

**Answer all questions. Write legibly. Show your work wherever necessary for full credit.**

- 1.** For a population of five individuals, television ownership is as follows:

Name	Number of television sets owned
Allen	2
Betty	1
Chuck	3
Dave	4
Eddie	2

- a. Calculate the population mean and the population standard deviation.
  - b. For the sample size  $n = 2$ , create the sampling distribution of the mean.
  - c. Calculate the expected mean and the standard error for the sampling distribution.
- 2.** A civic organization includes 200 members, who have an average income of \$58,000, with a standard deviation of \$10,000. A simple random sample of  $n = 30$  members is selected to participate in the annual fund-raising drive.

What is the probability that the average income of the fund-raising group will be

- a. at least \$60,000?
  - b. between \$56,000 and \$60,000?
  - c. no more than \$58,000?
- 3.** For each of the following confidence levels (CL), determine  $\alpha$  (total tail probability), the t-values at the given degrees of freedom, and the corresponding z-value:

CL	$\alpha$	$t_{df=1}$	$t_{df=50}$	$t_{df=100}$	z-value
0.80					
0.90					
0.95					
0.98					
0.99					

4. For a random variable that is normally distributed, with  $\mu = 200$  and  $\sigma = 20$ , determine the probability that a simple random sample of 4 items will have a mean that is:
- a. greater than 210      b. between 190 and 230      c. less than 225.
5. According to the US Census Bureau, 85% of adult residents of Oklahoma have completed high school.

What is the probability that no more than 80% of persons in a simple random sample of 200 adult residents of Oklahoma have finished high school?

6. Of the 629 passenger vehicles imported by the small country of Malta in a recent year, 117 were Volvos. A simple random sample of 300 imported passenger vehicles is taken.

What is the probability that at least 15% of the vehicles in this sample will be Volvos?

7. A simple random sample of 30 has been collected from a population for which it is known that  $\sigma = 10.0$ . The sample mean has been calculated as 240.0.

Construct and interpret the 90% and 95% confidence intervals for the population mean. In each case, note the size of the sampling error.

8. From past experience, the population standard deviation of rod diameters produced by a machine has been found to be  $\sigma = 0.053$  inches. For a simple random sample of  $n=30$  rods, the average diameter is found to be  $\bar{x} = 1.400$  inches.

What is the 95% confidence interval for the population mean and the accuracy?

9. A simple random sample of  $n=90$  manufacturing employees has been selected from those working throughout a state. The average number of overtime hours worked last week was  $\bar{x} = 8.46$  hours with a sample standard deviation of  $s = 3.61$  hours.

What is the 98% confidence interval for the population mean?

- 10.** A simple random sample of 33 owners of a certain model of automobile were asked how many defects had to be corrected within the first six months of ownership. The sample showed an average of 3.7 defects, with a sample standard deviation of 1.8 defects.
- a. Construct a 95% confidence interval for  $\mu$  = the average number of defects.  
What is the size of the accuracy?
- b. Assume that the sample size increases to 120, and the sample average and standard deviation remain the same. Construct a 95% confidence interval for  $\mu$ .  
What is the size of the accuracy?
- 11.** In a large industry where well over 100,000 employees are represented by a single union, a simple random sample of 100 union members finds that 57% of those in the sample intend to vote for the new labor contract. What is the 99% confidence interval for the population proportion of employees who intend to vote for the labor contract?
- 12.** A marketing manager wants to estimate the population mean usage of home heating oil within 50 gallons of the true value. On the basis of a study taken in the previous year, he believes that the standard deviation is 325 gallons. What is the sample size needed to estimate the population mean at the 95% confidence level?
- 13.** A tourist agency would like to determine the proportion of U.S. adults who have ever vacationed in Mexico. What sample size is necessary to have 95% confidence that the sample proportion will be within 0.03 (3 percentage points) of the actual population proportion?