

SVD-LLM V2: Optimizing Singular Value Truncation for Large Language Model Compression

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<https://github.com/AIoT-MLSys-Lab/SVD-LLM>

Abstract

Despite significant advancements, the practical deployment of Large Language Models (LLMs) is often hampered by their immense sizes, highlighting the need for effective compression techniques. Singular Value Decomposition (SVD) is a promising LLM compression technique. However, existing SVD-based compression methods fall short in reducing truncation losses, leading to less competitive performance in compressed models. In this work, we introduce SVD-LLM V2, a SVD-based LLM compression method that optimizes singular value truncation in SVD compression with two techniques. First, SVD-LLM V2 proposes to use theoretical truncation loss of weight matrices to assign a unique compression ratio to each weight matrix at different layers to accommodate weight redundancy heterogeneity. Second, SVD-LLM V2 proposes loss-optimized weight truncation to ensure that the truncated singular values result in a lower and more stable truncation loss in practice. We evaluate SVD-LLM V2 on ten datasets and five LLMs at various scales. Our results show SVD-LLM V2 outperforms state-of-the-art SVD-based LLM compression methods. Our code is available at <https://github.com/AIoT-MLSys-Lab/SVD-LLM>.

1 Introduction

Despite the outstanding performance Large Language Models (LLMs) exhibit in various tasks (Zhao et al., 2023; Gozalo-Brizuela and Garrido-Merchán, 2023; Wan et al., 2024b; Shen et al., 2024; Wan et al., 2025), the significant resources consumed limit their widespread accessibility (Wan et al., 2024a; Wang et al., 2024a; Zhou et al., 2024). Model compression (Zhu et al., 2023; Shen et al., 2025) is one effective approach to reduce resource consumption. To avoid resource-intensive retraining, LLM compression is often conducted in a post-training manner. Techniques such as LLM quantization (Yuan et al., 2024; Huang

	Compression Ratio	Truncation Loss	PPL
SVD-LLM	Homogeneous	L = 0.8961	P = 11.8 ✗
SVD-LLM V2	Heterogeneous	L = 0.7351	P = 8.01 ✓

Figure 1: Comparison between SVD-LLM V2 and SVD-LLM. We randomly select a weight matrix from LLaMA-3 8B and compare the normalized truncation loss and perplexity (PPL) under 20% compression ratio.

et al., 2024), unstructured pruning (Frantar and Alistarh, 2023), and structured pruning (Ma et al., 2023; Ashkboos et al., 2024; Zhong et al., 2024) have been proposed.

Low-rank approximation, such as Singular Value Decomposition (SVD) is also an effective technique for compressing LLMs. Compared with quantization and unstructured pruning, SVD compression is more hardware-friendly. Recently, a few SVD-based LLM compression methods have been proposed. At a high level, these methods all focus on reducing the truncation loss during SVD compression to reserve accuracy. Specifically, FWSVD (Hsu et al., 2022) reduces truncation loss by estimating weight importance and preserving more important weights. ASVD (Yuan et al., 2023) injects a scaling matrix to reduce the truncation loss but was not able to achieve theoretical minimum truncation loss at each LLM layer. SVD-LLM (Wang et al., 2024b), on the other hand, fills this gap by proposing a whitening matrix that obtains theoretical minimum truncation loss at each LLM layer, demonstrating superior performance.

Despite such advantage, SVD-LLM has two limitations. First, SVD-LLM applies a homogeneous compression ratio to all the weight matrices. This coarse-grained setup unfortunately overlooks the heterogeneity of weight redundancy across different LLM layers. Second, SVD-LLM utilizes Cholesky decomposition for weight truncation. However, Cholesky decomposition requires the ma-

trix being decomposed to be positive-definite, a condition that is challenging to fulfill in practice. Moreover, Cholesky decomposition introduces numerical instability throughout its iterative process. As a consequence, SVD-LLM could still lead to high truncation loss in practice.

In this paper, we propose SVD-LLM V2, a SVD-based post-training LLM compression method that effectively addresses the two limitations of SVD-LLM. First, to address the heterogeneity of weight redundancy across layers, SVD-LLM V2 uses the theoretical truncation loss of weight matrices at each layer as the guidance to assign a unique compression ratio to each weight matrix based on its type at different layers. Second, SVD-LLM V2 substitutes the Cholesky decomposition with two rounds of SVD for weight truncation, which we prove to achieve the theoretical minimum truncation under the optimized compression ratio. In doing so, SVD-LLM V2 is able to achieve better perplexity with lower truncation loss than SVD-LLM (Figure 1).

We evaluate SVD-LLM V2 on ten datasets covering various language modeling, classification, and generation tasks as well as five LLMs with various backbones and scales. Our results demonstrate the superiority of SVD-LLM V2 with three key findings:

- SVD-LLM V2 consistently outperforms state-of-the-art SVD-based LLM compression methods across all ten datasets and five LLMs.
- SVD-LLM V2 outperforms state-of-the-art structured pruning-based LLM compression methods with up to 28% lower perplexity under 7 GB memory budget. When comparing to state-of-the-art 1-bit quantization-based LLM compression methods, SVD-LLM V2 outperforms PB-LLM and achieves 5% lower perplexity. Moreover, by combining with 2-bit quantization, SVD-LLM V2 is able to outperform 1-bit BiLLM, demonstrating the promise of combining SVD and quantization-based methods for advancing the frontier of post-training LLM compression.
- LLMs compressed by SVD-LLM V2 achieve inference speedup on real hardware. In particular, LLMs compressed by SVD-LLM V2 are able to achieve a throughput speedup of up to 2.71 \times compared to the original LLMs on a single NVIDIA A100 GPU.

2 Related Work

2.1 Large Language Model Compression

Large Language Models (LLMs) typically contain billions of parameters, making traditional model compression techniques impractical due to the need for resource-intensive retraining. To address this, post-training methods that bypass retraining during compression have been developed. These methods generally fall into four categories: unstructured pruning, structured pruning, quantization, and low-rank approximation. Unstructured pruning (Frantar and Alistarh, 2023) sets the individual weight values to zero without changing the overall architecture. However, its irregular sparsity is feasible only for speedups or memory savings on certain hardware. In contrast, structured pruning (Ma et al., 2023; Ashkboos et al., 2024; Zhong et al., 2024) removes entire channels from LLMs, simplifying hardware implementation but often suffering from accuracy degradation. Quantization (Frantar et al., 2022; Zhao et al., 2024) reduces the precision of the weight matrices for compression. However, it often fails to provide the desired inference speedups (Lin et al., 2024b) and offers a limited range of compression options—typically between 2 to 8 bits—which hinders optimal memory utilization. Recent efforts (Yuan et al., 2024; Huang et al., 2024) have explored 1-bit post-training quantization. Nevertheless, these approaches still suffer from accuracy drop, indicating that 1-bit quantization is still challenging in LLM compression.

2.2 SVD for LLM Compression

Singular Value Decomposition (SVD) reduces matrix sizes by truncating the smallest singular values. It then constructs two smaller, lower-rank matrices to approximate the original matrix (Golub et al., 1987). SVD is also feasible for LLM (Hsu et al., 2022; Yuan et al., 2023; Wang et al., 2024b; Lin et al., 2024a). To ensure better compression performance, existing post-training SVD-based LLM compression methods attempt to lower the truncation loss L in the form of Frobenius norm as follows during LLM compression:

$$L = \|WX - W'X\|_F \quad (1)$$

where W is the weight matrix of the original LLM, X is the activation of W , and W' is the compressed low-ranking weight matrix. For example, Yuan et al. (2023) propose ASVD, which scales the weight matrix using a diagonal matrix to normalize

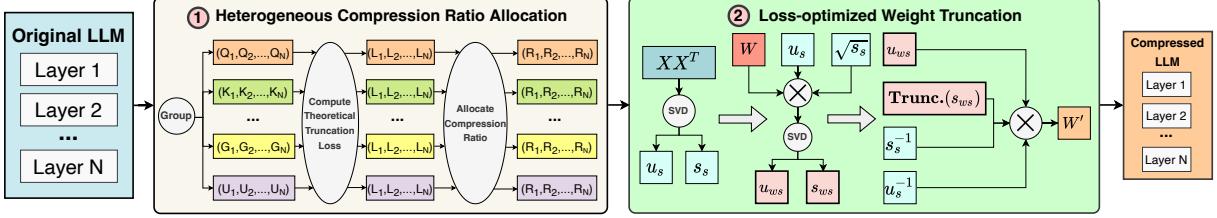


Figure 2: Overview of SVD-LLM V2.

the impact of input channels on the weights to reduce the truncation loss. Wang et al. (2024b) make further advancement by whitening the input matrix to mitigate its impact on SVD truncation with the guarantee of minimal theoretical truncation loss. Despite these progresses, existing methods still suffer from high truncation loss in practice, leading to accuracy degradation.

3 SVD-LLM V2

Figure 2 provides an overview of SVD-LLM V2. Specifically, SVD-LLM V2 groups the weight matrices across all the layers in the original LLM by type, such as query (Q) and key (K) in attention blocks, and Gate (G) and Up (U) in MLP blocks. It then computes the theoretical truncation loss of the weight matrices and assigns a unique compression ratio to each weight matrix within each group based on the computed truncation loss. Lastly, SVD-LLM V2 performs loss-optimized weight truncation to obtain the compressed LLM. Below, we describe the details of the two main components of SVD-LLM V2: (1) heterogeneous compression ratio allocation and (2) loss-optimized weight truncation.

3.1 Heterogeneous Compression Ratio Allocation

Motivation: Since different weight matrices in LLMs often exhibit different levels of redundancy, applying a homogeneous compression ratio to all the weight matrices would incur high truncation loss for those with low redundancy (Zhong et al., 2024; He et al., 2024; Li et al., 2024). To demonstrate this, we use SVD-LLM to measure the truncation loss of the query matrix across different layers in LLaMA-3 8B on WikiText-2 dataset with 50% compression ratio. As shown in Figure 3, the truncation loss varies at different layers. For example, the query matrix in the 27th layer has a much higher truncation loss than that of the first layer, indicating the 27th layer should be compressed under a smaller compression ratio, while a larger com-

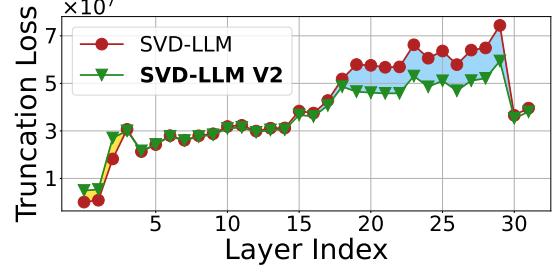


Figure 3: Comparison between SVD-LLM and SVD-LLM V2 on the truncation loss of the query weight matrix across different layers in LLaMA-3 8B on WikiText-2 dataset with 50% compression ratio.

Algorithm 1 Pseudocode of Heterogeneous Compression Ratio Allocation in SVD-LLM V2

Input: M : Original LLM
 x : Input activation
 R : Target compression ratio

Output: R_d : A list of allocated compression ratios

```

1: procedure RATIO_ALLOCATION( $M, S, R$ )
2:    $G \leftarrow \text{Group}(M)$             $\triangleright$  Group the weight by types
3:    $R_d \leftarrow \emptyset$             $\triangleright$  Initialize the compression ratio list
4:   for  $g$  in  $G$  do
5:      $L_G \leftarrow \emptyset$             $\triangleright$  Initialize the loss list in the group
6:     for  $w$  in  $g$  do
7:        $L_{min} \leftarrow \text{Theoretical\_Loss}(w, x, R)$ 
8:        $L_G \leftarrow L_G \cup L_{min}$ 
9:     end for
10:     $L_G \leftarrow 1/\text{Log}(L_G)$             $\triangleright$  Normalize  $L_G$ 
11:     $r \leftarrow \text{Len}(L_G) \times R \times L_{min}/\text{Sum}(L_G)$ 
12:     $R_d \leftarrow R_d \cup r$             $\triangleright$  Append  $r$  to the list  $R_d$ 
13:  end for
14:  return  $R_d$ 
15: end procedure
```

pression ratio should be applied to the first layer. However, existing SVD-based LLM compression methods either overlook this variation or require resource-intensive operations to determine the specific compression ratios, making them impractical for compressing LLMs at larger scales. Therefore, it is essential to develop a more efficient approach to apply different compression ratios at different weight matrices to reduce the truncation loss.

Key Design: The pseudocode of the heterogeneous compression ratio allocation is listed in Algorithm 1. Specifically, given that different types of

weight matrices, such as query (Q) and key (K) in attention blocks, and Gate (G) and Up (U) in MLP blocks play different roles in an LLM. SVD-LLM V2 first groups the weight matrices across all the layers in the original LLM according to their types. Next, SVD-LLM V2 computes the theoretical minimum truncation loss of the weight matrices, i.e., $L_{min} = \|C - C'\|_F$, where C is the original matrix of WX and C' is its compressed version by SVD, respectively. It then inverses and normalizes L_{min} by $1/\log(L_{min})$. Finally, given the target model compression ratio R , the compression ratio of each weight matrix within a group is determined as $\text{Len}(L_G) \times R \times L_{min}/\text{Sum}(L_G)$, where L_G denotes the list of theoretical truncation loss for all matrices within the same group, $\text{Len}(L_G)$ denotes the group size and $\text{Sum}(L_{min})$ denotes the sum of the loss within this group. In this way, SVD-LLM V2 bypasses the need to measure end-to-end perplexity to determine compression ratios, as done in ASVD and is time-consuming. Instead, it utilizes truncation loss, which is easy to obtain and thereby enhancing the efficiency of the algorithm. As shown in Figure 3, with the proposed heterogeneous compression ratio allocation scheme, SVD-LLM V2 effectively reduces the truncation loss (the blue area) with only a small increase of several small truncation losses (the yellow area).

In the next section, we describe the details of the proposed loss-optimized weight truncation.

3.2 Loss-optimized Weight Truncation

Motivation: After determining the specific compression ratio for each weight matrix in the LLM, the next step is to truncate the weights according to their assigned compression ratios. To reduce truncation loss $L = \|WX - W'X\|_F$ during SVD compression, SVD-LLM first constructs the whitening matrix S by applying Cholesky decomposition on XX^T . It then performs SVD and truncation on WS . Although SVD-LLM has been theoretically proven to achieve the lowest truncation loss at a given compression ratio, our empirical study shows that its actual truncation loss is frequently above the theoretical minimum. This is mainly due to the numerical instability involved in performing the Cholesky decomposition on a large-scale matrix during truncation. Moreover, the Cholesky decomposition requires XX^T to be positive definite, which is often hard to satisfy.

To demonstrate this, we randomly select two weight matrices, A and B , in LLaMA-3 8B and

Algorithm 2 Pseudocode of Loss-optimized Weight Truncation in SVD-LLM V2

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Input:  $W$ : Original weight matrix
        $X$ : Input activation
        $R$ : Target compression ratio
Output:  $W'$ : Compressed weight matrix
1: procedure WEIGHT_TRUNCATION( $W, X, R$ )
2:    $S \leftarrow XX^T$             $\triangleright$  Construct matrix  $S$  from  $X$ 
3:    $U_s, S_s, V_s \leftarrow \text{SVD}(S)$   $\triangleright$  Perform SVD on matrix  $S$ 
4:    $D \leftarrow W \times U_s \times \sqrt{S_s}$             $\triangleright$  Construct matrix  $D$ 
5:    $U_{ws}, S_{ws}, V_{ws} \leftarrow \text{SVD}(D)$             $\triangleright$  Perform SVD on matrix  $D$ 
6:    $T_s \leftarrow \text{Truncate}(S_{ws}, R)$             $\triangleright$  Perform SVD truncation on matrix  $S_{ws}$  based on compression ratio  $R$ 
7:    $W' \leftarrow U_{ws} \times T_s \times S_s^{-1} \times U_s^{-1}$             $\triangleright$  Construct  $W'$ 
8:   return  $W'$ 
9: end procedure

```

compute their truncation loss by SVD-LLM using 256 randomly selected data in the C4 dataset under compression ratios 20% and 60%. As shown in Table 1, because XX^T is not positive definite, SVD-LLM fails to compress matrix A . For matrix B , even when the compression ratio is as low as 20%, SVD-LLM still achieves a larger truncation loss in practice than in theory, and this difference even increases with increasing compression ratio.

SVD-based LLM compression methods such as Balco (Ji et al., 2024) have been proposed that utilize pooled covariance matrices to precisely estimate the feature distribution to reduce truncation loss. However, these methods cannot guarantee their theoretical optimality during SVD truncation. Therefore, it is necessary to design a new way to optimize the truncation loss for SVD compression.

Table 1: Comparison of the normalized truncation loss (\downarrow) between SVD-LLM and SVD-LLM V2 on two randomly selected weight matrices in LLaMA-3 8B using 256 calibration data on C4 under 20% and 60% compression ratios. **Fail** means the algorithm raises an error during the SVD compression.

	MATRIX A		MATRIX B	
RATIO	20%	60%	20%	60%
Theoretical	0.5982	2.3251	0.7351	3.5245
SVD-LLM	Fail	Fail	0.8961	5.9834
SVD-LLM V2	0.5982	2.3251	0.7351 (\downarrow 18%)	3.5245 (\downarrow 41%)

Key Design: The pseudocode of the proposed loss-optimized weight truncation is provided in Algorithm 2. Different from SVD-LLM, SVD-LLM V2 bypasses the Cholesky decomposition, resulting in a more straightforward process with improved numerical stability. Specifically, given the input activation X , SVD-LLM V2 conducts SVD on XX^T to obtain the decomposed matrices U_s, S_s, V_s , where

S_s is the diagonal matrix with singular values. It then conducts another round of SVD on $W \times U_s \times \sqrt{S_s}$ to obtain U_{ws}, S_{ws}, V_{ws} . The final compressed weight matrix W' can be obtained via $U_{ws} \times \text{Trunc.}(S_{ws}) \times S_s^{-1} \times U_s^{-1}$, where $\text{Trunc.}(C)$ denotes the rank-k truncation of matrix C during SVD compression.

In the following, we provide a theoretical proof on why such truncation offers the same theoretical minimum truncation loss as SVD-LLM.

Theorem 3.1. *If U_s, S_s, V_s are obtained by SVD decomposition of XX^T and U_{ws}, S_{ws}, V_{ws} are obtained by SVD decomposition of $W \times U_s \times \sqrt{S_s}$, the compressed weight matrix $W' = U_{ws} \times \text{Trunc.}(S_{ws}) \times V_{ws} \times \sqrt{S_s}^{-1} \times U_s^{-1}$ ensures the theoretical minimum truncation loss.*

Proof. Since XX^T is the symmetric matrix, suppose that the singular vectors and values of input activation X is U_x, S_x, V_x , we have $U_s = U_x$ and $\sqrt{S_s} = S_x$. Suppose $S = U_s \times \sqrt{S_s}$, thus $S^{-1} = \sqrt{S_s}^{-1} \times U_s^{-1}$, and we have:

$$\begin{aligned} S^{-1}X &= \sqrt{S_s}^{-1}U_s^{-1}X = S_x^{-1}U_x^{-1}X \\ &= S_x^{-1}U_x^{-1}U_xS_xV_x = Vx \end{aligned} \quad (2)$$

Therefore, $S^{-1} \times X$ is orthogonal and $\|A \times S^{-1} \times X\|_F = \|S^{-1} \times X\|_F$, and the final truncation loss could be derived as:

$$\begin{aligned} L^2 &= \|WX - W'X\|_F^2 \\ &= \|WSS^{-1}X - U_{ws} \times \text{Trunc.}(S_{ws}) \times V_{ws} \times S^{-1}X\|_F^2 \\ &= \|(WS - U_{ws} \times \text{Trunc.}(S_{ws}) \times V_{ws})S^{-1}X\|_F^2 \\ &= \|WS - U_{ws} \times \text{Trunc.}(S_{ws}) \times V_{ws}\|_F^2 \\ &= \|\text{SVD}(WS)\|_F^2 = \|\text{SVD}(W \times U_x \times S_x)\|_F^2 \\ &= \|\text{SVD}(W \times U_x \times S_x \times V_x)\|_F^2 \\ &= \|\text{SVD}(WX)\|_F^2 = L_{min}^2 \end{aligned} \quad (3)$$

Therefore, the designed SVD truncation ensures the theoretical minimum truncation loss. \square

For a better demonstration, we also implement the new loss-optimized weight truncation by SVD-LLM V2 on LLaMA-3-8B. As shown in Table 1, SVD-LLM V2 achieves better numerical stability and lower truncation loss than SVD-LLM.

4 Experiments and Analysis

Baselines. We compare SVD-LLM V2 against two groups of methods. (1) Three state-of-the-art SVD-based LLM compression methods: FWSVD (Hsu et al., 2022), ASVD (Yuan et al., 2023), and SVD-LLM (Wang et al., 2024b) (Section 4.1). (2) Other

types of LLM compression methods. These include three state-of-the-art pruning-based LLM compression methods: LLM-Pruner (Ma et al., 2023), SliceGPT (Ashkboos et al., 2024), and Block-Pruner (Zhong et al., 2024), and two state-of-the-art quantization-based LLM compression methods: PB-LLM (Yuan et al., 2024), and BiLLM (Huang et al., 2024) (Section 4.4).

Models and Datasets. To demonstrate the generability of our method, we evaluate the performance of SVD-LLM V2 on five models at various scales (LLaMA-7B, 13B, 30B, LLaMA3-8B (Touvron et al., 2023), OPT-6.7B (Zhang et al., 2022)) and ten datasets including two language modeling datasets (WikiText-2 (Merity et al., 2017) and C4 (Raffel et al., 2020)), six classification datasets (OpenbookQA (Mihaylov et al., 2018), WinoGrande (Sakaguchi et al., 2020), HellaSwag (Zellers et al., 2019), Arc_e (Clark et al., 2018), PIQA (Bisk et al., 2020), MathQA (Amini et al., 2019)), and two generation datasets (TruthfulQA (Lin et al., 2022) and GSM8K (Cobbe et al., 2021)) with the LM-Evaluation-Harness framework (Gao et al., 2023).

Implementation Details. We randomly select 256 WikiText-2 samples as the calibration data. To mitigate the error raised by the Choleksy decomposition in SVD-LLM due to positive definite, we followed the implementation of SVD-LLM (Wang et al., 2024b) to add the small noise into the decomposed matrices. The compression ration in our experiments refers to the parameter reduction of LLM achieved through compression. All of the experiments are conducted on A100 GPUs.

4.1 Performance Comparison

We first compare SVD-LLM V2 against state-of-the-art SVD-based LLM compression methods from four aspects: (1) performance on different LLMs, (2) performance on LLMs with larger scales, (3) performance under different compression ratios, and (4) compression speed.

Performance on Different LLMs. We compare the performance between SVD-LLM V2 and the baselines on three different LLMs, including LLaMA-7B, OPT-6.7B, and LLaMA-3 8B under 20% compression ratio on ten datasets. As shown in Table 2, SVD-LLM V2 consistently achieves better and more stable performance than all the SVD-based LLM compression baselines across all three LLMs and all ten datasets. In particular, SVD-LLM V2 achieves

Table 2: Performance of OPT-6.7B, LLaMA-7B, and LLaMA-3 8B compressed by SVD-LLM V2 and baselines under 20% compression ratio on two language modeling datasets (measured by perplexity (\downarrow)), six classification datasets (measured by both individual and average accuracy (\uparrow)), two generation datasets (TruthfulQA measured by BLEU score (\uparrow), and GSM8K measured by Exact Match Accuracy (\uparrow)). The best performance is marked in bold. The relative performance gain compared to the best-performing baseline is marked in green inside bracket.

	METHOD	WikiText-2 \downarrow	C4 \downarrow	Openb.	ARC_e	WinoG.	HellaS.	PIQA	MathQA	Average \uparrow	TruthfulQA \uparrow	GSM8K \uparrow
LLaMA-7B	Original	5.68	7.34	0.34	0.75	0.70	0.57	0.79	0.27	0.57	0.30	0.09
	FWSVD	1727	1511	0.09	0.11	0.05	0.08	0.10	0.05	0.08	0.00	0.00
	ASVD	11.14	15.93	0.29	0.53	0.64	0.41	0.68	0.17	0.45	0.21	0.04
	SVD-LLM	7.94	15.84	0.31	0.71	0.68	0.49	0.71	0.22	0.52	0.24	0.06
SVD-LLM V2		7.12 (\downarrow 10%)	10.47 (\downarrow 34%)	0.32	0.72	0.70	0.52	0.75	0.24	0.54 (\uparrow 4%)	0.27 (+0.03)	0.07 (+0.01)
OPT-6.7B	Original	10.87	12.50	0.28	0.66	0.65	0.50	0.76	0.25	0.52	0.29	0.01
	FWSVD	14559	17898	0.03	0.08	0.02	0.01	0.05	0.01	0.03	0.01	0.00
	ASVD	82	102	0.16	0.41	0.30	0.36	0.61	0.07	0.32	0.09	0.00
	SVD-LLM	16.04	21.27	0.21	0.56	0.59	0.47	0.73	0.21	0.46	0.22	0.00
SVD-LLM V2		13.46 (\downarrow 16%)	17.72 (\downarrow 17%)	0.25	0.61	0.62	0.49	0.74	0.22	0.49 (\uparrow 7%)	0.24 (+0.02)	0.01 (+0.01)
LLaMA-3 8B	Original	6.14	9.47	0.35	0.80	0.73	0.60	0.80	0.40	0.61	0.49	0.45
	FWSVD	4782	8195	0.01	0.04	0.01	0.02	0.02	0.01	0.02	0.00	0.00
	ASVD	17.55	28.41	0.20	0.59	0.61	0.41	0.69	0.30	0.47	0.37	0.28
	SVD-LLM	11.82	20.05	0.29	0.77	0.64	0.51	0.72	0.30	0.54	0.45	0.31
SVD-LLM V2		8.01 (\downarrow 32%)	11.72 (\downarrow 42%)	0.33	0.79	0.70	0.58	0.77	0.36	0.59 (\uparrow 9%)	0.46 (+0.01)	0.40 (+0.09)

up to 42% perplexity reduction and 9% accuracy improvement with better generation ability compared to prior state-of-the-art method SVD-LLM on LLaMA-3 8B.

Performance on LLMs with Larger Scales. We compare the performance between SVD-LLM V2 and the baselines on LLaMA-13B and LLaMA-30B under 20% compression ratio on WikiText-2 and six classification datasets. As shown in Table 3, SVD-LLM V2 consistently outperforms all the baselines on both 13B and 30B model sizes.

Table 3: Perplexity (\downarrow) on WikiText-2 and average accuracy (\uparrow) of six classification datasets of LLaMA-13B and LLaMA-30B under 20% compression ratio.

METHOD	LLAMA-13B		LLAMA-30B	
	Perplexity \downarrow	Accuracy \uparrow	Perplexity \downarrow	Accuracy \uparrow
Original	5.09	0.59	4.10	0.61
FWSVD	15.98	0.43	20.54	0.42
ASVD	6.74	0.54	22.71	0.44
SVD-LLM	6.61	0.55	5.63	0.57
SVD-LLM V2	5.46 (\downarrow 17%)	0.56 (\uparrow 2%)	4.71 (\downarrow 16%)	0.60 (\uparrow 5%)

Performance under Different Compression Ratios.

We compare the performance between SVD-LLM V2 and the baselines on LLaMA-7B under compression ratio ranging from 20% to 80% on WikiText-2 and six classification datasets. As shown in Figure 4, SVD-LLM V2 consistently outperforms all baselines, and the performance gain compared to the best-performing baseline increases as the compression ratio increases.

Compression Speed. Besides measuring the per-

formance of the compressed LLMs, we also evaluate the compression speed. Specifically, we measure the A100 GPU hours used by SVD-LLM V2 and the baseline methods for compressing LLaMA-7B under 20% compression ratio. Our results show that FWSVD takes about 6 GPU hours, ASVD takes about 5.5 GPU hours, SVD-LLM takes about 15 minutes, and SVD-LLM V2 takes about 18 minutes to finish the compression. FWSVD requires gradient calculation, thus consumes a significant amount of time for compression. For the other methods, the main reason for such a variation is their respective techniques for allocating compression ratios among weight matrices. SVD-LLM assigns the same compression ratio to all weight matrices, enabling the fastest operation but sacrificing accuracy. ASVD, however, determines the compression ratio by regularly evaluating the end-to-end perplexity, which slows down its compression process. In contrast, SVD-LLM V2 allocates the compression ratio directly from its truncation loss, making it significantly faster than ASVD.

4.2 Inference Speedup of SVD-LLM V2

To evaluate the inference speedup of models compressed by SVD-LLM V2, we measure the numbers of tokens generated per second from both the original LLaMA-7B and the model compressed by SVD-LLM V2 under different compression ratios on a single NVIDIA A100 GPU. For a fair comparison, we fix the batch size to 4, the prefill length to 1024, and the decoding length to 256. As shown in Figure 5,

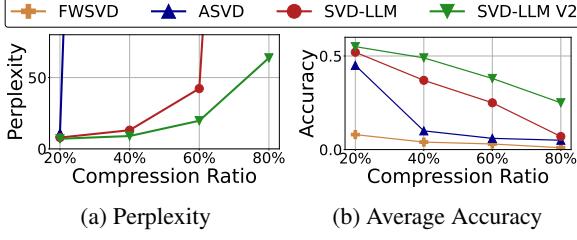


Figure 4: Perplexity on WikiText-2 and average accuracy on six classification datasets of LLaMA-7B compressed by SVD-LLM V2 and other SVD-based LLM compression baselines under 20% to 80% compression ratios. The perplexity values of FWSVD and ASVD are larger than 100, thus are not shown in the figure.

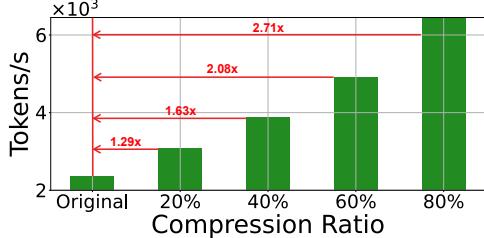


Figure 5: Throughput (Tokens/s) achieved by original LLaMA-7B and its compressed version by SVD-LLM V2 under different compression ratios on a single NVIDIA A100 GPU. We fix the batch size to 4, prefill length to 1024, and decoding length to 256. The speedup over the original LLM is marked in red.

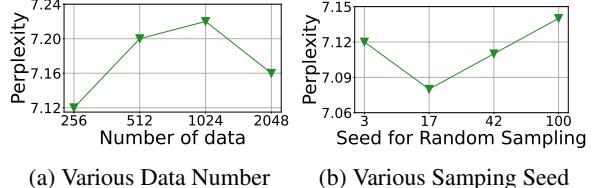
SVD-LLM V2 consistently achieves faster token generation speeds across all the compression ratios. More importantly, the speedup becomes more significant as the compression ratio increases, resulting in a speedup of 1.29x under 20% compression ratio, 1.63x under 40% compression ratio, 2.08x under 60% compression ratio, and 2.71x under 80% compression ratio.

Table 4: Perplexity (\downarrow) of compressed LLaMA-7B by SVD-LLM and SVD-LLM V2 with individual / both components under 20% compression ratio on WikiText-2.

SVD-LLM	SVD-LLM V2 (A)	SVD-LLM V2 (T)	SVD-LLM V2
7.94	7.91 (\downarrow 1%)	7.43 (\downarrow 6%)	7.12 (\downarrow 10%)

4.3 Ablation Study

SVD-LLM V2 has two key components, both of which optimize the truncation loss. In our ablation study, we first evaluate the individual contribution of each of the two components to the compression performance. Next, since both components fully utilize the whitening matrix S , which is calculated with a randomly selected calibration set, we evaluate the impacts of different calibration data on the



(a) Various Data Number (b) Various Sampling Seed

Figure 6: Perplexity of LLaMA-7B under 20% compression ratio using calibration data sampled with different numbers or seeds from WikiText-2.

performance of SVD-LLM V2.

Component Sensitivity Study. We first evaluate the individual contribution of the two components (i.e., heterogeneous compression ratio allocation and loss-optimized weight truncation) of SVD-LLM V2. Let SVD-LLM V2 (A) denote the version of SVD-LLM V2 with heterogeneous compression ratio allocation only; and SVD-LLM V2 (T) denote the version of SVD-LLM V2 with loss-optimized weight truncation only. The results are shown in Table 4. We have two observations. (1) Both SVD-LLM V2 (A) and SVD-LLM V2 (T) outperform SVD-LLM, demonstrating the effectiveness of each of these two components alone in achieving superior compression performance. (2) SVD-LLM V2 outperforms SVD-LLM V2 (A) and SVD-LLM V2 (T), demonstrating the necessity of having both components.

Impact of Calibration Set. Next, we examine the impact of the calibration set on the compression performance of SVD-LLM V2. Specifically, we measure the changes in perplexity of LLaMA-7B compressed by SVD-LLM V2 under 20% compression ratio on WikiText-2 when using the default calibration set but with various numbers of data and sampling seeds. As shown in Figure 6, the changes in both data number and sampling seed in the calibration set incur no more than 1% fluctuation in the final performance, demonstrating that SVD-LLM V2 is not sensitive to the calibration set.

4.4 Comparison with Other Types of Post-training LLM Compression Methods

SVD-LLM V2 is orthogonal to other post-training LLM compression methods, including quantization and pruning. In this experiment, we compare the performance of SVD-LLM V2 with state-of-the-art structured pruning-based and quantization-based LLM compression methods.

Table 5: Perplexity (\downarrow) of LLaMA-7B compressed by structured pruning methods and SVD-LLM V2 under various weight memory budgets on WikiText-2.

	PERPLEXITY (\downarrow) UNDER WEIGHT MEMORY BUDGET			
METHOD	10 GB	9 GB	8 GB	7 GB
LLM-Pruner	9.88	12.21	18.94	21.68
SliceGPT	8.78	12.73	16.39	27.41
BlockPruner	9.40	12.76	19.78	43.05
SVD-LLM V2	7.84 ($\downarrow 17\%$)	8.48 ($\downarrow 34\%$)	10.17 ($\downarrow 49\%$)	15.62 ($\downarrow 28\%$)

Table 6: Average accuracy (\uparrow) of LLaMA-7B compressed by structured pruning methods and SVD-LLM V2 under various weight memory budgets.

	AVERAGE ACCURACY (\uparrow) UNDER WEIGHT MEMORY BUDGET			
METHOD	10 GB	9 GB	8 GB	7 GB
LLM-Pruner	0.49	0.47	0.35	0.31
SliceGPT	0.51	0.46	0.38	0.29
BlockPruner	0.48	0.46	0.33	0.20
SVD-LLM V2	0.52 ($\uparrow 2\%$)	0.50 ($\uparrow 6\%$)	0.42 ($\uparrow 11\%$)	0.35 ($\uparrow 13\%$)

Comparison with Structured Pruning. First, we compare SVD-LLM V2 with three state-of-the-art post-training structured pruning-based LLM compression methods: LLM-Pruner (Ma et al., 2023), SliceGPT (Ashkboos et al., 2024), and BlockPruner (Zhong et al., 2024) under various weight memory budgets, ranging from 10 GB to 7 GB. The perplexity results are shown in Table 5 and the average accuracy results are shown in Table 6. As shown, SVD-LLM V2 outperforms all three state-of-the-art structured pruning-based LLM compression methods. In particular, under 7 GB memory budget, SVD-LLM V2 achieves 28% reduction in perplexity and 13% higher average accuracy.

Comparison with Quantization. Next, we compare SVD-LLM V2 with post-training quantization-based LLM compression methods. We first compare SVD-LLM V2 with GPTQ (Frantar et al., 2022) under 3-bit quantization. As shown in Table 7, while SVD-LLM V2 achieves worse perplexity compared to GPTQ under 3-bit memory budget, combining SVD-LLM V2 (30% compression ratio) with GPTQ-4-bit achieves superior perplexity compared to GPTQ-3-bit under the same memory budget. In other words, we find that under the same memory budget, by first compressing the original 16-bit LLM with SVD-LLM V2 at 30% compression ratio, then quantizing the compressed LLM to 4-bit using GPTQ, we are able to achieve better perplexity compared to directly quantizing the original LLM to 3-bit. Finally, we compare SVD-LLM V2 with two state-of-the-art post-training quantization-based LLM compression methods: BiLLM (Huang et al., 2024) and PB-LLM (Yuan et al., 2024), which push the frontier to 1-bit quantization. The results are shown in Table 8. We have two observations: (1) Without combining with quanti-

zation techniques, SVD-LLM V2 (16-bit) outperforms PB-LLM with 5% lower perplexity. (2) By combining with quantization techniques, SVD-LLM V2 (2-bit) outperforms state-of-the-art 1-bit post-training quantization method BiLLM. In particular, SVD-LLM V2 (2-bit) achieves 69% lower perplexity than BiLLM, showing the promise of combining SVD-based and quantization-based compression methods for pushing the frontier of post-training LLM compression forward.

Table 7: Perplexity (\downarrow) of LLaMA-7B compressed by GPTQ and SVD-LLM V2 on WikiText-2.

METHOD	WEIGHT MEMORY	PERPLEXITY
GPTQ-3bit	2.8 GB	16.28
SVD-LLM V2	2.8 GB	119
SVD-LLM V2 + GPTQ-4bit	2.8 GB	9.97 ($\downarrow 39\%$)

Table 8: Perplexity (\downarrow) of LLaMA-7B compressed by 1-bit post-training quantization methods and SVD-LLM V2 on WikiText-2.

METHOD	DATA TYPE	WEIGHT MEMORY	PERPLEXITY
PB-LLM	1-bit	1.9 GB	104.83
BiLLM	1-bit	1.5 GB	47.67
SVD-LLM V2	16-bit	1.5 GB	99.64
SVD-LLM V2	2-bit	1.5 GB	14.73 ($\downarrow 69\%$)

5 Conclusion

In this paper, we present SVD-LLM V2, a SVD-based post-training LLM compression method. SVD-LLM V2 addresses the limitation of existing methods about high truncation loss during compression. Specifically, SVD-LLM V2 first employs a heterogeneous compression ratio allocation strategy to effectively balance truncation loss across different weight matrices of the LLM. It further introduces a loss-optimized weight truncation to ensure a lower and more stable truncation loss. Our evaluation results demonstrate the superiority of SVD-LLM V2 over state-of-the-art SVD-based post-training LLM compression methods.

6 Limitations

While SVD-LLM V2 outperforms existing SVD-based LLM compression methods, there is still space for further improvement. For example, under 90% compression ratio, there is a small performance gap compared with state-of-the-art quantization methods. We aim to fill this gap in future.

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