

ASSIGNMENT → IRDM — SHUBHAM SWAMI - A02315672

Q28.14) frequent item set. * / Minimum support value = 0.2 *

| Item. | frequency | Support- |
|----------|-----------|----------|
| Milk | 5 | 0.5 |
| Bread. | 4. | 0.4 |
| Eggs. | 4. | 0.4. |
| Juice | 3 | 0.3 |
| butter. | 2 | 0.2 |
| cookies. | 2 | 0.2 |
| Coffee. | 3. | 0.3. |

since minimum support val = 0.2

∴ all items are frequent

Items as all support values are greater than 0.2.

and, all 1-set items are valid.

| 2-Item Set. → | frequency → | support- |
|-------------------|-------------|----------|
| (Milk, Bread) | 4 | 0.4 * |
| (Milk, Eggs). | 3 | 0.3 * |
| (Milk, Juice) | 1. | 0.1 |
| (bread, eggs) | 3. | 0.3. ← |
| (bread, cookies). | 1 | 0.1. |
| (Juice, butter) | 1 | 0.1 |
| (cookies, butter) | 1 | 0.1 |
| (cookies, eggs). | 1 | 0.1 |
| (coffee, eggs). | 1 | 0.1 |
| (coffee, juice) | 1 | 0.1. |

all support values

less than 0.2

are not frequent-items.

| | |
|-------------|------|
| Milk, Bread | 0.4 |
| Milk, eggs | 0.3 |
| Bread, eggs | 0.3. |

3-Set items.

Milk - Bread - eggs

frequency

Support-

3

0.3. *

0.

Milk - eggs → Bread

Eggs Bread - Eggs - Milk

∴ 3 item set with

Support > 0.2 = Milk - Bread - Eggs → 0.3

Q: 28-15: The above question has only one frequent set of size 3.

i.e. Milk Eggs Bread with support > 0.2 .

$$\text{Milk bread eggs} = \frac{\text{Support}(\text{milk, bread, eggs})}{\text{Support}(\text{Milk, bread})} = \frac{0.3}{0.4}$$

$$\underline{\underline{\text{Milk - bread - eggs} = \frac{3}{4} = 0.75}}$$

$$\text{Confidence of } \underline{\underline{\text{milk eggs bread}}} = \frac{\text{Support}(\text{MUBOE})}{\text{Support}(\text{MUE})} = \frac{0.3}{0.3} = \underline{\underline{1}}$$

$$\text{Milk} \rightarrow \text{eggs} \rightarrow \text{bread} = \underline{\underline{1}}$$

Q 28-19

Class Attribute = Repeat Customer.

$$n(\text{Repeat Customer} = \text{'yes'}) = 7$$

$$n(\text{Repeat Customer} = \text{'no'}) = 3$$

$$\therefore \text{info gain} = - \left[\frac{3}{10} \log_2 \left(\frac{3}{10} \right) + \frac{7}{10} \log_2 \left(\frac{7}{10} \right) \right] = \underline{\underline{0.88}}$$

→ Age attribute

① age (20-30) $\text{freq} = 5 \cdot (4 \text{ yes } 1 \text{ no})$

$$\text{info gain} = - \left[\frac{4}{5} \log_2 \left(\frac{4}{5} \right) + \frac{1}{5} \log_2 \left(\frac{1}{5} \right) \right] = 0.72$$

age (31-40) = $\text{freq} (2) \cdot (1 \text{ yes } 1 \text{ no})$

$$\text{Info gain} = - \left[\frac{1}{2} \log_2 \left(\frac{1}{2} \right) + \frac{1}{2} \log_2 \left(\frac{1}{2} \right) \right] = 1$$

age (41-50) = $\text{freq} (2)$

$$\text{info gain} = - \left[\frac{2}{2} \log_2 \frac{2}{2} \right] = 0$$

age (51-60) = $\text{freq} (1)$

$$\text{info gain} = 0$$

$$E(\text{Age}) = (0.5 \times 0.72) + (0.2 \times 1) + 0 + 0 \\ = \underline{\underline{0.56}}$$

$$I_{\text{gain}}(\text{Age}) = 0.88 - 0.56 = 0.32$$

city ① NY frequency = 7 (5 yes, 2 no)

$$\text{info gain} = - \left[\frac{2}{7} \log(2/7) + \frac{5}{7} \log(5/7) \right] = - \left[\frac{2}{7} (1.79) + \frac{5}{7} (0.5) \right] \\ = \underline{\underline{0.86}}$$

② LA freq = 2. (1 y, 1 no)

$$\text{info gain} = - \left[\log(1/2) \right] = \underline{\underline{1}}$$

③ SF = freq = 1. \therefore Info gain = 0

$$E(\text{city}) = (0.7 \times 0.86) + (0.2) + 0 = 0.8 \quad \& \quad I_{\text{gain}} = \underline{\underline{0.88 - 0.8 = 0.08}}$$

Gender: ① F freq (7) (2 n 5 y)

$$\text{info gain} = - \left[\frac{2}{7} \log(2/7) + \frac{5}{7} \log(5/7) \right] = 0.86.$$

② M freq = 3.

$$I_{\text{gain}} = - \left[\frac{2}{3} \log(2/3) + \frac{1}{3} \log(1/3) \right] \\ = \underline{\underline{0.92}}$$

$$E(\text{gender}) = (0.7)(0.86) + (0.3)(0.92) = 0.88$$

$$I_{\text{gain}}(\text{gender}) = \underline{\underline{0}}$$

Education:

① College $\text{freq} = 6 \cdot (1, 5)$

$$I_{\text{gain}} = -1 \left[\frac{1}{6} \log\left(\frac{1}{6}\right) + \frac{5}{6} \log\left(\frac{5}{6}\right) \right] = 0.65$$

② Grad = $\text{freq} = 2$

$$I_{\text{g}} = \log(1) = 0$$

③ High School $\text{freq} = 2$, $\therefore I_{\text{g}} = \log(2) = 0$

$$E(\text{education}) = (0.6 \times 0.65) + 0 + 0 = 0.39$$

$$\text{Gain}(\text{Ed}) = \underline{\underline{0.49}}$$

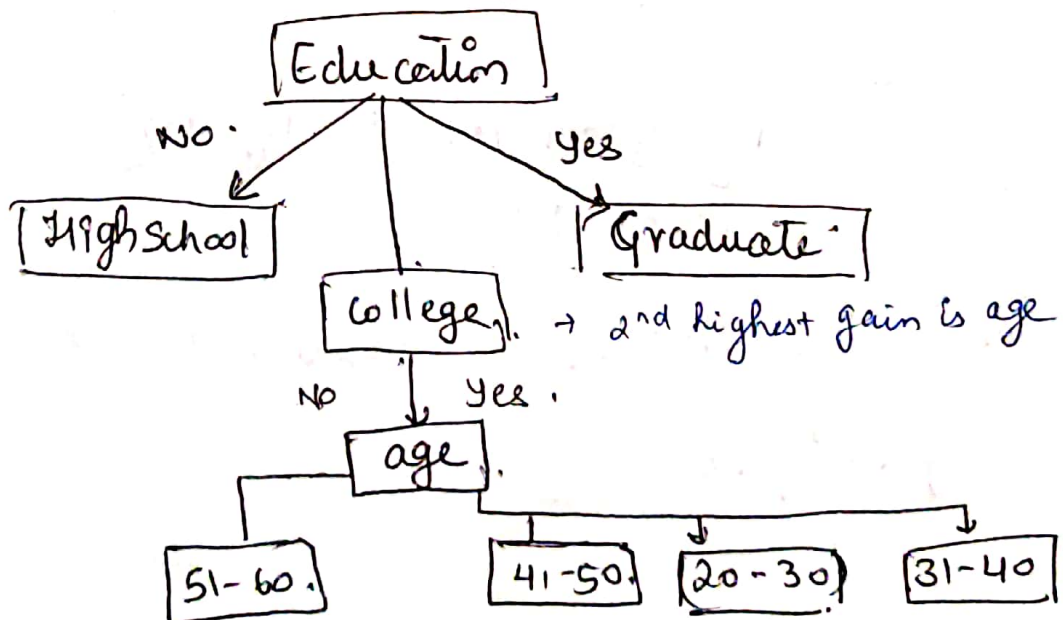
$$\text{gain}(\text{Edu}) = 0.49$$

$$\text{gain}(\text{age}) = 0.32$$

$$\text{gain}(\text{city}) = 0.08$$

$$\text{gain}(\text{gender}) = 0$$

Decision Tree



Q4 Korth & Silberschatz:

$$\text{Support (Hammer)} = 1/3 = 33\% \quad \& \quad \text{Support (Nails)} = 1/4 = 25\%$$

Rule 1: \forall Transactions T , true \Rightarrow buys (T, hammer)
Support = 33% Confidence = 33%

Rule 2: \forall Transactions T , true \Rightarrow buys (T, nails)
Support = 25% Confidence = 25%

Rule 3: \forall transactions T , buys $(T, \text{Hammer}) \Rightarrow$ buys (T, Nails)
Support = 16.5%, Confidence = $\frac{\text{Support(Rule 3)}}{\text{Support Rule 1}} \times 100 = \frac{33}{2 \times 33} \times 100$

$$\text{Support} = 16.5\%, \quad \text{Confidence} = 50\%$$

Rule 4: \forall transactions T buys $(T, \text{Nails}) \Rightarrow$ buys (T, Hammer)

$$\text{Support} = 16.5\%, \quad \text{Confidence} = \frac{S(\text{Rule 4})}{S(\text{Rule 2})} \times 100 = \frac{33}{2002} \times \frac{4^2}{14} \times 100 = 66\%$$

Q5 Total Documents = 20

$$\text{Total Returned Docs} = 10 + 8 = 18$$

$$\text{Precision} = \frac{\text{Relevant Docs}}{\text{Total Docs Returned}} = \frac{8}{18} = 0.44$$

$$\text{Recall} = \frac{\text{Relevant Docs}}{\text{Total Docs}} = \frac{8}{20} = 0.4$$

Q6. Frequency of word in following doc

| Doc | computer | Doctoral | Algorithms | Watson |
|-----|----------|----------|------------|--------|
| 1 | 2 | 1 | 0 | 0 |
| 2 | 8 | 0 | 2 | 1 |
| 3 | 20 | 0 | 5 | 0 |
| 4 | 2 | 2 | 0 | 0 |
| 5 | 20 | 0 | 0 | 2 |

$$IDF = \log \left(\frac{\text{Total Docs}}{\text{no of docs with term}} \right) \Rightarrow IDF(\text{computer}) = \log_2 \left(\frac{5}{2} \right) = 1.32$$

$$IDF(\text{Doctoral}) = \log_2 \left(\frac{5}{2} \right) = 1.32 \checkmark$$

$$IDF(\text{Algorithms}) = \log_2 \left(\frac{5}{2} \right) = 1.32 \checkmark$$

$$IDF(\text{Watson}) = \log_2 \left(\frac{5}{2} \right) = 1.32 \checkmark$$

TF = $f_i / \sum_{j=1}^V f_{ij}$ TF_{ij} → normalized freq.
 f_{ij} → no of occurrences V → features

| Doc | computer | Doctoral | Algorithm | Watson |
|-----|----------------|--------------|---------------|---------------|
| 1. | $2/3 = 0.67$ | $1/3 = 0.33$ | 0 | 0 |
| 2 | $8/11 = 0.73$ | 0 | $2/11 = 0.18$ | $1/11 = 0.09$ |
| 3 | $20/25 = 0.8$ | 0 | $5/25 = 0.2$ | 0 |
| 4. | $2/4 = 0.5$ | $2/4 = 0.5$ | 0 | 0 |
| 5 | $20/22 = 0.91$ | 0 | 0 | $2/22 = 0.09$ |