

In [1]:

```
%matplotlib inline
import warnings
warnings.filterwarnings("ignore")
import numpy as np;
import pandas as pd
import matplotlib.pyplot as plt
from sklearn.datasets import load_boston
from sklearn import preprocessing
from sklearn.metrics import mean_squared_error as MSE
#getting boston house price data from sklearn
boston = load_boston()
```

In [2]:

```
#finding no of datapoints in boston data
print(type(boston['data']))
X = pd.DataFrame(data=boston['data'], columns=boston['feature_names']);
print("Shape of feature matrix: ", X.shape)
print(X.head(5))

print('*'*100)

y = pd.DataFrame(np.array(boston['target']))
print("Shape of output matrix", y.shape)
```

<class 'numpy.ndarray'>

Shape of feature matrix: (506, 13)

	CRIM	ZN	INDUS	CHAS	NOX	RM	AGE	DIS	RAD	TAX	\
0	0.00632	18.0	2.31	0.0	0.538	6.575	65.2	4.0900	1.0	296.0	
1	0.02731	0.0	7.07	0.0	0.469	6.421	78.9	4.9671	2.0	242.0	
2	0.02729	0.0	7.07	0.0	0.469	7.185	61.1	4.9671	2.0	242.0	
3	0.03237	0.0	2.18	0.0	0.458	6.998	45.8	6.0622	3.0	222.0	
4	0.06905	0.0	2.18	0.0	0.458	7.147	54.2	6.0622	3.0	222.0	

	PTRATIO	B	LSTAT
0	15.3	396.90	4.98
1	17.8	396.90	9.14
2	17.8	392.83	4.03
3	18.7	394.63	2.94
4	18.7	396.90	5.33

Shape of output matrix (506, 1)



In [3]:

```
scaler = preprocessing.StandardScaler().fit(X)
X = scaler.transform(X)
X = pd.DataFrame(data=X, columns=boston['feature_names'])
X.head()
```

Out[3]:

	CRIM	ZN	INDUS	CHAS	NOX	RM	AGE	DIS	RAD	TAX	PTRATIO	B	LSTAT
0	0.419782	0.284830	1.287909	0.272599	0.144217	0.413672	0.120013	0.140214	0.982843	0.666608	1.459000	0.441052	1.075562
1	0.417339	0.487722	0.593381	0.272599	0.740262	0.194274	0.367166	0.557160	0.867883	0.987329	0.303094	0.441052	0.492439
2	0.417342	0.487722	0.593381	0.272599	0.740262	1.282714	0.265812	0.557160	0.867883	0.987329	0.303094	0.396427	1.208727
3	0.416750	0.487722	1.306878	0.272599	0.835284	1.016303	0.809889	1.077737	0.752922	1.106115	0.113032	0.416163	1.361517
4	0.412482	0.487722	1.306878	0.272599	0.835284	1.228577	0.511180	1.077737	0.752922	1.106115	0.113032	0.441052	1.026501

In [53]:

```
k = X.values;
k[1][2]
```

Out[53]:

-0.5933810131002436

In [12]:

```
class LinearRegression():
    def __init__(self, X, y, plot_error_per_iteration = False):
        self.X = X
        self.y = y #dimension: n*1
        self.data = pd.concat([X, y], axis=1);
        self.lr = 0.01 #defining learning rate
        self.b = np.random.normal(0,1,1);
        self.w = np.ones((self.X.shape[1], 1)) #generating intial weight vector of dimension 1*d, w
here d is no of columns/features
        self.MSE_list = [];
        self.plot_error_per_iteration = plot_error_per_iteration
        self.n_iterations=500

    def matrixMultiplication1(self, x, y):
        # y = pd.DataFrame(y)
        rows = x.shape[0];
        columns = y.shape[1];
        rows2 = y.shape[0]
        result = [];
        for i in range(rows):
            med_res = [];
            for j in range(columns):
                temp = 0;
                for k in range(rows2):
                    temp = temp + (x[i, k] * y[k, j]);
                med_res.append(temp);
                temp = 0;
            result.append(med_res);
        return np.array(result);

    def matrixMultiplication(self, x, y):
        a = np.tile(y[0], (x.shape[0],1))
        res = x * a;
        res = np.sum(res, axis=1)
        res = res.reshape(-1, 1)
        return res;

    def computeDerivative(self, X, y):
        """
        function to obtain derivative value which is  $-2 * x * (y - W_T * X)$ 
        """
        X = X.values;
        y = y.values;
        wT_x = np.dot(X, self.w) #calculating x * w => multiplying X(n*d - dim) with weight(d*1), ou
tput will be of n*1 - dim
        y_wT_x = y - (wT_x + self.b) #calculating y - (w_t * x) => output will be of dimension n*1
        x_prod = -2 * X;
        der = (x_prod*y_wT_x).sum(axis=0).reshape(-1,1) #der will be of dimension 1 * d
        # print('der ', type(der))
        # print('der',der.shape)
        return self.w - self.lr * (der / y.shape[0]);

    def computeIntercept(self, X, y):
        """
        function to compute new intercept
        """
        X = X.values;
        y = y.values;
        wT_x = np.dot(X, self.w) #calculating x * w => multiplying X(n*d - dim) with weight(d*1), ou
tput will be of n*1 - dim
        y_wT_x = y - (wT_x + self.b) #calculating y - (w_t * x) => output will be of dimension n*1
        y_prod = -2 * y_wT_x
        # print(y_prod.shape)
```

```

intercept = y_prod.sum(axis=0).reshape(-1,1)
#print('intercept',intercept.shape)
#intercept = intercept[0]
diff_in_intercept = self.b - self.lr * (intercept / y_prod.shape[0])
# print(type(diff_in_intercept))
return diff_in_intercept

def predict(self, X):
    """
    function to predict output given query points
    """
    wT_x = np.dot(self.w.T, X.T)
    y = wT_x + self.b;
    return y.T

def addMSE(self, ):
    """
    function to add mean squared error for each W, obtain in each iteration
    """
    y_pred = self.predict(self.X);
    self.MSE_list.append(MSE(y, y_pred));

def plotError(self, ):
    """
    function to plot error
    """
    plt.plot(np.arange(0, len(self.MSE_list)), self.MSE_list);
    plt.ylabel('MSE');
    plt.xlabel('iterations')
    plt.grid();
    plt.show();

def fit(self, ):
    while self.n_iterations>0:
        sample_data = self.data.sample(n=30)
        X = sample_data.loc[:, sample_data.columns != 0];
        y = sample_data.loc[:, [0]]
        new_w = self.computeDerivative(X, y);
        new_b = self.computeIntercept(X, y);
        if (np.all(new_w - self.w) < 0.00001 and np.all(new_b - self.b) < 0.00001):
            self.w = new_w
            self.b = new_b
            if self.plot_error_per_iteration:
                self.addMSE();
                self.plotError();
            break
        else:
            #self.lr /= 2
            self.w = new_w
            self.b = new_b
            self.n_iterations-=1
            if self.plot_error_per_iteration:
                self.addMSE()

```

In [13]:

```

LR = LinearRegression(X, y, plot_error_per_iteration=True);
LR.fit()
y_pred = LR.predict(X);
self_model_error = MSE(y, y_pred)
print(self_model_error)

```

22.368216627128106

In [14]:

```

from sklearn import linear_model
model = linear_model.SGDRegressor(penalty='none');
model.fit(X, y);
y_pred = model.predict(X);
sgd_model_error = MSE(y, y_pred)
print(sgd_model_error)

```

22.87212701556153

22.87212701556153

In [15]:

```
from prettytable import PrettyTable

x = PrettyTable()
x.field_names = ["Model", "Mean squared error"]
x.add_row(["SGDRegressor", sgd_model_error])
x.add_row(["our created model",self_model_error ])
print(x)
```

```
+-----+-----+
|      Model      | Mean squared error |
+-----+-----+
|  SGDRegressor   | 22.87212701556153  |
| our created model | 22.368216627128106 |
+-----+-----+
```

In []: