# Semi-Supervised Dependency Parsing with Variational Autoencoder

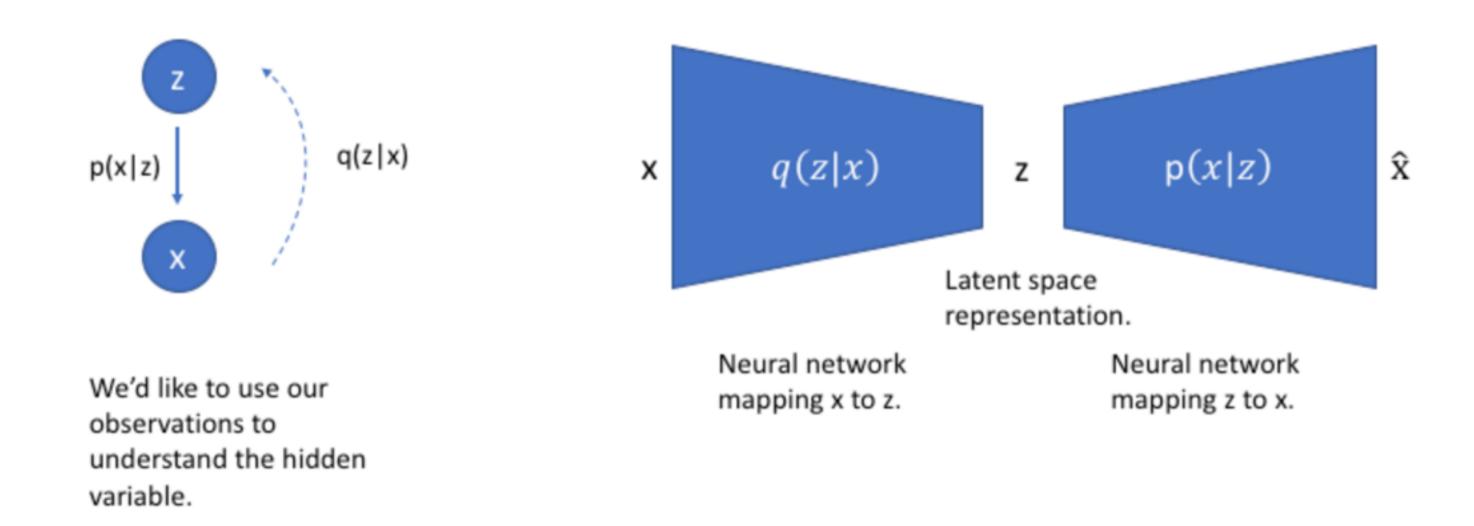
Wang Ge 2019/3/20

#### Why is Semi-Supervised Learning Necessary

- Learning a reliable dependency parser requires a large amount of labelled data, e.g. Penn Treebank (39000+ sentence for training).
- Labelling data with dependency parse trees is a challenging and laborious work. For many languages, enough labelled data are not available.
- Unsupervised methods require POS tag information, lacking robustness over different annotation criteria such as WSJ and UD

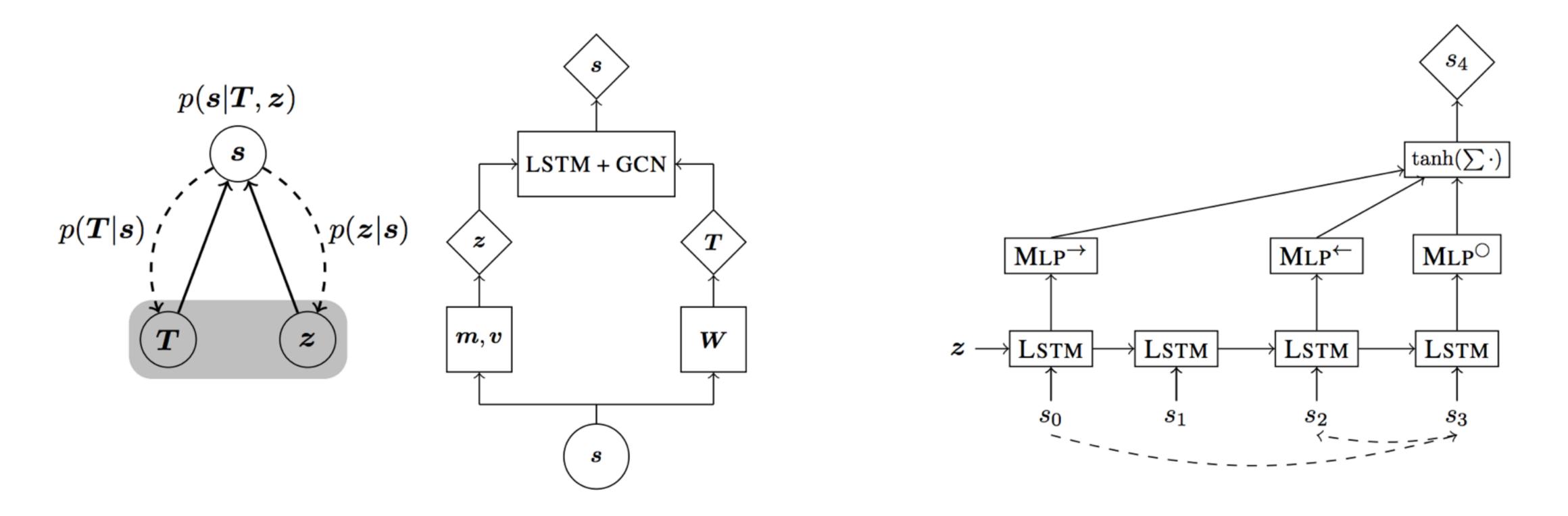
### Variational Autoencoder

An elegant generative model with latent variables



 Easy to be applied to semi-supervised learning, not suitable for structured latent variable like parse tree

# Recent Work Combining Semi-Supervised Parsing with VAE



Graphical Model and Computational Graph

Decoder Implementation

### Model Detail

Generative Story

$$T \sim p(T|n)$$

$$\boldsymbol{z} \sim p(\boldsymbol{z}|n)$$

$$\boldsymbol{s} \sim p(\boldsymbol{s}|\boldsymbol{T},\boldsymbol{z},n)$$

Objective Function

$$\log p_{\theta}(\boldsymbol{s}) = \mathbb{E}_{q_{\phi}(\boldsymbol{T},\boldsymbol{z}|\boldsymbol{s})}[\log p_{\theta}(\boldsymbol{s}|\boldsymbol{T},\boldsymbol{z})] - \text{KL}[q_{\phi}(\boldsymbol{T},\boldsymbol{z}|\boldsymbol{s})|p(\boldsymbol{T},\boldsymbol{z})] + \text{KL}[q_{\phi}(\boldsymbol{T},\boldsymbol{z}|\boldsymbol{s})||p_{\theta}(\boldsymbol{T},\boldsymbol{z}|\boldsymbol{s})]$$

$$\log p_{\theta}(\boldsymbol{s}) \geq \mathbb{E}_{q_{\phi}(\boldsymbol{T},\boldsymbol{z}|\boldsymbol{s})}[\log p_{\theta}(\boldsymbol{s}|\boldsymbol{T},\boldsymbol{z})] - \text{KL}[q_{\phi}(\boldsymbol{T},\boldsymbol{z}|\boldsymbol{s})|p(\boldsymbol{T},\boldsymbol{z})] = \tilde{\mathcal{E}}_{\theta,\phi}(\boldsymbol{s})$$

$$\bar{\mathcal{E}}_{\theta,\phi}(\boldsymbol{s},\boldsymbol{T}) = \mathbb{E}_{q_{\phi}(\boldsymbol{z}|\boldsymbol{s})}[\log p_{\theta}(\boldsymbol{s}|\boldsymbol{T},\boldsymbol{z})] - \mathrm{KL}[q_{\phi}(\boldsymbol{z}|\boldsymbol{s})|p(\boldsymbol{z})]$$

$$\bar{\mathcal{E}}_{\theta,\phi}(\boldsymbol{s},\boldsymbol{T}) = \mathbb{E}_{q_{\phi}(\boldsymbol{z}|\boldsymbol{s})}[\log p_{\theta}(\boldsymbol{s}|\boldsymbol{T},\boldsymbol{z})] - \mathrm{KL}[q_{\phi}(\boldsymbol{z}|\boldsymbol{s})|p(\boldsymbol{z})]$$

### Encoder and Decoder

For the encoder:

$$m{W} = ext{DepWeights}(m{s})$$
  $m{m}, \log m{v}^2 = ext{EmbParams}(m{s})$   $q_{\phi}(m{T}|m{s}) = rac{\exp(\sum_{i,j} W_{i,j} T_{i,j})}{\sum_{m{T}'} \exp(\sum_{i,j} W_{i,j} T'_{i,j})}$   $q_{\phi}(m{z}|m{s}) = \mathcal{N}(m{z}|m{m}, m{v})$ 

For the decoder:

$$oldsymbol{g}^i = anh\left( ext{MLP}^{\bigcirc}(oldsymbol{o}^i) + \sum_{h=0}^{i-1} T_{h,i} imes ext{MLP}^{\curvearrowright}(oldsymbol{o}^h) + \sum_{m=0}^{i-1} T_{i,m} imes ext{MLP}^{\curvearrowleft}(oldsymbol{o}^m) 
ight)$$

### Differentiable Perturb-and-Parse

Sampling dependency tree by perturbing weight matrix

Sampling dependency tree by perturbing weight matrix
 Replace the one-hot-argmax
 peaked-softmax

$$o_i = \mathbb{1}[\forall 1 \le j \le k, j \ne i : v_i > v_j]$$
 with  $o_i = \frac{\exp(1/\tau \ v_i)}{\sum_{1 \le j \le k} \exp(1/\tau \ v_j)}$ 

## Experiment Results

#### (a) Parsing results

	English	French	Swedish
Supervised	88.79 / 84.74	84.09 / 77.58	86.59 / 78.95
VAE w. z	89.39 / 85.44	84.43 / 77.89	86.92 / 80.01
VAE w/o z	89.50 / 85.48	84.69 / 78.49	86.97 / 79.80
Kipperwasser & Goldberg	89.88 / 86.49	84.30 / 77.83	86.93 / 80.12

#### (b) Dependency length analysis

Distance	Supervised Re / Pr	Semi-sup. Re / Pr
(to root)	93.46 / <b>89.30</b>	93.84 / <b>92.41</b>
1	95.61 / 94.07	95.33 / 94.57
2	93.01 / 90.88	92.50 / 92.09
36	85.95 / 88.13	87.31 / 87.93
<b>&gt;7</b>	<b>72.47</b> / 83.26	<b>78.72</b> / 83.11

#### (c) Dependency label analysis

Label	Supervised	Semi-sup.	
Label	Re / Pr	Re / Pr	
mwe	75.58 / 81.25	90.70 / 84.78	
advmod	87.27 / 85.95	87.32 / 87.51	
appos	77.49 / 80.27	81.39 / 81.03	