System of Non linear Equations

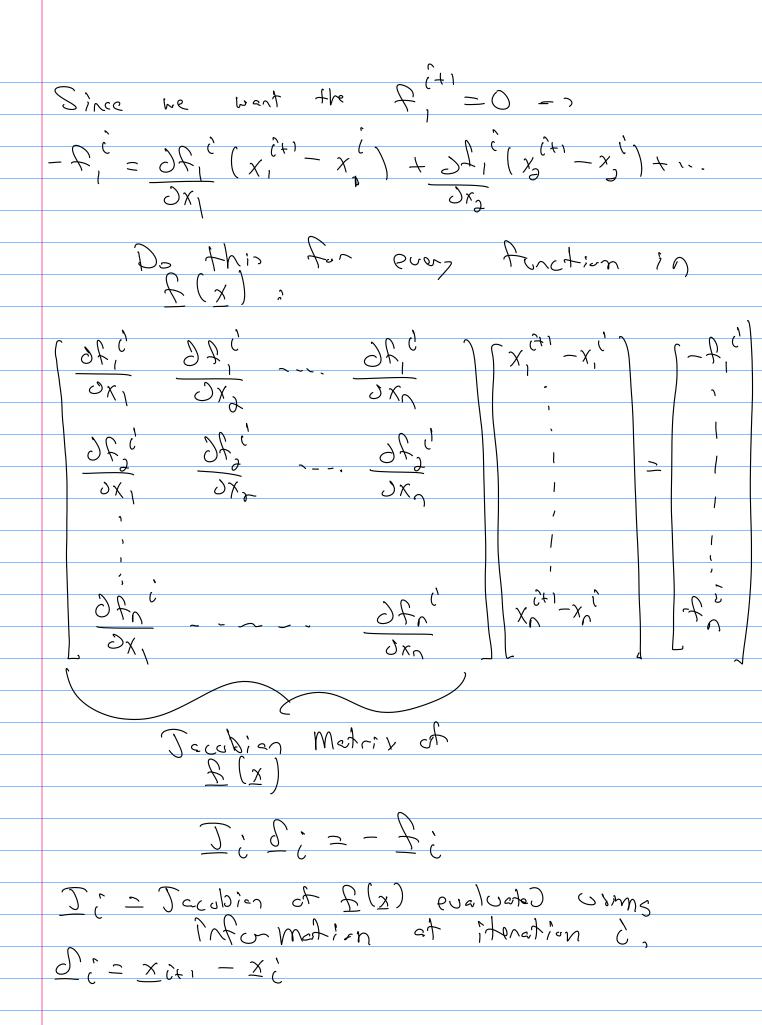
$$f(x_1, x_2, \dots, x_n) = 0$$

$$f(x_1, x_2, \dots, x_n) \geq 0$$

$$f(x_1, x_2, \dots, x_n) = f(x_1, x_2, \dots, x_n) \leq 0$$

$$f(x_1, x_2, \dots, x_n) = 0$$

$$f(x_1, x_2, \dots,$$



$$f_{i} = f(x_{i}) \leftarrow \text{"restrobust"}$$

$$= \frac{1}{2} \sum_{i=1}^{n} f_{i}$$

$$= \frac{1}{2} \sum_{i+1}^{n} - x_{i} = -\frac{1}{2} \int_{i}^{n} f_{i}$$

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	Mote! If the instial guess Is is not close to the solution, It, it might not converge.
	not close to the solution, xx,
	it might not converge.
	a Damped neuton - method.
	a Damped newton-method.
	J'=-2, F; Py year
	·
	$\chi_{i+1} = \chi_i + \alpha_i \Omega_i$, $\alpha_i \in (0, 1)$ that
	Mones ICHI Clare to Xx,
_	
	$x_1^2 + x_2^2 - V_1 x_3$
	Fixed pont: [X] [-X, 2 +]
	Fixed point: $x_1 = x_2 = x_3 = x_4 = x_5 = x_5$
	,
	Define $\epsilon_i = 11 \pm (x_i) 11_{\infty}$
	$\frac{1}{\lambda^{0}}$ $\frac{-1}{\lambda^{0}}$

$$\frac{1}{1} \frac{1,25}{1,25} \frac{0,75}{0,75} \frac{0,2125}{0,725} \frac{2,75}{2,75}$$

$$\frac{3}{2} \frac{-1,5}{-0,78} \frac{-0,22}{0,72} \frac{5,75}{5,75}$$

$$\frac{1}{2} \frac{1}{2} \frac{1}$$

Damped? $\frac{10}{10} \frac{3}{10} \frac{3}{10} \frac{3}{10} \frac{3}{10} \frac{10}{10} \frac{10}{10$ Doing this Damped iteration 2000 not relp the first 20. $\int_{1}^{2} (\chi^{1} \chi^{2})$ - f, (x11 x2) Non my Newton - Phasson $\frac{T - \left(1 + 2x_1 + y_2 - x_1\right)}{x_2} = \frac{x_1}{2x_1} = \frac{2x_2}{-u}$

χ_γ

7~~ XO =

Matlab functions: from - Pauts of one equation f solve -> Routs of nonlinear system, Same basic input: func(f, xo) exi) frenc(@(x) sin(x), 3,14) ex,) Isulce (QF, XO) function (f) = f(x)

	Minimization
	Clurchy related to not finding,
	Start w/ one-variable functions, f(x)
	Find the minimum (on meximum) of f(x),
(1)	Brent's Method.
	Let (a,b,c) be a friplet suin that
	Q < b < C
	f(a)>f(b) and f(b) cf(c)
	,
	=> A minimum must exist in Ca,C)
	Construit a 200 - unden, quadratic polynomial
	through ()
	(a, f(a)), (b, f(b)), (c, f(c)),
	then find where the derivative is zero.
	(C)
	£(b)
	6
	$\mathcal{C}_{\mathcal{A}}$

(et that minimum be X, Choone (a, x, b) on (b, x, c) es Repeat until Convergence, New to keep an eye on Styr size, new to make sure that f(a))f(x) & f(x) cf(b) for example, 2 Newton's Method for Minimization Let x_n be the current approximate solution to the true minimum location x^* , $t(x^{\nu}+\nu x)=t(x^{\nu})+\nu xt_{\prime}(x^{\nu})+\tau \nu x_{1,\prime}(x^{\nu})+\alpha \nu_{s})$ Minimum occus when It = 0 => fno nx such that 2+(x+ nx)=0 => 0 = t,(x") + vx t,,(x") + orbxg) $= \frac{\xi_{1,(x^{\prime})}}{\xi_{1,(x^{\prime})}}$

(ct
$$bx = x_{n+1} - x_n = -f'(x_n)$$

$$= x_{n+1} = x_n - \frac{f'(x_n)}{f''(x_n)}$$
The newton iteration to find the root $f'(x) = 0$

Steepost (Trod ront Descent)

More wished if $f'(x) = 0$

Leat at $f(x)$

$$f(x_n)$$

Construct en iteration that takes a Step in - It : $\chi^{U+1} = \chi^{U} - \alpha^{U} \frac{\partial \lambda}{\partial f(\lambda^{U})}$ where on is chosen every time stop Such that If(xn-xnf'(xn)) < f(xn)) These are called line-Search methods, as the minimization problem now be comes how to choose &, Mure later