

Master of Computer Applications  
MCAE 404: Digital Image Processing  
Unique Paper Code: 223402404  
Semester IV  
May-2022

Year of Admission: 2020

Time: Three Hours

Max. Marks: 70

Attempt all questions.  
Parts of a question must be answered together.

1.

- a) Consider the two image subsets  $S_1$  and  $S_2$  shown in the figure below:

	$S_1$				$S_2$				
0	0	0	0	0	0	0	1	1	0
1	0	0	1	0	0	1	0	0	1
1	0	0	1	0	1	1	0	0	0
0	0	1	1	1	0	0	0	0	0
0	0	1	1	1	0	0	1	1	1

Assuming  $V = \{1\}$ , determine whether these two subsets are

- i. 4-adjacent
- ii. 8-adjacent
- iii. m-adjacent

giving proper explanation to you answers.

- b) Differentiate between Histogram equalization and specification in image processing. [6]

2.

- a) Find all the bit planes of the following 4-bit image: [4]

0	1	8	6
2	2	1	1
1	15	14	12
3	6	9	10

- b) Write in brief about RGB, CMY and HSI color models. [3]

- c) How many different shades of gray are there in a color RGB system whose three component images are 8 bit images? [3]

3.

- a) Give a procedure for computing the median of an  $n \times n$  neighborhood. [2]
- b) You are given the following kernel and image.

$$w = \begin{bmatrix} 1 & 2 & 1 \\ 2 & 4 & 2 \\ 1 & 2 & 1 \end{bmatrix} \quad f = \begin{bmatrix} 0 & 0 & 0 & 0 & 0 \\ 0 & 0 & 1 & 0 & 0 \\ 0 & 0 & 1 & 0 & 0 \\ 0 & 0 & 1 & 0 & 0 \\ 0 & 0 & 0 & 0 & 0 \end{bmatrix}$$

Compute the convolution  $w * f$  using the minimum zero padding needed. Show the details of your computations when the kernel is centered on point (2,3) of  $f$ ; and then show the final full convolution result. [4]

- c) Use the sifting property of the impulse to show that convolving a 1-D continuous function,  $f(t)$ , with an impulse located at  $t_0$  shifts the function so that its origin is moved to the location of the impulse (if the impulse is at the origin, the function is not shifted). [4]

4.

a)

Show that

$$\mathcal{F}\{e^{j2\pi t_0 t}\} = \delta(\mu - t_0).$$

where  $t_0$  is a constant.

Or

A continuous Gaussian low pass filter in the continuous frequency domain has the transfer function

$$H(\mu, \nu) = A e^{-(\mu^2 + \nu^2)/2\sigma^2}$$

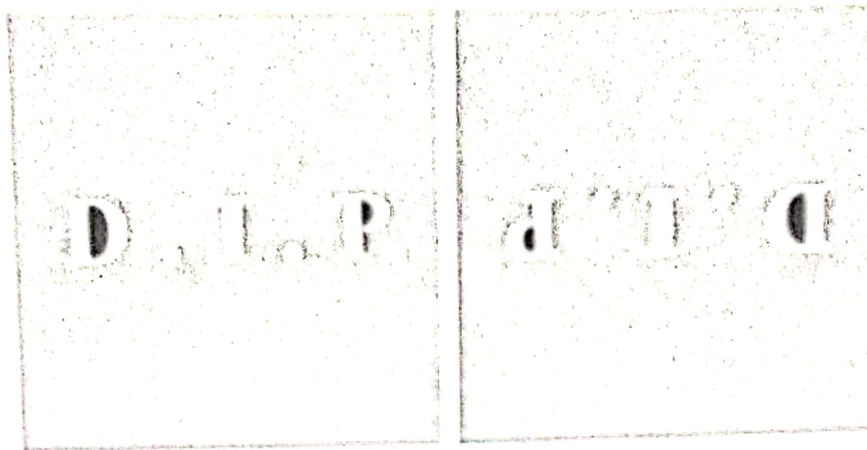
Show that the corresponding filter kernel in the continuous spatial domain is

$$h(t, z) = A 2\pi\sigma^2 e^{-2\pi^2\sigma^2(t^2 + z^2)}$$

[6]

b)

Consider the images shown. The image on the right was obtained by: (i) multiplying the image on the left by  $(-1)^{x+y}$ ; (ii) computing the DFT; (iii) taking the complex conjugate of the transform; (iv) computing the inverse DFT; and (v) multiplying the real part of the result by  $(-1)^{x+y}$ . Explain (mathematically) why the image on the right appears as it does. [4]



- 5.
- Use the LZW coding algorithm to encode the 7-bit ASCII string "aaaaaaaaaa" (Assume that the first 256 codes in the starting dictionary are the ASCII codes and ASCII code of "a" is 97). [4]
  - A  $1024 \times 1024$  8-bit image with 5.3 bits/pixel entropy (computed from its histogram) is to be Huffman coded. [6]
    - What is the maximum compression that can be expected?
    - Is it possible to obtain the maximum compression?
    - If a greater level of lossless compression is required, what else can be done?
- 6.
- Explain what would happen in image erosion and dilation if the structuring element is a single point, valued 1. Give reason(s) for your answer. [4]
  - How an image is compressed using JPEG image compression standard? Describe the process with the help of an example. [6]
- 7.
- A binary image contains straight lines oriented horizontally, vertically, at  $45^\circ$ , and at  $-45^\circ$ . Give a set of  $3 \times 3$  kernels that can be used to detect one-pixel breaks in these lines. Assume that the intensities of the lines and background are 1 and 0, respectively. [4]
  - The arithmetic decoding process is the reverse of the encoding procedure. Decode the message 0.23355 given the coding model. [6]

Symbol	Probability
A	0.2
E	0.3
I	0.1
O	0.2
U	0.1
!	0.1