FullyConnectedNets

October 30, 2021

```
[]: # This mounts your Google Drive to the Colab VM.
from google.colab import drive
drive.mount('/content/gdrive', force_remount=True)

# TODO: Enter the foldername in your Drive where you have saved the unzipped
# assignment folder, e.g. 'cs231n/assignments/assignment1/'
FOLDERNAME = 'Coursework/Fall 2021/682/Assignments/assignment2'
assert FOLDERNAME is not None, "[!] Enter the foldername."

# Now that we've mounted your Drive, this ensures that
# the Python interpreter of the Colab VM can load
# python files from within it.
import sys
sys.path.append('/content/gdrive/My Drive/{}'.format(FOLDERNAME))
```

Mounted at /content/gdrive

```
[]: # This downloads the CIFAR-10 dataset to your Drive
# if it doesn't already exist.
%cd gdrive/My\ Drive/$FOLDERNAME/cs682/datasets/
!bash get_datasets.sh
#Switch to working directory
%cd /content/gdrive/My\ Drive/$FOLDERNAME
```

```
2021-10-29 17:28:50 (40.9 MB/s) - cifar-10-python.tar.gz saved [170498071/170498071]

cifar-10-batches-py/
cifar-10-batches-py/data_batch_4
cifar-10-batches-py/readme.html
cifar-10-batches-py/test_batch
cifar-10-batches-py/data_batch_3
cifar-10-batches-py/batches.meta
cifar-10-batches-py/data_batch_2
cifar-10-batches-py/data_batch_5
cifar-10-batches-py/data_batch_1
/content/gdrive/My Drive/Coursework/Fall 2021/682/Assignments/assignment2
```

```
[]: %cd cs682/
!python setup.py build_ext --inplace
```

/content/gdrive/My Drive/Coursework/Fall 2021/682/Assignments/assignment2/cs682 running build_ext

1 Fully-Connected Neural Nets

In the previous homework you implemented a fully-connected two-layer neural network on CIFAR-10. The implementation was simple but not very modular since the loss and gradient were computed in a single monolithic function. This is manageable for a simple two-layer network, but would become impractical as we move to bigger models. Ideally we want to build networks using a more modular design so that we can implement different layer types in isolation and then snap them together into models with different architectures.

In this exercise we will implement fully-connected networks using a more modular approach. For each layer we will implement a forward and a backward function. The forward function will receive inputs, weights, and other parameters and will return both an output and a cache object storing data needed for the backward pass, like this:

```
def layer_forward(x, w):
    """ Receive inputs x and weights w """
    # Do some computations ...
    z = # ... some intermediate value
    # Do some more computations ...
    out = # the output

cache = (x, w, z, out) # Values we need to compute gradients
    return out, cache
```

The backward pass will receive upstream derivatives and the cache object, and will return gradients with respect to the inputs and weights, like this:

```
def layer_backward(dout, cache):
    """"
    Receive dout (derivative of loss with respect to outputs) and cache,
    and compute derivative with respect to inputs.
    """"
    # Unpack cache values
    x, w, z, out = cache

# Use values in cache to compute derivatives
    dx = # Derivative of loss with respect to x
    dw = # Derivative of loss with respect to w
return dx, dw
```

After implementing a bunch of layers this way, we will be able to easily combine them to build classifiers with different architectures.

In addition to implementing fully-connected networks of arbitrary depth, we will also explore different update rules for optimization, and introduce Dropout as a regularizer and Batch/Layer Normalization as a tool to more efficiently optimize deep networks.

```
[]: # As usual, a bit of setup
   from __future__ import print_function
   import time
   import numpy as np
   import matplotlib.pyplot as plt
   from cs682.classifiers.fc_net import *
   from cs682.data utils import get CIFAR10 data
   from cs682.gradient_check import eval_numerical_gradient,_
    →eval_numerical_gradient_array
   from cs682.solver import Solver
   %matplotlib inline
   plt.rcParams['figure.figsize'] = (10.0, 8.0) # set default size of plots
   plt.rcParams['image.interpolation'] = 'nearest'
   plt.rcParams['image.cmap'] = 'gray'
   # for auto-reloading external modules
   # see http://stackoverflow.com/questions/1907993/
    \rightarrow autoreload-of-modules-in-ipython
   %load ext autoreload
   %autoreload 2
   def rel_error(x, y):
     """ returns relative error """
     return np.max(np.abs(x - y) / (np.maximum(1e-8, np.abs(x) + np.abs(y))))
[]: #Switch to working directory
   %cd /content/gdrive/My\ Drive/$FOLDERNAME
```

```
[]: # Load the (preprocessed) CIFAR10 data.

data = get_CIFAR10_data()
for k, v in list(data.items()):
    print(('%s: ' % k, v.shape))

('X_train: ', (49000, 3, 32, 32))
('y_train: ', (49000,))
('X_val: ', (1000, 3, 32, 32))
('y_val: ', (1000,))
('X_test: ', (1000,))
('y_test: ', (1000,))
```

2 Affine layer: foward

Open the file cs682/layers.py and implement the affine_forward function.

Once you are done you can test your implementation by running the following:

```
[]: # Test the affine forward function
   num inputs = 2
   input\_shape = (4, 5, 6)
   output dim = 3
   input_size = num_inputs * np.prod(input_shape)
   weight_size = output_dim * np.prod(input_shape)
   x = np.linspace(-0.1, 0.5, num=input_size).reshape(num_inputs, *input_shape)
   w = np.linspace(-0.2, 0.3, num=weight_size).reshape(np.prod(input_shape),_
    →output dim)
   b = np.linspace(-0.3, 0.1, num=output dim)
   out, _ = affine_forward(x, w, b)
   correct_out = np.array([[ 1.49834967, 1.70660132, 1.91485297],
                            [ 3.25553199, 3.5141327, 3.77273342]])
   # Compare your output with ours. The error should be around e-9 or less.
   print('Testing affine_forward function:')
   print('difference: ', rel_error(out, correct_out))
```

Testing affine_forward function: difference: 9.769849468192957e-10

3 Affine layer: backward

Now implement the affine_backward function and test your implementation using numeric gradient checking.

```
[]: # Test the affine backward function
   np.random.seed(231)
   x = np.random.randn(10, 2, 3)
   w = np.random.randn(6, 5)
   b = np.random.randn(5)
   dout = np.random.randn(10, 5)
   dx_num = eval_numerical_gradient_array(lambda x: affine_forward(x, w, b)[0], x,_
    →dout)
   dw_num = eval_numerical_gradient_array(lambda w: affine_forward(x, w, b)[0], w,_
    dout) →
   db_num = eval_numerical_gradient_array(lambda b: affine_forward(x, w, b)[0], b,_
    ⇔dout)
   _, cache = affine_forward(x, w, b)
   dx, dw, db = affine_backward(dout, cache)
   # The error should be around e-10 or less
   print('Testing affine_backward function:')
   print('dx error: ', rel_error(dx_num, dx))
   print('dw error: ', rel error(dw num, dw))
   print('db error: ', rel_error(db_num, db))
```

Testing affine_backward function: dx error: 5.399100368651805e-11 dw error: 9.904211865398145e-11 db error: 2.4122867568119087e-11

4 ReLU activation: forward

Implement the forward pass for the ReLU activation function in the relu_forward function and test your implementation using the following:

```
print('Testing relu_forward function:')
print('difference: ', rel_error(out, correct_out))
```

```
Testing relu_forward function: difference: 4.999999798022158e-08
```

5 ReLU activation: backward

Now implement the backward pass for the ReLU activation function in the relu_backward function and test your implementation using numeric gradient checking:

```
[]: np.random.seed(231)
    x = np.random.randn(10, 10)
    dout = np.random.randn(*x.shape)

dx_num = eval_numerical_gradient_array(lambda x: relu_forward(x)[0], x, dout)

_, cache = relu_forward(x)
    dx = relu_backward(dout, cache)

# The error should be on the order of e-12
    print('Testing relu_backward function:')
    print('dx error: ', rel_error(dx_num, dx))
```

```
Testing relu_backward function: dx error: 3.2756349136310288e-12
```

5.1 Inline Question 1:

We've only asked you to implement ReLU, but there are a number of different activation functions that one could use in neural networks, each with its pros and cons. In particular, an issue commonly seen with activation functions is getting zero (or close to zero) gradient flow during backpropagation. Which of the following activation functions have this problem? If you consider these functions in the one dimensional case, what types of input would lead to this behaviour? 1. Sigmoid 2. ReLU 3. Leaky ReLU

5.2 Answer:

- 1. Sigmoid This suffers from vanishing gradient issue at high saturation points for input x, i.e. at high values of x, gradient tends to 0.
- 2. ReLU This function faces an issue where the gradient is killed for values of x less than 0 (Dying gradient). However, it does not face saturation issue in positive region. In a one-dimensional case where all input values are negative, this issue will be faced.
- 3. Leaky ReLU This function is a modified version of ReLU aimed to solve the dying gradient problem. For negative values of x, the function will have some gradient. The only 1-D case where there will be gradient tending to 0 will be when the input is all set to origin (example [0,0,0]).

6 "Sandwich" layers

There are some common patterns of layers that are frequently used in neural nets. For example, affine layers are frequently followed by a ReLU nonlinearity. To make these common patterns easy, we define several convenience layers in the file cs682/layer_utils.py.

For now take a look at the affine_relu_forward and affine_relu_backward functions, and run the following to numerically gradient check the backward pass:

```
[]: from cs682.layer_utils import affine_relu_forward, affine_relu_backward
   np.random.seed(231)
   x = np.random.randn(2, 3, 4)
   w = np.random.randn(12, 10)
   b = np.random.randn(10)
   dout = np.random.randn(2, 10)
   out, cache = affine_relu_forward(x, w, b)
   dx, dw, db = affine_relu_backward(dout, cache)
   dx_num = eval_numerical_gradient_array(lambda x: affine_relu_forward(x, w,__
    \rightarrowb)[0], x, dout)
   dw_num = eval_numerical_gradient_array(lambda w: affine_relu_forward(x, w,__
    \rightarrowb)[0], w, dout)
   db_num = eval_numerical_gradient_array(lambda b: affine_relu_forward(x, w,_
    \rightarrowb)[0], b, dout)
   # Relative error should be around e-10 or less
   print('Testing affine_relu_forward and affine_relu_backward:')
   print('dx error: ', rel error(dx num, dx))
   print('dw error: ', rel_error(dw_num, dw))
   print('db error: ', rel_error(db_num, db))
```

Testing affine_relu_forward and affine_relu_backward:

dx error: 2.299579177309368e-11 dw error: 8.162011105764925e-11 db error: 7.826724021458994e-12

7 Loss layers: Softmax and SVM

You implemented these loss functions in the last assignment, so we'll give them to you for free here. You should still make sure you understand how they work by looking at the implementations in cs682/layers.py.

You can make sure that the implementations are correct by running the following:

```
[]: np.random.seed(231)
  num_classes, num_inputs = 10, 50
  x = 0.001 * np.random.randn(num_inputs, num_classes)
  y = np.random.randint(num_classes, size=num_inputs)
```

Testing svm_loss:
loss: 8.999602749096233
dx error: 1.4021566006651672e-09
Testing softmax_loss:
loss: 2.302545844500738
dx error: 9.384673161989355e-09

8 Two-layer network

In the previous assignment you implemented a two-layer neural network in a single monolithic class. Now that you have implemented modular versions of the necessary layers, you will reimplement the two layer network using these modular implementations.

Open the file cs682/classifiers/fc_net.py and complete the implementation of the TwoLayerNet class. This class will serve as a model for the other networks you will implement in this assignment, so read through it to make sure you understand the API. You can run the cell below to test your implementation.

```
[]: np.random.seed(231)
N, D, H, C = 3, 5, 50, 7
X = np.random.randn(N, D)
y = np.random.randint(C, size=N)

std = 1e-3
model = TwoLayerNet(input_dim=D, hidden_dim=H, num_classes=C, weight_scale=std)

print('Testing initialization ... ')
W1_std = abs(model.params['W1'].std() - std)
```

```
b1 = model.params['b1']
W2_std = abs(model.params['W2'].std() - std)
b2 = model.params['b2']
assert W1_std < std / 10, 'First layer weights do not seem right'</pre>
assert np.all(b1 == 0), 'First layer biases do not seem right'
assert W2_std < std / 10, 'Second layer weights do not seem right'
assert np.all(b2 == 0), 'Second layer biases do not seem right'
print('Testing test-time forward pass ... ')
model.params['W1'] = np.linspace(-0.7, 0.3, num=D*H).reshape(D, H)
model.params['b1'] = np.linspace(-0.1, 0.9, num=H)
model.params['W2'] = np.linspace(-0.3, 0.4, num=H*C).reshape(H, C)
model.params['b2'] = np.linspace(-0.9, 0.1, num=C)
X = np.linspace(-5.5, 4.5, num=N*D).reshape(D, N).T
scores = model.loss(X)
correct_scores = np.asarray(
  [[11.53165108, 12.2917344, 13.05181771, 13.81190102, 14.57198434, 15.
\rightarrow33206765, 16.09215096],
   [12.05769098, 12.74614105, 13.43459113, 14.1230412, 14.81149128, 15.
→49994135, 16.18839143],
   [12.58373087, 13.20054771, 13.81736455, 14.43418138, 15.05099822, 15.
→66781506, 16.2846319 ]])
scores diff = np.abs(scores - correct scores).sum()
assert scores_diff < 1e-6, 'Problem with test-time forward pass'
print('Testing training loss (no regularization)')
y = np.asarray([0, 5, 1])
loss, grads = model.loss(X, y)
correct_loss = 3.4702243556
assert abs(loss - correct_loss) < 1e-10, 'Problem with training-time loss'
model.reg = 1.0
loss, grads = model.loss(X, y)
correct_loss = 26.5948426952
assert abs(loss - correct_loss) < 1e-10, 'Problem with regularization loss'
# Errors should be around e-7 or less
for reg in [0.0, 0.7]:
 print('Running numeric gradient check with reg = ', reg)
 model.reg = reg
 loss, grads = model.loss(X, y)
 for name in sorted(grads):
   f = lambda : model.loss(X, y)[0]
   grad_num = eval_numerical_gradient(f, model.params[name], verbose=False)
   print('%s relative error: %.2e' % (name, rel error(grad num, grads[name])))
```

```
Testing initialization ...

Testing test-time forward pass ...

Testing training loss (no regularization)

Running numeric gradient check with reg = 0.0

W1 relative error: 1.83e-08

W2 relative error: 3.12e-10

b1 relative error: 9.83e-09

b2 relative error: 4.33e-10

Running numeric gradient check with reg = 0.7

W1 relative error: 2.53e-07

W2 relative error: 2.85e-08

b1 relative error: 1.56e-08

b2 relative error: 7.76e-10
```

9 Solver

In the previous assignment, the logic for training models was coupled to the models themselves. Following a more modular design, for this assignment we have split the logic for training models into a separate class.

Open the file cs682/solver.py and read through it to familiarize yourself with the API. After doing so, use a Solver instance to train a TwoLayerNet that achieves at least 50% accuracy on the validation set.

```
[]: model = TwoLayerNet()
 solver = None
 # TODO: Use a Solver instance to train a TwoLayerNet that achieves at least #
 # 50% accuracy on the validation set.
 solver = Solver(model, data,
            update_rule='sgd',
            optim_config={
             'learning_rate': 1e-3,
            },
            lr_decay=0.95,
            num_epochs=10, batch_size=100,
            print_every=100)
 solver.train()
 END OF YOUR CODE
  ~~~~~
```

```
(Iteration 1 / 4900) loss: 2.304060
(Epoch 0 / 10) train acc: 0.116000; val_acc: 0.094000
(Iteration 101 / 4900) loss: 1.829613
(Iteration 201 / 4900) loss: 1.857390
(Iteration 301 / 4900) loss: 1.744448
```

```
(Iteration 401 / 4900) loss: 1.420187
(Epoch 1 / 10) train acc: 0.407000; val_acc: 0.422000
(Iteration 501 / 4900) loss: 1.565913
(Iteration 601 / 4900) loss: 1.700510
(Iteration 701 / 4900) loss: 1.732213
(Iteration 801 / 4900) loss: 1.688361
(Iteration 901 / 4900) loss: 1.439529
(Epoch 2 / 10) train acc: 0.497000; val_acc: 0.468000
(Iteration 1001 / 4900) loss: 1.385772
(Iteration 1101 / 4900) loss: 1.278401
(Iteration 1201 / 4900) loss: 1.641580
(Iteration 1301 / 4900) loss: 1.438847
(Iteration 1401 / 4900) loss: 1.172536
(Epoch 3 / 10) train acc: 0.490000; val_acc: 0.466000
(Iteration 1501 / 4900) loss: 1.346286
(Iteration 1601 / 4900) loss: 1.268492
(Iteration 1701 / 4900) loss: 1.318215
(Iteration 1801 / 4900) loss: 1.395750
(Iteration 1901 / 4900) loss: 1.338233
(Epoch 4 / 10) train acc: 0.532000; val acc: 0.497000
(Iteration 2001 / 4900) loss: 1.343165
(Iteration 2101 / 4900) loss: 1.393173
(Iteration 2201 / 4900) loss: 1.276734
(Iteration 2301 / 4900) loss: 1.287951
(Iteration 2401 / 4900) loss: 1.352778
(Epoch 5 / 10) train acc: 0.525000; val_acc: 0.475000
(Iteration 2501 / 4900) loss: 1.390234
(Iteration 2601 / 4900) loss: 1.276361
(Iteration 2701 / 4900) loss: 1.111768
(Iteration 2801 / 4900) loss: 1.271688
(Iteration 2901 / 4900) loss: 1.272039
(Epoch 6 / 10) train acc: 0.546000; val_acc: 0.509000
(Iteration 3001 / 4900) loss: 1.304489
(Iteration 3101 / 4900) loss: 1.346667
(Iteration 3201 / 4900) loss: 1.325510
(Iteration 3301 / 4900) loss: 1.392728
(Iteration 3401 / 4900) loss: 1.402001
(Epoch 7 / 10) train acc: 0.567000; val acc: 0.505000
(Iteration 3501 / 4900) loss: 1.319024
(Iteration 3601 / 4900) loss: 1.153287
(Iteration 3701 / 4900) loss: 1.180922
(Iteration 3801 / 4900) loss: 1.093164
(Iteration 3901 / 4900) loss: 1.135902
(Epoch 8 / 10) train acc: 0.568000; val_acc: 0.490000
(Iteration 4001 / 4900) loss: 1.191735
(Iteration 4101 / 4900) loss: 1.359396
(Iteration 4201 / 4900) loss: 1.227283
(Iteration 4301 / 4900) loss: 1.024113
```

```
(Iteration 4401 / 4900) loss: 1.327583

(Epoch 9 / 10) train acc: 0.592000; val_acc: 0.504000

(Iteration 4501 / 4900) loss: 0.963330

(Iteration 4601 / 4900) loss: 1.445619

(Iteration 4701 / 4900) loss: 1.007542

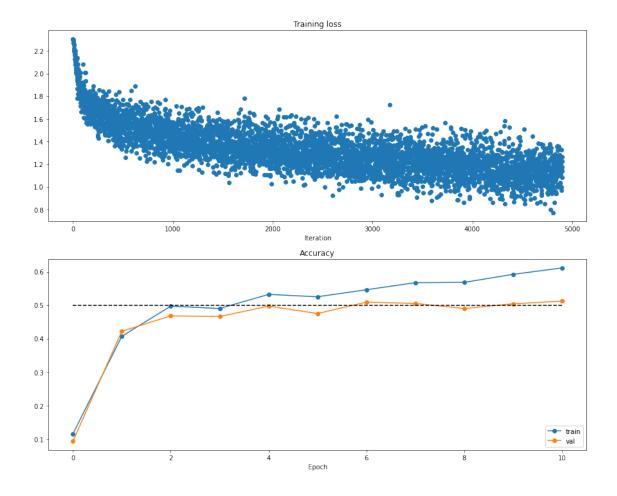
(Iteration 4801 / 4900) loss: 1.005175

(Epoch 10 / 10) train acc: 0.611000; val_acc: 0.512000
```

```
[]: # Run this cell to visualize training loss and train / val accuracy

plt.subplot(2, 1, 1)
plt.title('Training loss')
plt.plot(solver.loss_history, 'o')
plt.xlabel('Iteration')

plt.subplot(2, 1, 2)
plt.title('Accuracy')
plt.plot(solver.train_acc_history, '-o', label='train')
plt.plot(solver.val_acc_history, '-o', label='val')
plt.plot([0.5] * len(solver.val_acc_history), 'k--')
plt.xlabel('Epoch')
plt.legend(loc='lower right')
plt.gcf().set_size_inches(15, 12)
plt.show()
```



10 Multilayer network

Next you will implement a fully-connected network with an arbitrary number of hidden layers. Read through the FullyConnectedNet class in the file cs682/classifiers/fc_net.py.

Implement the initialization, the forward pass, and the backward pass. For the moment don't worry about implementing dropout or batch/layer normalization; we will add those features soon.

10.1 Initial loss and gradient check

As a sanity check, run the following to check the initial loss and to gradient check the network both with and without regularization. Do the initial losses seem reasonable?

For gradient checking, you should expect to see errors around 1e-7 or less.

```
[]: np.random.seed(231)
N, D, H1, H2, C = 2, 15, 20, 30, 10
X = np.random.randn(N, D)
y = np.random.randint(C, size=(N,))
```

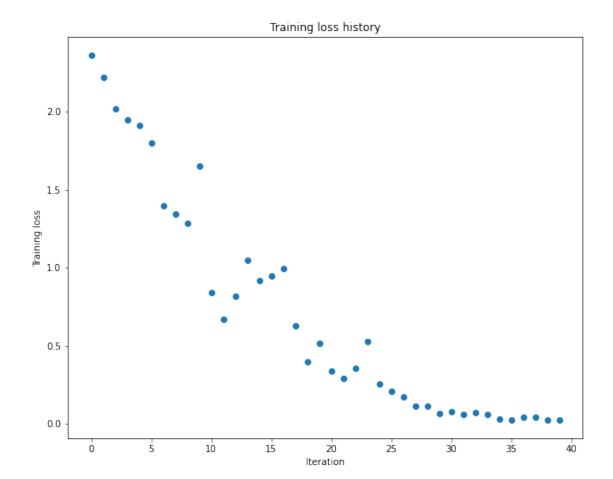
```
Running check with reg = 0
Initial loss: 2.3004790897684924
W1 relative error: 1.48e-07
W2 relative error: 2.21e-05
W3 relative error: 3.53e-07
b1 relative error: 5.38e-09
b2 relative error: 2.09e-09
b3 relative error: 5.80e-11
Running check with reg = 3.14
Initial loss: 7.052114776533016
W1 relative error: 7.36e-09
W2 relative error: 6.87e-08
W3 relative error: 3.48e-08
b1 relative error: 1.48e-08
b2 relative error: 1.72e-09
b3 relative error: 1.80e-10
```

As another sanity check, make sure you can overfit a small dataset of 50 images. First we will try a three-layer network with 100 units in each hidden layer. In the following cell, tweak the learning rate and initialization scale to overfit and achieve 100% training accuracy within 20 epochs.

```
[]: # TODO: Use a three-layer Net to overfit 50 training examples by
    # tweaking just the learning rate and initialization scale.

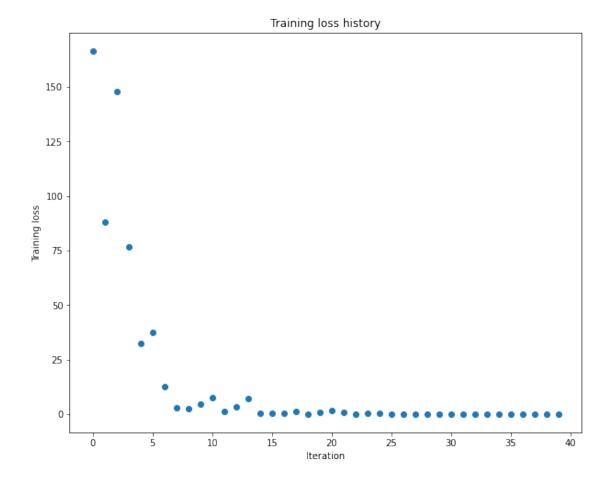
num_train = 50
small_data = {
    'X_train': data['X_train'][:num_train],
    'y_train': data['y_train'][:num_train],
    'X_val': data['X_val'],
    'y_val': data['Y_val'],
}
```

```
(Iteration 1 / 40) loss: 2.363364
(Epoch 0 / 20) train acc: 0.180000; val_acc: 0.108000
(Epoch 1 / 20) train acc: 0.320000; val_acc: 0.127000
(Epoch 2 / 20) train acc: 0.440000; val_acc: 0.172000
(Epoch 3 / 20) train acc: 0.500000; val_acc: 0.184000
(Epoch 4 / 20) train acc: 0.540000; val_acc: 0.181000
(Epoch 5 / 20) train acc: 0.740000; val_acc: 0.190000
(Iteration 11 / 40) loss: 0.839976
(Epoch 6 / 20) train acc: 0.740000; val acc: 0.187000
(Epoch 7 / 20) train acc: 0.740000; val acc: 0.183000
(Epoch 8 / 20) train acc: 0.820000; val_acc: 0.177000
(Epoch 9 / 20) train acc: 0.860000; val_acc: 0.200000
(Epoch 10 / 20) train acc: 0.920000; val_acc: 0.191000
(Iteration 21 / 40) loss: 0.337174
(Epoch 11 / 20) train acc: 0.960000; val_acc: 0.189000
(Epoch 12 / 20) train acc: 0.940000; val_acc: 0.180000
(Epoch 13 / 20) train acc: 1.000000; val_acc: 0.199000
(Epoch 14 / 20) train acc: 1.000000; val_acc: 0.199000
(Epoch 15 / 20) train acc: 1.000000; val_acc: 0.195000
(Iteration 31 / 40) loss: 0.075911
(Epoch 16 / 20) train acc: 1.000000; val_acc: 0.182000
(Epoch 17 / 20) train acc: 1.000000; val_acc: 0.201000
(Epoch 18 / 20) train acc: 1.000000; val acc: 0.207000
(Epoch 19 / 20) train acc: 1.000000; val_acc: 0.185000
(Epoch 20 / 20) train acc: 1.000000; val acc: 0.192000
```



Now try to use a five-layer network with 100 units on each layer to overfit 50 training examples. Again you will have to adjust the learning rate and weight initialization, but you should be able to achieve 100% training accuracy within 20 epochs.

```
(Iteration 1 / 40) loss: 166.501707
(Epoch 0 / 20) train acc: 0.240000; val_acc: 0.116000
(Epoch 1 / 20) train acc: 0.240000; val_acc: 0.085000
(Epoch 2 / 20) train acc: 0.340000; val_acc: 0.110000
(Epoch 3 / 20) train acc: 0.460000; val acc: 0.139000
(Epoch 4 / 20) train acc: 0.700000; val_acc: 0.134000
(Epoch 5 / 20) train acc: 0.800000; val_acc: 0.120000
(Iteration 11 / 40) loss: 7.619979
(Epoch 6 / 20) train acc: 0.800000; val_acc: 0.140000
(Epoch 7 / 20) train acc: 0.820000; val_acc: 0.128000
(Epoch 8 / 20) train acc: 0.880000; val_acc: 0.140000
(Epoch 9 / 20) train acc: 0.920000; val_acc: 0.121000
(Epoch 10 / 20) train acc: 0.920000; val_acc: 0.127000
(Iteration 21 / 40) loss: 1.669786
(Epoch 11 / 20) train acc: 0.960000; val acc: 0.131000
(Epoch 12 / 20) train acc: 0.980000; val acc: 0.125000
(Epoch 13 / 20) train acc: 1.000000; val_acc: 0.137000
(Epoch 14 / 20) train acc: 1.000000; val_acc: 0.132000
(Epoch 15 / 20) train acc: 1.000000; val_acc: 0.132000
(Iteration 31 / 40) loss: 0.000445
(Epoch 16 / 20) train acc: 1.000000; val_acc: 0.132000
(Epoch 17 / 20) train acc: 1.000000; val_acc: 0.132000
(Epoch 18 / 20) train acc: 1.000000; val_acc: 0.132000
(Epoch 19 / 20) train acc: 1.000000; val_acc: 0.132000
(Epoch 20 / 20) train acc: 1.000000; val_acc: 0.132000
```



10.2 Inline Question 2:

Did you notice anything about the comparative difficulty of training the three-layer net vs training the five layer net? In particular, based on your experience, which network seemed more sensitive to the initialization scale? Why do you think that is the case?

10.3 Answer:

The 5-layer net is more sensitive to the initialization scale. This is probably due to the fact that as more layers are involved, the changes in gradients deeper into the network are more pronounced, i.e. there are more chances of vanishing gradient or exploding gradient. As we are not normalizing the outputs at each layer, we will see more standard deviation and variance, which propagates and increases as we go deeper into the network.

11 Update rules

So far we have used vanilla stochastic gradient descent (SGD) as our update rule. More sophisticated update rules can make it easier to train deep networks. We will implement a few of the most commonly used update rules and compare them to vanilla SGD.

12 SGD+Momentum

Stochastic gradient descent with momentum is a widely used update rule that tends to make deep networks converge faster than vanilla stochastic gradient descent. See the Momentum Update section at https://compsci682-fa19.github.io/notes/neural-networks-3/#sgd for more information.

Open the file cs682/optim.py and read the documentation at the top of the file to make sure you understand the API. Implement the SGD+momentum update rule in the function sgd_momentum and run the following to check your implementation. You should see errors less than e-8.

```
[]: from cs682.optim import sgd momentum
   N, D = 4, 5
   w = np.linspace(-0.4, 0.6, num=N*D).reshape(N, D)
   dw = np.linspace(-0.6, 0.4, num=N*D).reshape(N, D)
   v = np.linspace(0.6, 0.9, num=N*D).reshape(N, D)
   config = {'learning_rate': 1e-3, 'velocity': v}
   next_w, _ = sgd_momentum(w, dw, config=config)
   expected_next_w = np.asarray([
     [0.1406,
                0.20738947, 0.27417895, 0.34096842, 0.40775789],
     [ 0.47454737, 0.54133684, 0.60812632, 0.67491579, 0.74170526],
     [ 0.80849474, 0.87528421, 0.94207368, 1.00886316, 1.07565263],
     [ 1.14244211, 1.20923158, 1.27602105, 1.34281053, 1.4096
                                                                    11)
   expected velocity = np.asarray([
     [0.5406,
                0.55475789, 0.56891579, 0.58307368, 0.59723158],
     [0.61138947, 0.62554737, 0.63970526, 0.65386316, 0.66802105],
     [0.68217895, 0.69633684, 0.71049474, 0.72465263, 0.73881053],
     [ 0.75296842, 0.76712632, 0.78128421, 0.79544211, 0.8096
   # Should see relative errors around e-8 or less
   print('next_w error: ', rel_error(next_w, expected_next_w))
   print('velocity error: ', rel_error(expected_velocity, config['velocity']))
```

next_w error: 8.882347033505819e-09 velocity error: 4.269287743278663e-09

Once you have done so, run the following to train a six-layer network with both SGD and SGD+momentum. You should see the SGD+momentum update rule converge faster.

```
[]: num_train = 4000
small_data = {
    'X_train': data['X_train'][:num_train],
    'y_train': data['y_train'][:num_train],
    'X_val': data['X_val'],
    'y_val': data['y_val'],
}
solvers = {}
```

```
for update_rule in ['sgd', 'sgd_momentum']:
  print('running with ', update_rule)
  model = FullyConnectedNet([100, 100, 100, 100, 100], weight_scale=5e-2)
  solver = Solver(model, small_data,
                  num_epochs=5, batch_size=100,
                  update_rule=update_rule,
                  optim_config={
                    'learning_rate': 1e-2,
                  },
                  verbose=True)
  solvers[update_rule] = solver
  solver.train()
 print()
plt.subplot(3, 1, 1)
plt.title('Training loss')
plt.xlabel('Iteration')
plt.subplot(3, 1, 2)
plt.title('Training accuracy')
plt.xlabel('Epoch')
plt.subplot(3, 1, 3)
plt.title('Validation accuracy')
plt.xlabel('Epoch')
for update_rule, solver in list(solvers.items()):
 plt.subplot(3, 1, 1);
 plt.plot(solver.loss_history, 'o', label=update_rule);
 plt.subplot(3, 1, 2);
 plt.plot(solver.train_acc_history, '-o', label=update_rule);
 plt.subplot(3, 1, 3);
 plt.plot(solver.val_acc_history, '-o', label=update_rule);
for i in [1, 2, 3]:
 plt.subplot(3, 1, i);
 plt.legend(loc='upper center', ncol=4)
plt.gcf().set_size_inches(15, 15)
plt.show();
```

```
running with sgd
(Iteration 1 / 200) loss: 2.559978
(Epoch 0 / 5) train acc: 0.103000; val_acc: 0.108000
```

```
(Iteration 11 / 200) loss: 2.291086
(Iteration 21 / 200) loss: 2.153591
(Iteration 31 / 200) loss: 2.082693
(Epoch 1 / 5) train acc: 0.277000; val_acc: 0.242000
(Iteration 41 / 200) loss: 2.004172
(Iteration 51 / 200) loss: 2.010409
(Iteration 61 / 200) loss: 2.023753
(Iteration 71 / 200) loss: 2.026621
(Epoch 2 / 5) train acc: 0.352000; val acc: 0.312000
(Iteration 81 / 200) loss: 1.807163
(Iteration 91 / 200) loss: 1.914256
(Iteration 101 / 200) loss: 1.917176
(Iteration 111 / 200) loss: 1.706193
(Epoch 3 / 5) train acc: 0.405000; val_acc: 0.322000
(Iteration 121 / 200) loss: 1.697995
(Iteration 131 / 200) loss: 1.768837
(Iteration 141 / 200) loss: 1.784967
(Iteration 151 / 200) loss: 1.823291
(Epoch 4 / 5) train acc: 0.431000; val_acc: 0.324000
(Iteration 161 / 200) loss: 1.626499
(Iteration 171 / 200) loss: 1.901366
(Iteration 181 / 200) loss: 1.550534
(Iteration 191 / 200) loss: 1.716921
(Epoch 5 / 5) train acc: 0.436000; val_acc: 0.330000
running with sgd_momentum
(Iteration 1 / 200) loss: 3.153778
(Epoch 0 / 5) train acc: 0.105000; val_acc: 0.093000
(Iteration 11 / 200) loss: 2.145874
(Iteration 21 / 200) loss: 2.032562
(Iteration 31 / 200) loss: 1.985848
(Epoch 1 / 5) train acc: 0.311000; val_acc: 0.281000
(Iteration 41 / 200) loss: 1.882354
(Iteration 51 / 200) loss: 1.855372
(Iteration 61 / 200) loss: 1.649133
(Iteration 71 / 200) loss: 1.806432
(Epoch 2 / 5) train acc: 0.415000; val acc: 0.324000
(Iteration 81 / 200) loss: 1.907840
(Iteration 91 / 200) loss: 1.510681
(Iteration 101 / 200) loss: 1.546872
(Iteration 111 / 200) loss: 1.512047
(Epoch 3 / 5) train acc: 0.434000; val_acc: 0.321000
(Iteration 121 / 200) loss: 1.677301
(Iteration 131 / 200) loss: 1.504686
(Iteration 141 / 200) loss: 1.633253
(Iteration 151 / 200) loss: 1.745081
(Epoch 4 / 5) train acc: 0.460000; val_acc: 0.353000
(Iteration 161 / 200) loss: 1.485411
```

(Iteration 171 / 200) loss: 1.610416 (Iteration 181 / 200) loss: 1.528331 (Iteration 191 / 200) loss: 1.449159

(Epoch 5 / 5) train acc: 0.507000; val_acc: 0.384000

/usr/local/lib/python3.7/dist-packages/ipykernel_launcher.py:39:

MatplotlibDeprecationWarning: Adding an axes using the same arguments as a previous axes currently reuses the earlier instance. In a future version, a new instance will always be created and returned. Meanwhile, this warning can be suppressed, and the future behavior ensured, by passing a unique label to each axes instance.

/usr/local/lib/python3.7/dist-packages/ipykernel_launcher.py:42:

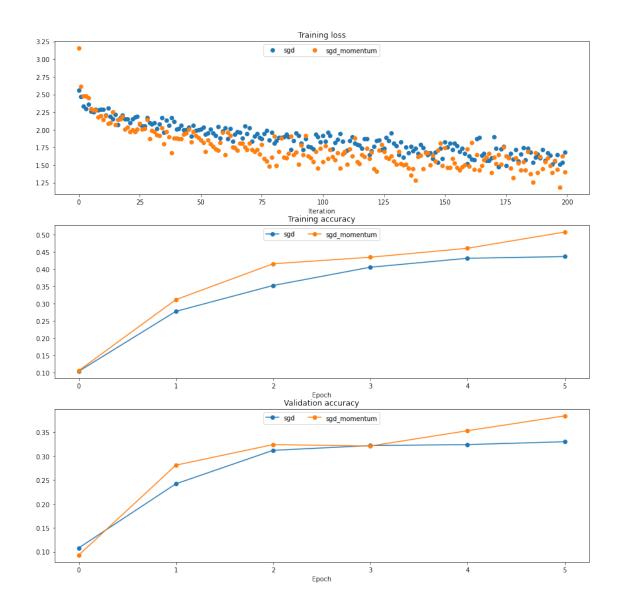
MatplotlibDeprecationWarning: Adding an axes using the same arguments as a previous axes currently reuses the earlier instance. In a future version, a new instance will always be created and returned. Meanwhile, this warning can be suppressed, and the future behavior ensured, by passing a unique label to each axes instance.

/usr/local/lib/python3.7/dist-packages/ipykernel_launcher.py:45:

MatplotlibDeprecationWarning: Adding an axes using the same arguments as a previous axes currently reuses the earlier instance. In a future version, a new instance will always be created and returned. Meanwhile, this warning can be suppressed, and the future behavior ensured, by passing a unique label to each axes instance.

/usr/local/lib/python3.7/dist-packages/ipykernel launcher.py:49:

MatplotlibDeprecationWarning: Adding an axes using the same arguments as a previous axes currently reuses the earlier instance. In a future version, a new instance will always be created and returned. Meanwhile, this warning can be suppressed, and the future behavior ensured, by passing a unique label to each axes instance.



13 Train a good model!

Train the best fully-connected model that you can on CIFAR-10, storing your best model in the best_model variable. We require you to get at least 50% accuracy on the validation set using a fully-connected net.

If you are careful it should be possible to get accuracies above 55%, but we don't require it for this part and won't assign extra credit for doing so. Later in the assignment we will ask you to train the best convolutional network that you can on CIFAR-10, and we would prefer that you spend your effort working on convolutional nets rather than fully-connected nets.

You might find it useful to complete the BatchNormalization.ipynb and Dropout.ipynb notebooks before completing this part, since those techniques can help you train powerful models.

```
[]: best_model = None
  best_val_acc = -1
  # TODO: Train the best FullyConnectedNet that you can on CIFAR-10. You might
  # find batch/layer normalization and dropout useful. Store your best model in L
   →#
  # the best model variable.
   →#
  dropouts = [0.5]
  weight_scales = np.logspace(-2, -1.5, 6)
  learning_rates = np.logspace(-3.5, -2.5, 4)
  #regs =
  for d in dropouts:
    for ws in weight_scales:
     for lr in learning rates:
      model = FullyConnectedNet([100, 100], dropout=d,__
   →normalization='layernorm', weight_scale=ws)
       solver = Solver(model, data,
                      update_rule='adam',
                      optim_config={
                       'learning_rate': lr,
                      },
                      lr_decay=0.95,
                      num_epochs=10, batch_size=100,
                      verbose = False)
       solver.train()
       print(f"Validation Acc: {solver.best val acc} achieved with ws = {ws}, lr,
   \Rightarrow = \{lr\}"\}
       if solver.best_val_acc > best_val_acc:
        best_val_acc = solver.best_val_acc
        best model = model
  #
                         END OF YOUR CODE
```

```
Validation Acc: 0.499 achieved with ws = 0.01, lr = 0.00031622776601683794 Validation Acc: 0.497 achieved with ws = 0.01, lr = 0.0006812920690579615 Validation Acc: 0.497 achieved with ws = 0.01, lr = 0.0014677992676220691 Validation Acc: 0.496 achieved with ws = 0.01, lr = 0.0031622776601683794 Validation Acc: 0.495 achieved with ws = 0.012589254117941675, lr = 0.00031622776601683794 Validation Acc: 0.488 achieved with ws = 0.012589254117941675, lr =
```

```
0.0006812920690579615
Validation Acc: 0.503 achieved with ws = 0.012589254117941675, lr =
0.0014677992676220691
Validation Acc: 0.496 achieved with ws = 0.012589254117941675, lr =
0.0031622776601683794
Validation Acc: 0.498 achieved with ws = 0.015848931924611134, lr =
0.00031622776601683794
Validation Acc: 0.499 achieved with ws = 0.015848931924611134, lr =
0.0006812920690579615
Validation Acc: 0.503 achieved with ws = 0.015848931924611134, lr =
0.0014677992676220691
Validation Acc: 0.51 achieved with ws = 0.015848931924611134, lr =
0.0031622776601683794
Validation Acc: 0.492 achieved with ws = 0.0199526231496888, lr =
0.00031622776601683794
Validation Acc: 0.51 achieved with ws = 0.0199526231496888, lr =
0.0006812920690579615
Validation Acc: 0.493 achieved with ws = 0.0199526231496888, lr =
0.0014677992676220691
Validation Acc: 0.486 achieved with ws = 0.0199526231496888, lr =
0.0031622776601683794
Validation Acc: 0.495 achieved with ws = 0.025118864315095794, lr =
0.00031622776601683794
Validation Acc: 0.494 achieved with ws = 0.025118864315095794, lr =
0.0006812920690579615
Validation Acc: 0.503 achieved with ws = 0.025118864315095794, lr =
0.0014677992676220691
Validation Acc: 0.486 achieved with ws = 0.025118864315095794, lr =
0.0031622776601683794
Validation Acc: 0.497 achieved with ws = 0.03162277660168379, lr =
0.00031622776601683794
Validation Acc: 0.499 achieved with ws = 0.03162277660168379, lr =
0.0006812920690579615
Validation Acc: 0.508 achieved with ws = 0.03162277660168379, lr =
0.0014677992676220691
Validation Acc: 0.495 achieved with ws = 0.03162277660168379, lr =
0.0031622776601683794
```

Best model achieves 51% validation accuracy.

14 Test your model!

Run your best model on the validation and test sets. You should achieve above 50% accuracy on the validation set.

```
[]: y_test_pred = np.argmax(best_model.loss(data['X_test']), axis=1)
y_val_pred = np.argmax(best_model.loss(data['X_val']), axis=1)
print('Validation set accuracy: ', (y_val_pred == data['y_val']).mean())
```

```
print('Test set accuracy: ', (y_test_pred == data['y_test']).mean())
```

Validation set accuracy: 0.515

Test set accuracy: 0.483