

Title: Cohen-Sutherland line clipping algorithm

Problem statement: write a C++ program to implement Cohen-Sutherland line clipping algorithm.

Learning Outcomes:

- ① learn Cohen-Sutherland line clipping algorithm
- ② Implement the algorithm

Software & Hardware Requirements:

64-bit open source OS creator
Windows 10 operating system.
8GB RAM, 112GB SSD with 64-bit architecture.

Theory:

① Cohen-Sutherland line clipping algorithm is a 2D line clipping algorithm.

② The main advantage of the algorithm is that it vastly reduces the number of line intersections that were to be calculated in scan conversions.

③ It operates in two phases:

④ Region of code generation

⑤ Line clipping

⑥ Region code-generation

It divides plane into a region & determines the visible portion using outcodes at the end points. Outcode is a four-bit number. Values of the bit is set to 1 if condition is satisfied.



⑦ Set first bit if a point lies above the clipping window i.e. $y > y_{max}$



- ⑤ Self second bit of a point lies to the right of the window i.e. $x > x_{max}$
- ⑥ Self third bit of a point lies to the right of the window i.e. $y < y_{min}$
- ⑦ Self the fourth bit if a point lies left of window i.e. $x < x_{min}$

1001	1000	1010	y_{max}
0001	0000	0010	y_{min}
0101	0100	0110	
x_{min}	x_{max}		

4. Clipping procedure

The algorithm quickly detects two cases if both end points are inside the window then line is completely visible & is accepted. It needs no clipping.

Case I: The line is completely inside window, if logical

② OR operation yields 0000

Case II: If logical OR is not 0000 then there are two possibilities. Either it is completely invisible ① or partially visible

- The line is completely outside the clipping window if logical AND operation of outcode doesn't yield to 0000.
- Above test are performed in the same order i.e. Case II is applicable only if Case I is not true.

Case III:

- if logical AND of the outcode is not 0000 the line is partially invisible therefore it needs to be clipped
- if logical AND of outcode is 0000 the line may/may not pass from clipping window.
- now compare the endpoints of the endpoints of boundary that how much line needs to be accepted



- consider the line with endpoints (x_1, y_1) (x_2, y_2)

$$\text{slope } (m) = \frac{y_2 - y_1}{x_2 - x_1}$$

- Using $y = mx + c$, compute $c = y - mx$.

- As both the points are known 'c' can be known.

- let's put $(x_1, y_1) \Rightarrow c = y_1 - mx_1$

The co-ordinate of an intersection with a vertical window boundary can be calculated as $y = mx + c$. i.e. either x_{\min} or x_{\max} , depends on the which vertical line we are calculating y .

$$y = mx_{\min} + c \quad \text{left edge}$$

$$y = mx_{\max} + c \quad \text{right edge}$$

- Similarly, x-coordinate of an intersection with a horizontal window can be computed as.

$$x = \frac{y_{\min} - c}{m} \quad \text{bottom edge}$$

$$x = \frac{y_{\max} - c}{m} \quad \text{top edge}$$

* Algorithm

1. Start

2. Read (x_{\min}, y_{\min}) & (x_{\max}, y_{\max})

for lower left & top right corner of clipping window.

3. Read $A(x_1, y_1)$ & $B(x_2, y_2)$ end points of the line.

4. Compute Outcode of A & B

if $y_1 > y_{\max}$ then, outcode $A(1) = 1$ else 0.

if $y_1 < y_{\min}$ then, outcode $A(2) = 1$ else 0

if $x_1 > x_{\max}$ then, outcode $A(3) = 1$ else 0

if $x_1 < x_{\min}$ then, outcode $A(4) = 1$ else 0

if $y_2 > y_{\max}$ then, outcode $A(5) = 1$ else 0


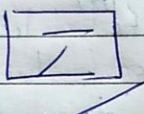
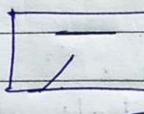
if $x_2 > x_{\max}$ then, outcode $A(6) = 1$ else 0

if $y_2 < y_{\min}$ then, outcode $A(7) = 1$ else 0

if $x_2 < x_{\min}$ then, outcode $A(8) = 1$ else 0

5. If outcode A or outcode B = 0000 then display entire line, go to step 5.
- else if outcode A & outcode B \neq 0000 then reject the entire line.
- Else compute the intersection point with window boundaries.
6. Repeat step 4.
6. End program

Test Cases

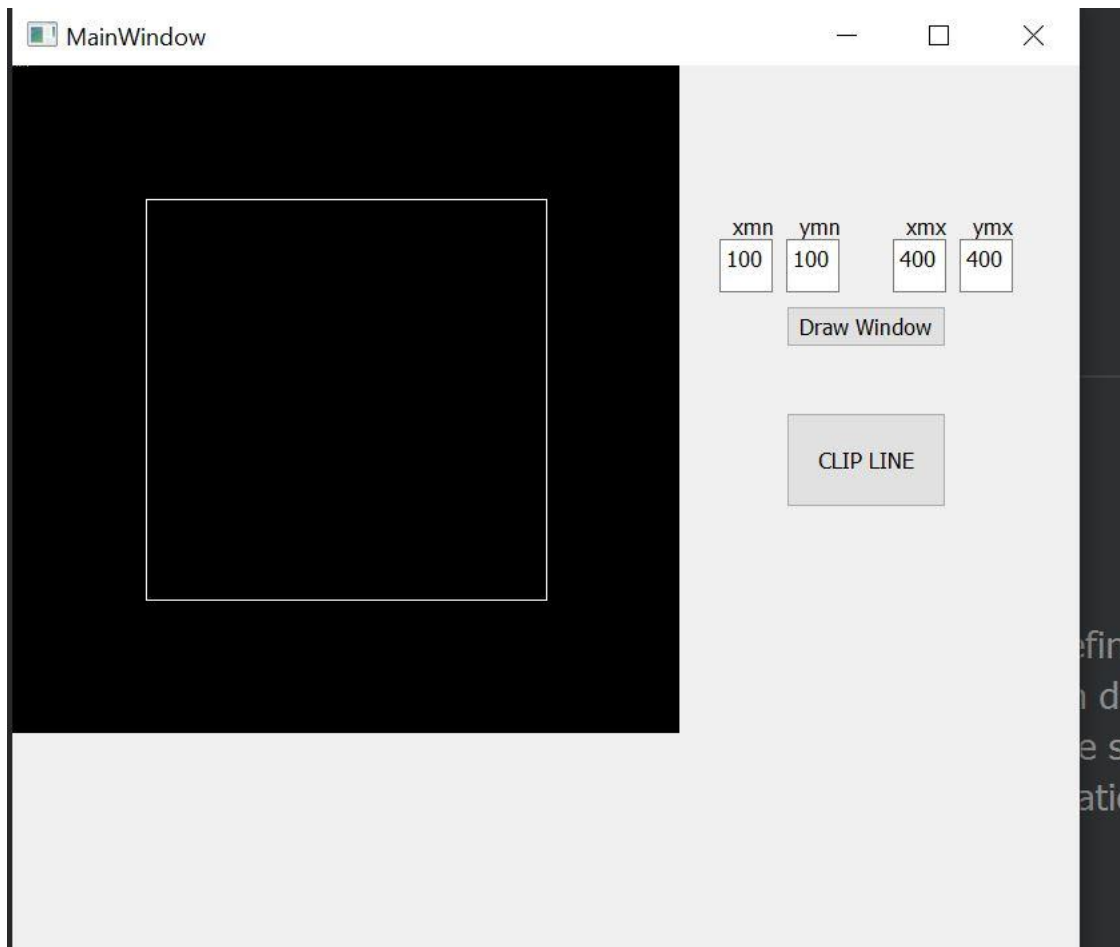
Test No.	Input	Expected output	Actual o/p	Result
1				Pass

Conclusion

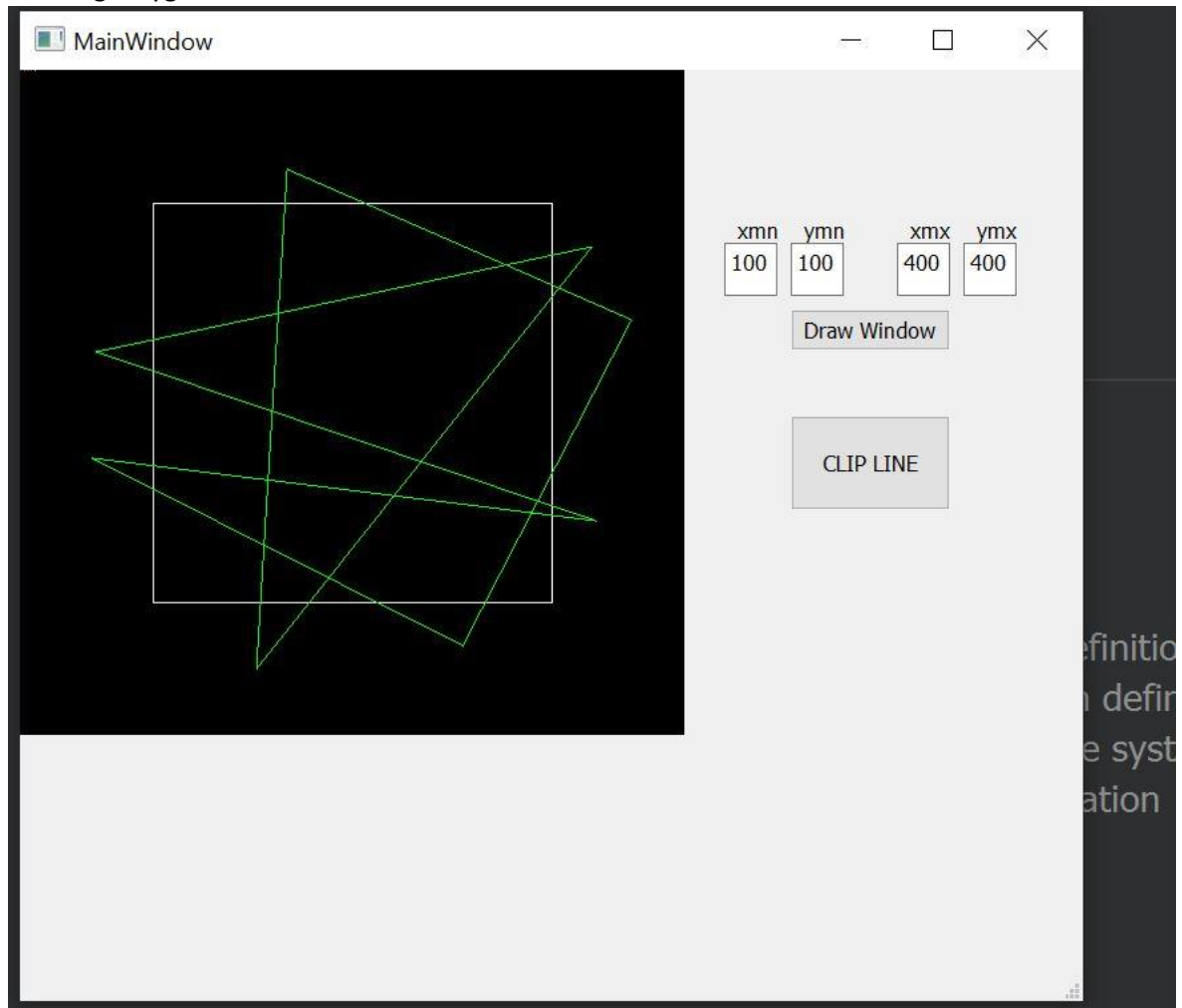
We understood the concept of Cohen-Sutherland line clipping algorithm & were able to implement it.

Output:

1. Drawing Window



2. Drawing Polygon



3. Clipping Polygon using cohen Sutherland line clipping algorithm

