

# Fast Generalized Distillation for Semi-supervised Domain Adaptation

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**Abstract.** Semi-supervised domain adaptation (SDA) is a typical setting when we face the problem of domain adaptation in real applications. How to effectively utilize the unlabeled data is an important issue in SDA. In this paper, we propose a new paradigm, called *Generalized Distillation Semi-supervised Domain Adaptation* (GDSDA) to solve the SDA problem. We first demonstrate that GDSDA can effectively utilize the unlabeled data to transfer the knowledge from the source models. We illustrate that the imitation parameter of GDSDA can greatly affect the performance of the target model. Based on this, we propose GDSDA-SVM which uses SVM as the base classifier and can effectively estimate the imitation parameter. Specifically, the imitation parameter is estimated by minimizing the Leave-one-out cross-validation loss on the target data using our novel objective function. Experiment results show that GDSDA-SVM can effectively utilize the unlabeled data to transfer the knowledge between different domains under the SDA setting.

## 1 Introduction

Domain adaptation can be used in many real applications, which addresses the problem of learning a target domain with the help of a different but related source domain. In real applications, it can be very expensive to obtain sufficient labeled examples while there are abundant unlabeled ones. *Semi-supervised domain adaptation* (SDA) tries to exploit the knowledge from the source domain and use a certain amount of unlabeled examples and a few labeled ones from the target domain to learn a target model. Typically, the labeled examples in the target domain are too few to construct a good classifier alone. How to effectively utilize the unlabeled examples is an important issue in SDA.

In previous work of SDA, many methods have been proposed to leverage the source knowledge with the unlabeled data. Duan et al.[8] proposed a method to measure the domain shift with Maximum Mean Discrepancy (MMD) between source and target domains using the labeled and unlabeled data. Daumé et al.[4] utilized unlabeled data as a co-regularizer and forced the hypotheses learned from different domains to agree on the unlabeled data. Meanwhile, Yao et al.[20] used the unlabeled target examples to discover the underlying intrinsic information in the target domain. Donahue et al.[6] show that using the smoothness constraints on the classifier scores over the unlabeled data can lead to the improved transfer result. The previous work in SDA requires to access the source data to measure

the data distribution mismatch between the source and target domain. However, in some situations, we may not be able to access each of the source examples for many reasons. When we use a large dataset as our source domain, for example, it is tedious to compare each of the source examples with the target data to estimate the data distribution mismatch.

Recently, a framework called *Generalized Distillation (GD)*[13] was proposed, which allows the knowledge to be transferred between different models effectively. GD includes two different models, the teacher model and student model. The student model tries to learn from the teacher model by mimicking the outputs of the teacher model on the training data. Remarkably, in GD, the knowledge can be directly transferred from the teacher model to the student model without accessing the data used to train the teacher. Moreover, GD can be used to exploit the information of the unlabeled data in a semi-supervised scenario[13]. Given that GD has such ability, it is natural to ask the following two questions: (1) Can GD framework be applied to solve the SDA problem? (2) How to improve its effectiveness when we apply GD to real SDA applications?

To answer these two questions, in this paper, we first propose a new paradigm, called *Generalized Distillation Semi-supervised Domain Adaptation (GDSDA)*, to solve the SDA problem. We show that, with GDSDA the knowledge of the source models can be effectively transferred to the target domain using the unlabeled data. Specifically, the target model is trained with the help of the soft labels, i.e. the predictions of the target domain examples given by the source models. Therefore, without accessing each of the source examples, GDSDA is more efficient especially when the source domain is relatively large and there is a well-trained source model.

Then we argue that the imitation parameter of GDSDA which controls the amount of knowledge transferred from the source model can greatly affect the performance of the target model. However, according to the previous work[13, 17], the imitation parameter is a hyperparameter and can only be determined by either brute force search or background knowledge. Therefore, we propose a novel imitation parameter estimation method for GDSDA, called GDSDA-SVM, which uses SVM as the base classifier and can determine the imitation parameter automatically. In particular, we use the Mean Square Error loss for GDSDA-SVM and show that the Leave-one-out cross validation (LOOCV) loss can be calculated in a closed form. By minimizing the LOOCV loss on the target training data, we can find the optimal imitation parameter for the target model. In our experiments, we show that GDSDA-SVM can effectively find the optimal imitation parameter and achieve competitive performance compared to methods using brutal force search but with faster speed.

To summarize, the main contributions of this paper include: (1) We propose the paradigm of GDSDA that can directly transfer the knowledge from the source model with the help of unlabeled data for the SDA problems. (2) We propose the GDSDA-SVM that can effectively find the optimal imitation parameter for real SDA applications.

## 2 Generalized Distillation for Semi-supervised Domain Adaptation

GDSDA is a paradigm using GD for the SDA problem. In this section, we first give a brief review of GD. Then we show the process of GDSDA and demonstrate the reason why GDSDA can work for the SDA problem. Finally, we show the importance of the imitation parameter.

### 2.1 An overview of Generalized Distillation and GDSDA

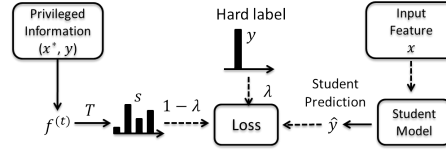


Fig. 1: Illustration of Generalized Distillation training process.

Generalized Distillation can be considered as the hybrid of two famous learning paradigms *Distillation*[10] and *Learning Using Privileged Information*(LUPI)[19]. In GD, the training data can be represented as a collection of triples:

$$\{(x_1, x_1^*, y_1), (x_2, x_2^*, y_2) \dots (x_n, x_n^*, y_n)\}$$

$x^*$  is the privileged information for data  $x$ , which is only available in the training process and  $y$  is the corresponding label. The process of generalized distillation is as follows: in step 1, a teacher model  $f^{(t)}$  is trained using the input-output pairs  $\{x_i^*, y_i\}_{i=1}^n$ . In step 2, use  $f^{(t)}$  to generate the soft label  $s_i$  for each training example  $x_i$  using the softmax function  $\sigma$ :

$$s_i = \sigma(f^{(t)}(x_i)/T) \quad (1)$$

where  $T$  is a hyperparameter called *temperature* to control the smoothness of the soft label. In step 3, learn the student  $f^{(s)}$  from the pairs  $\{(x_i, y_i), (x_i, s_i)\}_{i=1}^n$  using:

$$f^{(s)} = \arg \min_{f^{(s)} \in \mathcal{F}^{(s)}} \frac{1}{n} \sum_{i=1}^n \left[ \lambda \ell(y_i, f^{(s)}(x_i)) + (1 - \lambda) \ell(s_i, f^{(s)}(x_i)) \right] \quad (2)$$

Here,  $\ell(\cdot, \cdot)$  is the loss function and  $\lambda$  is the *imitation parameter* to balance the importance between the hard label  $y_i$  and the soft label  $s_i$ . When testing, the student model can predict with the data  $x$  alone without the assistance of the privileged information.

In domain adaptation, when we consider the source model is the teacher and the predictions of the target data give by the source models as the privileged

information, GD can be naturally applied to SDA. This leads to *Generalized Distillation Semi-supervised Domain Adaptation* (**GDSDA**). Moreover, in GDSDA, we also consider the multi-source scenario and extend the GD paradigm to fit this scenario. To be consistent with other work in domain adaptation, we use source model and target model to denote the teacher model and the student model in the rest of our paper in GDSDA.

An important issue of applying GD to SDA is that, in Eq. (2), each target example is assigned with a hard label  $y$  (true label) and a soft label  $s$  (class probabilities from the teacher). However, in SDA, we are not able to obtain the hard labels of the unlabeled data. Here we follow [13] and use the “fake label” strategy to label the unlabeled data: for the labeled examples, we use *one-hot* strategy to encode their labels while using 0s as the labels of the unlabeled examples. Thus, each example in the target domain is assigned with a label. It is arguable that the “fake label” strategy would introduce extra noise and degrade the performance. However, we will show in our experiment that this noise can be well controlled by setting a proper value to the imitation parameter and we can still achieve improved performance (See the single source experiment).

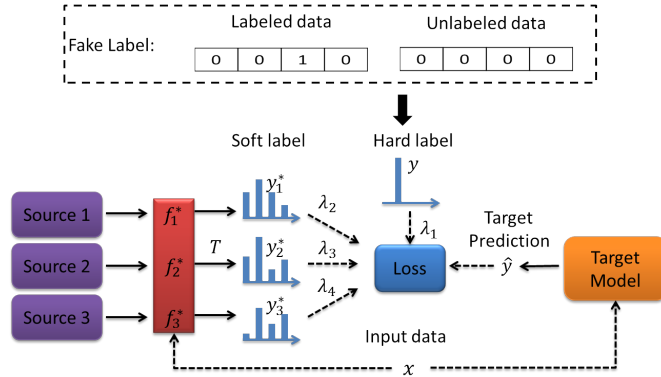


Fig. 2: Illustration of GDSDA training process and the “fake label” strategy.

The process of GDSDA is shown in Figure 2. Suppose we have  $M - 1$  source domains denoted as  $D_s^{(j)} = \{X^{(j)}, Y^{(j)}\}_{j=1}^{M-1}$  and the target domain  $D_t = \{X, Y\}$  encoded with the “fake label” strategy. The process of GDSDA is as follows:

1. Train the source models  $f_j^*$  for each of the  $M - 1$  domains with  $\{X^{(j)}, Y^{(j)}\}$ .
2. For each of the training example  $x_i$  in the target domain, computer the corresponding soft label  $y_{ij}^*$  with each of the source model  $f_j^*$  and the temperature  $T > 0$ .
3. Learn the target model  $f_t$  with the  $(M+1)$ -tuples  $\{x_i, y_i, y_{i1}^*, \dots, y_{i(M-1)}^*\}_{i=1}^L$  and the imitation parameters  $\{\lambda_i\}_{i=1}^M$  using (3):

$$f_t(\lambda) = \arg \min_{f_t \in \mathcal{F}} \frac{1}{L} \sum_{i=1}^L \left[ \lambda_1 \ell(y_i, f_t(x_i)) + \sum_{j=1}^{M-1} \lambda_{j+1} \ell(y_{ij}^*, f_t(x_i)) \right] \quad (3)$$

Compared to other work of SDA which requires to use each example of the source domain, by either re-weighting [6, 8] or feature augmentation [4], GDSDA only requires the trained model from the source domain to generate the soft labels. Meanwhile, GDSDA is able to handle the multi-class scenario while some previous work, such as SHFA[7] can only solve the binary classification problem in SDA. Moreover, GDSDA is able to transfer the knowledge from any type of source model that is able to output the soft label (class probabilities) without accessing the source data.

## 2.2 Why does GDSDA work

In this part, we demonstrate the scenarios where GDSDA would work. Before we provide our analysis, we first introduce the two basic assumptions of GDSDA: the *assumption of distillation* and the *assumption of the source model*.

**Assumption of distillation:** *The capacity (VC dimension) of the target model  $f_t$  is smaller than the capacity of source model  $f^*$ .* This assumption is inherited from GD. **Assumption of the source model:** *The source model  $f^*$  should work better than a target model  $f'_t$  trained only with the hard labels.* This assumption is based on a simple fact that it is more effective to learn from a superior model. This assumption is very common especially in SDA where the labeled examples are often too few to build a good target model. For example, when we only have a single labeled example for each class in the target training set, it is reasonable to assume that the source model trained from another domain could outperform a model trained only with the target training data on the target task.

Suppose the complex source model  $f^*$  can generalize well on target domain. The simple target model  $f_t$  that has the similar training error to the source model  $f^*$  would typically do better than the source model  $f^*$  itself as well as the target model trained only with hard labels on the target domain (according to the assumption of the source model). This indicates the knowledge can be transferred smoothly between models. Specifically, as it is suggested in [10], the transfer process can be achieved by letting the target model mimick the outputs of the source model (soft labels) on the training set without considering the true labels of the training examples. In another word, the useful source knowledge can be effectively transferred with the unlabeled data.

As the source models are trained from the source domains, it is necessary to weigh the source knowledge due to the domain shift[11] when we apply it to the target domain. In Eq. (3), we use the imitation parameter, to control the relative importance between the soft labels and the hard labels, which in turn reflects the amount of the knowledge transferred from each of the source models. Specifically, the larger the imitation parameter, the more important the soft labels are and more knowledge can be transferred from the source domains. For example, in Figure 2, when we set  $\lambda_2 = 0$ , we actually ignore the knowledge

from source domain 1. As a result, with the proper imitation parameter, GDSDA can effectively transfer the knowledge from each of the source models under the setting of SDA (for more details, please see the experiment section).

How to choose the imitation parameter is essential for GDSDA. Many previous studies have addressed the importance of knowledge transfer control in domain adaptation[7, 8]. Without carefully controlling the amount of knowledge transferred from the source domain, the target model can easily get degraded performance or even suffer from negative transfer[15]. However, in the previous studies, the imitation parameter can only be determined by either brute force search[13] or background knowledge[17] which scale poorly with the number of available source models and imitation parameters. In this paper, we propose our method, called GDSDA-SVM that can estimate the transfer parameter automatically.

### 3 GDSDA-SVM

In this section, we propose our method GDSDA-SVM that uses SVM as the base classifier and can effectively estimate the imitation parameter.

#### 3.1 Distillation with multiple sources

As we have mentioned previously, imitation parameter is a hyperparameter in GDSDA. A common method to estimate the hyperparameter is to use cross-validation. Here we show that it is possible to obtain a closed form cross-validation error[2] in GDSDA-SVM. As a result, GDSDA-SVM can estimate the imitation parameter effectively with the gradient descent method.

In our GDSDA-SVM, instead of using hinge loss, we use Mean Squared Error (MSE) as our loss function to train the GDSDA-SVM for the following two reasons: (1) Many recently studies [1, 14, 16, 18] show that MSE is an efficient measurement for the target model to distill the knowledge from the source model. (2) MSE can provide a closed form cross-validation error estimation, so we can estimate the imitation parameter more effectively.

Suppose we have  $L$  examples  $\{\mathbf{x}_j, \mathbf{y}_j\}_{j=1}^L$  from  $N$  classes in the target domain where  $X \in R^{L \times d}$ ,  $Y \in R^{L \times N}$ . Meanwhile, there are  $M - 1$  the source (teacher) models providing the soft labels  $Y^* = \{\mathbf{y}_{ij}^* | j = 1, \dots, L; i = 1, \dots, M - 1\}$  for each of the  $L$  examples. For simplicity, we concatenate the hard label  $Y$  and soft label  $Y^*$  into a new label matrix  $S$  to denote them, where:

$$S = [Y; Y^*] = [Y_1; \dots; Y_M]; S \in R^{L \times M \times N}$$

To solve this  $N$ -class classification problem, we build  $N$  binary SVMs. To obtain the  $n$ th binary SVM, we have to solve the following optimization problem:

$$\min_{\mathbf{w}_n} \quad \frac{1}{2} \|\mathbf{w}_n\|^2 + C \sum_j e_{jn}^2 \quad s.t. \quad e_{jn} = \sum_i \lambda_i s_{ijn} - \mathbf{w}_n \mathbf{x}_j \quad (4)$$

The Lagrangian of above optimization problem:

$$\mathcal{L} = \frac{1}{2} \|\mathbf{w}_n\|^2 + C \sum_j e_{jn}^2 + \sum_j \eta_{jn} \left( \sum_i \lambda_i s_{ijn} - \mathbf{w}_n \mathbf{x}_j - e_{jn} \right) \quad (5)$$

To find the saddle point,

$$\frac{\partial \mathcal{L}}{\partial \mathbf{w}_n} = 0 \rightarrow \mathbf{w}_n = \sum_j \eta_{jn} \mathbf{x}_j; \quad \frac{\partial \mathcal{L}}{\partial e_{jn}} = 0 \rightarrow \eta_{jn} = 2C \lambda_i e_{ijn} \quad (6)$$

For each example  $\mathbf{x}_j$  and its constraint of label  $s_{ijn}$ , we have  $e_{jn} + \mathbf{w}_n \mathbf{x}_j = \sum_i \lambda_i s_{ijn}$ . Replacing  $\mathbf{w}_n$  and  $e_{ijn}$ , we have:

$$\mathbf{x}_j \sum_k \eta_{kn} \mathbf{x}_k + \frac{\eta_{jn}}{2C} = \sum_i \lambda_i s_{ijn} \quad (7)$$

Here we use  $\Omega$  to denote the matrix  $\Omega = [K + \frac{\mathbf{I}}{2C}]$  where  $K$  is the linear kernel matrix  $K = \{\mathbf{x}_i \mathbf{x}_j^T | i, j \in 1 \dots L\}$ . To simplify our notation, let  $\eta'_n = M^{-1} S_n$  where  $S_n$  is the matrix  $S_n = \{s_{ijn} | i \in M; j \in L\}$  and  $\Omega^{-1}$  is the inverse of matrix  $\Omega$ .

According to [2], the Leave-one-out estimation of the example  $\mathbf{x}_j$  for the  $n$ th binary SVM can be written as:

$$\hat{y}_{jn} = \sum_i \lambda_i s_{ijn} - \frac{\eta_{jn}}{\Omega_{jj}^{-1}} \quad (8)$$

where  $\Omega_{jj}^{-1}$  is the  $j$ th diagonal element of  $\Omega^{-1}$ .

### 3.2 Cross-entropy loss for imitation parameter estimation

From the previous part, we have already found a effective way to calculate the leave-one-out estimation of the target model. The optimal imitation parameters can be found by minimizing the leave-one-out cross-validation error on the target data:

$$\min_{\lambda} L_c(\lambda) = \frac{1}{2} \sum_i \|\lambda_i\|^2 + \frac{1}{L} \sum_{j,n} \ell(y_{in}, \hat{y}_{jn}(\lambda)) \quad (9)$$

Here we use the  $\ell_2$  regularization term to control the complexity of  $\lambda$  so that the target model can achieve better generalization performance even with a small training set. For the loss function  $\ell(\cdot, \cdot)$ , we use the cross-entropy loss function.

$$\ell(y_{in}, \hat{y}_{jn}(\lambda)) = y_{in} \log(P_{jn}) \quad \text{for} \quad P_{jn} = \frac{e^{\hat{y}_{jn}}}{\sum_h e^{\hat{y}_{jh}}} \quad (10)$$

Typically, cross-entropy pays less attention to a single incorrect prediction which reduces the affect of the outliers of the training data. Moreover, cross-entropy has its own advantage with our "fake label" strategy. As we have mentioned

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**Algorithm 1** GDSDA-SVM

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**Input:** Input examples  $X = \{\mathbf{x}_1, \dots, \mathbf{x}_L\}$ , number of classes  $N$ , number of sources  $M$ , 3-D label matrix,  $S = [Y_1, Y_2, \dots, Y_M]$  with size  $L \times M \times N$ , temperature  $T$

**Output:** Target model  $f_t = Wx$

Compute  $\Omega = [K + \frac{\mathbf{I}}{2C}]$

Compute imitation parameter  $\lambda$  with Algorithm 2

Generate the new label  $Y_{new} = \sum_i \lambda_i Y_i$

Compute  $\eta = \Omega^{-1} Y_{new}$

Compute  $w_n = \sum_j \eta_{jn} x_j$

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**Algorithm 2**  $\lambda$  Optimization

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**Input:** Input examples  $X$ , number of classes  $N$ , size of sources  $M$ , 3D label matrix  $S$ , optimization iteration  $iter$ , Kernel matrix  $\Omega$

**Output:** Imitation parameter  $\lambda$

Initialize  $\lambda = \frac{1}{M}$ ,

Let  $S_n$  be the label matrix of  $S$  for class  $n$

**for** Each label  $S_n$  **do**

    Compute  $\eta'_n = \Omega^{-1} S_n$

**end for**

**for**  $it \in \{1, \dots, iter\}$  **do**

    Compute  $\hat{y}_{jn}$  and  $P_{jn}$  with (8) and (10)

**for** each  $\mathbf{x}_j$  in  $X$  **do**

$\Delta_\lambda = \Delta_\lambda + \sum_{j,n} s_{ijn} (P_{jn} - y_{jn})$

**end for**

$\Delta_\lambda = \Delta_\lambda / L$ ,  $\lambda = \lambda - \frac{1}{it} (\Delta_\lambda + \lambda)$

**end for**

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previously, we use gray code to encode the unlabeled examples. When we use cross-entropy loss, it can automatically ignore penalties of the unlabeled examples and reduce the affect of the noise introduced by our "fake label" strategy. As a result, the derivative of Eq. (10) can be calculated as:

$$\frac{\partial \ell(\lambda)}{\partial \lambda} = \sum_{j,n} s_{ijn} (P_{jn} - y_{jn}) \quad (11)$$

To summarize, we describe GDSDA-SVM in Algorithm 1. As the optimization problem (9) is strongly convex, we can prove that Algorithm 2 can converge to the optimal  $\lambda$  with the rate of  $O(\log(t)/t)$  where  $t$  is the optimization iteration (We are not able to show our proof here due to the space limit).

## 4 Experiments

In this section, we show the empirical performance of our algorithm GDSDA-SVM on the benchmark dataset Office. Specifically, we provide two different settings: single source and multi-source transfer scenarios for GDSDA-SVM.



**Dataset:** There are 3 subsets in Office datasets, Webcam (795 examples), Amazon (2817 examples) and DSLR (498 examples), sharing 31 classes. In our experiments, we use DSLR and Webcam as the source domain and Amazon as the target domain. We use the features extracted from Alexnet [12] FC7 as the input features for both source and target domain. The source models are trained with multi-layer perception (MLP) on the whole source dataset.

#### 4.1 Single Source for Office datasets

In this experiment, we compare our algorithm under the setting where there is just one source model. Specifically, we perform two groups of experiments using Amazon dataset as the target domain and DSLR and Webcam datasets as the source domains respectively. As we mentioned, there are significantly fewer labeled examples than unlabeled ones in real SDA applications. Therefore, in each group of experiment, we just use 1 labeled example per class with 3 different sizes of unlabeled example (10, 15 and 20 per class).

To demonstrate the effectiveness of GDSDA-SVM, we show the performance of GDSDA using brute force to search the imitation parameter  $\lambda$  in the range  $[0, 0.1, \dots, 1]$  with different temperature  $T$  as the baselines. Meanwhile, we show the performance of the source model on the target task, denoted as "Source" and the performance of a target model (using LIBLINEAR[9]) trained with only labeled examples in the target domain denoted as "No transfer"<sup>1</sup>. To avoid the randomness, we perform each experiment 10 times and report the average result. For GDSDA-SVM, we use temperature  $T = 20$  for all experiments in this part. The experimental results are shown in Figure 3.

From the results of brutal force search, it is clear that the value of imitation parameter can greatly affect the performance of the target model. Also, we can see that, when we only use the unlabeled data for distillation, i.e.  $\lambda = 0$ , as we expected, GDSDA can still slightly outperform the source model. This means GDSDA can effectively transfer the knowledge between different domains under the unsupervised scenario. As we increase the value of imitation parameter, i.e. introducing the hard labels from the target domain, the performance of GDSDA can be further improved. As we mentioned before, even though our "fake label" strategy would introduce extra noise, the noise can be limited by setting the proper value to imitation parameter and the target model can still get improved performance compared to the baselines.

Moreover, we can see that GDSDA-SVM can achieve the competitive results compared to baselines using brutal force search in  $D \rightarrow A$  experiments. In  $W \rightarrow A$  experiments, it achieves the best performances on all 3 different unlabeled sizes. This indicates that we can effectively (about 6 times faster than brutal force search) obtain a good target model with GDSDA-SVM.

<sup>1</sup> We fail to achieve a better performance using semi-supervised learning method [5] on the target data as the no transfer baseline (may due to the size of the initial labeled examples).

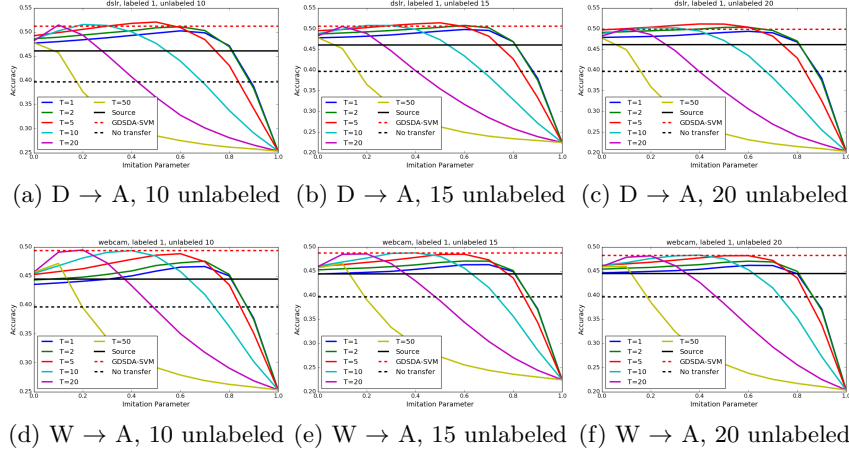


Fig. 3: Experiment results on DSLR→Amazon and Webcam→Amazon when there are just one labeled examples per class. The results of DSLR→Amazon and Webcam→Amazon are shown in figure (a)-(c) and (d)-(e) respectively. GDSDA-SVM is trained with temperature  $T = 20$ .  $\lambda$  on the X-axis denotes the imitation parameter of the hard label and the corresponding imitation parameter of the soft label is set to  $1 - \lambda$ .

## 4.2 Multi-Source for Office datasets

In this experiment, we show the performance of GDSDA-SVM under the multi-source SDA scenario. Specifically, we train the target model for the Amazon dataset and adapt the knowledge from the rest of two source domains, Webcam and DSLR. We use the similar settings as our single source experiment and perform 2 groups of experiments using 1 labeled and 2 labeled examples per class respectively. We use temperature  $T = 5$  and the results of multi-source GDSDA-SVM are denoted as SVM\_Multi. Here we use two single source GDSDA-SVMs (SVM\_w and SVM\_d trained with Webcam and DSLR respectively) as the baselines. We also show the best performance of the brutal force search model (SVM\_BF). We search temperature in range  $T = [1, 2, 5, 10, 20, 50]$  and each imitation parameter in range  $[0, 0.1, \dots, 1]$ . The experiment results are shown in Figure 4.

From the results, we can see that, given 2 source domains, SVM\_Multi can still leverage the knowledge effectively and outperform any single source model trained with GDSDA. This shows that the imitation parameter estimated by our method can effectively balance the importance of each source to achieve improved performance. SVM\_Multi performs slightly worse than the best result found by brutal force search in some experiments. However, considering their time complexity (GDSDA-SVM is around 30 times faster than brutal force search), SVM\_Multi still has its advantage in real applications.

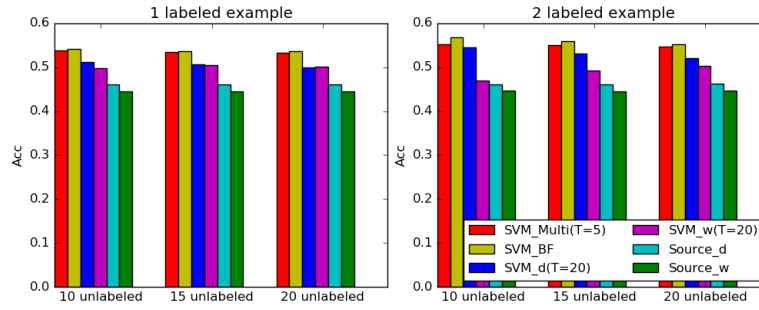


Fig. 4:  $D+W \rightarrow A$ , Multi-source results comparison.

## 5 Conclusion

In this paper, we propose a framework called Generalized Distillation Semi-supervised Domain Adaptation that can effectively leverage the knowledge from the source domain using the unlabeled data of the SDA problem. To make GDSDA more effective in real applications, we proposed a method called GDSDA-SVM and show that GDSDA-SVM can effectively estimate the imitation parameter for GDSDA. Experiment results show that GDSDA-SVM can effectively leverage the knowledge from one or more source models for the real SDA applications.

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