
 Consider $h(k) = (2k+3) \bmod m$, where quadratic probing is used for collision resolution.
 Keys : 45, 29, 16, 50, 25, 150, 120, 8, 10

Given $m = 15$, $h(k) = (2k+3) \bmod m$

| Key | Index (Location) | Probes |
|-----|------------------|--------|
| 45 | 3 | 1 1 |
| 29 | 1 | 1 1 |
| 16 | 5 | 1 1 |
| 50 | 13 | 1 1 |
| 25 | 8 | 1 1 |
| 150 | 4 | 2 |
| 120 | 7 | 3 |
| 8 | 9 | 1 2 |
| 10 | 10 | 1 |

- i) $45 \rightarrow h = 2(45) + 3 \% 15 = 3 \rightarrow (aa) \leftarrow 61$
- ii) $29 \rightarrow h = 2(29) + 3 \% 15 = 1 \rightarrow (bb) \leftarrow 42$
- iii) $16 \rightarrow h = 2(16) + 3 \% 15 = 5 \rightarrow (pp) \leftarrow 18$
- iv) $50 \rightarrow h = 2(50) + 3 \% 15 = 13 \rightarrow (ss) \leftarrow 10$
- v) $25 \rightarrow h = 2(25) + 3 \% 15 = 8 \rightarrow (dd) \leftarrow 01$
- vi) $150 \rightarrow h = 2(150) + 3 \% 15 = 3 \rightarrow (ee) \leftarrow 72$
- vii) $120 \rightarrow h = 2(120) + 3 \% 15 = 3 \rightarrow (mm) \leftarrow 11$
- viii) $8 \rightarrow h = 2(8) + 3 \% 15 = 8 \rightarrow (cc) \leftarrow 06$
- ix) $10 \rightarrow h = 2(10) + 3 \% 15 = 10 \rightarrow (bb) \leftarrow 22$

2) Insert following keys, size $m=24$ and no. of probes for each key. Consider $h_1(k) = (2k+1) \bmod m$ and $h_2(k) = (3+k) \bmod m$.

Keys: 122, 24, 99, 36, 100, 50, 144, 120, 88, 10

Given, $m=24$; $h_1(k) = (2k+1) \bmod m$

$h_2(k) = (3+k) \bmod m$

Key:

| Key | Index (Location) | Probe |
|-----|------------------|-------|
|-----|------------------|-------|

| | | |
|-----|----|---|
| 122 | 5 | 1 |
| 24 | 1 | 1 |
| 99 | 7 | 1 |
| 36 | 16 | 2 |
| 100 | 8 | 1 |
| 50 | 10 | 2 |
| 144 | 0 | 1 |
| 120 | 3 | 2 |
| 88 | 19 | 2 |
| 10 | 23 | 0 |

- i) $122 \rightarrow 2(122) + 1 \% 24 = 5 + (0) \Rightarrow 5$
- ii) $24 \rightarrow 2(24) + 1 \% 24 = 1 + (0) \Rightarrow 1$
- iii) $99 \rightarrow 2(99) + 1 \% 24 = 7 + (1) \Rightarrow 8$
- iv) $36 \rightarrow 2(36) + 1 \% 24 = 1 + (3+36) \% 24 = 15 \Rightarrow 16$
- v) $100 \rightarrow 2(100) + 1 \% 24 = 8 + 1 = 9$
- vi) $50 \rightarrow 2(50) + 1 \% 24 = 8 + 1 = 9 \Rightarrow (3+50) \% 24 = 5 \Rightarrow 10$
- vii) $144 \rightarrow 2(144) + 1 \% 24 = 0 \Rightarrow (3+144) \% 24 = 3 \Rightarrow 3$
- viii) $120 \rightarrow 2(120) + 1 \% 24 = 0 \Rightarrow (3+120) \% 24 = 3 \Rightarrow 3$
- ix) $88 \rightarrow 2(88) + 1 \% 24 = 9 \Rightarrow (3+88) \% 24 = 10 \Rightarrow 19$
- x) $10 \rightarrow 2(10) + 1 \% 24 = 10 \Rightarrow (3+10) \% 24 = 13 \Rightarrow 23$