

Measurement of Branching Fraction of $B^- \rightarrow D^0 \pi^- \pi^+ \pi^-$

Shubhajit Sana

Roll: PH18B004

Guide: Prof. James F. Libby



Department of Physics,
Indian Institute of Technology Madras,
Chennai 600036, India

November 22, 2022

Outline



SuperKEKB accelerator



- Super KEKB: 4 GeV e^+ and 7 GeV e^- asymmetric collider at KEK, Japan.
- 3 km circumference and 41 mrad crossing angle.
- The center-of-mass energy is close to the mass of $\Upsilon(4S)$, which decays later to $B\bar{B}$ pair.
- A 30-fold increase in Luminosity over Belle, $L = 6 \times 10^{35} \text{ cm}^{-2} \text{ s}^{-1}$.
- Uses the nano-beam scheme (minimization of vertical beta function); hence doubled current.
- Better performance and can tolerate the much higher level of beam-related backgrounds due to the increase in instantaneous luminosity.
- **Belle II detector** is at the interaction point.

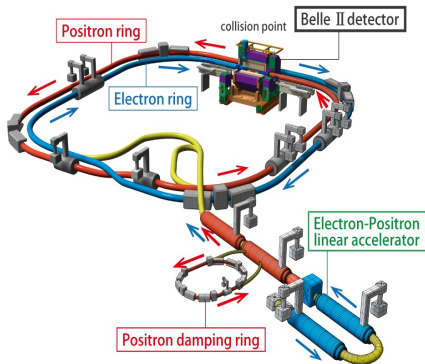


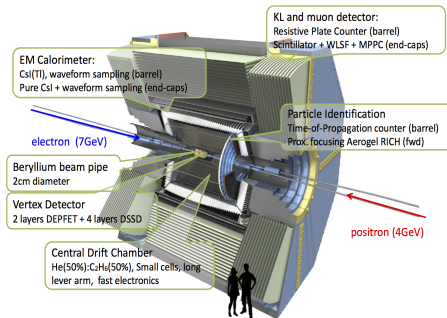
Figure: SuperKEKB accelerator

Belle II detector



- Vertex detector (PXD+SVD): two layers of pixel detector and four layers of SVD to determine B meson decay vertices.
- Central drift chamber (CDC): A large gaseous detector that acts as the principal tracking device.
- Aerogel Ring Imaging Cherenkov Counter (ARICH): Used for particle identification, mainly to distinguish between pions and kaons.
- Time-of-Propagation Counters (TOP): Cerenkov radiation totally internally reflected within quartz bars for particle identification.
- Electromagnetic calorimeter (ECAL): Detects photons and measures their energy and position with thallium-doped caesium iodide crystals.

Belle II Detector

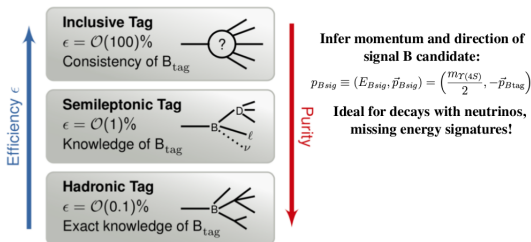
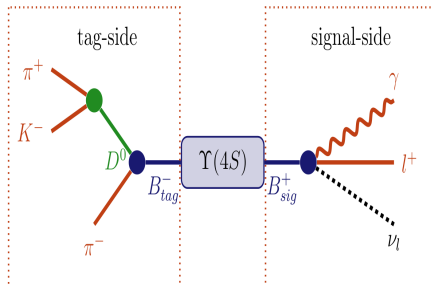


- K-Long and muon detector (KLM): Detects muons and long-lived neutral kaons, and distinguishes between them using scintillators along with RPCs.
- Superconducting Solenoid : Provides a homogeneous magnetic field of 1.5T along the beam axis.



Full Event Interpretation

- Implement tagging, where one B referred to as B_{tag} is exclusively reconstructed using hadronic or semi-leptonic modes.
- The remaining tracks and clusters are then attributed to B_{sig} , on which the search or measurement of a particular decay is done.
- Any missing energy is attributed to the B_{sig} .





Full Event Interpretation

- Final-state particle candidates are selected and corresponding classification methods are trained using the detector information.
- Intermediate particle candidates are reconstructed and a multivariate classifier is trained for each employed decay channel.
- Employs over 200 Boosted Decision Trees to reconstruct more than 10000 B decay modes.

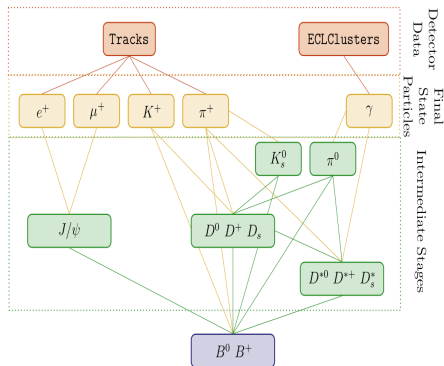
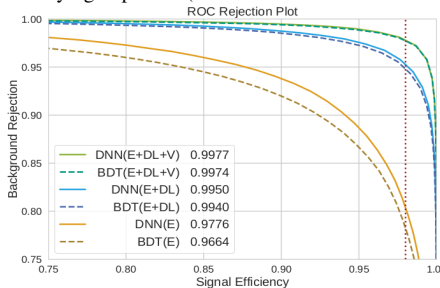


Figure: MVC algorithm with Hierarchical approach

Boosted Decision Tree



- Boosted Decision Trees (BDTs) are a specific type of a machine learning model used for classification tasks.
- The name decision tree refers to the general structure: the classification is done with a series of “decisions”.
- Decisions are logical operations (like “>”, “<”, “=”, etc.) on the input variables of each data point, by the outcome of which the data points are separated into groups.
- The word boosted refers to the specific way the tree is formed: gradient boosting. Gradient boosting means, that a final tree is made by combining a series of smaller trees of a fixed depth.
- The BDT is a supervised machine learning method, i.e. it needs to be trained on a dataset where we know the true class that we are trying to predict (this variable is called the target variable).
- FastBDT is the fastest contestant for small models (depth of the trees <5 and number of trees <300), whereas XGBoost has a slightly better scaling behaviour for large models.
- Used in FEI and to reject continuum background.





Motivation

- Inclusive and exclusive $b \rightarrow ul\nu$ and $b \rightarrow cl\nu$ transitions are crucial for the determination of the CKM matrix elements $|V_{ub}|$ and $|V_{cb}|$.

$$V = \begin{pmatrix} \begin{array}{c|c|c} \text{d} & & \\ \hline \text{u} & n \xrightarrow{e^-} \bar{p} & p \xrightarrow{\ell^-} \bar{\pi} \\ \hline \text{c} & D \xrightarrow{\ell^-} \bar{\pi} & D \xrightarrow{\ell^-} \bar{K} \\ \hline \text{t} & B^0 \xrightarrow{\ell^-} \bar{B}^0 & B_s \xrightarrow{\ell^-} \bar{B}_s \end{array} & \begin{array}{c|c|c} \text{s} & & \\ \hline K & \xrightarrow{\ell^-} \bar{\pi} & \\ \hline D & \xrightarrow{\ell^-} \bar{K} & \\ \hline B_s & \xrightarrow{\ell^-} \bar{B}_s & \end{array} & \begin{array}{c|c|c} \text{b} & & \\ \hline B & \xrightarrow{\ell^-} \bar{\pi} & \\ \hline B & \xrightarrow{\ell^-} \bar{D} & \\ \hline t & \xrightarrow{W} b & \end{array} \end{pmatrix}$$

- FEI is a powerful technique to reconstruct such decays with missing energy.
- Tag decays include high branching fraction decays like $B^- \rightarrow D^0 \pi^- \pi^+ \pi^-$.

$$\text{BF} = (5.6 \pm 2.1) \times 10^{-3}$$

- However it is not well simulated in MC because of the large uncertainty on the branching fraction.
- Goal is to improve the accuracy of the branching fraction measurement of $B^- \rightarrow D^0 \pi^- \pi^+ \pi^-$.



Formalism & Approach

- The BF measurements are based on the following equations:

$$\mathcal{B}(B^+ \rightarrow \bar{D}^0 \pi^+ \pi^- \pi^+) = \frac{N_{sig}}{2 \cdot \varepsilon \cdot L \cdot \sigma_{B^+ B^-} \cdot \mathcal{B}(\bar{D}^0 \rightarrow K^+ \pi^-)}$$

- Data Set: MC14ri_a inclusive MC ($100 fb^{-1}$)

- **Track selection:**

- ▶ Transverse impact parameter $|d_0| < 0.2$ cm.
- ▶ Longitudinal impact parameter $|z_0| < 1$ cm.
- ▶ Polar angle $\rightarrow 0 < \theta < 126.87$: $\cos\theta \geq -0.6$

- Selection on kinematic variables:

- ▶ Mass of D^0 meson: $1.84 < M < 1.89$ GeV/c²
- ▶ Beam constrained mass (M_{bc}) > 5.27 GeV/c², defined as

$$M_{bc} = \sqrt{E_{beam}^2 - (\Sigma \vec{p}_i)^2}$$

- ▶ Beam-energy Difference $|\Delta E| < 0.15$ GeV, defined as $\Delta E = \Sigma E_i - E_{beam}$.

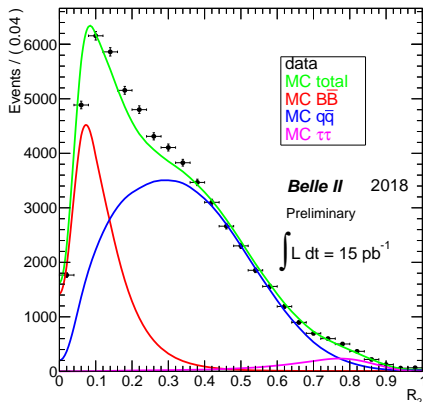


Continuum Suppression

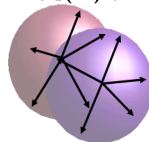
- R_2 : Ratio of second and zeroth Fox-Wolfram moment.

$$H_l = \sum_{ij} \boxed{p_i} \boxed{p_j} \boxed{P_l(\cos\theta_{ij})}$$

$i, j = \text{charged } \& \gamma$ Momentum of particle i and j Legendre polynomial Angle between particle i and j

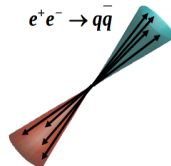


$e^+e^- \rightarrow \Upsilon(4S) \rightarrow B\bar{B}$



Spherical

$e^+e^- \rightarrow q\bar{q}$



Jet-like

- Spherical limit: $R_2 \rightarrow 0$; jet-like limit: $R_2 \rightarrow 1$.
- So we are on $\Upsilon(4S)$ resonance and recording $B\bar{B}$ pairs.

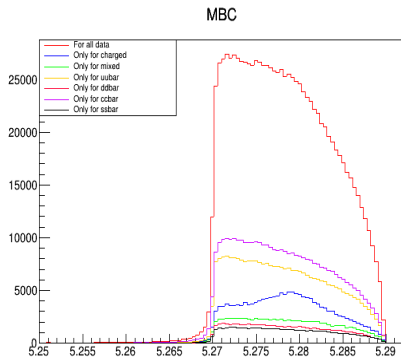
M_{bc} 

Figure: Plotting M_{bc} for different set

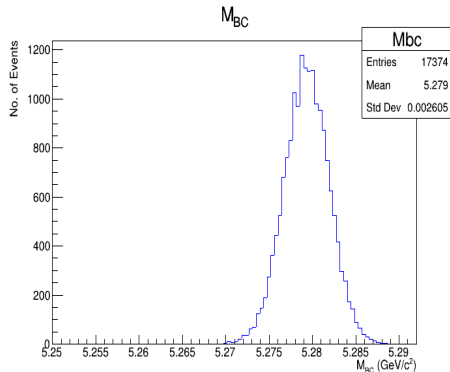


Figure: Plotting M_{bc} for signal

Delta E

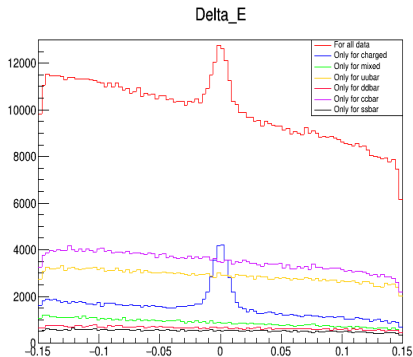


Figure: Plotting ΔE for different set

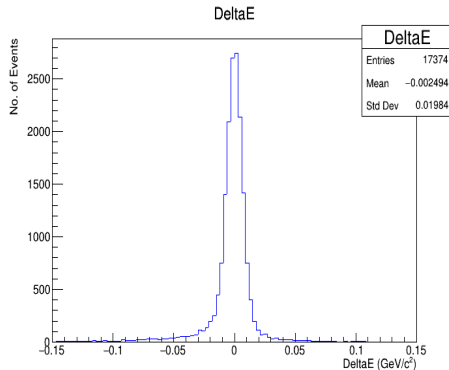
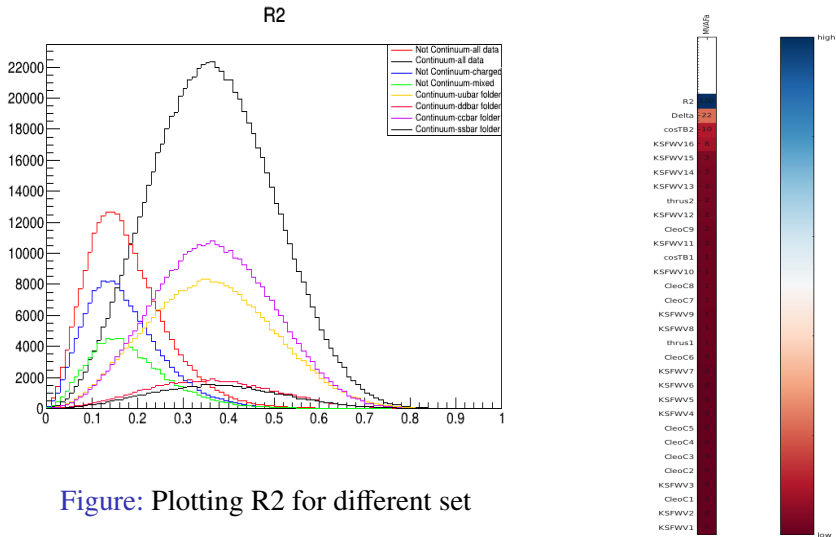
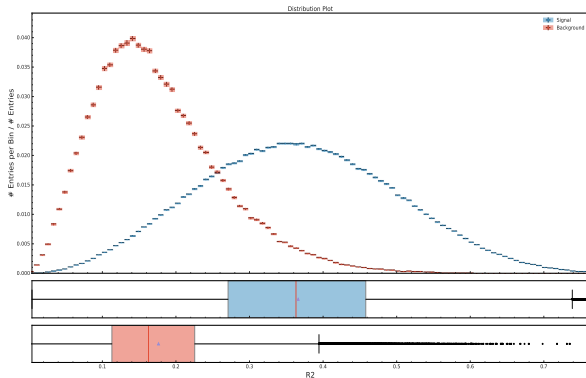


Figure: Plotting ΔE for signal





FBDT output of R2 variable



● Future plan:

- ▶ Train FBDT in various way to get better cuts for continuum suppression.
- ▶ Finding all $B\bar{B}$ mesons using Hadronic and Semileptonic tag in FEI.



- The Belle II Physics Book (KEK Preprint 2018-27)
- The Physics of the B Factories (KEK Preprint 2014-3)
- Observables for the Analysis of Event Shapes in e^+e^- Annihilation and Other Processes (1978)(7811220, CALT-688680)
- Belle II Software Documentation→ software.belle2.org
- Root Data Analysis Framework user Guide→ <https://root.cern/>

Thank you!

