# **Problem 1: Array Operations**

```
public class ArrayOperations {
  public static void main(String[] args) {
    int[] arr = {10, 0, 5, 20, 0, 8, 15};
    System.out.println("Second largest element: " + findSecondLargest(arr));
    moveZerosToEnd(arr);
    System.out.print("Array after moving zeros: ");
    for (int num : arr) System.out.print(num + " ");
  }
  static int findSecondLargest(int[] arr) {
    int largest = Integer.MIN_VALUE, secondLargest = Integer.MIN_VALUE;
    for (int num: arr) {
      if (num > largest) {
         secondLargest = largest;
         largest = num;
      } else if (num > secondLargest && num != largest) {
         secondLargest = num;
      }
    }
    return secondLargest;
  }
  static void moveZerosToEnd(int[] arr) {
    int index = 0;
    for (int num : arr) {
      if (num != 0) arr[index++] = num;
    }
```

```
while (index < arr.length) arr[index++] = 0;
  }
}
Problem 2: String Operations
import java.util.Arrays;
public class StringOperations {
  public static void main(String[] args) {
    String str1 = "listen", str2 = "silent";
    String sentence = "Practice makes a man perfect";
    System.out.println("Are '" + str1 + "' and '" + str2 + "' anagrams? " + areAnagrams(str1,
str2));
    System.out.println("Longest word: " + findLongestWord(sentence));
    int[] counts = countVowelsAndConsonants(sentence);
    System.out.println("Vowels: " + counts[0] + ", Consonants: " + counts[1]);
  }
  static boolean areAnagrams(String s1, String s2) {
    char[] arr1 = s1.toCharArray(), arr2 = s2.toCharArray();
    Arrays.sort(arr1);
    Arrays.sort(arr2);
    return Arrays.equals(arr1, arr2);
  }
  static String findLongestWord(String sentence) {
    String[] words = sentence.split(" ");
    String longest = "";
```

```
for (String word : words) if (word.length() > longest.length()) longest = word;
    return longest;
  }
  static int[] countVowelsAndConsonants(String sentence) {
    int vowels = 0, consonants = 0;
    for (char c : sentence.toLowerCase().toCharArray()) {
      if ("aeiou".indexOf(c) != -1) vowels++;
      else if (Character.isLetter(c)) consonants++;
    }
    return new int[]{vowels, consonants};
  }
}
Problem 3: Sorted Array Operations
import java.util.Arrays;
public class SortedArrayOperations {
  public static void main(String[] args) {
    int[] arr = {1, 3, 3, 3, 5, 6, 8}, peakArr = {1, 2, 18, 4, 5, 0};
    int key = 3;
    System.out.println("Key found at index: " + binarySearch(arr, key));
    System.out.println("First occurrence: " + findFirstOccurrence(arr, key));
    System.out.println("Last occurrence: " + findLastOccurrence(arr, key));
    System.out.println("Total count of key: " + countOccurrences(arr, key));
    System.out.println("Peak element: " + findPeakElement(peakArr));
  }
```

```
static int binarySearch(int[] arr, int key) {
  int low = 0, high = arr.length - 1;
  while (low <= high) {
    int mid = low + (high - low) / 2;
    if (arr[mid] == key) return mid;
    if (arr[mid] < key) low = mid + 1;
    else high = mid - 1;
  }
  return -1;
}
static int findFirstOccurrence(int[] arr, int key) {
  int low = 0, high = arr.length - 1, result = -1;
  while (low <= high) {
    int mid = low + (high - low) / 2;
    if (arr[mid] == key) {
       result = mid;
       high = mid - 1;
    } else if (arr[mid] < key) low = mid + 1;
     else high = mid - 1;
  return result;
}
static int findLastOccurrence(int[] arr, int key) {
  int low = 0, high = arr.length - 1, result = -1;
  while (low <= high) {
    int mid = low + (high - low) / 2;
```

```
if (arr[mid] == key) {
         result = mid;
         low = mid + 1;
       } else if (arr[mid] < key) low = mid + 1;
       else high = mid - 1;
    }
    return result;
  }
  static int countOccurrences(int[] arr, int key) {
    return findLastOccurrence(arr, key) - findFirstOccurrence(arr, key) + 1;
  }
  static int findPeakElement(int[] arr) {
    for (int i = 1; i < arr.length - 1; i++)
       if (arr[i] > arr[i - 1] && arr[i] > arr[i + 1]) return arr[i];
    return arr[0] > arr[arr.length - 1] ? arr[0] : arr[arr.length - 1];
  }
}
Problem 4: Recursive Operations
public class RecursiveOperations {
  public static void main(String[] args) {
    int num = 7, fibIndex = 6, a = 2, b = 5;
    String str = "racecar";
    int numForSum = 1234;
    System.out.println("Is prime: " + isPrime(num, 2));
```

```
System.out.println("Is "" + str + "" a palindrome? " + isPalindrome(str, 0, str.length() - 1));
  System.out.println("Sum of digits of " + numForSum + ": " + sumOfDigits(numForSum));
  System.out.println("Fibonacci(" + fibIndex + "): " + fibonacci(fibIndex));
  System.out.println(a + "^" + b + " = " + power(a, b));
}
static boolean isPrime(int n, int i) {
  if (n \le 2) return n == 2;
  if (n % i == 0) return false;
  if (i * i > n) return true;
  return isPrime(n, i + 1);
}
static boolean isPalindrome(String str, int left, int right) {
  if (left >= right) return true;
  if (str.charAt(left) != str.charAt(right)) return false;
  return isPalindrome(str, left + 1, right - 1);
}
static int sumOfDigits(int n) {
  if (n == 0) return 0;
  return n % 10 + sumOfDigits(n / 10);
}
static int fibonacci(int n) {
  if (n <= 1) return n;
  return fibonacci(n - 1) + fibonacci(n - 2);
}
```

```
static int power(int a, int b) {
    if (b == 0) return 1;
    return a * power(a, b - 1);
}

Dry Run and Analysis

void printTriangle(int n) {
    for (int i = 0; i < n; i++)
        for (int j = 0; j <= i; j++)
        System.out.print("*");
}</pre>
```

# **Dry Run for n=4n = 4n=4:**

Iterations:

```
    i = 0 → 1 print (*)
    i = 1 → 2 prints (**)
    i = 2 → 3 prints (***)
    i = 3 → 4 prints (****)
```

• Total: 1+2+3+4=101 + 2 + 3 + 4 = 101+2+3+4=10.

# **Time Complexity:**

- Outer loop runs nnn times.
- Inner loop runs i+1i + 1i+1 times for each iii.
- Total: 1+2+3+...+n=n(n+1)21+2+3+...+n=\frac{n(n+1)}{2}1+2+3+...+n=2n(n+1).
- Time Complexity: O(n2)O(n^2)O(n2).

# **Question 2: Pattern Printing**

java

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```
void printPattern(int n) {
  for (int i = 1; i <= n; i *= 2)
    for (int j = 0; j < n; j++)
        System.out.println(i + "," + j);
}</pre>
```

#### **Dry Run for n=8n = 8n=8:**

- Outer loop (i): 1,2,4,81, 2, 4, 81,2,4,8  $\rightarrow$  runs log  $\frac{1}{2}$ (n)\log 2(n)\log 2(n)\log 2(n) times.
- Inner loop (j): runs nnn times for each iii.

#### **Total Iterations:**

•  $\log_{10}(n) \times n = 4 \times 8 = 32 \setminus \log_{10}(n) \times n = 4 \times 8 = 32 \log_{10}(n) \times n = 4 \times 8 \log_{10}(n) \times n = 4 \log_{10}(n) \times n =$ 

# **Time Complexity:**

- Outer loop: O(log!@n)O(\log n)O(logn).
- **Inner loop:** O(n)O(n)O(n).
- Combined: O(nlog n)O(n \log n)O(nlogn).

#### **Question 3: Recursive Half**

```
java
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void recHalf(int n) {
  if (n <= 0) return;
  System.out.print(n + " ");
  recHalf(n / 2);
}</pre>
```

# **Dry Run for n=20n = 20n=20:**

- $n=20\rightarrow10\rightarrow5\rightarrow2\rightarrow1\rightarrow0$   $n=20\rightarrow10\rightarrow5\rightarrow2\rightarrow1\rightarrow0$   $n=20\rightarrow10\rightarrow5\rightarrow2\rightarrow1\rightarrow0$ .
- Recursive calls: 5.
- Printed values: 20 10 5 2 1.

#### Time Complexity:

• Number of calls proportional to log 2(n)\log 2(n)\log 2(n)\log 2(n).

• Time Complexity: O(log@n)O(\log n)O(logn).

#### vQuestion 4: Exponential Recursion

```
java
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void fun(int n) {
  if (n == 0) return;
  fun(n - 1);
  fun(n - 1);
}
```

# **Dry Run for n=3n = 3n=3:**

- Calls Breakdown:
  - o fun(3) $\rightarrow$ fun(2),fun(2)fun(3)  $\rightarrow$  fun(2), fun(2)fun(3) $\rightarrow$ fun(2),fun(2).
  - o fun(2)→fun(1),fun(1)fun(2) → fun(1), fun(1)fun(2)→fun(1),fun(1).
  - o fun(1)→fun(0),fun(0)fun(1) → fun(0), fun(0)fun(1)→fun(0),fun(0).
- Total calls:  $2n-1=23-1=72^n 1 = 2^3 1 = 72n-1=23-1=7$ .

# **Time Complexity:**

•  $T(n)=2T(n-1)+1T(n)=2T(n-1)+1T(n)=2T(n-1)+1 \rightarrow O(2n)O(2^n)O(2n)$ .

# **Question 5: Triple Nested Loops**

#### **Dry Run for n=3n = 3n=3:**

• Total iterations: n3=33=27n^3 = 3^3 = 27n3=33=27.

# **Time Complexity:**

- Each loop runs nnn times.
- Combined: O(n3)O(n^3)O(n3).