## **Problem 7**

## Find the 10001st prime

We do not know what answer to expect so we will try to solve this problem using trial division. However, if a good upper bound for the target prime is known in advance, using a sieve of Eratosthenes is a much more efficient method.

Some useful facts:

1 is not a prime.

All primes except 2 are odd.

All primes greater than 3 can be written in the form 6k+/-1.

Any number *n* can have only one primefactor greater than  $\sqrt{n}$ .

The consequence for primality testing of a number n is: if we cannot find a number f less than or equal  $\sqrt{n}$  that divides n then n is prime: the only primefactor of n is n itself

Let's design an algorithm that tests the primality of a number *n* based on these facts:

```
Function isPrime(n) if n=1 then return false else if n<4 then return true //2 and 3 are prime else if n mod 2=0 then return false else if n mod 2=0 then return false else if n<9 then return true // we have already excluded 4,6 and 8. else if n mod 3=0 then return false else  r=floor(\sqrt{n}) //\sqrt{n}  rounded to the greatest integer r so that r*r<=n f=5  while f<=r if n mod f=0 then return false (and step out of the function) if n mod(f+2)=0 then return false (and step out of the function) f=f+6 endwhile return true (in all other cases) End Function
```

We can use this function with:

```
limit=10001
count=1 //we know that 2 is prime
candidate=1
repeat
   candidate=candidate+2
   if isPrime(candidate) then count=count+1
until count=limit
output candidate
```

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