

JADAVPUR UNIVERSITY

BRAIN MR IMAGE SEGMENTATION USING RBF NEURAL NETWORK

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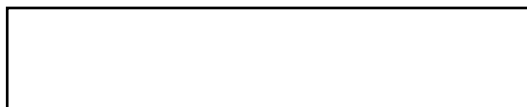
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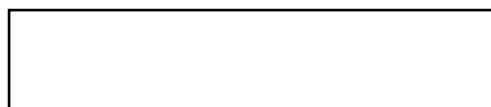
To whom it may concern

I hereby recommend that the project **“BRAIN MR IMAGE SEGMENTATION USING RBF NEURAL NETWORK”** has been carried out by **SHRUTI PATHAK** (Registration No.: 163613 of 2022 - 2023, Class Roll No.: 002210503021, Exam Roll No.: MCA) under my guidance and supervision and be accepted in partial fulfillment of the requirement for the degree of **MASTER of COMPUTER APPLICATION** in **DEPARTMENT of COMPUTER SCIENCE and ENGINEERING, JADAVPUR UNIVERSITY**, during the academic year 2023-2024.



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CERTIFICATE OF APPROVAL

This is to certify that the project entitled “**BRAIN MR IMAGE SEGMENTATION USING RBF NEURAL NETWORK**” is a bonafide record of work carried out by **SHRUTI PATHAK** in partial fulfillment of the requirements for the award of the degree of **MASTER of COMPUTER APPLICATION** in the **DEPARTMENT of COMPUTER SCIENCE & ENGINEERING, JADAVPUR UNIVERSITY**. It is understood that by this approval the undersigned do not necessarily endorse or approve any statement made, opinion expressed or conclusion drawn therein but approve the project work only for the purpose for which it has been submitted.

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DECLARATION OF ORIGINALITY AND COMPLIANCE OF ACADEMIC PROJECT

I hereby declare that this thesis work holds literature survey and original research work by the undersigned candidate, as a student of **MASTER OF COMPUTER APPLICATION**. All the information in this document have been obtained and presented in accordance with academic rules and ethical conduct. I also declare that, as required by these rules and conduct, I have fully cited and referenced all the material results that are not original to this work.

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1) Introduction :

In medical image analysis, image segmentation is a fundamental task, especially when it comes to brain MRIs (Magnetic Resonance Imaging). It is essential for several applications, including surgical planning, brain tissue classification, and tumor identification. Among the numerous segmentation methods available, the Radial Basis Function (RBF) [1] algorithm has gained significant attention and proven to be effective in handling the complexity and variability of brain MRI data.

Image segmentation plays an important role in medical imaging, particularly when analyzing magnetic resonance imaging (MRI) scans of the brain. Since MRI offers detailed information on the brain, it is a valuable diagnostic and research tool for a wide range of neurological conditions. However, in order to extract useful information from these complex images, it is necessary to correctly segment the relevant brain structures.

The act of dividing an MRI scan of the brain into distinct areas or structures, such as white matter, gray matter, cerebrospinal fluid(CSF), and anatomical regions like the cortex, ventricles, or tumors, is known as brain MRI segmentation.

Accurate segmentation of brain MRI scans is complicated due to the inconsistencies and differences between brain structures, images, and the images obtained. To address these issues and produce dependable segmentation results, researchers and specialists have created a wide range of computational approaches, ranging from conventional image processing techniques to sophisticated machine learning and deep learning. It also provides an overview of commonly used segmentation techniques, highlighting their strengths, limitations, and future directions in the brain.

The Radial Basis Function (RBF) method proves to be an effective tool for brain MRI segmentation, skillfully managing complicated data. Its kernel functions accurately delineate brain structures by modeling complex interactions in an efficient manner. RBF's effectiveness in capturing tissue boundaries and accommodating intensity variations bolsters medical image analysis. From surgical planning to neurological research, RBF helps with diagnosis, treatment planning, and advancements in neuro-imaging, and it promises further improvements in the use of MRIs.

In this article, we investigate a distinctive approach using the Radial Basis Function (RBF) algorithm for brain MR image segmentation across various data volumes with different noise and intensity. Our exploration aims to discern the algorithm's efficacy amidst diverse conditions, offering insights into its robustness and adaptability in real-world applications.

1.1) Image Segmentation :

One popular technique for processing and analyzing digital images is image segmentation. Its goal is to separate the image into distinct sections or areas, usually using pixel attribute measurement. These concepts can influence how the foreground and background are separated, or they can group pixels together according to color or shape consistency. For instance, image segmentation is frequently used in medical science to recognize and label pixels or 3D voxels that represent tumors in the patient's brain or other organs.

To put it another way, image segmentation is the process of breaking apart an image into separate, recognizable areas or objects according to attributes like color, texture, shape, or brightness. The purpose of image segmentation is to simplify the image representation and transform it into a useful and identifiable form. In this process, each pixel is assigned a label so that pixels with similar characteristics can be placed in the same category.

Image segmentation is instrumental across multiple sectors. In medicine, it facilitates diagnosis and treatment planning by outlining organs and anomalies in images, while in satellite imagery, it supports land classification and disaster response efforts. Robotics and computer vision benefit from segmentation for object detection and navigation, while manufacturing relies on it for quality control. Similarly, in agriculture, segmentation aids in crop monitoring and yield estimation. Overall, segmentation enables precise analysis and automation, enhancing efficiency and decision-making in diverse domains.

Two types of image segmentation commonly used are:

- **Semantic Segmentation:** Semantic segmentation involves classifying each pixel in an image into predefined categories or classes, without distinguishing between instances of the same class. This type of segmentation assigns a label to every pixel in the image, resulting in a pixel-wise segmentation map that delineates different objects or regions.
- **Instance Segmentation:** Instance segmentation goes a step further than semantic segmentation by not only classifying pixels into categories but also distinguishing between individual object instances within the same class. In instance segmentation, each object instance in the image is uniquely identified and segmented, providing a more detailed understanding of the scene compared to semantic segmentation.

1.2) Brain MR Image Segmentation :

The brain, which is the body's central nervous system, controls speech, memory, cognition, and movement function in addition to acting as a warning system for body control. The rise in brain diseases caused by many factors like high stress, fast-paced lifestyle, stress on the brain and emotions, frequent injuries and the elderly has become more alarming in recent years. The health of people is gravely threatened by these circumstances.

Brain illnesses are commonly diagnosed in medicine using magnetic resonance imaging (MRI) equipment. The shape and function of the brain's tissues can be electronically visualized with magnetic resonance imaging (MRI), a cutting-edge medical procedure. Doctors can benefit from non-invasive, non-radiation, but more precise and superior solutions with comparable tissues by using this technique.

In general, brain image segmentation methods are categorized as intensity-based [2] , machine learning [3] , hybrid [4] etc. These methods are both progressive and collaborative. Segmenting (i) healthy brain tissues, (ii) brain sub-structures, and (iii) tumor and intra-tumor regions is the overall goal of the method. Conversely, a progressive approach makes the procedure more complex.

Tesla MRI [5] is generally used to detect tumours, aneurysms etc. in brain and any blockages in blood vessels in heart. A Tesla MRI produces substantially sharper images in less time by using magnetic fields that are twice as strong as a standard MRI.

1.2.A) Need of Brain MR Image Segmentation :

There are several reasons why a brain MRI - which produces incredibly precise image might be necessary. If doctors asked for an MRI of the brain, its not indicate to the worst case such as brain tumor or some other deadly condition. But the reality is that brain MRI is a diagnostic tool for a wide range of disorders involving the brain and spinal cord.

➤ **Stroke:**

When a blood artery in the brain becomes blocked or starts to bleed, a stroke [6] occurs. Within minutes, brain tissue begins to degrade due to this disturbance of oxygenated circulation. Brain MRI is a useful diagnostic technique for determining whether a cerebral hemorrhage or stroke has caused brain tissue damage. It helps medical professionals to evaluate damage and decide quickly on the best course of action. Medical professionals can identify the next steps required for successful therapy by using information from brain MRIs.

➤ **Tumors or Cysts:**

In addition to helping diagnose brain disorders, magnetic resonance imaging (MRI) scans can find small cysts [7] that CT scans might miss. In certain instances, doctors may administer an intracranial injection of a specialized contrast agent prior to the scan in order to enhance the visibility of various brain regions. Doctors are able to spot tumors and cysts that are challenging to detect with other procedures thanks to the better and more detailed images provided by this modern technology.

➤ **Traumatic Brain Injury and Abnormalities :**

The severity of traumatic brain injuries [8] can vary, and a brain MRI is an important tool to accurately diagnose the location and extent of the injury. It offers crucial details regarding the impact of the damage, such as brain swelling or hemorrhage. Doctors can evaluate brain MRI results to identify treatment plans based on the severity of injury, such as cerebral palsy, birth defects, etc.

➤ **Multiple Sclerosis :**

The degenerative disease known as multiple sclerosis (MS) [9] affects the brain and central nervous system, leading to an immune system attack on the tissue surrounding the nerves. To quantify the severity and course of multiple sclerosis, as well as to confirm a diagnosis, doctors frequently use brain MRI scans.

➤ **Aneurysms or Hemorrhages :**

Brain MRI is important for identifying aneurysms [10] and bleeding in the brain. A ruptured aneurysm can lead to serious consequences such as brain damage, stroke, and even death. By performing an MRI of the brain, doctors can detect aneurysms and measure their size and location, allowing timely intervention to prevent rupture.

Moreover, irregular blood flow in the brain can be found with an MRI scan. An abnormal blood flow can result in the brain receiving insufficient oxygen, which may result in a stroke or other brain damage. Doctors can diagnose these issues with a brain MRI and develop a suitable treatment plan to restore blood flow and lower the risk of further complications.

1.2.B) Challenges in Segmenting Brain Structures :

Segmenting brain structures presents several challenges, including the complexity of anatomical variations across individuals, the presence of noise and artifacts in imaging data, and the difficulty in distinguishing between adjacent structures with similar intensity or contrast. These challenges often require sophisticated algorithms and manual interventions to achieve accurate segmentation results.

➤ **Different shapes :**

Brain tumors can develop anywhere in the brain and have a variety of functions. Without prior knowledge, this heterogeneity makes it challenging to develop a predictive model, particularly for tiny tumors.

➤ **Intensity inhomogeneity:**

The difficulty in segmentation arise from the uneven utilization of homogenous tissue and changes in spatial density in each dimension.

➤ **Bias field:**

The bias field [11] is caused by the defects in the acquisition sequences or radiofrequency coil imperfections, which also makes problems when segmenting.

➤ **Imbalance Data:**

It is a main problem in Brain segmentation. It is the inconsistent information on MR images. This uncertainty is due to regional differences between healthy and abnormal brain regions.

➤ **Data scarcity :**

For supervised segmentation techniques, insufficient data is a challenge for analyzing medical images, particularly when the brain is involved. Limited training data often leads to overfitting and have difficulty generalizing to new, unseen data.

1.3) Techniques of Brain MR Image Segmentation :

Brain MR image segmentation employs various techniques, including thresholding [12, 13], region-based methods [14], clustering algorithms [4] like k-means [15] or fuzzy c-means [16], and machine learning approaches [17] such as support vector machines (SVM) [18], k-Nearest Neighbours (k-NN) [19] , Artificial Neural Networks (ANN) [20] , Radial Basis Functions (RBF) [1, 21] , and deep learning techniques [22, 23] have gained prominence in brain MR image segmentation. Each technique has its advantages and limitations, with the choice often dependent on factors like image quality, the complexity of structures, and computational resources available. Integrating multiple methods or developing hybrid approaches can enhance segmentation accuracy and robustness.

1.3.A) Intensity-Based Approaches :

i) Thresholding :

Thresholding [12, 13] is a simple image segmentation approach that uses reference histograms to determine a specific value, called the threshold (τ) to distinguish between different classes. By specifying these thresholds, the segmentation process categorizes the pixels falling from the threshold, resulting in a segmented image.

The advantage of thresholding for image segmentation lies in its simplicity, speed, and computational efficiency, making it suitable for quickly separating objects or regions of interest based on intensity differences in images.

Thresholding is fast and computationally efficient method but sensitive to noise and intensity inhomogeneities. Although it use to separate background from the brain tissue in brain image segmentation.

ii) Region-Based :

Region-based [14] methods help extract connected regions from an image based on predefined criteria such as pixel or voxel matching. This approach usually involves three steps: (a) select initial seed points, (b) identify points in objects or regions, and (c) select content-related points that start with similar results. In recent studies, regional methods have been widely used in the classification of brain tissue and show their effectiveness in this regard.

The advantage of using region-based methods for image segmentation lies in their ability to extract connected regions efficiently based on predefined criteria, facilitating the classification of complex structures like brain tissue accurately.

The main disadvantage of the region based method is its sensitivity to the initialization of seed point. By selecting a different seed point, the segmentation result can be completely different.

iii) Clustering :

Clustering methods [4] are unsupervised segmentation techniques that group pixels/voxels with similar intensities in an image without relying on training data. These methods use the available image data to train themselves. segmentation and training happen in parallel by iterating between data clustering and estimating tissue class properties. The popular clustering methods are k-means clustering [15] and fuzzy C-means clustering [16] .

The advantage of using clustering methods for image segmentation lies in their ability to automatically group pixels/voxels with similar intensities, without requiring labeled training data, enabling unsupervised segmentation of images efficiently.

Clustering techniques may struggle with high-dimensional data and require predefined cluster numbers, making them sensitive to initialization and potentially leading to suboptimal results. Additionally, they might struggle with handling overlapping or irregularly shaped clusters, limiting their effectiveness in segmenting complex brain structures accurately.

1.3.B) Machine Learning :

i) Traditional Machine Learning :

Any fundamental algorithmic structure to solve given problem will come under Traditional Machine Learning [17] . These algorithms learn from the data, where choice of algorithm and features (inputs) to be fed into algorithm are made by subject matter experts. Traditional ML models expects all inputs are in the format of structured data like numbers. Traditional ML models can be used to solve classification, segmentation, regression, clustering, dimensionality reduction problems.

Some common types of traditional machine learning techniques used in brain MRI segmentation are: Support Vector Machines (SVM) [18] , k-Nearest Neighbours (k-NN) [19] , Artificial Neural Networks (ANN) [20] , Radial Basis Functions (RBF) [1, 21] ,etc.

➤ Support Vector Machines (SVM) :

Support Vector Machines (SVM) work by finding the optimal hyperplane that best separates data points into different classes, maximizing the margin between them. In image segmentation, SVM can be employed to classify pixels or image regions into different classes based on features extracted from the images.

Advantages of SVM in image segmentation include its ability to handle high-dimensional feature spaces efficiently, robustness against overfitting, and effectiveness in handling non-linear decision boundaries through kernel tricks.

However, SVMs may struggle with large datasets due to their computational complexity, and they require careful selection of hyperparameters. Additionally, SVMs might not perform optimally when dealing with highly imbalanced datasets, where certain classes are underrepresented.

➤ **k-Nearest Neighbours (k-NN) :**

The k-Nearest Neighbours (KNN) algorithm works by assigning a class label to an input sample based on the majority class among its k nearest Neighbours in feature space.

For image segmentation, KNN can be applied by treating each pixel or image patch as a data point with features derived from its intensity values or other characteristics, and then assigning a class label based on the majority class among its nearest Neighbours.

Advantages of KNN in image segmentation include its simplicity and ease of implementation, as well as its ability to handle multi-class classification tasks without assuming any underlying distribution of the data.

However, KNN's performance can be sensitive to the choice of the number of Neighbours (k) and the distance metric used, which may require careful tuning. Additionally, KNN can be computationally expensive, especially with large datasets, as it requires calculating distances between the query point and all training samples. Furthermore, KNN may not perform well in high-dimensional feature spaces or when dealing with noisy or irrelevant features.

➤ **Artificial Neural Networks (ANN) :**

Artificial Neural Networks (ANN) consist of interconnected nodes arranged in layers, including an input layer, one or more hidden layers, and an output layer. Each node applies a weighted sum of inputs followed by a non-linear activation function. During training, the network adjusts the weights to minimize the difference between predicted and actual outputs using techniques like backpropagation.

In image segmentation, Artificial Neural Networks (ANNs) work by processing input image data through interconnected layers of nodes, extracting features relevant to segmentation tasks. These features are then used to predict class labels or segmentation masks for each pixel or region in the image. Through training on labeled data, ANNs learn to map input images to corresponding segmentation outputs, optimizing their parameters to minimize prediction errors and accurately delineate object boundaries.

ANNs in image segmentation include their ability to capture complex relationships in data, adaptability to various image characteristics, and potential for high accuracy. Another advantage of Artificial Neural Networks (ANNs) in image segmentation is their capacity to learn from large datasets efficiently, enabling robust performance across diverse imaging modalities and complex segmentation tasks.

However, ANNs often require large amounts of labeled training data and significant computational resources for training, and they may be prone to overfitting if not properly regularized. Additionally, the interpretability of ANN-based segmentation models may be limited compared to simpler techniques like thresholding or clustering.

➤ Radial Basis Functions (RBF) :

Radial Basis Function Networks (RBF) are a type of artificial neural network that operates by mapping input data into a high-dimensional feature space using radial basis functions. The network consists of three layers: an input layer, a hidden layer with radial basis functions, and an output layer. During training, the centers and widths of the radial basis functions are adjusted to minimize the difference between predicted and actual outputs.

For image segmentation, RBF networks can be employed by treating pixel intensities or image features as input data and training the network to assign class labels to different regions of the image. RBF networks excel in capturing complex non-linear relationships in the data, making them well-suited for tasks like segmenting structures with irregular shapes or intensity distributions.

One advantage of RBF networks in image segmentation is their ability to approximate complex non-linear decision boundaries, allowing for accurate segmentation of intricate structures in images. Additionally, RBF networks are capable of handling high-dimensional feature spaces efficiently, making them suitable for segmentation tasks involving large and complex datasets. Another advantage of RBF networks is their inherent ability to generalize well to unseen data, thanks to their capability to model complex relationships between features and class labels. This enhances their robustness and ensures reliable performance even in scenarios with limited training data or noisy input images.

However, RBF networks may require careful tuning of hyperparameters, such as the number and distribution of radial basis functions, to achieve optimal segmentation performance. Moreover, training RBF networks typically requires a significant amount of computational resources, especially for large-scale image datasets, which can pose challenges in terms of time and computational cost. Despite these challenges, RBF networks remain a powerful tool for image segmentation, particularly in scenarios where capturing complex relationships in the data is crucial for achieving accurate segmentation results.

ii) Deep Learning :

Deep learning [22, 23] encompasses a range of neural network architectures, notably Convolutional Neural Networks (CNNs) [24], which excel in learning hierarchical features from data. For image segmentation, deep learning works by training CNNs to predict segmentation masks directly from input images, leveraging the network's ability to capture complex spatial relationships and features.

Advantages of deep learning for image segmentation include its capability to automatically learn intricate patterns and features from data, adaptability to various imaging modalities and structures, and state-of-the-art performance in many segmentation tasks.

However, deep learning models often require large amounts of labeled data for training, extensive computational resources, and time for training. Overfitting can also be a concern, especially with limited training data, and deep learning models may lack interpretability compared to traditional techniques. Additionally, deploying and fine-tuning deep learning models can be challenging, requiring expertise in both machine learning and domain-specific knowledge.

1.3.C) Hybrid Segmentation Approaches :

Brain MRI segmentation problems need to be continuously investigated and new methods introduced. Selecting the most appropriate technique for a given application can be difficult and often requires a combination of techniques to achieve accurate segmentation. Therefore, the hybrid or combined segmentation method [4] has gained great popularity in many brain MRIs. There are three sub category of Hybrid Segmentation Approaches :- a) contour-based and machine learning, [25] (ii) metaheuristic, and machine learning [26] and (iii) deep learning and machine learning [27].

Several examples of hybrid brain MRI segmentation methods have been developed. Kapoor et al. [28] Segmentation of multiple brain tissues in adults in 2D MRI using a combination of Contour-Based and Machine Learning. Masutani et al. [29] Combining model-based region growth with local quality information for accurate segmentation of cerebral vessels. An unsupervised brain MRI segmentation is developed by Xue et al. [30] by combining minimum error global thresholding and a spatial-feature-based *FCM* clustering to segment 3D MRI in a “slice-by-slice” manner.

The main disadvantage of the hybrid (combined) segmentation method is its complexity, usually compared to the individual method. This challenge requires more time and more parameters to be adjusted for specific applications. Therefore, the design of the hybrid segmentation method must be carefully considered to ensure efficiency and high-quality segmentation results.

2) Proposed Method :

In this project, a Radial Basis Function Neural Network (RBFNN) [1] is employed specifically for the segmentation of brain MR images into cerebrospinal fluid (CSF), grey matter, and white matter regions. This methodology harnesses the unique capabilities of RBFNN to accurately delineate these crucial anatomical structures, thereby facilitating more precise medical image analysis and aiding in the diagnosis and treatment planning of neurological conditions. By leveraging the RBFNN's capacity to capture intricate relationships within the image data, this research contributes to advancements in brain MR image segmentation techniques, enhancing our understanding of brain anatomy and pathology.

2.1) Description of RBFNN:

A radial basis function (RBF) neural network is a type of artificial neural network that uses radial basis functions as activation functions. Three layers usually make up this structure: an input layer, a hidden layer, and an output layer. The input is subjected to a radial basis function—typically a Gaussian function—by the hidden layer. The final output is then produced by the output layer by linearly combining these outputs. Due to their great adaptability, RBF neural networks are commonly used in many machine learning applications, function approximation, and pattern categorization tasks. They are particularly well-known for their proficiency with non-linear problems.

2.1.A) RBF Neural Network Architecture :

The typical architecture of a radial basis functions neural network consists of an input layer, hidden layer, and summation layer.

- **Input Layer :**

Each predictor variable has a single neuron in the input layer. Every neuron in the buried layer receives the value from the input neurons. For categorical values, N-1 neurons are employed, where N is the number of categories. By deducting the median and dividing by the interquartile range, the range of values is normalized. Pass the value to each neuron in the hidden layer. N-1 neurons are used for categorical values, where N denotes the number of categories. The range of values is standardized by subtracting the median and dividing by the interquartile range.

- **Hidden Layer :**

The hidden layer contains a variable number of neurons (the ideal number determined by the training process). A radial basis function centered on a point is present in every neuron. The number of predictor variables and the number of dimensions match. For every dimension, the RBF function's radius or spread can change.

A hidden neuron determines the Euclidean distance between the test case and the neuron's center point when it receives an x vector of input values from the input layer. Next, it uses the spread values to apply the kernel function. The summation layer receives the output value.

- **Output Layer or Summation Layer :**

The value derived from the hidden layer is sent to the summation after being multiplied by a neuron-related weight. In this case, the network's output is shown as the total of the weighted values. Each target category in a classification issue has a single output, the value of which is the likelihood that the instance under consideration falls into that category.

- **The Input Vector :**

It is the n -dimensional vector that we're attempting to classify. The whole input vector is presented to each of the RBF neurons.

- **The RBF Neurons**

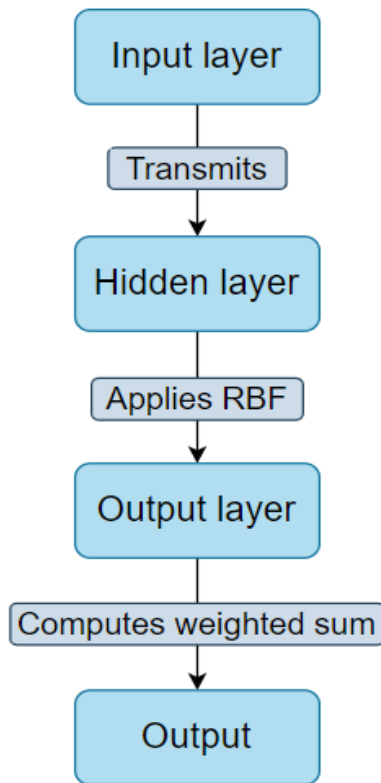
A prototype vector, often referred to as the neuron's center, is stored by each RBF neuron from among the training set's vectors. When an RBF neuron compares an input vector to its prototype, it produces a similarity score that ranges from 0 to 1. The output of the neuron is 1 if an input is the same as the prototype. The output decreases exponentially to zero as the disparity between the input and prototype increases. The RBF neuron's response takes the form of a bell curve. Another name for the response value is the activation value.

- **The Output Nodes**

The output of the network consists of a set of nodes for every category that has to be classified. For each output node, a score is calculated for the relevant category. When making a categorization choice, we typically allocate the input to the category that has the greatest score.

A weighted sum of the activation levels from each RBF neuron is used to compute the score. It often assigns a negative weight to other RBF neurons and a positive weight to those that fall into its group. Every output node possesses a unique set of weights.

Here's the basic flow diagram of the RBF neural network:



2.1.B) Mathematical background :

The output y of an RBF network is a linear combination of radial basis functions. It is given by:

$$y(x) = \sum_{i=1}^N w_i \phi(\|x - c_i\|)$$

where:

- \mathbf{x} is the input vector
- \mathbf{N} is the number of neurons in the hidden layer
- $\mathbf{w_i}$ are the weights of the connections from the hidden layer to the output layer
- $\mathbf{c_i}$ are the centers of the radial basis functions

- $\|x - ci\|$ is the Euclidean distance between the input vector and the center of the radial basis function
- ϕ is the radial basis function, usually chosen to be a Gaussian function:

$$\phi(r) = e^{-\beta r^2}$$

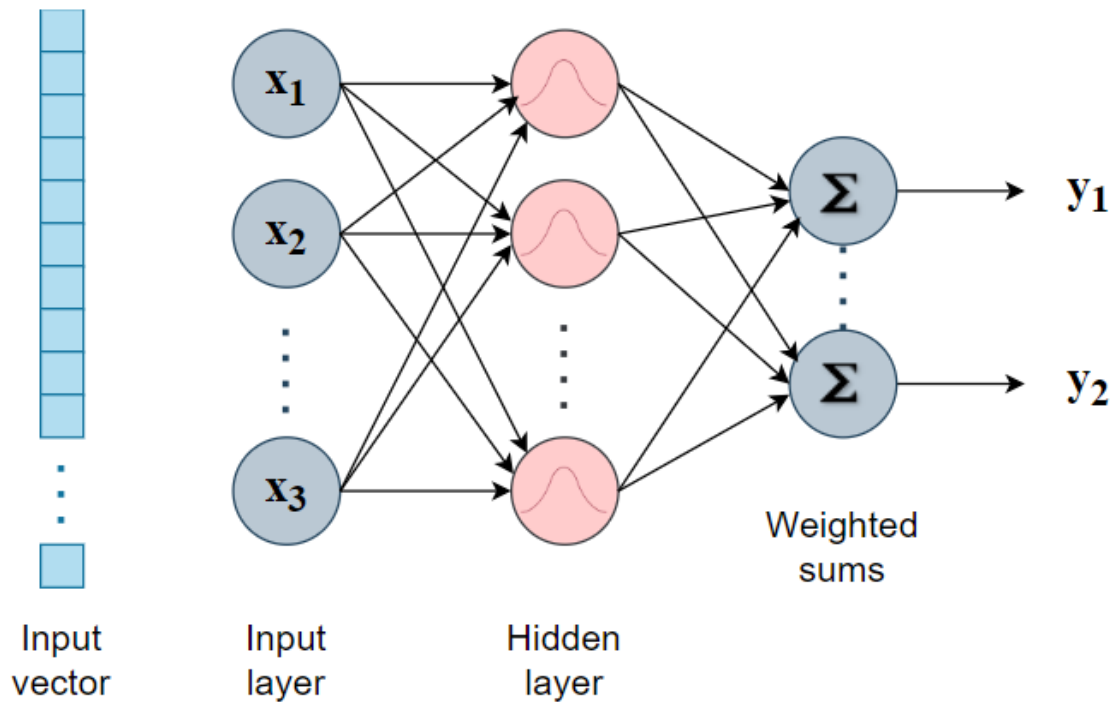
2.1.C) How RBF works? :

Radial basis function networks (RBFNs) work by comparing the input to known examples from the training data to classify it.

Here's a simplified explanation:

- RBFNs start with an input vector. This vector is fed into the input layer of the network.
- The network also has a hidden layer, which comprises radial basis function (RBF) neurons.
- Each of these RBF neurons has a center, and they measure how close the input is to their center. They do this using a special function called a Gaussian transfer function. The output of this function is higher when the input is close to the neuron's center and lower when the input is far away.
- The outputs from the hidden layer are then combined in the output layer. Each node in the output layer corresponds to a different category or class of data. The network determines the input's class by calculating a weighted sum of the outputs from the hidden layer.
- The final output of the network is a combination of these weighted sums, which is used to classify the input.

2.1.D) Visual Representation :



2.2) Training :

The training process includes selecting these parameters:

- The prototype (μ)
- Beta coefficient for every RBF neuron, and
- The matrix of output weights between the neurons and output nodes.

I. Selecting the Prototypes :

There doesn't appear to be a single "wrong" way to choose the RBF neuron prototypes. Actually, there are two ways to go about this: either build an RBF neuron for each training example, or choose k prototypes at random from the training set. The loose constraints stem from the fact that an RBF network can establish any arbitrarily complicated decision boundary provided an adequate number of RBF neurons. Put otherwise, we can always use additional RBF neurons to increase its accuracy.

Ultimately, the matter boils down to efficiency: utilizing fewer RBF neurons to attain high accuracy is preferable than employing more RBF neurons, which in turn require more computation time.

One of the approaches for making an intelligent selection of prototypes is to perform k-Means clustering [15] on the training set and to use the cluster centers as the prototypes. When applying k-means, we first have to separate the training examples by category– we don't want the clusters to include data points from multiple classes.

It is necessary to choose the number of clusters for each class "heuristically." Greater prototype numbers allow for a more intricate decision boundary, but they also increase the number of computations required to assess the network.

II. Selecting Beta values :

Setting sigma to the average distance between each point in the cluster and the cluster center is an easy way to specify the beta coefficients if you use k-means clustering to choose your prototypes.

$$\sigma = \frac{1}{m} \sum_{i=1}^m \|x_i - \mu\|$$

Here, μ is the cluster centroid,

m is the number of training samples belonging to this cluster, and

x_i is the i th training sample in the cluster.

Once we have the sigma value for the cluster, we compute beta as:

$$\beta = \frac{1}{2\sigma^2}$$

III. Output Weights :

The output weights are the final set of parameters to be trained. These can be trained using gradient descent (also known as least mean squares).

First, find the RBF neurons' activation levels for each data point in your training set. Gradient descent uses these activation values as training inputs.

We always start the vector of activation values with a fixed value of "1" since the linear equation requires a bias term.

It is necessary to conduct gradient descent independently for every output node, or every class in your data set.

2.3) For Image Segmentation :