# Heterogeneous Donor Circles for Fair Liver Transplant Allocation\*

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The United States (U.S.) Department of Health and Human Services is interested in increasing geographical equity in access to liver transplant. The geographical disparity in the U.S. is fundamentally an outcome of variation in organ supply to patient demand (s/d) ratios across the country. To design a fairer system, we develop a nonlinear integer programming model that allocates organ supply to maximize the minimum s/d ratios across all transplant centers. We design circular donation regions that can address issues raised in legal challenges to earlier organ distribution frameworks. This allows us to reformulate our model as a set-partitioning problem. Our policy can be viewed as a heterogeneous donor circle policy, where the integer program optimizes the radius of the circle around each donation location, where transplant centers within each donation location's circle get priority access to livers. Compared to the current policy that has fixed radius circles around donation locations, the heterogeneous donor circle policy greatly improves both the worst s/d ratio, and the range between the maximum and minimum s/d ratio. We found that with the fixed radius policy of 500 nautical miles (NM) the s/d ratio ranges from 0.37 to 0.84 at transplant centers, while with the heterogeneous circle policy capped at a maximum radius of 500NM the s/d ratio ranges from 0.55 to 0.60, closely matching the national s/d ratio of 0.5983. Our model matches supply and demand in a more equitable fashion than existing policies, and has a significant potential to improve the liver transplantation landscape.

Key words: health care policy, liver transplant, geographical disparity, set partitioning

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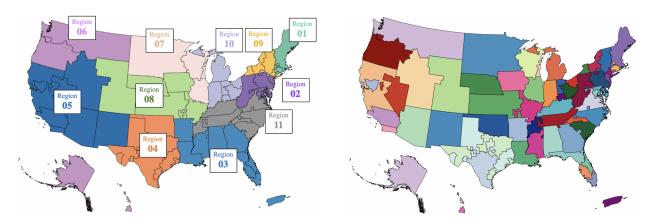


Figure 1 Pre February 4, 2020 policy divided the US in to 11 regions (left), which comprised of 58 DSAs (right).

# 1. Introduction

In 2018, 8250 liver transplants took place in the United States (U.S.) while there were more than 13,000 patients on the waiting list. Unfortunately, in 2018, on average three people in the U.S. died every day awaiting a liver transplant for a total of 1,155 lives lost. Since demand for liver transplant outstrips supply, allocating deceased donor livers judiciously and justly is extremely important. For thirty years (from 1989 to Feb. 4, 2020) transplant allocation policy divided the U.S. into 58 Donation Service Areas (DSAs) that were grouped into 11 geographical regions (Figure 1). Livers were offered to the candidates in a DSA in decreasing order of medical urgency, quantitatively measured by Model for End-stage Liver Disease (MELD) score. (Pediatric End-Stage Liver Disease (PELD) severity score, a measure calculated slightly differently, is used for patients  $\leq$  12 years old.) MELD score reflects the probability of death within a 3-month period and ranges from 6 to 40; a higher score indicates greater mortality risk (Freeman et al. 2002). More serious patients are assigned Status 1A and 1B, and their number is fewer than 50 nationwide at any time.

By law, the deceased donor organs are national resources in the U.S. The U.S. government created the Organ Procurement and Transplantation Network (OPTN) in 1984 to coordinate a nationwide transplant system and optimize the usage of the limited resource of donor organs for transplants. Since 1986, the United Network for Organ Sharing (UNOS), a non-profit private organization has overseen the operations of the OPTN. A key regulatory framework that guides organ transplantation is the "Final Rule" that was adopted in 1998 by the Department of Health and Human Services (HHS) to establish a more detailed framework for the structure and operations of the OPTN (HHS 1998). The Final Rule requires that policies shall not be based on the candidate's place of residence or place of listing, except to the extent required by the other requirements of the Rule.

Geographic inequity in access to liver transplantation across DSAs is well documented in the literature (see Yeh et al. 2011). Indeed, as early as 2008 a HHS Advisory Committee on Transplantation recommended that organ allocation be evidence-based and not on the arbitrary boundaries of the DSAs; and in 2012 the OPTN board adopted a strategic plan that included reducing geographic disparities in access to transplantation. Despite implementation in 2013 of broader sharing of organs in a region for candidates with MELD scores  $\geq 35$ ; geographic inequities remained in the system. The U.S. Scientific Registry of Transplant Recipient's (SRTR) Liver Transplant Waiting List Outcomes Tool<sup>1</sup> (that is built on historical data from 2017 to 2019) shows that for waitlist candidates in Los Angeles with MELD score in the range 25-29, only 15% received a transplant within 90 days, while for candidates in Indianapolis (with MELD scores in the range 25-29), 72% received a transplant within 90 days. The DSA/Region allocation policy resulted in significant disparities even for candidates on transplant lists in close proximity. For example, SRTR's Liver Transplant Waiting List Outcomes Tool shows that for waitlist candidates in New York City with MELD score in the range 25-29, only 15% received a transplant within 90 days, while for similar candidates in Newark, New Jersey, just 15 miles away, 41% received a transplant within 90 days. Since MELD scores directly correlate with the probability of death in the absence of an organ transplant in the next 90 days, different transplant wait times for candidates with the same MELD score across DSAs implies (i) significantly different mortality rates for candidates with the same MELD score in different DSAs, and (ii) a significant variation in the median MELD score at transplant (MMaT).<sup>2</sup> Indeed variance of MMaT has typically been used by UNOS as a key metric in evaluating the effectiveness of a proposal in mitigating geographic disparity (i.e., a lower value of the variance of MMaT indicates less disparity).

In November 2017, a New York City resident Miriam Holman (a patient who had a rare form of pulmonary hypertension for which there is no medical therapy, and which is rapidly fatal without lung transplantation) filed a lawsuit (hereafter, "lung lawsuit") against HHS.<sup>3</sup> Due to the particular lung allocation policy in place at that time, a donor lung could become available across the river in New Jersey (less than four miles away), but because the location of the donor lung is in a different geographical DSA, it would be offered to every candidate waiting for lungs in that New Jersey DSA (even to candidates who are much further away and far less medically critical) before it could be offered to Miriam (Glazier 2018). In July 2018, six liver transplant waiting list patients in New York, California, and Massachusetts filed a lawsuit (hereafter, "liver lawsuit") against HHS.<sup>4</sup> The

<sup>1</sup> https://www.srtr.org/reports-tools/waiting-list-calculator/

<sup>&</sup>lt;sup>2</sup> This is seen for example in 2016 data (Kim et al. 2018) where the highest MMaT is 39 and the lowest MMaT is 20.

<sup>&</sup>lt;sup>3</sup> Miriam Holman v. HHS, (S.D.N.Y 17-CV-09041)

<sup>&</sup>lt;sup>4</sup> Cruz et al. v. HHS, (S.D.N.Y 18-CV-06371)

liver lawsuit pointed out the wide geographical variability in the median MELD scores in recipients for deceased donor transplants, arguing that place of residence largely determines the chances of one's survival in the policy in place.

To address these issues, in June 2018, the UNOS board (based on the recommendations of a Geography Committee formed in December 2017) adopted the following set of principles to guide future organ transplant policy relating to geographic aspects of organ distribution (that were also identified to be consistent with the final rule).

- 1. Reduce inherent differences in the ratio of donor supply and demand across the country.
- 2. Reduce travel time expected to have a clinically significant effect on ischemic time and organ quality.
  - 3. Increase organ utilization and prevent organ wastage.
  - 4. Increase efficiencies of donation and transplant system resources.

The Geography Committee identified three potential distribution frameworks that fit with these four principles: (1) fixed distance from the donor hospital, (2) mathematically optimized boundaries, and (3) continuous scoring (candidates to be ranked on the offer list on a combination of their clinical characteristics and proximity to a donor).<sup>5</sup>

Following public comment, on December 3, 2018, the UNOS board adopted an Acuity Circles Policy (an implementation of the fixed distance from the donor hospital framework that we discuss in Section 2.2). Although there were legal challenges and political pressures from several quarters to maintain the existing system, the new Acuity Circles policy was implemented on May 14, 2019. However, within a day, on May 15, 2019; a federal court issued an injunction and UNOS was required to revert to the prior system while the legal challenges to the policy were pending. On January 16, 2020, the federal court reversed itself and decided not to keep the injunction in place while the case is pending. Subsequently, the Acuity Circles policy was implemented again on February 4, 2020.

In this paper, we use UNOS's stated principle of reducing inherent differences in the ratio of supply to demand (s/d) as our objective explicitly within a mathematical optimization framework to design heterogeneous sized areas around the donation locations. One approach to reduce inequity is through the central distributive principle, proposed by Rawls (1971): the least well-off group in the society should be made as well off as possible. We use this *maximin* principle to design heterogeneous sized areas that maximize the minimum value of the s/d ratio across all transplant centers (or DSAs). We then apply a secondary optimization to minimize the disparity between the transplant centers (or DSAs) with the highest and lowest s/d ratios.

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<sup>&</sup>lt;sup>5</sup> https://optn.transplant.hrsa.gov/media/2565/geography\_publiccomment\_201808.pdf

Our mathematical optimization model can be applied using zip codes or DSAs as the geographical units. When using zip codes as the geographical units the model may be viewed as a heterogeneous circle policy (as compared to a fixed circle policy). When using DSAs as the geographical units the model may be viewed as a type of neighborhood model (Kilambi and Mehrotra 2017), where the neighborhood around a DSA is somewhat circular in shape.

Without the sharing of organs between DSAs, we found that the s/d ratio ranges from 0.31 to 1.98. With 500 nautical miles (NM) fixed circles, the s/d ratio improves and ranges from 0.37 to 0.84. We show that using heterogeneous circles around the donation zip codes, the s/d ratio ranges from 0.55 to 0.60, meaning that there is a much lower disparity in access to organs between the transplant centers. Further, when we examine the s/d ratio disparity for transplant centers that are close to one another (specifically, within 150 NM of each other) the heterogeneous circle policy reduces the s/d ratio disparity to one-fourth compared to the fixed 500 NM circle policy.

We ran simulations with SRTR's Liver Simulated Allocation Model (LSAM, version 2014) using historical patient and organ donor data. The version of the tool available to us was based on DSAs. Hence, we compared our optimized geographical neighborhoods using DSAs. The results show that in comparison to the prior OPTN 11 region policy (in place till February 4, 2020), an allocation policy based on our optimized heterogeneous circular neighborhoods (around DSAs), with a maximum radius of 500 NM and full regional sharing of all organs with MELD  $\geq$  15, drastically reduces the variance of MMaT across DSAs (from 13.66 to 2.00) and average annual deaths (from 3745 to 3568), for a modest increase in average travel distance (from 199 NM to 258 NM).

A key policy insight is that the one-size-fits-all framework (i.e., the currently proposed Acuity Circles Policy) approach taken by UNOS does not adequately address the problem of reducing the differences in the ratio of donor supply to demand across the country. Rather, a customized approach that accounts for where organ supply and demand occur, and adjusts radii of the circles, more effectively addresses UNOS stated goal of equalizing s/d ratios. The remainder of the paper is organized as follows. In the next section, we give a brief overview of the liver allocation system in the U.S., and review proposals and related research. Section 3 presents our optimization methodology. Section 4 describes our findings and the projected outcomes. Section 5 summarizes and provides concluding remarks.

# 2. Liver Allocation Policy and Literature Review

UNOS supervises the transplantation network in the U.S. Its primary responsibilities are to manage the national transplant waiting list, match organs from deceased donors to candidates, establish medical criteria for allocating organs, facilitate organ distribution, frame equitable policies, etc.

Sequence #	Candidates that are within:	And are:
1	OPO's region	Adult status 1A or pediatric status 1A/1B
2	OPO's region	$MELD/PELD \ge 35$
3	OPO's DSA	$MELD/PELD \ge 15$
4	OPO's region	$MELD/PELD \ge 15$
5	Nation	Adult status 1A or pediatric status 1A/1B
6	Nation	$MELD/PELD \ge 15$
7	OPO's DSA	$MELD/PELD \le 15$
8	OPO's region	$MELD/PELD \le 15$
9	Nation	$MELD/PELD \le 15$

Table 1 Liver Allocation Policy (a.k.a. Share 35) prior to February 4, 2020

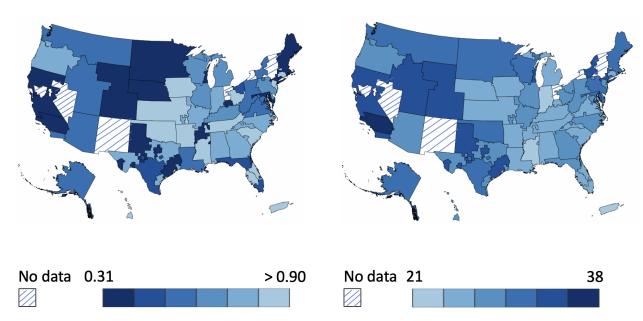
Some of the main UNOS members are the 142 liver transplant centers and Organ Procurement Organizations (OPOs) in the 58 DSAs. The OPO coordinates the local procurement of deceased donor organs and allocation in a DSA.

Each transplant center evaluates patients and adds candidates to the waitlist. The medical data about the candidates is shared with UNOS. This pooled data of candidates across all transplant hospitals is constantly updated when new candidates get added and existing candidates are either removed or their medical conditions (e.g. MELD scores) are updated. When a deceased donor organ becomes available, the OPO sends medical data about the organ donor to UNOS. Subsequently, the UNOS matching system compares the donor information with the candidate pool to rank the candidates for the organ offer as per the allocation policy. Upon receiving an offer, the transplant surgeon or physician, in consultation with the candidate decides whether to accept the offer.

# 2.1. Share 35 Policy

In the previous allocation policy (a.k.a. Share 35) in place from June 18, 2013, until February 4, 2020, deceased donor livers were offered hierarchically to candidates, in decreasing order of MELD scores within each hierarchy, according to the priority list in Table 1. First, an organ was offered to Status 1A and 1B candidates in the region, followed by candidates with MELD  $\geq$  35. After that, candidates with MELD score between 15 and 35 in the OPO's DSA were preferred over candidates outside the DSA. Next in the hierarchy were candidates with MELD score between 15 and 35 in the OPO's region, followed by candidates with MELD score between 15 and 35 outside the OPO's region. Finally, candidates with MELD  $\leq$  15 in the DSA were preferred over candidates with MELD  $\leq$  15 outside the DSA but in the region, who in turn were preferred over candidates with MELD  $\leq$  15 outside the region.

Due to differences in demographics, disease incidence, and mortality leading to organ donations among the DSAs, there was a huge disparity in the s/d ratios across the DSAs. Figure 2 shows the wide variability in the s/d ratio (left), and an inverse relationship of this variability with observed



Lower supply to demand (s/d) ratios at a DSA (left) correspond to a higher MMaT at the DSA Figure 2 (right). The time period of analysis is from July, 2013 to June, 2017.

MMaT scores (right). The s/d ratios (at DSAs) varied from 0.31 in NYRT (a DSA in New York) to 1.98 in FLWC (a DSA in Florida). This disparity primarily drove the differences in MMaT among the DSAs. In a study by Wey et al. (2018), the s/d ratios in a DSA were found to be associated with MMaT in DSAs (r = -0.56; P < 0.001).

#### 2.2. Current Policy: Acuity Circles

This policy progressively shares organs in circles of radius 150 NM, 250 NM, and 500 NM around the donor hospital, with the following hierarchy: (1) Status 1 candidates within 500 NM; (2) candidates with MELD score  $\geq 37$  within 150 NM, then 250 NM, then 500 NM; (3) candidates with MELD score  $\geq 33$  within 150 NM, then 250 NM, then 500 NM; (4) candidates with MELD score  $\geq 29$ within 150 NM, then 250 NM, then 500 NM; (5) candidates with MELD score  $\geq$  15 within 150 NM, then 250 NM, then 500 NM, and then nationally.<sup>6</sup> This is a "one-size-fits-all" policy because it does not account for the organ arrival rate, the candidate waiting list, nor the distances of the transplant centers from a donor hospital. Based on the formulation of s/d ratio introduced and defined in this paper (Section 3.1), Haugen et al. (2019) studied transplant center level s/d ratios and compared distribution frameworks based on fixed-distance circles (150 miles or 400 miles radius), and fixed-population (12 or 50 million) circles. They concluded that neither of these circles significantly reduced the geographical disparity!

<sup>&</sup>lt;sup>6</sup> https://unos.org/policy/liver-distribution/

#### 2.3. Related Research

Redistricting is a problem that occurs frequently in multiple domains (e.g., political redistricting, school redistricting, and sales territory assignment) where a finite, denumerable set of non-overlapping geographical units are aggregated into regions/districts subject to some criteria. Hess et al. (1965) and Garfinkel and Nemhauser (1970) introduced the use of optimization techniques for political redistricting. Zoltners and Sinha (1983) discuss an application of redistricting in sales territory assignment, and Caro et al. (2004) discuss school redistricting using integer programming. Much of the redistricting literature is focused on political redistricting (see Gopalan et al. 2013, Kim and Xiao 2017, Ricca et al. 2013). Two important considerations in redistricting problems are the contiguity and compactness of the districts. In this regard, Shirabe (2009) proposed a flow-based model for contiguity constraints, that has been typically used in subsequent integer programming approaches. However, contiguity constraints make redistricting problems notoriously hard to solve exactly (see Kim and Xiao 2017, Ricca et al. 2013).

Focusing on transplant, and disregarding geographical equity for the moment, Kong et al. (2010) studied the problem of maximizing the efficiency, by maximizing total intraregional transplants through the redesign of the liver allocation regions. They formulate the problem as a set-partitioning problem and use a branch-and-price algorithm to approximate solutions. Stahl et al. (2005) consider geographical equity as measured using intraregional transplant rates in their objective function along with efficiency (measured by total intraregional transplants) but they restrict their regions to contain up to eight DSAs due to computational challenges. Extending their work, Demirci et al. (2012) developed a branch-and-price algorithm to incorporate a larger set of potential regions and explored the efficient frontier in a trade-off between efficiency and geographical equity. Their metric of geographical equity maximizes the minimum in-district viability-adjusted transplant rates per waiting list candidate, which is sensitive to the number of waiting list patients added by the transplant centers and thus problematic. For low MELD patients, the survival benefit of transplantation is minimal (Merion et al. 2005) and the chances of receiving an organ vary across geographies, and consequently, the transplant centers differ in their practices of adding low MELD patients to the waiting list.

Gentry et al. (2015) used optimization to reorganize DSAs into regions/districts to reduce geographical disparity. Their objective was to minimize the sum of absolute differences between the number of deceased-donor livers recovered in each district and the ideal number of livers that would be offered in each district if each liver was given to the medically most urgent candidate in the country. Working closely with the liver committee of UNOS, they proposed eight-district and four-district (reorganized DSA) maps. The proposed maps were under active consideration by

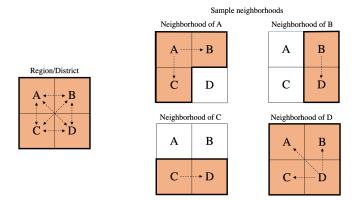


Figure 3 Illustration of difference between Regions/Districts and neighborhoods. Let DSAs A, B, C and D form a region or district. They all share with each other. However, the neighborhood of A consists of DSAs A, B and C, therefore A shares with only A, B and C. Similarly, B shares with B and D, and so on.

UNOS from 2015 to 2017, but ultimately after significant debate and public comment were not adopted.

Kilambi and Mehrotra (2017) introduced the neighborhood framework in organ allocation as a way to provide for broader sharing and improve geographic equity. Each DSA has its own neighborhood, which consists of a unique set of other DSAs (or neighbors) to which it shares its organs. A DSA can be part of multiple neighborhoods, therefore the neighborhoods can be overlapping, which makes the representation of all neighborhoods on a single map difficult. Interconnectivity and overlap among neighborhoods provide resilience to supply and demand uncertainty. The neighborhood framework reduces to redistricting when all the DSAs in a neighborhood have the identical neighborhood. Thus, the redistricting framework can be viewed as a special case of a neighborhood framework. Figure 3 illustrates the difference between regions/districts and neighborhood framework. Using the neighborhood framework Kilambi and Mehrotra (2017) developed an optimization model to design DSA neighborhoods to minimize the absolute deviation of the s/d ratios across the neighborhoods from the national average.

Ata et al. (2017) used fluid approximation and game theory to show that multiple listings (a patient lists at more than one transplant center (potentially in other DSA or region) so that he/she can get organ offers from multiple places) can reduce geographical disparity in kidney allocation. However, fewer than 2% of patients (On June 4, 2020, the OPTN website shows 201 out of 12513 candidates on the waiting list are multiple listed) waiting for liver transplant multiple list. Bertsimas et al. (2020) suggest the use of tradeoff curves for the assessment of the three organ distribution frameworks identified by the Geography Committee. Running a massive number of simulations for the three distribution frameworks, they plot tradeoff curves of efficiency (measured as average travel distance) versus fairness (measured as deaths or variance of MMaT). For a given value of the

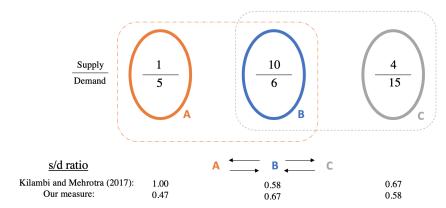


Figure 4 Comparing our s/d ratio measure with that of Kilambi and Mehrotra (2017). Their measure artificially inflates the s/d ratio.

efficiency metric, the tradeoff curve then identifies the policy with the greatest fairness. However, they did not consider the neighborhood and heterogeneous circles distribution frameworks in their study.

# 3. Model Formulation

Consistent with UNOS's stated principles, our approach is to design an organ distribution policy that equalizes s/d ratios across the transplant centers and thus mitigates geographical disparities. We start by aggregating the historical supply and demand of organs by geographical location for the period of study. We assume that the distribution of organ quality and patient's health characteristics are similar across the donor hospitals and transplant centers. While there are certainly differences currently in the patient health characteristics from state to state (e.g., presently California has a higher proportion of high MELD candidates than Tennessee), this is largely a function of accumulated disparity over the years; in steady state, the distribution of MELD scores should be similar.

We formulate an Integer Programming model (IP) that uses a neighborhood framework. Each supply location (DSA, zip code, or donor hospital) is assigned a unique set of demand locations (DSA or transplant center), which is referred to as its neighborhood. In a setting where geographical units of supply and demand are DSAs, a neighborhood of a DSA consists of other DSAs (including itself) to which it shares its organs.

Kilambi and Mehrotra (2017) pioneered the idea of defining neighborhoods for DSAs. However, their definition of supply to demand ratio at a DSA is somewhat problematic. They model the s/d ratio of a DSA as the ratio of total supply to total demand in the DSA's neighborhood. In other words, they treat all the DSAs in that neighborhood as a single unit, but a DSA can also be part of another neighborhood, which results in the artificial inflation of the s/d ratio. To illustrate, consider three DSAs A (Supply: 1, Demand: 5), B (Supply: 10, Demand: 6), and C (Supply: 4,

Notation	Description
$i \in \mathcal{I} = \{1,, N_{sup}\}$	Supply locations
$j \in \mathcal{J} = \{1,, N_{dem}\}$	Demand locations
Parameters:	
$s_i$	Number of livers from deceased donors recovered (or supply) at $i$
$d_{j}$	Number of incident waiting list additions (or demand) at $j$
$ au_{ij}$	Distance between location $i$ and $j$
$ au_{max}$	Maximum permissible distance from a supply location to a demand location
$c_{j}$	Number of transplant centers in demand location $j$
$c_{i}^{(r)}$	Number of transplant centers that are $\leq r$ distance units away from supply location $i$
$c_{min}$	Minimum number of transplant centers a supply location must share its organs with
$\lambda_{[S-1]}^* top s_{ij}^{(r)}$	Minimum s/d ratio value to be used in Stage 2 optimization
$s_{ij}^{(r)}$	Apportioned share of organs from $i$ to $j$ when the farthest demand location in $i's$ neighborhood is $r$ units away
Decision variables:	
$x_{ij}$ (General model)	1 if $i$ shares its organs with $j$ , and 0 otherwise
$x_{ir}$ (Set-partitioning model)	1 if the farthest member in the neighborhood of $i$ is $r$ units away
wir (see partitioning model)	from $i$ , and 0 otherwise
$\lambda$	Minimum s/d ratio for an allocation
$_{-}$	Maximum s/d ratio for an allocation

Table 2 Model Notation

Demand: 15) as shown in Figure 4. A shares with B and receives from B, B shares with and receives from both A and C, and C shares with B and receives from C. The neighborhood of A consists of A and B, neighborhood of B consists of A, B and C, and neighborhood of C consists of B and C. Kilambi and Mehrotra (2017) compute the s/d ratios of A, B and C as 1.00 (11/11), 0.58 (15/26), and 0.67 (14/21), respectively. But, in aggregate the s/d ratio for this three region system is only 0.58! Further, their objective function is to minimize the absolute deviation of the s/d ratios from a target value (the national average), which effectively treats deviations below the average identically to deviations above the average. Unfortunately, locations with deviations below the average (i.e., lower s/d ratios and higher MMaT scores) have poorer outcomes (greater chances of dying while waiting for a transplant) than locations with deviations above the average. Thus, in a setting where the desire is to minimize the disparities it does not seem appropriate to treat these two deviations identically. By maximizing the worst s/d ratio, our primary focus is on minimizing the deviation below the national average. Finally, we note that our model does not require symmetric organ sharing (which they enforce) giving more flexibility in optimization.

#### 3.1. Supply-Demand Ratio Calculation

First, we define our s/d ratio measure. Recall that we assumed the MELD scores of candidates across the geographies are independent and identically distributed (i.i.d), and when an organ is

recovered, all locations in the neighborhood are treated alike. For a given demand location j that is in the neighborhood of supply location i, we model the expected supply received (by j) from i to be proportional to j's demand over the total demand competing for i's supply. Using this expected allocation of supply in the example in Figure 4, we find that 5/11 units of the supply from A are allotted to A, and 6/11 units of the supply from A are allotted to B. Similarly,  $(5/26) \times 10$ ,  $(6/26) \times 10$ , and  $(15/26) \times 10$  units of the supply from B are allotted to A, B, and C, respectively. Finally,  $(6/21) \times 4$  units of the supply from C are allotted to B, and  $(15/21) \times 4$  units of the supply from C are allotted to C. Dividing the expected supply provided to each location by its demand we find s/d ratios of 0.47, 0.67 and 0.58 for A, B, and C, respectively, with our measure. Using the notations described in Table 2 we formally calculate,

Expected supply from 
$$i$$
 to  $j = \frac{d_j}{\sum_{k=1}^{N_{dem}} d_k x_{ik}} s_i x_{ij}$ 

To determine overall supply to demand ratio, we first sum the expected supply over all supply locations and then divide by j's demand,  $d_j$  giving:

s/d ratio at 
$$j = \sum_{i=1}^{N_{sup}} \frac{1}{\sum_{k=1}^{N_{dem}} d_k x_{ik}} s_i x_{ij}$$

We note that the way we calculate the expected s/d ratio does not account for organs that a DSA may receive due to national sharing. However, these organs are generally a very small fraction and should not significantly impact the s/d ratios realized in practice.

## 3.2. General Model

We now describe our model, which solves the problem in two stages. In Stage 1, we apply the maximin equity principle to maximize the performance of the worst demand location (i.e., we maximize the value of the lowest s/d ratio across all demand locations). In Stage 2, we reduce the disparity among the different demand locations. To do this, we minimize the disparity between the best and worst demand locations, while ensuring the s/d ratio of the worst demand location remains at the optimum value obtained from the Stage 1 optimization. We now present Mixed-Integer Linear Programs (MIPs) for the different stages.

**3.2.1.** Stage 1 Formulation: In Stage 1, we seek to maximize the s/d ratio of the worst demand location.

[S-1] Maximize 
$$\lambda$$
 (1)

subject to: 
$$\lambda \leq \sum_{i=1}^{N_{sup}} \frac{1}{\sum_{k=1}^{N_{dem}} d_k x_{ik}} s_i x_{ij} \quad \forall j \in \mathcal{J}$$
 (2)

$$x_{ij} \tau_{ij} \le \tau_{max} \qquad \forall i \in \mathcal{I}, j \in \mathcal{J}$$
 (3)

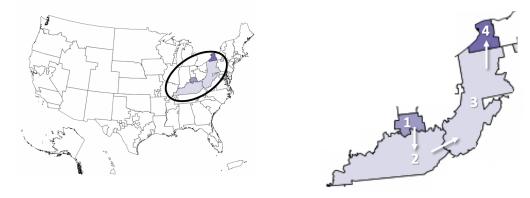


Figure 5 Illustration of sharing and receiving contiguity. If  $x_{14} = 1$ , with sharing contiguity,  $x_{12} = x_{13} = 1$ ; and with receiving contiguity  $x_{24} = x_{34} = 1$ .

$$x_{ij} = 1 \qquad \forall i = j, i \in \mathcal{I}, j \in \mathcal{J} \tag{4}$$

$$\sum_{i=1}^{N_{dem}} c_j x_{ij} \ge c_{min} \qquad \forall i \in \mathcal{I}$$
 (5)

$$x_{ij} \in \{0,1\}$$
  $\forall i \in \mathcal{I}, j \in \mathcal{J}$  (7)

Constraint (2) models  $\lambda$  as the lower bound of the s/d ratios across all the demand locations, and the objective is to maximize this lower bound. Constraint (3) limits the size of the neighborhood (by limiting how far an organ can be transported for transplant), constraint (4) implies that if a supply and demand location coincide (e.g., a DSA or zip code that has both a donor hospital and a transplant center) it must share with itself, and constraint (5) ensures that there are at least  $c_{min}$  transplant centers in a neighborhood. We also include contiguity constraints to ensure that the designed neighborhoods are contiguous and somewhat compact in shape. This is enforced by an adjacency matrix that describes locations that are geographically adjacent to each other, and two types of contiguity constraints. Sharing contiguity ensures that if location r supplies organs to location t that is not adjacent to it, then all locations between r and t also receive organs from location r. Receiving contiguity ensures that if location r supplies organs to location t that is not adjacent to it, then all locations between r and t also supply organs to location t. Figure 5 illustrates receiving and sharing contiguity, ensuring that if location 1 shares its organs with location 4, locations 2 and location 3 also share their organs with location 4; and locations 2 and 3 also receive organs from location 1. Appendix A describes flow-based mathematical constraints applying Shirabe (2009)'s approach, that can be used to enforce sharing and receiving contiguity

<sup>&</sup>lt;sup>7</sup> Deceased-donor livers vary in quality, and marginal livers are more likely to be used and less likely to be discarded when more competition exists among transplant centers (Halldorson et al. 2013, Garonzik-Wang et al. 2013). Thus UNOS requires that a minimum number of transplant centers be in contention for organs from a supply location.

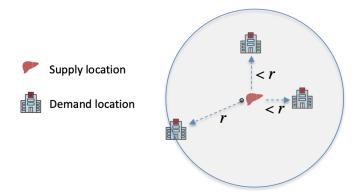


Figure 6 Illustration of circular contiguity: If a neighborhood is r units in radius around the supply location, then all demand locations that are within r units must be in the neighborhood.

with any geographical shapes, as well as a linearization of constraint (2) in the non-linear integer programming model [S-1].

**3.2.2.** Stage 2 Formulation: In Stage 2, we minimize the maximum absolute difference of s/d ratios among demand locations. This is achieved by constraining the lowest s/d ratio value to be greater than or equal to the Stage 1 objective  $\lambda_{[S-1]}^*$ , and minimizing the maximum s/d ratio value across all the demand locations.

[S-2] 
$$Minimize \beta$$

s.t. 
$$\beta \ge \sum_{i=1}^{N_{sup}} \frac{1}{\sum_{k=1}^{N_{dem}} d_k x_{ik}} s_i x_{ij} \quad \forall j \in \mathcal{J}$$
 (8)

$$\lambda \ge \lambda_{[S-1]}^* \tag{9}$$

The optimal values of  $x_{ij}$  obtained by optimizing [S-1] followed by [S-2] are used to construct the new optimized geographical scheme.

## 3.3. Circular Contiguity and a Set-Partitioning Model

One of the chief complaints in the liver and lung lawsuits was that a candidate receiving the transplant organ may be geographically further away from the donated organ than another sicker candidate. In other words, neighborhood boundaries that allow an organ to be transported further away to a less sick candidate than a closer sicker candidate (because the sicker candidate is outside the neighborhood) goes against generally accepted perceptions of fairness. This suggests that we consider (roughly) circular contiguity for neighborhoods. If the radius of a neighborhood is r units around the supply location, then all demand locations that are within r units away be in the neighborhood (Figure 6).

Circular contiguity allows for a more computationally tractable reformulation of the previous model. For a neighborhood of a given radius r, one can easily calculate (a priori) the amount of supply allocated to each demand location in the neighborhood. This enables us to reformulate [S-1] and [S-2] linearly as Set-Partitioning Problems, which also makes them scalable. In the setpartitioning formulation,  $x_{ir}$  is a binary decision variable that takes value 1 if the radius of the neighborhood of i is r units (all demand locations  $\leq r$  units from i are part of the neighborhood) and is 0 otherwise.

#### 3.3.1. Stage 1 Formulation:

[SP-1] Maximize 
$$\lambda$$
 (11)

subject to: 
$$\lambda \leq \sum_{i=1}^{N_{sup}} \sum_{r \in \mathcal{R}_i} \frac{x_{ir} s_{ij}^{(r)}}{d_j} \quad \forall j \in \mathcal{J}$$

$$\sum_{r \in \mathcal{R}_i} x_{ir} = 1 \qquad \forall i \in \mathcal{I}$$

$$\sum_{r \in \mathcal{R}_i} c_i^{(r)} x_{ir} \geq c_{min} \qquad \forall i \in \mathcal{I}$$

$$x_{ir} \in \{0, 1\} \qquad \forall i \in \mathcal{I}$$

$$(12)$$

$$\sum_{r \in \mathcal{R}_i} x_{ir} = 1 \qquad \forall i \in \mathcal{I}$$
 (13)

$$\sum_{r \in \mathcal{R}_i} c_i^{(r)} x_{ir} \ge c_{min} \qquad \forall i \in \mathcal{I}$$
 (14)

$$x_{ir} \in \{0, 1\} \qquad \forall i \in \mathcal{I} \tag{15}$$

For a given radius r,  $s_{ij}^{(r)}$  denotes the apportioned share of i's organs that are expected to be offered to location j. In other words,  $s_{ij}^{(r)} = \frac{d_j}{\sum_{k:\tau_{ik} \leq r} d_k} s_i$ , which can be precomputed for a given radius r. Note that for a given supply location i, we do not need to consider a continuum of possible neighborhood radii. Rather (because this apportionment or organs will only change when a new demand location is added to the neighborhood) we only need to consider a finite set of values of r that correspond to the distance from i to each of the other demand locations that are within  $\tau_{max}$ . In [SP-1], the set  $\mathcal{R}_i$  contains the possible values of r created accordingly. Constraint (12) models  $\lambda$  as the lower bound of the s/d ratios across all the demand locations, and the objective is to maximize this lower bound. Constraint (13) allows one assignment of r to each supply location, and constraint (14) ensures a minimum number of transplant centers in the neighborhood.

**Stage 2 Formulation:** Once the optimal solution  $\lambda_{[SP-1]}^*$  to [SP-1] is obtained, we can solve [SP-2] to minimize the maximum s/d ratio while ensuring that the minimum s/d ratio remains at least  $\lambda_{[SP-1]}^*$ .

[SP-2] 
$$Minimize \beta$$

s.t. 
$$\beta \ge \sum_{i=1}^{N_{sup}} \sum_{r} \frac{x_{ir} s_{ij}^{(r)}}{d_j} \qquad \forall j \in \mathcal{J}$$
 (16)

$$\lambda \ge \lambda_{[SP-1]}^* \tag{17}$$

### 4. Data and Results

This study used data from SRTR. The SRTR data system includes data on all donor, wait-listed candidates, and transplant recipients in the US, submitted by the members of the OPTN. The Health Resources and Services Administration (HRSA), U.S. Department of Health and Human Services provides oversight to the activities of the OPTN and SRTR contractors.

In the data, encompassing the four years starting July 2013 and ending June 2017, the supply or the total number of livers (from deceased donors) donated from all donor hospitals in the US is 26,899. The patient pool is dynamic: new patients enlist, waiting candidates die or become too sick for transplant and are removed, and the MELD scores get updated periodically. We measure demand (44,959) as the total incident<sup>8</sup> adult patients whose MELD scores became at least 15 during the four years; which gives a national s/d ratio of 0.5983. There are two reasons for excluding low MELD patients from the demand: (1) patients with MELD <15 have no survival benefit from transplantation (Merion et al. 2005), therefore our demand measure is less sensitive to the number of low-MELD score patients added to the waiting list, and (2) transplant centers differ in their practices of listing low MELD score patients across the country.

We present two versions of the set-partitioning models optimization results: a zip-code cluster version where supply locations are zip-code clusters (clustered by the first three-digits and first four-digits) and demand locations are the 142 transplant centers, and a DSA version where supply and demand locations are the DSAs. We restrict r (radius around the supply locations) within the range 150 NM to  $\tau_{max}$  for every  $\mathcal{R}_i$ , constraining the minimum and maximum size of the neighborhoods. We set  $c_{min} = 3$ , ensuring that at least three transplant centers are present in a neighborhood. We used R 3.5.1 and a commercial solver Gurobi 8.0-1 to solve the set-partitioning optimization models on an Intel Xeon 3.5 GHz machine with 32 GB RAM running Windows 10.

#### 4.1. Zip-code Cluster Version

The location of zip codes and transplant centers are indicated by their latitude and longitude values. To calculate the distance between a three-digit (four-digit) zip-code cluster and a transplant center, we first find the centroid of the zip-codes in the cluster having the same first three digits (four digits) and then use the "geosphere" package in R to calculate the shortest distance between two points (centroid of the zip cluster and transplant center) according to the "Vincenty (ellipsoid)" method.

There are a total of 641 three-digit and 1380 four-digit zip-code clusters with supply in our data. We vary  $\tau_{max}$  from 350 NM to 700 NM in steps of 50 NM. We do not include the zip codes

<sup>&</sup>lt;sup>8</sup> We consider incident patients so that the model parameters are not biased because of accumulated disparity and thus are exogenous to the geographical scheme.

in Hawaii and Puerto Rico in our analysis, since they are more than 1000 miles from transplant centers in mainland U.S. Consistent with the current policy zip codes in Alaska are considered to be situated at the Seattle Tacoma Airport in Washington State. We require that the minimum radius of a neighborhood be 150 NM. Since a transplant hospital may not necessarily be exactly at 150 NM from a zip-code cluster, this is enforced by ensuring the closest transplant center greater than or equal to 150 NM away is included in the neighborhood, unless it is greater than  $\tau_{max}$  miles away.

Table 3 provides a comparison of the s/d ratios. To compare against the fixed radius type of policy in place currently (i.e., acuity circles), we also computed the s/d ratio for homogeneous radii circles by fixing the radius of each zip-code cluster to  $\tau_{max}$ . Compared to the heterogeneous radius circle policy, the "one-size-fits-all" fixed radius policy does a poor job in equalizing s/d ratios across transplant centers. The heterogeneous circle policy at  $\tau_{max} = 500$  NM is able to keep the ratio at transplant centers between 0.55 and 0.60 (compared to the national s/d ratio of 0.5983), while the fixed 500 NM radius circle policy has an s/d ratio variation between 0.37 and 0.84.

We also examine the difference in the s/d ratio of nearby transplant centers (defined as being within 150 NM). Table 3 provides both the maximum and the median values of this difference. As is evident, in the heterogeneous circles policy the value of the s/d ratio at nearby transplant centers is very similar—which can hopefully lead to more equitable transplant outcomes in nearby transplant centers. For most of the transplant centers, the difference in s/d ratio is in the scale of  $10^{-4}$ , as implied by the median values.

As we increase  $\tau_{max}$  from 350 NM to 700 NM, the minimum s/d ratio increases, and the range of s/d ratio decreases. When  $\tau_{max} = 400$  NM the s/d ratio range is already quite narrow at 0.53-0.61, and once  $\tau_{max} = 500$  NM, the s/d ratio range stays steady at 0.55-0.60. Figure 7 shows the quartiles of radii when using four-digit zip-code clusters. When  $\tau_{max}$  is 500 NM, the first, second, and third quartiles of radii are 211, 305, and 415 NM, respectively. Compared to the fixed radii circles policy, the heterogeneous radii circles policy achieves an equalization in the s/d ratio (near the national average) while keeping transport distances lower. This has an added benefit. Since the radii of the circles are smaller, each donor zip-code cluster on average has 24 (median 20) transplant centers, as compared to the fixed radii circles that have on average 39 transplant centers (median 43). The logistics of a donor hospital (zip-code cluster) coordinating with a smaller number of transplant centers can be simpler.

We note that Haugen et al. (2019)'s study (using the s/d metric as defined in this paper) report identical ranges (to our fixed 350 NM circles) for fixed 400 miles ( $\approx 348$  NM) circles. They also study a neighborhood defined by population circles around a transplant center. They find that

	s/d ratio		Maximum (Median) s/d ratio	
Allocation Policy	Range	Std. deviation		
$\tau_{max} = 350 \text{ NM}$				
Fixed radius circles (Three-digit zip)	0.39 - 1.09	0.123	$0.59920 \ (0.04611)$	
Fixed radius circles (Four-digit zip)	0.38 - 1.09	0.123	$0.60235 \ (0.04559)$	
Three-digit zip-code cluster model	0.51 - 0.88	0.098	$0.33043 \ (0.05047)$	
Four-digit zip-code cluster model	0.51 - 0.88	0.103	$0.33813 \ (0.07085)$	
$ \underline{\tau_{max}} = 400 \text{ NM} $				
Fixed radius circles (Three-digit zip)	0.37 - 0.85	0.112	$0.23255 \ (0.03690)$	
Fixed radius circles (Four-digit zip)	0.37 - 0.84	0.112	$0.22818 \; (0.03633)$	
Three-digit zip-code cluster model	0.53 - 0.62	0.033	$0.08571 \ (0.00042)$	
Four-digit zip-code cluster model	0.53 - 0.61	0.030	$0.07763 \; (0.00028)$	
450 373 5				
$ \frac{\tau_{max} = 450 \text{ NM}}{\text{Fixed radius circles (Three-digit zip)}} $	0.20 0.00	0.104	0.90690 (0.09000)	
rixed radius circles (Three-digit zip)	0.38-0.88	0.124	0.20629 (0.02900)	
Fixed radius circles (Four-digit zip)	0.38-0.87	0.124	$0.19770 \ (0.02048)$	
Three-digit zip-code cluster model	0.54-0.61	0.023	$0.05277 \ (0.00108)$	
Four-digit zip-code cluster model	0.54-0.61	0.024	$0.06125 \ (0.00043)$	
$\tau = 500 \text{ NM}$				
$ \frac{\tau_{max} = 500 \text{ NM}}{\text{Fixed radius circles (Three-digit zip)}} $	0.37-0.84	0.137	0.20941 (0.03632)	
Fixed radius circles (Timee-digit zip) Fixed radius circles (Four-digit zip)	0.37-0.84	0.137 $0.137$	0.20851 (0.04489)	
Three-digit zip-code cluster model	0.55-0.60	0.137 $0.022$	0.2031 (0.04439)	
Four-digit zip-code cluster model	0.55-0.60	0.022	0.04921 (0.00003)	
Four-digit zip-code cluster moder	0.00-0.00	0.021	0.04322 (0.00020)	
$\tau_{\rm max} = 550 \text{ NM}$				
$ \frac{\tau_{max} = 550 \text{ NM}}{\text{Fixed radius circles (Three-digit zip)}} $	0.37 - 0.91	0.145	$0.17331 \ (0.03808)$	
Fixed radius circles (Four-digit zip)	0.36-0.91	0.146	$0.17213 \ (0.03882)$	
Three-digit zip-code cluster model	0.55 - 0.60	0.020	$0.05070 \ (0.00029)$	
Four-digit zip-code cluster model	0.55 - 0.60	0.019	0.04387 (0.00025)	
2			,	
$\tau_{max} = 600 \text{ NM}$				
Fixed radius circles (Three-digit zip)	0.34 - 0.97	0.152	0.17767 (0.04866)	
Fixed radius circles (Four-digit zip)	0.34 - 0.96	0.152	0.17819 (0.04473)	
Three-digit zip-code cluster model	0.55 - 0.60	0.018	0.05407 (0.00113)	
Four-digit zip-code cluster model	0.55 - 0.60	0.018	$0.03613 \ (0.00015)$	
$\tau_{max} = 650 \text{ NM}$				
Fixed radius circles (Three-digit zip)	0.33 - 0.94	0.152	$0.16743 \ (0.02449)$	
Fixed radius circles (Four-digit zip)	0.33 - 0.93	0.152	$0.17091 \ (0.02457)$	
Three-digit zip-code cluster model	0.55 - 0.60	0.017	$0.05049 \; (0.00016)$	
Four-digit zip-code cluster model	0.55 - 0.60	0.018	$0.03336 \ (0.00012)$	
700 NA 5				
$\tau_{max} = 700 \text{ NM}$	0.00.004	0.145	0.15001 (0.04550)	
Fixed radius circles (Three-digit zip)	0.32-0.94	0.145	0.17881 (0.04773)	
Fixed radius circles (Four-digit zip)	0.32-0.94	0.145	0.18275 (0.04654)	
Three-digit zip-code cluster model	0.55-0.60	0.016	0.05100 (0.00010)	
Four-digit zip-code cluster model	0.55-0.60	0.017	0.03402 (0.00007)	

Table 3 Comparison of s/d ratios between fixed and heterogeneous circles (supply and demand locations are zip-code clusters and transplant centers (TCs), respectively).

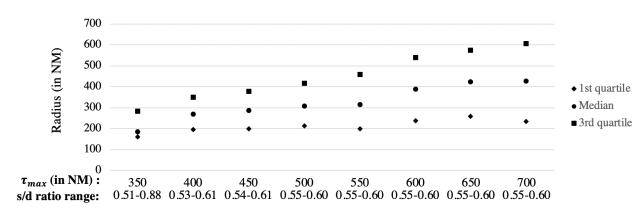


Figure 7 Quartiles of radii in the four-digit zip-code cluster models.

the range of s/d ratios for fixed population circles of size 12 million to be 0.27-2.14, and for fixed population circles of 50 million to be 0.43-1.01.

Since the current implementation of LSAM does not support schemes based on zip-code clusters, we could not evaluate our zip code based allocation policy via the LSAM simulation model. Instead, we use the results of the DSA version described in the next section and run the LSAM simulation on the neighborhoods it generates to evaluate the effectiveness of our allocation policy in reducing geographical disparity.

#### 4.2. DSA Version

Using DSAs as the geographical unit preserves the existing important relationships between donor hospitals and the OPO in each DSA. If indeed, the court rules in a manner that reinstates DSAs as a geographical unit, then our method shows how they could share organs to achieve equitable outcomes with regards to the s/d ratio.

The distance between any two DSAs i and j,  $\tau_{ij}$ , is calculated as the mean of the transplant-volume-weighted distance between donor hospitals in DSA i and transplant center in DSA j, and the reverse. Since six DSAs do not have a transplant hospital, there are 58 DSAs with supply and 52 DSAs with demand. Consistent with Gentry et al. (2015) and Kilambi and Mehrotra (2017), we allow (as exceptions to  $\tau_{max}$ ) the DSAs located in Hawaii, and Puerto Rico, to share and receive organs from other DSAs located in California and Oregon, and Florida, respectively.

Table 4 summarizes the results for  $\tau_{max}$  set to 500 NM, 600 NM and 700 NM, and compares it with the prior 11 region system and other proposed geographical allocation policies. As is evident, our model produces a neighborhood that results in the narrowest range of s/d ratios across DSAs: 0.15 when  $\tau_{max} = 500$  NM, 0.13 when  $\tau_{max} = 600$  NM and 0.10 when  $\tau_{max} = 700$  NM, as compared to 0.34 (OPTN 11 regions), 0.17 (Gentry et al. 2015, 8 districts) and 0.64 (Kilambi and Mehrotra 2017). Our model also produces relatively more uniform and smaller size neighborhoods. It does not contain any unusually large neighborhoods (as evidenced by the value of  $\tau_{max}$ ). Further, the average

Allocation Policy	S/	s/d ratio		Max. (Median) s/d ratio
Anocation 1 oney	Range	Std. deviation	(in NM)	difference among adjacent DSAs
OPTN 11 regions	0.42 - 0.76	0.109	843, 401	$0.228 \; (0.117)$
Gentry et al. (2015)	0.52 - 0.69	0.054	975, 569	$0.120 \ (0.036)$
Kilambi and Mehrotra (2017)	0.35 - 0.99	0.157	1380, 666	0.615 (0.246)
[SP-2], $\tau_{max} = 500 \text{ NM}$	0.50 - 0.65	0.054	500, 349	$0.151 \ (0.086)$
[SP-2], $\tau_{max} = 600 \text{ NM}$	0.52 - 0.65	0.051	600, 409	0.132(0.077)
[SP-2], $\tau_{max} = 700 \text{ NM}$	0.53 - 0.63	0.033	700, 422	$0.096\ (0.036)$

Table 4 Comparison of s/d ratios among different allocation policies in the DSA version (supply and demand locations are 58 DSAs and 52 DSAs, respectively).  $\tau_{max}$  and  $\bar{\tau}$  represent the maximum and average distance, respectively, of the farthest DSA in a neighborhood/region/district in each allocation policy.

distance of the farthest DSAs in the neighborhoods ( $\bar{\tau}$ ) is much smaller than Gentry et al. (2015), Kilambi and Mehrotra (2017) and is comparable with OPTN 11 regions. The maximum s/d ratio difference among adjacent DSAs is also reduced significantly. For example, with  $\tau_{max} = 700$  NM, the maximum difference of s/d ratio among adjacent DSAs is 0.096, much smaller compared to OPTN 11 regions (0.228).

Table 5 presents the s/d ratios for each DSA in the different proposals. This allows a deeper examination of how each DSA is affected by the proposed reallocations. The maximum and minimum s/d ratio values are highlighted in bold. The appendix describes the DSA neighborhoods obtained by our models for  $\tau_{max} = 500$ , 600, and 700 NM, respectively.

#### 4.2.1. Liver Simulated Allocation Model (LSAM) Results

Next, we wanted to see how the proposed (DSA based) allocation policies perform on metrics that policy makers have traditionally examined to evaluate policies, like the variance of MMaT across geographies, distance traveled, and the number of deaths. To that end, we use LSAM to simulate our neighborhoods [SP-2], OPTN 11 regions, Gentry et al. (2015) (8 districts), and Kilambi and Mehrotra (2017)'s neighborhoods. There are two main inputs to LSAM: (1) patient and organ arrival processes, and (2) allocation policy that includes geographical schemes and offer prioritization rules.

LSAM uses historical data of donors and patients to simulate waiting list patient's health state transitions, organ acceptance behavior, and post-transplant survival outcomes. When an organ becomes available, candidates on the waiting list are prioritized for the organ offer as per the allocation policy. When a candidate receives a transplant, the simulation determines the survival time of the transplanted organ, and uses this information to determine when in the future the candidate may die or relist. Using LSAM in its current form does have some limitations. It uses a probability acceptance function that is built on past data where distance is more strongly correlated with acceptance of an organ because of the lack of broader sharing. It also does not account for organ availability in determining organ acceptance. These limitations may underestimate the effects

				s/d ratio				
DSA	Local, or	OPTN 11 regions	Gentry et al. (2015)			S	P-2]	
	no sharing	$\tau_{max} = 843 \text{ NM}$	$\tau_{max} = 975 \text{ NM}$	$\tau_{max} = 1380 \text{ NM}$	$\tau_{max}$ :	500 NM	600 NM	700 NM
ALOB	0.72	0.76	0.61	0.56	·max·	0.62	0.65	0.63
AROR	0.97	0.76	0.61	0.96		0.65	0.52	0.58
AZOB	0.55	0.52	0.54	0.88		0.53	0.53	0.59
CADN	0.38	0.52	0.52	0.45		0.51	0.52	0.53
CAOP	0.39	0.52	0.52	0.5		0.54	0.53	0.53
CASD	0.55	0.52	0.52	0.35		0.5	0.53	0.59
CORS	0.37	0.64	0.54	0.77		0.51	0.54	0.53
CTOP	0.95	0.42	0.57	0.4		0.56	0.62	0.59
DCTC	0.58	0.57	0.57	0.46		0.64	0.64	0.63
FLFH	1.3	0.76	0.61	0.65		0.54	0.52	0.62
FLMP	0.5	0.76	0.61	0.65		0.61	0.65	0.61
FLUF	0.47	0.76	0.61	0.81		0.65	0.58	0.61
FLWC	1.98	0.76	0.61	0.65		0.64	0.52	0.62
GALL	0.72	0.76	0.57	0.99		0.65	0.65	0.62
HIOP	0.97	0.66	0.52	0.37		0.63	0.64	0.54
IAOP	1.23	0.64	0.64	0.58		0.62	0.64	0.61
ILIP	0.69	0.55	0.69	0.62		0.65	0.62	0.62
INOP	0.78	0.66	0.69	0.67		0.62	0.63	0.59
KYDA	0.66	0.76	0.69	0.69		0.65	0.64	0.6
LAOP	0.55	0.76	0.61	0.64		0.63	0.65	0.63
MAOB	0.39	0.42	0.57	0.4		0.54	0.61	0.56
MDPC	0.34	0.57	0.57	0.67		0.64	0.65	0.63
MIOP	0.68	0.66	0.69	0.49		0.54	0.64	0.63
MNOP	0.4	0.55	0.64	0.53		0.51	0.56	0.56
MOMA	0.71	0.64	0.61	0.73		0.65	0.63	0.63
MSOP	1.49	0.76	0.61	0.56		0.58	0.55	0.63
MWOB	1.04	0.64	0.64	0.7		0.5	0.52	0.56
NCCM	0.73	0.76	0.57	0.44		0.65	0.64	0.62
NCNC	0.77	0.76	0.57	0.63		0.65	0.6	0.62
NEOR	0.41	0.64	0.64	0.44		0.51	0.54	0.63
NJTO	1.19	0.57	0.57	0.47		0.65	0.65	0.63
NYFL	0.56	0.42	0.69	0.59		0.53	0.53	0.62
NYRT	0.31	0.42	0.57	0.47		0.65	0.65	0.63
OHLB	0.47	0.66	0.69	0.67		0.65	0.65	0.62
OHLP	0.9	0.66	0.69	0.83		0.65	0.61	0.62
OHOV	0.33	0.66	0.69	0.51		0.65	0.65	0.61
OKOP	0.91	0.53	0.64	0.81		0.58	0.52	0.63
ORUO	0.71	0.66	0.52	0.62		0.62	0.65	0.58
PADV	0.62	0.57	0.57	0.6		0.62	0.65	0.63
PATF	0.58	0.57	0.69	0.83		0.64	0.59	0.63
PRLL	1.69	0.76	0.57	0.56		0.54	0.6	0.53
SCOP	1.02	0.76	0.57	0.38		0.65	0.62	0.62
TNDS	1.17	0.76	0.69	0.77		0.65	0.64	0.63
TNMS	0.36	0.76	0.61	0.85		0.65	0.64	0.62
TXGC	0.36	0.53	0.61	0.52		0.64	0.58	0.63
TXSA	0.5	0.53	0.61	0.44		0.53	0.52	0.53
TXSB	0.77	0.53	0.61	0.5		0.64	0.55	0.62
UTOP	0.53	0.52	0.54	0.47		0.54	0.55	0.56
VATB	0.6	0.76	0.57	0.85		0.63	0.65	0.62
WALC	0.6	0.66	0.52	0.6		0.62	0.62	0.55
WIDN	0.4	0.55	0.69	0.5		0.5	0.54	0.62
WIUW	0.61	0.55	0.69	0.72		0.62	0.63	0.63

Table 5 Comparison of s/d ratios among different DSA based allocation policies (supply and demand locations are 58 DSAs and 52 DSAs, respectively).

of broader sharing and the equalization of the s/d ratios. Despite these limitations, it is instructive to use LSAM as a first step in evaluating the potential benefit of the heterogeneous radii circles policy.

In the simulation study (to model broader sharing within a circle) we allow for full sharing of organs to Status 1A/1B and  $MELD \geq 15$  candidates in the neighborhood or region/district in which the organ is recovered in the first level of allocation. In the next allocation level, the organ is offered nationally to Status 1A/1B, then nationally to candidates with  $MELD \geq 15$ . Next, it is offered to candidates with MELD < 15 locally (DSA in which the organ is recovered), then in the neighborhood or region/district, and then nationally, before being discarded after 100 offers. The above policy, that we refer to as "Enhanced Share 15", skips sequences # 2 and 3 of the Share 35 policy described in Table 1. For benchmarking, we also compared using the prior Share 35 policy.

	Avg. (Quartiles)	Waitlist	Total	I	Across DSAs
Allocation Policy	travel distance	deaths	deaths	Variance	Std. deviation of avg
	(in NM)	(annual)	(annual)	of MMaT	travel distance (NM)
OPTN 11 regions	258 (75, 194, 347)	1411.6	3658.8	7.26	109
Gentry et al. (2015)	309 (101, 226, 429)	1376.1	3600.0	5.22	124
Kilambi and Mehrotra (2017)	305 (124, 240, 395)	1348.2	3555.4	2.68	142
[SP-2], $\tau_{max} = 500 \text{ NM}$	258 (112, 220, 341)	1356.4	3567.7	2.00	56
[SP-2], $\tau_{max} = 600 \text{ NM}$	283 (125, 251, 384)	1343.6	3551.4	1.98	55
[SP-2], $\tau_{max} = 700 \text{ NM}$	293 (125, 250, 399)	1343.4	3544.6	1.61	64

Table 6 Comparison of LSAM simulation results for DSA-based allocation policies under Enhanced Share 15.

We simulated the different DSA-based geographical allocation policies using the organ and patient arrival data, consisting of 3 years (July 2013 to June 2016). We ran the simulation ten times (the maximum allowed by LSAM) by resampling the input files.

Table 6 compares the simulation results under Enhanced Share 15. The average number of annual waitlist deaths and total deaths is smallest for [SP-2],  $\tau_{max} = 700$  NM, with a projected savings of 114 lives annually compared to OPTN 11 regions. The average travel distance, although slightly higher in our allocation policy compared to OPTN 11 regions, is smaller than the other policies. To measure the differences between DSAs, we consider the variance of MMaT and the standard deviation of average organ travel distance, across DSAs. The variance of MMaT across the DSAs is smallest in our allocation policies (2.00 when  $\tau_{max} = 500$  NM, 1.98 when  $\tau_{max} = 600$  NM and 1.61 when  $\tau_{max} = 700$  NM), compared to 7.26, 5.22 and 2.68 in OPTN 11 regions, Gentry et al. (2015) and Kilambi and Mehrotra (2017) respectively. Since the different proposals vary in their efficiency (travel distance) and fairness (MMaT) metrics, it is instructive to compare the fairness of proposals with similar levels of efficiency. To that end comparing [SP-2],  $\tau_{max} = 500$  NM against OPTN 11 regions, shows a significant reduction in both total deaths and variance of MMaT. Similarly, comparing [SP-2],  $\tau_{max} = 700$  NM against Gentry et al. (2015) and Kilambi and Mehrotra (2017), shows a significant reduction in the variance of MMaT. Overall, we see that greater fairness can be achieved by DSA-based geographical allocation policies that equalize s/d ratios. The standard deviation of average travel distance across the DSAs (Hawaii and Puerto Rico are excluded from our distance analysis) in our allocation policies is less than half that of the others. This indicates that there is less disparity in travel distance between DSAs because our neighborhoods have relatively similar sizes.

Table 7 compares the LSAM simulation results under Share 35. We note that our neighborhoods are optimized under the assumption of full sharing, which is closer to Enhanced Share 15 than Share 35, and thus the full benefits of improved MMaT is less likely to be seen. Since there is less sharing under Share 35 (organs offers are restricted to within DSA patients (15≤MELD<35) before being offered broadly (neighborhood or region/district and nationally)) the average travel

	Avg. (Quartiles)	Waitlist	Total		Across DSAs
Allocation Policy	travel distance	deaths	deaths	Variance	Std. deviation of avg.
	(in NM)	(annual)	(annual)	of MMaT	travel distance (NM)
OPTN 11 regions	199 (20, 105, 258)	1455.5	3744.9	13.66	88
Gentry et al. (2015)	231 (25, 130, 314)	1419.5	3696.4	10.49	102
Kilambi and Mehrotra (2017)	230 (32, 150, 309)	1389.0	3656.3	11.87	104
[SP-2], $\tau_{max} = 500 \text{ NM}$	203 (29, 142, 291)	1399.9	3664.8	10.30	57
[SP-2], $\tau_{max} = 600 \text{ NM}$	221 (32, 157, 326)	1384.8	3645.2	8.80	57
[SP-2], $\tau_{max} = 700 \text{ NM}$	233 (36, 162, 344)	1397.3	3636.4	10.04	64

Table 7 Comparison of LSAM simulation results for DSA-based allocation policies under Share 35.

distance significantly decreased, and the number of the waitlist and total deaths increased for all policies. Even so, comparing [SP-2],  $\tau_{max} = 500$  NM against OPTN 11 regions, shows a significant reduction in both total deaths and variance of MMaT. Similarly, comparing [SP-2],  $\tau_{max} = 600$  NM against Gentry et al. (2015) and Kilambi and Mehrotra (2017), shows a significant reduction in the variance of MMaT. Like Enhanced Share 15, we observe again the standard deviation of average travel distances (across DSAs) is much lower for our allocation policies.

Ultimately comparing our allocation policy  $\tau_{max} = 500$  NM under Enhanced Share 15 against OPTN 11 regions under Share 35 shows that a drastic reduction in the variance of MMaT across DSAs (from 13.66 to 2.00) and deaths (from 3745 to 3568) can be achieved, for a modest increase in the average travel distance (from 199 NM to 258 NM).

# 5. Conclusions

We use the Rawlsian *maximin* principle to minimize the variability in deceased donor liver access across geographies. In contrast to the current fixed radius policy, we propose heterogeneous radii circles. The benefit of heterogeneous radii circles is that they account for where organ supply and demand occur, and adjust radii of the circles so that each transplant center's s/d ratio can be close to the national average. Moreover, equalizing the s/d ratios at the transplant centers is achieved without a significant increase in anticipated travel distance. In fact, the median radius is approximately 305 NM. In other words, the optimization model only increases the radii of donor circles when necessary.

By using DSA as the geographical unit, we demonstrate that low geographical variation in s/d ratio can be achieved while maintaining DSA boundaries by judiciously creating neighborhoods for each DSA. An LSAM evaluation of our DSA neighborhoods predicts significant reduction in the number of deaths, and the overall variation in MMaT and average travel distance across DSAs.

As noted earlier, there are limitations of our analysis since LSAM's organ acceptance function may not accurately reflect the change in candidate/transplant center behaviors when organ accessibility and availability changes. For instance candidates at organ rich locations might behave more

selectively in accepting organs, than at locations with low s/d ratios. Additionally, with broader sharing the correlation between organ acceptance probability and distance may decrease within the radius of a circle (or neighborhood). Studying changes in organ acceptance behavior with organ accessibility can be an interesting future research work.

In terms of a logistical implementation of the heterogeneous circles policy, we have a few suggestions. First, we believe the circles should be defined around the donor location (hospital, zip code, county, DSA, etc.) rather than the transplant location, else the issues raised in the lawsuits would not be addressed. Second, we expect small variations in supply and demand over time. Hence, we suggest that the optimization model be run occasionally to account for changes in demographics.

Our approach can be viewed as a combination of the fixed distance from a donor hospital and a mathematical optimized boundaries framework identified by the Geography Committee. There is considerable debate in the transplant community about using continuous scoring (the third distribution framework identified by the Geography Committee). Rather than a one-size-fits-all framework for continuous scoring, that we do not believe will address geographical inequities adequately, we would recommend a mathematically optimized continuous scoring function that accounts for regional differences in supply and demand.

Clearly the optimization concepts applied to mitigate geographical disparities in the liver transplantation setting could also be applied to other organs. We hope this research will spur similar work in the other organ transplantation settings, and thus reduce/mitigate the geographical disparities that are inherent to all of these systems!

# **Declarations**

- Funding: No funding was received for conducting this study.
- Conflict of interest/Competing interests: The authors have no relevant financial or non-financial interests to disclose.
  - Ethics approval: Ethics approval was not needed
  - Consent to participate: Not Applicable.
  - Consent for publication: Not Applicable.
- Availability of data and materials: The data reported here have been supplied by the Hennepin Healthcare Research Institute as the contractor for the Scientific Registry of Transplant Recipients (SRTR). The interpretation and reporting of these data are the responsibility of the authors and in no way should be seen as an official policy or interpretation by the SRTR or the U.S. Government. Due to the data protection laws, the dataset cannot be directly released to another organization. The interested readers can gain access to the dataset by establishing a data use agreement with the SRTR.
  - Code availability: The authors can provide the pseudo code upon request.
- Authors' contributions- Conceptualization: Shubham Akshat, Sommer E. Gentry, S. Raghavan; Methodology: Shubham Akshat, S. Raghavan; Formal analysis and investigation: Shubham Akshat, S. Raghavan; Writing original draft preparation: Shubham Akshat; Writing review and editing: Shubham Akshat, S. Raghavan

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# Linearization of s/d Ratio and Contiguity Constraints

To linearize the right hand side of constraint (2) in [S-1], i.e.,  $\sum_{i=1}^{N_{sup}} \frac{1}{\sum_{k=1}^{N_{dem}} d_k x_{ik}} s_i x_{ij}$ , we introduce auxiliary variables:  $y_{ij} \ge 0$  and  $t_i \ge 0$  that are defined as follows.

$$t_{i} = \frac{1}{\sum_{k=1}^{N_{dem}} d_{k} x_{ik}} \qquad \forall i \in \mathcal{I}$$

$$y_{ij} = t_{i} x_{ij} \qquad \forall i \in \mathcal{I}, j \in \mathcal{J}$$

$$(19)$$

$$y_{ij} = t_i x_{ij}$$
  $\forall i \in \mathcal{I}, j \in \mathcal{J}$  (20)

Together these imply:

$$\lambda \leq \sum_{i=1}^{N_{sup}} s_i y_{ij} \qquad \forall j \in \mathcal{J}$$

$$\sum_{k=1}^{N_{dem}} d_k y_{ik} = 1 \qquad \forall i \in \mathcal{I}$$
(21)

$$\sum_{k=1}^{N_{dem}} d_k y_{ik} = 1 \qquad \forall i \in \mathcal{I}$$
 (22)

We note that  $t_i \leq 1$  and,  $y_{ij} = \begin{cases} 0 & \text{if } x_{ij} = 0 \\ t_i & \text{if } x_{ij} = 1 \end{cases}$ . Since  $y_{ij}$  is a product of two variables and therefore nonlinear, the following linear constraints model  $y_{ij} = t_i x_{ij}$ :

$$y_{ij} \le t_i \qquad \forall i \in \mathcal{I}, j \in \mathcal{J}$$
 (23)

$$y_{ij} \le x_{ij} \qquad \forall i \in \mathcal{I}, j \in \mathcal{J}$$
 (24)

$$(1 - x_{ij}) + y_{ij} \ge t_i \qquad \forall i \in \mathcal{I}, j \in \mathcal{J}$$
 (25)

$$y_{ij}, t_i \ge 0 \qquad \forall i \in \mathcal{I}, j \in \mathcal{J}$$
 (26)

Therefore, constraint (2) in [S-1] can be replaced by constraints (21)-(26). Constraint (8) in [S-2] can be linearized identically.

Shirabe (2009) describes flow-based contiguity constraints for districting problems. We adapt those constraints to model receiving contiguity and sharing contiguity in our neighborhood framework through equations (27)-(29) and (30)-(32), respectively. With receiving (sharing) contiguity, the suppliers (recipients) assigned to a recipient (supplier) form a continuous geography on the map. Let  $m_1$  ( $m_2$ ) be the maximum number of supply (demand) locations that can be assigned to a demand (supply) location. Parameter  $a_{ik} = 1$ , if supply locations i and k are geographically adjacent, and 0 otherwise. We use flow variables  $f_{ik}^j$  to model receiving contiguity and flow variables  $g_{jk}^i$  to model sharing contiguity. Flow variable  $f_{ik}^j$  denotes the flow from i to k (only defined when  $a_{ik} = 1$ ) destined for demand location j, while flow variable  $g_{ik}^i$  denotes the flow from j to k (only defined when  $a_{jk} = 1$ ) destined for supply location i. The first three constraints involving the flow variables  $f_{ik}^j$  ensure that if  $x_{ij} = 1$  for a supply location i and a demand location j that are non-adjacent, then every supply location on the path from i to j also supplies demand location j. The next set of three constraints involving the flow variables  $g_{jk}^i$  ensure that if  $x_{ij} = 1$  for a supply location i and a demand location j that are non-adjacent, then every demand location on the path from i to j is also supplied by i.

$$\sum_{k=1}^{N_{sup}} f_{ik}^{j} a_{ik} - \sum_{k=1}^{N_{sup}} f_{ki}^{j} a_{ki} = x_{ij} \qquad \forall i \neq j, i \in \mathcal{I}, j \in \mathcal{J}$$
 (27)

$$\sum_{k=1}^{N_{sup}} f_{ki}^{j} a_{ki} \le (m_1 - 1) x_{ij} \ \forall i \in \mathcal{I}, j \in \mathcal{J}$$
 (28)

$$\sum_{k=1}^{N_{sup}} f_{jk}^{j} a_{jk} = 0 \qquad \forall j \in \mathcal{J}$$
 (29)

$$\sum_{k=1}^{N_{sup}} f_{jk}^{j} a_{jk} = 0 \qquad \forall j \in \mathcal{J}$$

$$\sum_{k=1}^{N_{dem}} g_{jk}^{i} a_{jk} - \sum_{k=1}^{N_{dem}} g_{kj}^{i} a_{kj} = x_{ij} \qquad \forall i \neq j, i \in \mathcal{I}, j \in \mathcal{J}$$

$$(30)$$

$$\sum_{k=1}^{N_{dem}} g_{kj}^{i} a_{kj} \le (m_2 - 1) x_{ij} \ \forall i \in \mathcal{I}, j \in \mathcal{J}$$
(31)

$$\sum_{k=1}^{N_{dem}} g_{ik}^{i} a_{ik} = 0 \qquad \forall i \in \mathcal{I}$$

$$f_{ik}^{j} \geq 0 \qquad \forall i, k \in \mathcal{I}, j \in \mathcal{J}$$

$$g_{jk}^{i} \geq 0 \qquad \forall i \in \mathcal{I}, k, j \in \mathcal{J}$$

$$(32)$$

$$(33)$$

$$f_{ik}^j \ge 0 \qquad \forall i, k \in \mathcal{I}, j \in \mathcal{J}$$
 (33)

$$g_{ik}^i \ge 0 \qquad \forall i \in \mathcal{I}, k, j \in \mathcal{J}$$
 (34)

Together constraints (27)-(34) refer to constraint (6) in [S-1].

# Appendix B: DSA Neighborhoods

Table 8, 9, and 10, present the neighborhoods obtained by our model based on the DSA version when the maximum distance to any DSA in the neighborhood is constrained to 500 NM, 600 NM, and 700 NM, respectively. The column, "Radius" provides the radius (in terms of the transplant volume weighted distance as discussed in Section 4.2) of each neighborhood. The column, "Neighbors" contains the DSAs to which the DSA in the first column will share its organs to.

The radii for each zip-code cluster in the zip-code version (which is too large to include as a table) can be obtained by contacting the authors.

	D . 1' .	
DSA	Radius (in NM)	Neighbors
ALOB	336	KYDA, ALOB, NCCM, TNDS, MSOP, AROR, SCOP, TNMS, FLUF, GALL, LAOP
AROR	305	MSOP, AROR, TXSB, TNMS, MOMA, MWOB, TXGC, LAOP, OKOP
AZOB	499	AZOB, CORS, UTOP, CASD, CAOP
$\begin{array}{c} \text{CADN} \\ \text{CAGS} \end{array}$	366	HIOP, CADN, CASD, CAOP
CAGS	318 499	HIOP, CADN, CAOP HIOP, AZOB, UTOP, CADN, CASD, CAOP
CASD	366	HIOF, AZOB, CADN, CASD, CAOP HIOP, AZOB, CADN, CASD, CAOP
CORS	316	CORS, UTOP
CTOP	203	MAOB, NYFL, CTOP, PADV, NJTO, NYRT
DCTC	339	OHOV, NCNC, MAOB, NYFL, PATF, NCCM, CTOP, DCTC, PADV, VATB, MDPC, OHLP, NJTO, OHLB, NYRT
$_{ m FLFH}$	$\frac{492}{472}$	NCNC, ALOB, PRLL, NCCM, TNDS, FLMP, MSOP, SCOP, FLFH, FLUF, FLWC, GALL PRLL, FLMP, SCOP, FLFH, FLUF, FLWC, GALL
FLUF	422	NCNC, ALOB, PRLL, NCCM, TNDS, FLMP, MSOP, SCOP, FLFH, FLUF, FLWC, GALL, LAOP
FLWC	488	NCNC, ALOB, PRLL, NCCM, FLMP, MSOP, SCOP, FLFH, FLUF, FLWC, GALL
GALL	484	OHOV, NCNC, KYDA, ALOB, PATF, NCCM, DCTC, TNDS, FLMP, MSOP, AROR, SCOP, TNMS, VATB, MOMA, OHLP, FLFH, OHLB, FLUF, INOP, FLWC, GALL, LAOP
HIOP	NA	HIOP, CADN, CASD, CAOP
IAOP	210	MNOP, WIUW, IAOP, NEOR
ILIP	447	OHOV, MNOP, KYDA, PATF, TNDS, WIUW, ILIP, AROR, IAOP, TNMS, MOMA, MWOB, OHLP, WIDN, NEOR, OHLB, INOP, MIOP
INOP	224	OHOV, KYDA, ILIP, OHLP, WIDN, OHLB, INOP, MIOP
KYDA	497	OHOV, NCNC, KYDA, ALOB, NYFL, PATF, NCCM, DCTC, TNDS, PADV, WIUW, ILIP, MSOP, AROR, IAOP, SCOP, TNMS, VATB, MDPC, MOMA, MWOB, OHLP, WIDN, OHLB, FLUF, INOP, GALL, MIOP
LAOP	396	TXSA, ALOB, MSOP, AROR, TXSB, TNMS, TXGC, LAOP, OKOP
MAOB	170	MAOB, CTOP, NJTO, NYRT
MDPC	308	NCNC, MAOB, NYFL, PATF, CTOP, DCTC, PADV, VATB, MDPC, OHLP, NJTO, OHLB, NYRT
MIOP	482	OHOV, MNOP, KYDA, NYFL, PATF, NCCM, DCTC, TNDS, PADV, WIUW, ILIP, IAOP, VATB, MDPC, MOMA,
		OHLP, NJTO, WIDN, OHLB, INOP, NYRT, MIOP
MNOP	270	MNOP, WIUW, IAOP, NEOR
MOMA	233	ILIP, AROR, TNMS, MOMA, MWOB
MSOP	406	ALOB, TNDS, MSOP, AROR, TXSB, TNMS, MOMA, TXGC, FLUF, GALL, LAOP
MWOB	477	MNOP, KYDA, WIUW, ILIP, AROR, IAOP, TXSB, TNMS, MOMA, MWOB, WIDN, CORS, NEOR, TXGC, INOP, OKOP
NCCM	403	OHOV, NCNC, KYDA, ALOB, PATF, NCCM, DCTC, TNDS, PADV, SCOP, VATB, MDPC, OHLP, FLFH, OHLB, FLUF, INOP, GALL
NCNC	489	OHOV, NCNC, KYDA, ALOB, NYFL, PATF, NCCM, CTOP, DCTC, TNDS, PADV, SCOP, VATB, MDPC, OHLP, NJTO, FLFH, OHLB, FLUF, INOP, FLWC, NYRT, GALL, MIOP
NEOR	390	MNOP, WIUW, IAOP, MOMA, MWOB, CORS, NEOR, OKOP
NJTO	188	MAOB, NYFL, CTOP, DCTC, PADV, MDPC, NJTO, NYRT
NMOP	282	AZOB
NVLV	308	AZOB, CADN, CASD, CAOP
NYAP	182	MAOB, NYFL, CTOP, PADV, NJTO, NYRT
NYFL	458	OHOV, MAOB, NYFL, PATF, CTOP, DCTC, PADV, VATB, MDPC, OHLP, NJTO, OHLB, INOP, NYRT, MIOP
NYRT	193	MAOB, NYFL, CTOP, PADV, MDPC, NJTO, NYRT
NYWN	234	NYFL, PATF, PADV, OHLB, MIOP OHOW NONG KYDA MAOD NYFL DATE NOOM CTOD DOTG TNDS DADV WHIW HID SCOD VATD MDDC
OHLB	459	OHOV, NCNC, KYDA, MAOB, NYFL, PATF, NCCM, CTOP, DCTC, TNDS, PADV, WIUW, ILIP, SCOP, VATB, MDPC, MOMA, OHLP, NJTO, WIDN, OHLB, INOP, NYRT, MIOP
OHLC	329	OHOV, KYDA, PATF, DCTC, TNDS, WIUW, ILIP, OHLP, WIDN, OHLB, INOP, MIOP
OHLE	307	OHOV, KYDA, PATF, NCCM, DCTC, TNDS, WIDW, ILIP, VATB, MDFC, OHLP, WIDN, OHLB, INOP, MIOP
OHOV	284	OHOV, KYDA, PATF, NCCM, TNDS, ILIP, OHLP, WIDN, OHLB, INOP, MIOP
OKOP	475	TXSA, MSOP, AROR, IAOP, TXSB, TNMS, MOMA, MWOB, CORS, NEOR, TXGC, LAOP, OKOP
ORUO	234	WALC, HIOP, ORUO
PADV	235	MAOB, NYFL, PATF, CTOP, DCTC, PADV, VATB, MDPC, NJTO, NYRT
PATF	278	OHOV, NCNC, NYFL, PATF, DCTC, PADV, VATB, MDPC, OHLP, NJTO, OHLB, NYRT, MIOP
PRLL	NA	PRLL, FLMP, FLWC
SCOP	326	NCNC, KYDA, ALOB, NCCM, TNDS, SCOP, VATB, FLFH, FLUF, GALL
TNDS	493	OHOV, NCNC, KYDA, ALOB, PATF, NCCM, DCTC, TNDS, ILIP, MSOP, AROR, SCOP, TNMS, VATB, MDPC,
TNMS	492	MOMA, MWOB, OHLP, WIDN, FLFH, OHLB, FLUF, INOP, GALL, MIOP, LAOP OHOV, KYDA, ALOB, NCCM, TNDS, ILIP, MSOP, AROR, IAOP, SCOP, TXSB, TNMS, MOMA, MWOB, OHLP,
TVCC	276	WIDN, TXGC, FLUF, INOP, GALL, LAOP, OKOP
TXGC TXSA	276 363	TXSA, TXSB, TXGC, LAOP, OKOP TXSA, TXSB, TXGC, LAOP
TXSA	218	TXSA, TXSB, TXGC, LAOP TXSA, TXSB, TXGC, OKOP
UTOP	480	AZOB, CORS, UTOP, CADN
VATB	196	NCNC, DCTC, PADV, VATB, MDPC
WALC	234	WALC, ORUO
WIDN	284	OHOV, WIUW, ILIP, IAOP, WIDN, INOP, MIOP
WIUW	426	OHOV, MNOP, WIUW, ILIP, IAOP, MOMA, MWOB, OHLP, WIDN, NEOR, OHLB, INOP, MIOP
	_	List Heart of DCA to the Company of

Table 8 Geographical allocation policy for DSAs when the maximum permitted distance to a neighboring DSA is 500 NM

DSA	Radius (in NM)	Neighbors
ALOB	517	OHOV, NCNC, KYDA, ALOB, NCCM, TNDS, MSOP, AROR, SCOP, TNMS, VATB, MOMA, OHLP, FLFH, TXGC,
AROR	569	FLUF, INOP, FLWC, GALL, LAOP OHOV, TXSA, KYDA, ALOB, TNDS, ILIP, MSOP, AROR, IAOP, TXSB, TNMS, MOMA, MWOB, WIDN, NEOR, TXGC, FLUF, INOP, GALL, LAOP, OKOP
AZOB	546	AZOB, CORS, UTOP, CADN, CASD, CAOP
CADN	366	HIOP, CADN, CASD, CAOP
CAGS	446	HIOP, ORUO, UTOP, CADN, CASD, CAOP
CAOP	499	HIOP, AZOB, UTOP, CADN, CASD, CAOP
CASD	265	HIOP, AZOB, CASD, CAOP
CORS	316	CORS, UTOP
CTOP	244	MAOB, NYFL, CTOP, PADV, MDPC, NJTO, NYRT
DCTC	346	OHOV, NCNC, MAOB, NYFL, PATF, NCCM, CTOP, DCTC, PADV, SCOP, VATB, MDPC, OHLP, NJTO, OHLB, NYRT
FLFH	578	NCNC, ALOB, PRLL, NCCM, TNDS, FLMP, MSOP, SCOP, TNMS, VATB, FLFH, FLUF, FLWC, GALL, LAOP
FLMP FLUF	573 $592$	NCNC, ALOB, PRLL, NCCM, FLMP, SCOP, FLFH, FLUF, FLWC, GALL OHOV, NCNC, KYDA, ALOB, PRLL, NCCM, TNDS, FLMP, MSOP, AROR, SCOP, TNMS, VATB, OHLP, FLFH, FLUF,
FLWC GALL	330 565	FLWC, GALL, LAOP PRLL, FLMP, FLFH, FLUF, FLWC, GALL OHOV, NCNC, KYDA, ALOB, PATF, NCCM, DCTC, TNDS, PADV, FLMP, ILIP, MSOP, AROR, SCOP, TNMS, VATB, MDPC, MOMA, OHLP, FLFH, OHLB, FLUF, INOP, FLWC, GALL, MIOP, LAOP
HIOP	NA	HIOP, CADN, CASD, CAOP
IAOP	335	MNOP, WIUW, ILIP, IAOP, MOMA, MWOB, WIDN, NEOR, INOP
ILIP INOP	365 571	OHOV, MNOP, KYDA, TNDS, WIUW, ILIP, IAOP, MOMA, MWOB, OHLP, WIDN, OHLB, INOP, MIOP OHOV, MNOP, NCNC, KYDA, ALOB, NYFL, PATF, NCCM, DCTC, TNDS, PADV, WIUW, ILIP, MSOP, AROR, IAOP, SCOP, TNMS, VATB, MDPC, MOMA, MWOB, OHLP, NJTO, WIDN, NEOR, OHLB, INOP, NYRT, GALL, MIOP, OKOP
KYDA	497	OHOV, NCNC, KYDA, ALOB, NYFL, PATF, NCCM, DCTC, TNDS, PADV, WIUW, ILIP, MSOP, AROR, IAOP, SCOP, TNMS, VATB, MDPC, MOMA, MWOB, OHLP, WIDN, OHLB, FLUF, INOP, GALL, MIOP
LAOP MAOB	396 170	TXSA, ALOB, MSOP, AROR, TXSB, TNMS, TXGC, LAOP, OKOP MAOB, CTOP, NJTO, NYRT
MDPC	407	OHOV, NCNC, KYDA, MAOB, NYFL, PATF, NCCM, CTOP, DCTC, PADV, SCOP, VATB, MDPC, OHLP, NJTO, OHLB, NYRT, MIOP
MIOP	594	OHOV, MNOP, NCNC, KYDA, MAOB, NYFL, PATF, NCCM, CTOP, DCTC, TNDS, PADV, WIUW, ILIP, IAOP, SCOP, TNMS, VATB, MDPC, MOMA, MWOB, OHLP, NJTO, WIDN, NEOR, OHLB, INOP, NYRT, GALL, MIOP
MNOP	270	MNOP, WIUW, IAOP, NEOR
MOMA	600	OHOV, MNOP, NCNC, KYDA, ALOB, PATF, NCCM, TNDS, WIUW, ILIP, MSOP, AROR, IAOP, SCOP, TXSB, TNMS, MOMA, MWOB, OHLP, WIDN, NEOR, OHLB, TXGC, FLUF, INOP, GALL, MIOP, LAOP, OKOP
MSOP MWOB	482 590	TXSA, KYDA, ALOB, NCCM, TNDS, MSOP, AROR, SCOP, TXSB, TNMS, MOMA, MWOB, FLFH, TXGC, FLUF, FLWC, GALL, LAOP, OKOP OHOV, TXSA, MNOP, KYDA, ALOB, TNDS, WIUW, ILIP, MSOP, AROR, IAOP, TXSB, TNMS, MOMA, MWOB,
NCCM	498	WIDN, CORS, NEOR, TXGC, INOP, MIOP, LAOP, OKOP OHOV, NCNC, KYDA, ALOB, PATF, NCCM, DCTC, TNDS, PADV, ILIP, MSOP, SCOP, TNMS, VATB, MDPC, MOMA,
NCNC	570	OHLP, NJTO, FLFH, OHLB, FLUF, INOP, FLWC, NYRT, GALL, MIOP OHOV, NCNC, KYDA, ALOB, MAOB, NYFL, PATF, NCCM, CTOP, DCTC, TNDS, PADV, ILIP, MSOP, SCOP, TNMS, VATB, MDPC, OHLP, NJTO, FLFH, OHLB, FLUF, INOP, FLWC, NYRT, GALL, MIOP
NEOR	377	MNOP, IAOP, MOMA, MWOB, CORS, NEOR, OKOP
NJTO	254	MAOB, NYFL, PATF, CTOP, DCTC, PADV, VATB, MDPC, NJTO, NYRT
NMOP	282	AZOB
NVLV	308	AZOB, CADN, CASD, CAOP
NYAP	182	MAOB, NYFL, CTOP, PADV, NJTO, NYRT
NYFL	582	OHOV, NCNC, KYDA, MAOB, NYFL, PATF, NCCM, CTOP, DCTC, PADV, WIUW, ILIP, SCOP, VATB, MDPC, OHLP, NJTO, WIDN, OHLB, INOP, NYRT, MIOP
NYRT	195	MAOB, NYFL, CTOP, DCTC, PADV, MDPC, NJTO, NYRT
NYWN	326	MAOB, NYFL, PATF, CTOP, DCTC, PADV, MDPC, OHLP, NJTO, OHLB, NYRT, MIOP
OHLB	457	OHOV, NCNC, KYDA, MAOB, NYFL, PATF, NCCM, CTOP, DCTC, TNDS, PADV, WIUW, ILIP, SCOP, VATB, MDPC, OHLP, NJTO, WIDN, OHLB, INOP, NYRT, MIOP
OHLC OHLP	346 366	OHOV, KYDA, PATF, NCCM, DCTC, TNDS, WIUW, ILIP, MDPC, MOMA, OHLP, WIDN, OHLB, INOP, MIOP OHOV, NCNC, KYDA, NYFL, PATF, NCCM, DCTC, TNDS, PADV, ILIP, SCOP, VATB, MDPC, OHLP, WIDN, OHLB, INOP, MIOP
OHOV	599	OHOV, MNOP, NCNC, KYDA, ALOB, NYFL, PATF, NCCM, CTOP, DCTC, TNDS, PADV, WIUW, ILIP, MSOP, AROR, IAOP, SCOP, TNMS, VATB, MDPC, MOMA, MWOB, OHLP, NJTO, WIDN, NEOR, OHLB, FLUF, INOP, NYRT, GALL, MIOP
OKOP	397	TXSA, AROR, TXSB, TNMS, MOMA, MWOB, NEOR, TXGC, LAOP, OKOP
ORUO	234	WALC, HIOP, ORUO
PADV	275	MAOB, NYFL, PATF, CTOP, DCTC, PADV, VATB, MDPC, NJTO, OHLB, NYRT
PATF	406	OHOV, NCNC, KYDA, MAOB, NYFL, PATF, NCCM, CTOP, DCTC, TNDS, PADV, ILIP, SCOP, VATB, MDPC, OHLP, NJTO, WIDN, OHLB, INOP, NYRT, MIOP
PRLL	NA	PRLL, FLMP
SCOP	450	OHOV, NCNC, KYDA, ALOB, PATF, NCCM, DCTC, TNDS, PADV, SCOP, TNMS, VATB, MDPC, OHLP, FLFH,
TNDS	525	OHLB, FLUF, INOP, FLWC, GALL OHOV, NCNC, KYDA, ALOB, PATF, NCCM, DCTC, TNDS, PADV, ILIP, MSOP, AROR, IAOP, SCOP, TNMS, VATB,
TNMS	594	MDPC, MOMA, MWOB, OHLP, WIDN, FLFH, OHLB, FLUF, INOP, FLWC, GALL, MIOP, LAOP OHOV, TXSA, NCNC, KYDA, ALOB, PATF, NCCM, TNDS, WIUW, ILIP, MSOP, AROR, IAOP, SCOP, TXSB, TNMS, VATB, MOMA, MWOB, OHLP, WIDN, NEOR, FLFH, OHLB, TXGC, FLUF, INOP, FLWC, GALL, MIOP, LAOP, OKOP
TXGC	276	TXSA, TXSB, TXGC, LAOP, OKOP
TXSA	179	TXSA, TXSB, TXGC
TXSB	598	TXSA, ALOB, MSOP, AROR, TXSB, TNMS, MOMA, MWOB, CORS, NEOR, TXGC, LAOP, OKOP
UTOP VATB	480 437	AZOB, CORS, UTOP, CADN OHOV, NCNC, KYDA, MAOB, NYFL, PATF, NCCM, CTOP, DCTC, TNDS, PADV, SCOP, VATB, MDPC, OHLP, NJTO, OHLP, NJOB, NYPT, CALL, MIOR
WATO	994	NJTO, OHLB, INOP, NYRT, GALL, MIOP
WALC WIDN	234 200	WALC, ORUO WIUW, ILIP, WIDN, INOP, MIOP
WIUW		WIUW, ILIP, WIDW, INOP, MIOP MNOP, WIUW, ILIP, IAOP, WIDN, MIOP
VV 1 U VV	248	MINOT, WIOW, ILLIT, IAOT, WILDIN, WILOT

Table 9 Geographical allocation policy for DSAs when the maximum permitted distance to a neighboring DSA is 600 NM.

DSA	Radius (in NM)	Neighbors
ALOB	684	OHOV, TXSA, NCNC, KYDA, ALOB, PATF, NCCM, DCTC, TNDS, PADV, FLMP, ILIP, MSOP, AROR, IAOP, SCOP, TXSB, TNMS, VATB, MDPC, MOMA, MWOB, OHLP, WIDN, FLFH, OHLB, TXGC, FLUF, INOP, FLWC, GALL,
AROR	297	MIOP, LAOP, OKOP MSOP, AROR, TXSB, TNMS, MOMA, MWOB, LAOP, OKOP
AZOB	546	AZOB, CORS, UTOP, CADN, CASD, CAOP
CADN	655	WALC, HIOP, AZOB, ORUO, UTOP, CADN, CASD, CAOP
CAGS	318	HIOP, CADN, CAOP
CAOP	316	HIOP, AZOB, CADN, CASD, CAOP
CASD	537	HIOP, AZOB, UTOP, CADN, CASD, CAOP
CORS	316	CORS, UTOP
CTOP	343	MAOB, NYFL, PATF, CTOP, DCTC, PADV, MDPC, NJTO, NYRT
DCTC	421	OHOV, NCNC, KYDA, MAOB, NYFL, PATF, NCCM, CTOP, DCTC, PADV, SCOP, VATB, MDPC, OHLP, NJTO, OHLB, INOP, NYRT, MIOP
FLFH FLMP	687 287	OHOV, NCNC, KYDA, ALOB, PRLL, NCCM, DCTC, TNDS, FLMP, MSOP, SCOP, TNMS, VATB, MDPC, OHLP, FLFH, FLUF, FLWC, GALL, LAOP PRLL, FLMP, FLFH, FLUF, FLWC
FLUF	674	OHOV, NCNC, KYDA, ALOB, PATF, PRLL, NCCM, DCTC, TNDS, FLMP, MSOP, AROR, SCOP, TNMS, VATB, MDPC, MOMA, OHLP, FLFH, OHLB, FLUF, INOP, FLWC, GALL, LAOP
FLWC	488	NCNC, ALOB, PRLL, NCCM, FLMP, MSOP, SCOP, FLFH, FLUF, FLWC, GALL
GALL	671	OHOV, NCNC, KYDA, ALOB, NYFL, PATF, NCCM, DCTC, TNDS, PADV, FLMP, ILIP, MSOP, AROR, SCOP, TNMS, VATB, MDPC, MOMA, MWOB, OHLP, NJTO, WIDN, FLFH, OHLB, TXGC, FLUF, INOP, FLWC, NYRT, GALL, MIOP, LAOP, OKOP
HIOP	NA	HIOP, CASD
IAOP	235	MNOP, WIUW, ILIP, IAOP, MWOB, WIDN, NEOR
ILIP	447	OHOV, MNOP, KYDA, PATF, TNDS, WIUW, ILIP, AROR, IAOP, TNMS, MOMA, MWOB, OHLP, WIDN, NEOR, OHLB, INOP, MIOP
INOP	510	OHOV, MNOP, NCNC, KYDA, ALOB, NYFL, PATF, NCCM, DCTC, TNDS, PADV, WIUW, ILIP, MSOP, AROR, IAOP, SCOP, TNMS, VATB, MDPC, MOMA, MWOB, OHLP, WIDN, NEOR, OHLB, INOP, GALL, MIOP
KYDA	696	OHOV, MNOP, NCNC, KYDA, ALOB, MAOB, NYFL, PATF, NCCM, CTOP, DCTC, TNDS, PADV, WIUW, ILIP, MSOP, AROR, IAOP, SCOP, TNMS, VATB, MDPC, MOMA, MWOB, OHLP, NJTO, WIDN, NEOR, FLFH, OHLB, TXGC, FLUF, INOP, FLWC, NYRT, GALL, MIOP, LAOP, OKOP
LAOP	396	TXSA, ALOB, MSOP, AROR, TXSB, TNMS, TXGC, LAOP, OKOP
MAOB	170	MAOB, CTOP, NJTO, NYRT
MDPC	645	OHOV, NCNC, KYDA, ALOB, MAOB, NYFL, PATF, NCCM, CTOP, DCTC, TNDS, PADV, WIUW, ILIP, SCOP, VATB,
		MDPC, OHLP, NJTO, WIDN, OHLB, FLUF, INOP, NYRT, GALL, MIOP
MIOP	216	OHOV, ILIP, OHLP, WIDN, OHLB, INOP, MIOP
MNOP	270	MNOP, WIUW, IAOP, NEOR
MOMA	694	OHOV, TXSA, MNOP, NCNC, KYDA, ALOB, PATF, NCCM, DCTC, TNDS, WIUW, ILIP, MSOP, AROR, IAOP, SCOP, TXSB, TNMS, VATB, MDPC, MOMA, MWOB, OHLP, WIDN, CORS, NEOR, OHLB, TXGC, FLUF, INOP, GALL, MIOP, LAOP, OKOP
MSOP MWOB	418 590	KYDA, ALOB, TNDS, MSOP, AROR, TXSB, TNMS, MOMA, TXGC, FLUF, GALL, LAOP, OKOP OHOV, TXSA, MNOP, KYDA, ALOB, TNDS, WIUW, ILIP, MSOP, AROR, IAOP, TXSB, TNMS, MOMA, MWOB, WIDN, CORS, NEOR, TXGC, INOP, MIOP, LAOP, OKOP
NCCM	238	NCNC, KYDA, NCCM, TNDS, SCOP, VATB, GALL
NCNC	320	NCNC, KYDA, PATF, NCCM, DCTC, TNDS, PADV, SCOP, VATB, MDPC, OHLP, GALL
NEOR	377	MNOP, IAOP, MOMA, MWOB, CORS, NEOR, OKOP
NJTO	254	MAOB, NYFL, PATF, CTOP, DCTC, PADV, MDPC, NJTO, NYRT
NMOP	282	AZOB
NVLV	311	AZOB, UTOP, CADN, CASD, CAOP
NYAP	182	MAOB, NYFL, CTOP, PADV, NJTO, NYRT
NYFL	186	NYFL, PADV
NYRT	195	MAOB, NYFL, CTOP, DCTC, PADV, MDPC, NJTO, NYRT
NYWN OHLB	153 484	NYFL, OHLB OHOV, NCNC, KYDA, MAOB, NYFL, PATF, NCCM, CTOP, DCTC, TNDS, PADV, WIUW, ILIP, SCOP, VATB, MDPC, MOMA, OHLP, NJTO, WIDN, OHLB, INOP, NYRT, GALL, MIOP
OHLC	678	OHOV, MNOP, NCNC, KYDA, ALOB, MAOB, NYFL, PATF, NCCM, CTOP, DCTC, TNDS, PADV, WIUW, ILIP, MSOP, AROR, IAOP, SCOP, TNMS, VATB, MDPC, MOMA, MWOB, OHLP, NJTO, WIDN, NEOR, OHLB, FLUF,
OHLP	624	INOP, NYRT, GALL, MIOP, OKOP OHOV, MNOP, NCNC, KYDA, ALOB, MAOB, NYFL, PATF, NCCM, CTOP, DCTC, TNDS, PADV, WIUW, ILIP, MSOP, AROR, IAOP, SCOP, TNMS, VATB, MDPC, MOMA, MWOB, OHLP, NJTO, WIDN, OHLB, FLUF, INOP,
OHOV	410	NYRT, GALL, MIOP OHOV, NCNC, KYDA, ALOB, PATF, NCCM, DCTC, TNDS, PADV, WIUW, ILIP, SCOP, TNMS, VATB, MDPC,
		MOMA, OHLP, WIDN, OHLB, INOP, GALL, MIOP
OKOP	418	TXSA, MSOP, AROR, TXSB, TNMS, MOMA, MWOB, NEOR, TXGC, LAOP, OKOP
ORUO	662	WALC, HIOP, ORUO, UTOP, CADN, CAOP
PADV PATF	235 544	MAOB, NYFL, PATF, CTOP, DCTC, PADV, VATB, MDPC, NJTO, NYRT OHOV, NCNC, KYDA, ALOB, MAOB, NYFL, PATF, NCCM, CTOP, DCTC, TNDS, PADV, WIUW, ILIP, SCOP, VATB, MDPC, MOMA, OHLP, NJTO, WIDN, OHLB, INOP, NYRT, GALL, MIOP
PRLL	NA	PRLL, FLMP, FLFH, FLWC
SCOP	263	NCNC, NCCM, TNDS, SCOP, VATB, FLUF, GALL
TNDS	694	OHOV, NCNC, KYDA, ALOB, NYFL, PATF, NCCM, CTOP, DCTC, TNDS, PADV, WIUW, FLMP, ILIP, MSOP, AROR,
TNMS	561	IAOP, SCOP, TXSB, TNMS, VATB, MDPC, MOMA, MWOB, OHLP, NJTO, WIDN, NEOR, FLFH, OHLB, TXGC, FLUF, INOP, FLWC, NYRT, GALL, MIOP, LAOP, OKOP OHOV, TXSA, NCNC, KYDA, ALOB, NCCM, TNDS, WIUW, ILIP, MSOP, AROR, IAOP, SCOP, TXSB, TNMS, MOMA,
		MWOB, OHLP, WIDN, NEOR, OHLB, TXGC, FLUF, INOP, GALL, MIOP, LAOP, OKOP
TXGC	276	TXSA, TXSB, TXGC, LAOP, OKOP
TXSA	179	TXSA, TXSB, TXGC
TXSB	598	TXSA, ALOB, MSOP, AROR, TXSB, TNMS, MOMA, MWOB, CORS, NEOR, TXGC, LAOP, OKOP
UTOP VATB	537 517	AZOB, ORUO, CORS, UTOP, CADN, CASD, CAOP OHOV, NCNC, KYDA, ALOB, MAOB, NYFL, PATF, NCCM, CTOP, DCTC, TNDS, PADV, SCOP, VATB, MDPC, OHLP, NJTO, OHLB, FLUF, INOP, NYRT, GALL, MIOP
WALC	234	WALC, ORUO
WIDN	423	OHOV, MNOP, KYDA, PATF, WIUW, ILIP, IAOP, MOMA, MWOB, OHLP, WIDN, OHLB, INOP, MIOP
WIUW	248	MNOP, WIUW, ILIP, IAOP, WIDN, MIOP

Table 10 Geographical allocation policy for DSAs when the maximum permitted distance to a neighboring DSA is 700 NM.