

Tutorial-7

q2:

- ↑ travel → ↑ probability of fraud.
- ↑ foreign purchase → ↑ fraud.
- ↑ Travel + Fraud → ↑ Foreign purchase.

q1. Classifying hidden variables.

$$P(\text{fraud} = \text{true} \mid \text{f.p} = \text{true})$$

$$= \alpha * [P(f = \text{true} \mid \text{travel} = \text{true}) * P(\text{f.p} = \text{true} \mid \text{travel} = \text{true}, \text{fraud} = \text{true}) \\ * P(t = \text{true}) +$$

$$P(f = \text{true} \mid t = \text{false}) * P(\text{f.p} = \text{true} \mid t = \text{false}, f = \text{true}) \\ * P(t = \text{false})]$$

$$= \alpha * [0.00045 + 0.00019]$$

$$= 0.00064\alpha$$

$$P(\text{fraud} = \text{False} \mid \text{f.p} = \text{true})$$

$$= \alpha * [P(f = \text{false} \mid t = \text{true}) * P(\text{f.p} = \text{true} \mid t = \text{true}, f = \text{false}) \\ * P(t = \text{true})] +$$

$$P(f = \text{false} \mid t = \text{false}) * P(\text{f.p} = \text{true} \mid t = \text{f}, f = \text{false}) \\ * P(t = \text{false})]$$

$$= 0.054031\alpha$$

$$\alpha = \frac{1}{\alpha_1 + \alpha_2} = 18.291$$

$$P(\text{fraud} = \text{true} \mid f.p = \text{true}) = 0.00064\alpha$$

$$= \underline{\underline{1.17\%}}$$

Q2. $P(\text{fraud} = \text{true} \mid f.p = \text{true}, \text{travel} = \text{true})$

$$= \alpha \cdot 0.00045$$

$$P(f = \text{false} \mid f.p = \text{true}, t = \text{true})$$

$$\alpha = \alpha * 0.000455$$

$$\alpha = \frac{1}{\alpha_1 + \alpha_2} = 22.222$$

$$P(f = \text{true} \mid f.p = \text{true}, \text{travel} = \text{true})$$

$$= 0.01$$

$$= 1\%$$