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A Complete Guide to Stepwise Regression in R

Stepwise regression is a procedure we can use to build a regression model from a set of predictor variables by entering and removing predictors in a stepwise manner into the model until there is no statistically valid reason to enter or remove any more.

The goal of stepwise regression is to build a regression model that includes all of the predictor variables that are statistically significantly related to the response variable.

This tutorial explains how to perform the following stepwise regression procedures in R:

- Forward Stepwise Selection
- Backward Stepwise Selection
- Both-Direction Stepwise Selection

For each example we'll use the built-in **mtcars** dataset:

```
#view first six rows of mtcars
head(mtcars)
```

```
                  mpg cyl disp  hp drat    wt  qsec vs am gear carb
Mazda RX4         21.0   6  160 110 3.90 2.620 16.46  0  1    4    4
Mazda RX4 Wag     21.0   6  160 110 3.90 2.875 17.02  0  1    4    4
Datsun 710        22.8   4  108  93 3.85 2.320 18.61  1  1    4    1
Hornet 4 Drive    21.4   6  258 110 3.08 3.215 19.44  1  0    3    1
Hornet Sportabout 18.7   8  360 175 3.15 3.440 17.02  0  0    3    2
Valiant           18.1   6  225 105 2.76 3.460 20.22  1  0    3    1
```

We will fit a multiple linear regression model using *mpg* (miles per gallon) as our response variable and all of the other 10 variables in the dataset as potential predictors variables.

For each example will use the built-in step() function from the stats package to perform stepwise selection, which uses the following syntax:

step(intercept-only model, direction, scope)

where:

- **intercept-only model**: the formula for the intercept-only model
- **direction:** the mode of stepwise search, can be either “both”, “backward”, or “forward”
- **scope:** a formula that specifies which predictors we’d like to attempt to enter into the model

Example 1: Forward Stepwise Selection

The following code shows how to perform forward stepwise selection:

```
#define intercept-only model
intercept_only <- lm(mpg ~ 1, data=mtcars)

#define model with all predictors
all <- lm(mpg ~ ., data=mtcars)

#perform forward stepwise regression
forward <- step(intercept_only, direction='forward', scope=formula(all), trace=0)

#view results of forward stepwise regression
forward$anova

   Step Df  Deviance Resid. Df Resid. Dev       AIC
1       NA        NA        31  1126.0472 115.94345
2  + wt -1 847.72525        30   278.3219  73.21736
3 + cyl -1  87.14997        29   191.1720  63.19800
4  + hp -1  14.55145        28   176.6205  62.66456

#view final model
forward$coefficients

(Intercept)          wt         cyl          hp
 38.7517874  -3.1669731  -0.9416168  -0.0180381
```

Note: *The argument trace=0 tells R not to display the full results of the stepwise selection. This can take up quite a bit of space if there are a large number of predictor variables.*

Here is how to interpret the results:

- First, we fit the intercept-only model. This model had an AIC of **115.94345**.
- Next, we fit every possible one-predictor model. The model that produced the lowest AIC and also had a statistically significant

reduction in AIC compared to the intercept-only model used the predictor *wt*. This model had an AIC of **73.21736**.

- Next, we fit every possible two-predictor model. The model that produced the lowest AIC and also had a statistically significant reduction in AIC compared to the single-predictor model added the predictor *cyl*. This model had an AIC of **63.19800**.
- Next, we fit every possible three-predictor model. The model that produced the lowest AIC and also had a statistically significant reduction in AIC compared to the two-predictor model added the predictor *hp*. This model had an AIC of **62.66456**.
- Next, we fit every possible four-predictor model. It turned out that none of these models produced a significant reduction in AIC, thus we stopped the procedure.

The final model turns out to be:

mpg ~ 38.75 – 3.17*wt – 0.94*cyl – 0.02*hyp

Example 2: Backward Stepwise Selection

The following code shows how to perform backward stepwise selection:

```
#define intercept-only model
intercept_only <- lm(mpg ~ 1, data=mtcars)

#define model with all predictors
all <- lm(mpg ~ ., data=mtcars)

#perform backward stepwise regression
backward <- step(all, direction='backward', scope=formula(all), trace=0)
```

```
#view results of backward stepwise regression
backward$anova

    Step Df   Deviance Resid. Df Resid. Dev      AIC
1        NA         NA        21   147.4944 70.89774
2  - cyl  1 0.07987121        22   147.5743 68.91507
3   - vs  1 0.26852280        23   147.8428 66.97324
4 - carb  1 0.68546077        24   148.5283 65.12126
5 - gear  1 1.56497053        25   150.0933 63.45667
6 - drat  1 3.34455117        26   153.4378 62.16190
7 - disp  1 6.62865369        27   160.0665 61.51530
8   - hp  1 9.21946935        28   169.2859 61.30730

#view final model
backward$coefficients

(Intercept)          wt        qsec          am
   9.617781   -3.916504    1.225886    2.935837
```

Here is how to interpret the results:

- First, we fit a model using all *p* predictors. Define this as M_p.
- Next, for k = p, p-1, … 1, we fit all k models that contain all but one of the predictors in M_k, for a total of k-1 predictor variables. Next, pick the best among these k models and call it M_{k-1}.
- Lastly, we pick a single best model from among $M_0 \ldots M_p$ using AIC.

The final model turns out to be:

mpg ~ 9.62 – 3.92*wt + 1.23*qsec + 2.94*am

Example 3: Both-Direction Stepwise Selection

The following code shows how to perform both-direction stepwise selection:

```
#define intercept-only model
intercept_only <- lm(mpg ~ 1, data=mtcars)

#define model with all predictors
all <- lm(mpg ~ ., data=mtcars)

#perform backward stepwise regression
both <- step(intercept_only, direction='both', scope=formula(all), trace=0)

#view results of backward stepwise regression
both$anova

   Step Df  Deviance Resid. Df Resid. Dev       AIC
1       NA        NA        31  1126.0472 115.94345
2  + wt -1 847.72525        30   278.3219  73.21736
3 + cyl -1  87.14997        29   191.1720  63.19800
4  + hp -1  14.55145        28   176.6205  62.66456

#view final model
both$coefficients

(Intercept)          wt         cyl          hp
 38.7517874  -3.1669731  -0.9416168  -0.0180381
```

Here is how to interpret the results:

- First, we fit the intercept-only model.
- Next, we added predictors to the model sequentially just like we did in forward-stepwise selection. However, after adding each predictor we also removed any predictors that no longer provided an improvement in model fit.
- We repeated this process until we reached a final model.

The final model turns out to be:

mpg ~ 9.62 – 3.92*wt + 1.23*qsec + 2.94*am

Note that forward stepwise selection and both-direction stepwise selection produced the same final model while backward stepwise selection produced a different model.

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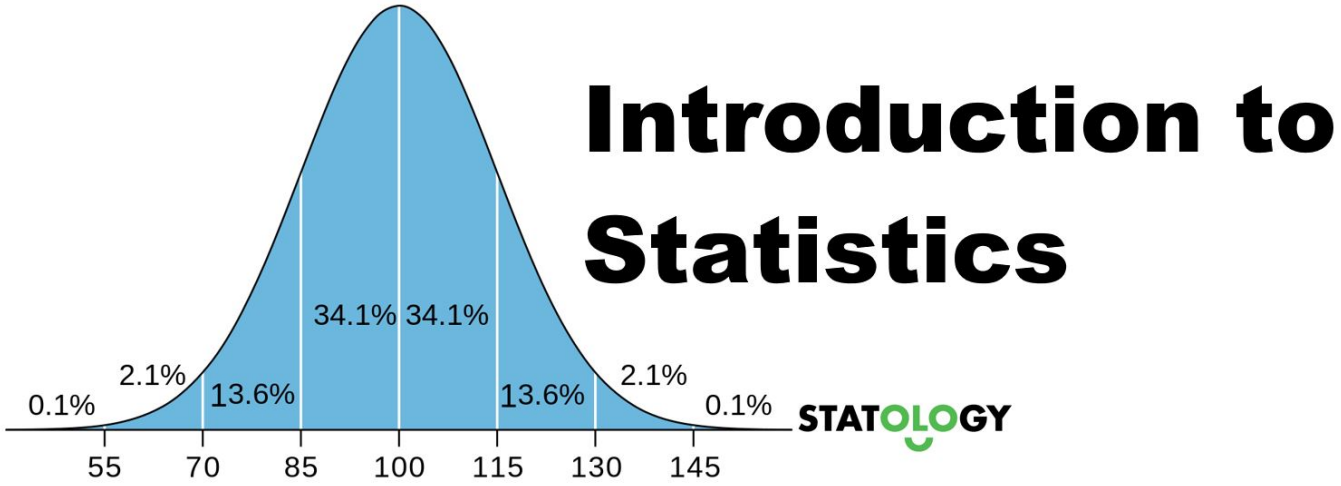

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