## Assignment - 1

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## **PROBLEM**

1. The co-ordinates of points A,B are  $(r_1,\theta_1)$ ,  $(r_2,\theta_2)$  referred to O as pole. The internal bisector of angle AOB meets the line AB in D. Find the co-ordinates of D.

## SOLUTION

Let the co-ordinates of point D be  $\binom{r}{\theta}$ .

Now, 
$$\theta = \frac{\theta_1 + \theta_2}{2}$$

$$Since, Area(\triangle AOD) + Area(\triangle DOB) = Area(\triangle AOB)$$
 (1)

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$$\frac{1}{2}||(r_1) \times (r \times sin(\frac{\theta}{2}))|| + \frac{1}{2}||(r_2) \times (r \times sin(\frac{\theta}{2}))|| = \frac{1}{2}||(r_1) \times (r_2 \times sin(\frac{\theta}{2}))||$$
(2)

Now, R.H.S = 
$$\frac{1}{2} ||(r_1) \times (r_2 \times sin(\theta))||$$

$$= \frac{1}{2} \| (r_1) \times (r_2 \times 2 \times \sin(\frac{\theta}{2}) \times \cos(\frac{\theta}{2})) \|$$
 (3)

On Comparing (2) and (3),

$$\therefore \frac{1}{2} \times ||r \times (r_1 + r_2)|| = ||r_1 \times r_2 \times \cos(\frac{\theta}{2})||$$
 (4)

Now , D has co-ordinates as  $\begin{pmatrix} r \\ \theta \end{pmatrix}$ 

$$\therefore \text{ Co-ordinates of } D \text{ are } \left( \frac{2r_1 \times r_2}{r_1 + r_2} \times \cos(\frac{\theta}{2}) \right)$$