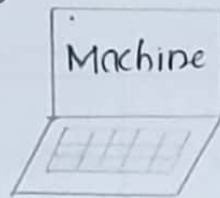


Introduction to Machine Learning :-

①

Height	Weight	Gender
180	90	Male
150	45	Female
175	85	Male
160	50	Female
155	50	Female



lookup/search → to do Task

Test

H/cm	W/kg	G
180	90	Male
150	50	Female
156	50	Female

By Range [Expert-System]

Let us consider we have a data set of height and weight in cm, kgs respectively for those dimensionality we easily predict the Gender of that data point in test phase because we have data information of Gender with r.to given height & column. So from this in-future also we easily predict Gender by naturally we do this process but in machine learning. process how we feed & intellectual to our machine about this task or predictions.

So in this situation we need the terminologies of AI & Data Science.

What is Artificial Intelligence :- We human beings are naturally intelligent but a machinery (like Computer, Car, Robot, etc) are dumb at initilly, we feed them by some input commands (like 'task's difference and do operations) and get outputs. ie generally machine mimics the intelligence of humans is called as Artificial Intelligence.

Now a days some machineries doing a job of human doing let us.

Consider Tesla cars this are self drive cars this follow road

Signals & System Commands according to that this car drive selfily.

even in our mobiles lot of operations done with ~~our~~ ~~ours~~ regarding AI such as Spam mail detection in gmail, in games like pubg or ludo there is machine play with human being, text speech notation commands from google search bar, recommended system in Amazon shopping, Youtube like several tasks completed as we human doing. So now a days in every where 'AI' involved. and do some tasks. (or) operations like human. So here entire this process we generally put commands to machine for doing some tasks.

So in above example we detect the gender of a person by giving their inputs (H/W) So generally height & weight of a person are positively correlated with each other (ie when height increases then weight also increases their existing some positive Correlationship b/w them.)

So first of all we train our data set to predict in future any given point is given to predict Gender. In this process we load the data set in Excel, CSV or any format and train our machine with some commands. So initially machine (ie computer) is dumb we have to train that by input data & commands. after train the data in table 2 from that we test data let in first step we give input H/W to machine predict Gender as Male & Female.

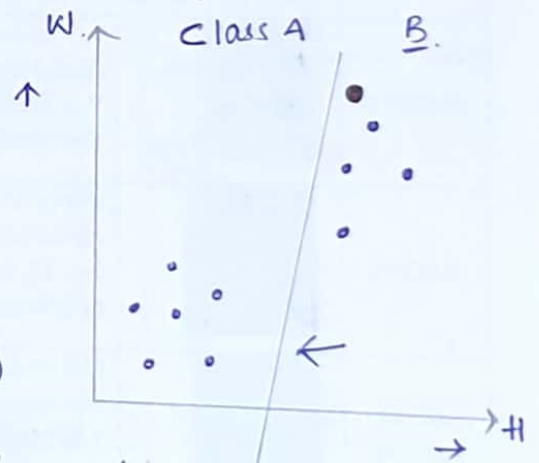
if we observe '3' case in this values are input's different which we didn't defined (ie 156, 50) new featured point comes then how to solve this task? for this we use expert system (if-else) condition. after we use this we get Gender of data point (ie. male/female).

By the above process we completed numerical tasks, tasks like in-format of (discrete / continuous) for suppose if we have categorical type of data. then how we do predictions (or) operations in such condition.

In this we can't use expert system or any other we used in numerical operation. So here we solved this problems by train a data for suppose if we have a image of apple we train our machine to it is a apple, if we have an image of any animal we train our machine to this is ~~any~~ animal. So how we do this entire process by using "Supervised data". In this process we train a machine in a such away to predict categorical outputs also. for given input, if we plot a scatterplot graph on the data.

We get like -

On X-axis we take height & y-axis take 'W' weight according to train the data plot respected points and make point representation in data. now this graph



plotted points observe in this simply we can plot line making that line differentiate this points in two classes (A, B) as female, male respectively. now if we have any new point we simply say as this line representation.

as reference - to division the two classes - from this line we can (4)
predict the new data point class. So this is a categorical type of data.
result, how we come up this result by line making, how-to we reach
this line making by "machine learning" Technique Under this we used "Supervised
machine learning technique" Under that classification type of problem.

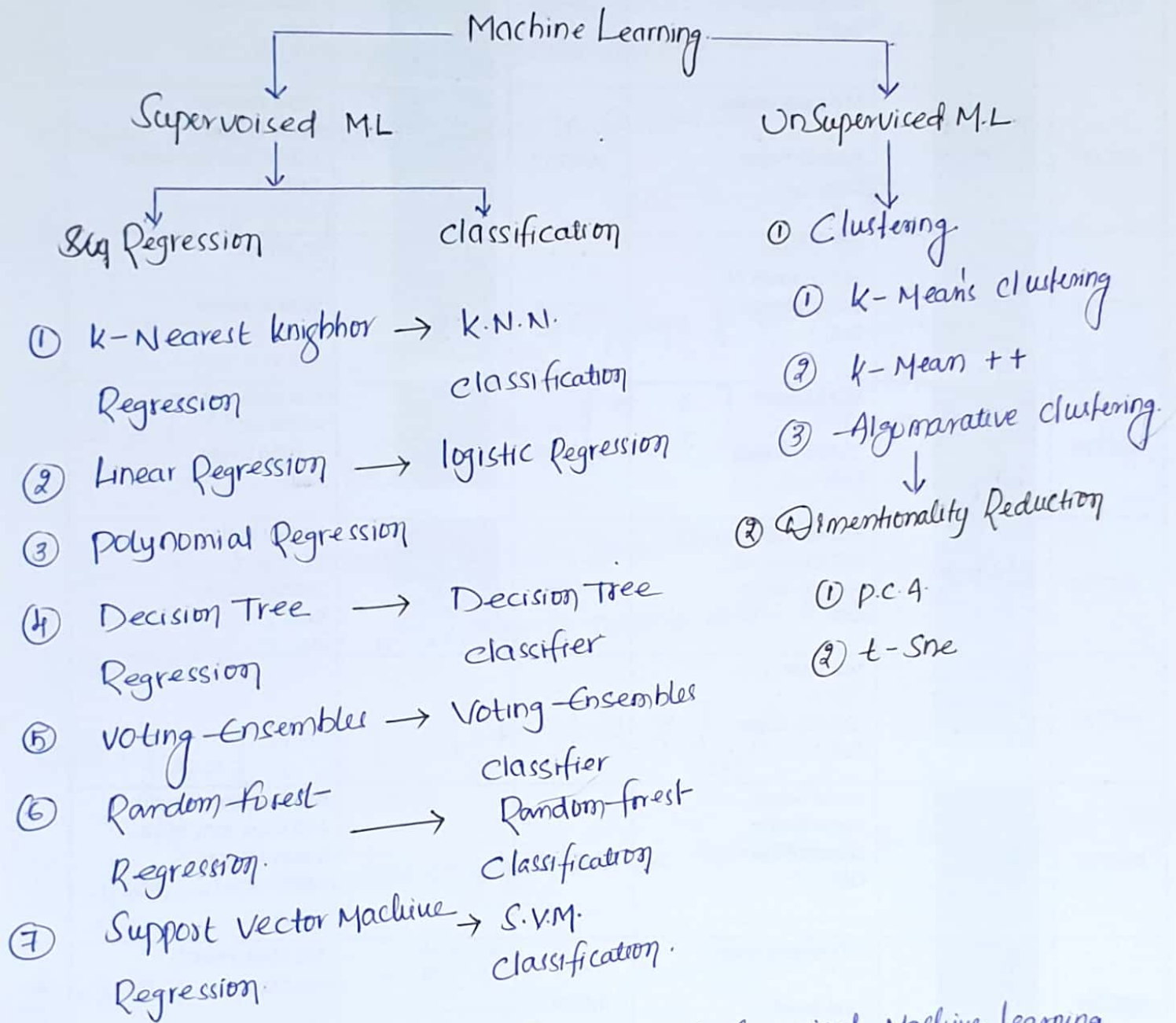
Machine learning :- it is a method of data analysis that automates
analytical model building. it is a branch of "Artificial Intelligence" based on the
idea that system can learn from data, identify patterns and make decisions
with minimal human intervention.

classification of Machine learning :- classification of ML is based on
variable, the given random variable (output/target) is which type of
variable if it is a discrete type of variable then we go to ^{classification} ~~Regression~~
Task in this we use Regression related algorithms, if it is a classification
type of variable that means the random variable is Continuous type then
do ^{Regression} ~~classification~~ related algorithms. this whole terminology comes under

"Supervised Machine learning" Technique.

Supervised Machine learning :- it is a subcategory of ML & AI, it is
defined by its use of labeled data sets to train algorithms that to classify
data or predict outcomes accurately. So here in this process we supervise
our data to give a good ~~model~~ or best model. (we have output variable)

UnSupervised Machine Learning :- In which users do not need to supervise the model, instead it allows the model to work on its own to discover patterns and information that was previously undetected, it mainly deals with the unlabeled data (we don't have output)



Here we just focused on Supervised, UnSupervised machine learning.

Techniques Under Supervised we learn diff algorithms as shown above graph.

Mainly Machine learning classified as - ① Supervised learning.
② UnSupervised learning, ③ Reinforcement learning. Hybrid learning process

- (4) Semi Supervised Learning, (5) Self Supervised Learning. (6) Multi-Instance learning. Statistical Inference. (7) Inductive learning, (8) Deductive learning.

Matrix :- It is a Set of numbers arranged in row and column format So as to form a rectangular array. The numbers are called the elements, or entries, of the matrix, represent in Capital alphabet

Ex: $A = \begin{bmatrix} & & \\ & & \\ & & \end{bmatrix}_{m \times n} \Rightarrow$ Here m - no of rows
 n - no of columns.

Size / Shape of Matrix - $m \times n$

Case - I

$$A = \begin{bmatrix} 1 & 2 \\ 3 & 4 \end{bmatrix}_{2 \times 2} + B = \begin{bmatrix} 5 & 6 \\ 7 & 8 \end{bmatrix}_{2 \times 2} = \begin{bmatrix} 1+5 & 2+6 \\ 3+7 & 4+8 \end{bmatrix} = \begin{bmatrix} 6 & 8 \\ 10 & 12 \end{bmatrix}$$

Here the both matrix are having same shape of (2×2) matrix So easily we can add the matrix ie addition is possible in this matrix

$$\text{Case - II } A = \begin{bmatrix} 1 & 0 \\ 0 & 1 \end{bmatrix}_{2 \times 2} + B = \begin{bmatrix} 2 & 2 \end{bmatrix}_{1 \times 2} \neq \begin{bmatrix} \end{bmatrix}$$

Here - Addition is not possible because the shape of the matrix is not similar.

Case - III

$$A + B = B + A$$

We can write or perform ' $A+B = B+A$ ' when shape of matrix should be similar

Multiplication of matrix can be possible, when matrix $A_{m \times n} * B_{n \times p}$ in-form where no of columns in matrix 'A' should be equal to no of rows in matrix 'B' Then only it is possible. then the form of 'B' is anything.

$$A_{m \times n} * B_{n \times p} \Rightarrow \begin{bmatrix} 1 & 2 \\ 3 & 4 \end{bmatrix}_{2 \times 2} * \begin{bmatrix} 1 \\ 1 \end{bmatrix}_{2 \times 1}$$

(7)

Where $\rightarrow A_m \rightarrow$ represent no of rows - $B_m \rightarrow$ no of rows
 $A_n \rightarrow$ number of columns $B_p \rightarrow$ no of columns

In Process of Multiplication Compulsary the Columns of given matrix should be similar with row of given other matrix then the result would be in the form of $m \times p$ at the above example the resultant matrix should be 2×1

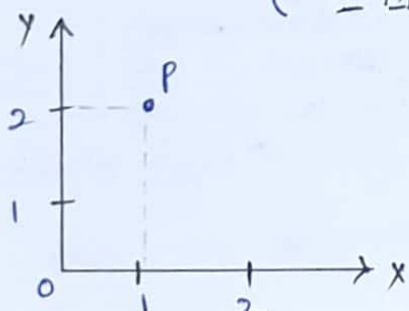
$$A = \begin{bmatrix} 1 & 2 \\ 3 & 4 \end{bmatrix}_{2 \times 2}, B = \begin{bmatrix} 1 \\ 1 \end{bmatrix}_{2 \times 1} \Rightarrow A * B = \begin{bmatrix} 1 \times 1 + 2 \times 1 \\ 3 \times 1 + 4 \times 1 \end{bmatrix} \Rightarrow \begin{bmatrix} 3 \\ 7 \end{bmatrix}_{2 \times 1}$$

Transposition of Matrix A^T :- Transposition of matrix is nothing but interchange the shape of matrix means if we have a matrix of shape $m \times n$, then interchange the rows into columns and columns into rows this process known as transposition of matrix (A^T) after transposition the matrix should be $n \times m$,

Ex: $A = \begin{bmatrix} 1 & 2 \\ 3 & 4 \end{bmatrix}_{\substack{m \times n \\ 2 \times 2}} \Rightarrow A^T = \begin{bmatrix} 1 & 3 \\ 2 & 4 \end{bmatrix}_{\substack{n \times m \\ 2 \times 2}}$

from this - $(A+B)^T = A^T + B^T = B^T + A^T$ (addition of Transpost)

$(A_{m \times n} * B_{n \times p})^T = B^T * A^T$ (Multiplication of Transpost)

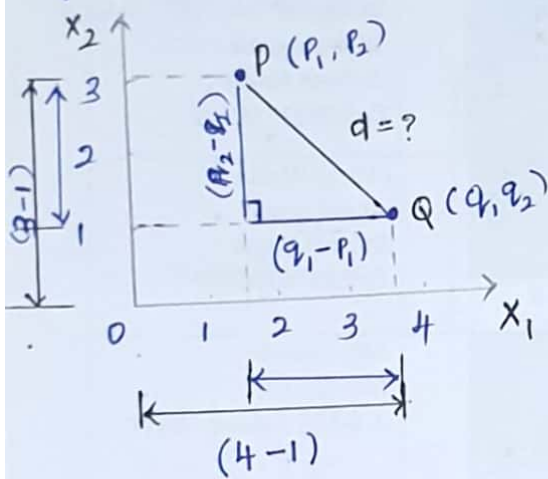


\Rightarrow P denotes the point In mathematical notation we represent this point (P) in Vector notations.

$$\vec{P} = \begin{bmatrix} 1 \\ 2 \end{bmatrix}$$

Vectors :- By the above graph we represent point in Vector notation
 Basically Vector is a row and Column Combination defaultly ie matrix represent
 -ation when ever we denoting point that should be in Column representation
 only not in row representation.

Euclidean Distance :- Distance between two points in Euclidian Space
 is the length of the line segment between the two points, it can be calculated
 from the Cartesian Coordinates of the points using the Pythagorean theorem.



$$\Rightarrow P = \begin{bmatrix} 1 \\ 3 \end{bmatrix} \begin{matrix} p_1 \\ p_2 \end{matrix} \quad Q = \begin{bmatrix} 4 \\ 1 \end{bmatrix} \begin{matrix} q_1 \\ q_2 \end{matrix}$$

-According to Pythagoras theorem

$$d^2 = (q_1 - p_1)^2 + (p_2 - q_2)^2$$

$$d = \sqrt{(p_1 - q_1)^2 + (p_2 - q_2)^2}$$

$$\sqrt{(1-4)^2 + (3-1)^2} = \sqrt{(-3)^2 + (2)^2}$$

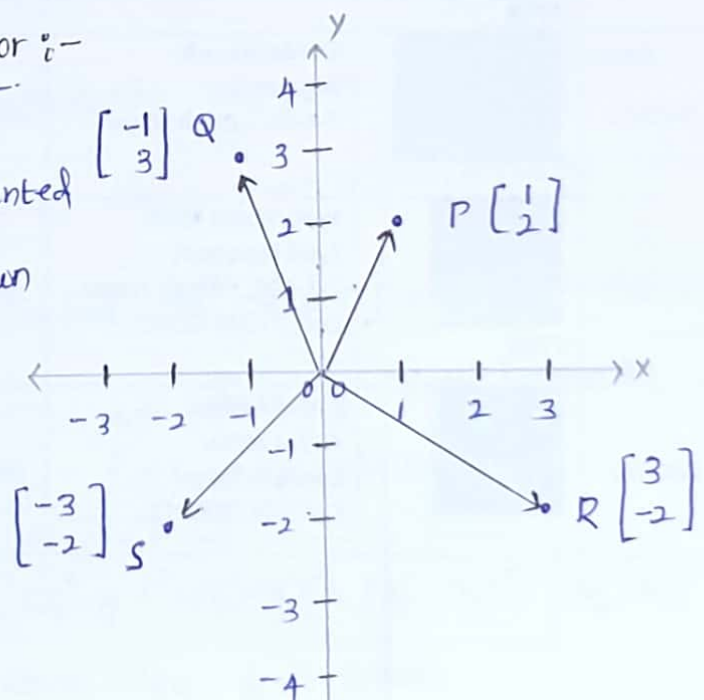
Euclidean Distance $\rightarrow d = \sqrt{13}$

Data point Representation using Vector :-

D_1	D_2
1	2
-1	3
3	-2
-3	-2

Data points are represented
 in vector notation as shown
 -this representation
 based on column vector.

Simply Data set it is having
 only two dimensionality. (2D)



This Data set can be represented in matrix-format also called as 'Data Matrix'. The given data set having only two columns less dimensionality.

$$\text{Data Matrix} = \begin{bmatrix} 1 & 2 \\ -1 & 3 \\ 3 & -2 \\ -3 & -2 \end{bmatrix} \begin{matrix} \nearrow \text{Dimensionality (\# columns)} \\ \searrow \text{no of Data points} \end{matrix}$$

But this Data matrix is not in correct format because in point vector representation of point is only in column notation (defaultly). So we have to change row as column wise so we have to do simply Transpose.

$$\begin{bmatrix} [1 \ 2]^T \\ [-1 \ 3]^T \\ [3 \ -2]^T \\ [-3 \ -2]^T \end{bmatrix} \Rightarrow \text{Point representation of Data Matrix}$$

$$P = \begin{bmatrix} x_1 \\ x_2 \end{bmatrix}_{2 \times 1} \quad Q = \begin{bmatrix} x_1 \\ x_2 \\ x_3 \end{bmatrix}_{3 \times 1} \quad R = \begin{bmatrix} x_1 \\ x_2 \\ x_3 \\ x_4 \end{bmatrix}_{4 \times 1} \Rightarrow x_i \Rightarrow \text{no of D.}$$

Point representation in 2D, 3D, 4D, ... x_n D (Dimensionality)

By visually we can see 2-dimensionality only, and some imaginary part vision also we can see (ie 3-D) above three dimensionality we can't see point representation. but we perform and place a point by mathematically but not we visualize it.

i = index of column / dimension
 j = no of data points.

x_1	x_2	x_3	x_4
x_1^0	x_2^0	x_3^0	x_4^0
x_1^1	x_2^1	x_3^1	x_4^1

$$\Rightarrow X_{ij}^0$$

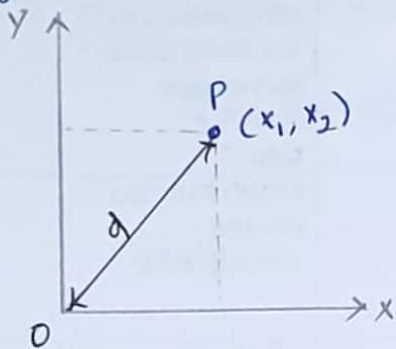
$$d = \sqrt{(x_1^0 - x_1^1)^2 + (x_2^0 - x_2^1)^2 + (x_3^0 - x_3^1)^2 + (x_4^0 - x_4^1)^2}$$

Distance b/w 4-D points.

(10)

Length of a vector :- A point which having Magnitude & Direction is called Vector, represent in (\vec{V}) . from this magnitude tells us the length of a vector; In Simply Distance between Origin to the point is called as "length of a vector". In other terms "Euclidean Distance" also called as Length of a vector represent as " $\|\vec{P}\|$ "

$$\vec{P} = \begin{bmatrix} x_1 \\ x_2 \end{bmatrix} \Rightarrow \|\vec{P}\| = \sqrt{x_1^2 + x_2^2} \quad \text{2 Dimension}$$

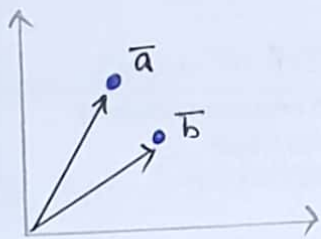


$$\vec{Q} = \begin{bmatrix} x_1 \\ x_2 \\ x_3 \\ x_4 \end{bmatrix} \Rightarrow \|\vec{Q}\| = \sqrt{x_1^2 + x_2^2 + x_3^2 + x_4^2}$$

↳ length of a vector.

[Origin] $\Rightarrow d$ represent Euclidean Distance as well length of a vector

Addition of a vector :-



$$\vec{a} + \vec{b} \Rightarrow \begin{bmatrix} a_1 \\ a_2 \end{bmatrix} + \begin{bmatrix} b_1 \\ b_2 \end{bmatrix} \Rightarrow \begin{bmatrix} a_1 + b_1 \\ a_2 + b_2 \end{bmatrix}_{2 \times 1}$$

Multiplication of a vector :- Basically we multiply the vectors by two methods they are 1) Cross product 2) Dot product

Dot product :-

$$\vec{a} = \begin{bmatrix} a_1 \\ a_2 \end{bmatrix} \quad \vec{b} = \begin{bmatrix} b_1 \\ b_2 \end{bmatrix} \Rightarrow \vec{a} \cdot \vec{b} = a_1 \times b_1 + a_2 \times b_2$$

NOTE :- The resultant should be a Scalar value.. (point)

Ex: $\vec{a} = \begin{bmatrix} 1 \\ 3 \end{bmatrix}$, $\vec{b} = \begin{bmatrix} 5 \\ 6 \end{bmatrix} \Rightarrow \vec{a} \cdot \vec{b} = 1 \times 5 + 3 \times 6 \Rightarrow 23 \rightarrow \text{Scalar}$

Simply we can say Dot product $\Rightarrow \vec{a} \cdot \vec{b} = \sum_{i=1}^n a_i b_i$ n-Dimension

for Suppose if we have (4-D) point vectors and we have to multi- ②

-ply them as Dot product method.

$$\vec{a} = \begin{bmatrix} a_1 \\ a_2 \\ a_3 \\ a_4 \end{bmatrix} \quad \vec{b} = \begin{bmatrix} b_1 \\ b_2 \\ b_3 \\ b_4 \end{bmatrix}$$

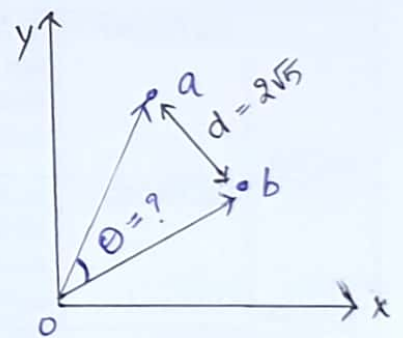
$$\vec{a} \cdot \vec{b} = a_1 b_1 + a_2 b_2 + a_3 b_3 + a_4 b_4 \Rightarrow \vec{a}^T * \vec{b} \text{ also written}$$

$$\text{from the above eqn } \begin{bmatrix} a_1 & a_2 & a_3 \end{bmatrix}_{m \times n} \times \begin{bmatrix} b_1 \\ b_2 \\ b_3 \end{bmatrix}_{n \times p} \text{ can be written,}$$

$$\therefore \text{ Simply } - \boxed{\vec{a} \cdot \vec{b} = \vec{a}^T * \vec{b} = \sum_{i=1}^n a_i b_i}$$

if we have data set and from that data. if we plot a scatterplot and the point representation in form of vector then we find the length of vector from Origin. in that process we calculate distance from Origin to every point in that situation if angle making in between two points let consider. then we know the how much angle making w.r.t to two vectors then we simply do dot product ie multiplication as shown in below

$$\boxed{\vec{a} \cdot \vec{b} = \vec{a}^T \cdot \vec{b} \Rightarrow \sum_{i=1}^n a_i b_i = \|\vec{a}\| \cdot \|\vec{b}\| \cdot \cos \theta_{\vec{a}, \vec{b}}}$$



Data	
C1	C2
1	2
5	-1
6	3
5	0

$$\Rightarrow \vec{a} = \begin{bmatrix} 1 \\ 2 \end{bmatrix}, \vec{b} = \begin{bmatrix} 5 \\ 0 \end{bmatrix} \Rightarrow \vec{a} \cdot \vec{b} = 1*5 + 2*0 = 5$$

$$\text{E. Distance} = \sqrt{(1-5)^2 + (2-0)^2} = \sqrt{4^2 + 2^2} = \sqrt{20} = 2\sqrt{5},$$

$$\Rightarrow \vec{a} \cdot \vec{b} = \|\vec{a}\| \cdot \|\vec{b}\| \cdot \cos \theta$$

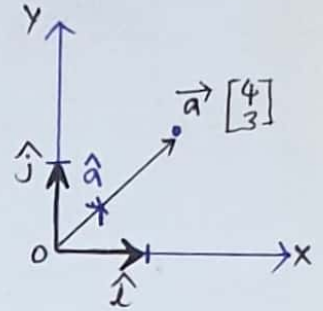
$$1*5 + 2*0 = \sqrt{1^2 + 2^2} * \sqrt{5^2 + 0^2} \cdot \cos \theta$$

$$5 = \sqrt{5} \cdot 5 \cdot \cos \theta \Rightarrow \theta = \cos^{-1}\left(\frac{1}{\sqrt{5}}\right),$$

Unit Vector :- A vector has both magnitude & direction, A vector (12)

That has magnitude of exactly '1' is called as "Unit vector" it is also called as direction vector represented as - $\hat{a} \Rightarrow \wedge$

$$(\text{Unit.v}) \hat{a} = \frac{\vec{a}}{\|\vec{a}\|} \quad \begin{matrix} \text{(Vector)} \\ \text{(length of vector)} \end{matrix}$$



Ex:

$$\vec{a} = \begin{bmatrix} 4 \\ 3 \end{bmatrix} \Rightarrow \|\vec{a}\| = \sqrt{4^2 + 3^2} = \sqrt{25} = 5$$

$$\hat{a} (\text{unit vector}) = \frac{\vec{a}}{5} \Rightarrow \frac{1}{5} \begin{bmatrix} 4 \\ 3 \end{bmatrix}$$

$$\hat{a} = \begin{bmatrix} 4/5 \\ 3/5 \end{bmatrix}$$

* Unit vector has a property that the magnitude should be 1.

Let's prove it, Magnitude is nothing but length of a unit vector

$$\|\hat{a}\| = \sqrt{\left(\frac{4}{5}\right)^2 + \left(\frac{3}{5}\right)^2} = \sqrt{\frac{16}{25} + \frac{9}{25}} = \sqrt{\frac{25}{25}} = \sqrt{1}$$

$$\|\hat{a}\| = 1, \text{ (Magnitude)}$$

distances calculated in different forms also there are several methods to calculate distances. Such as -

① Euclidean Distance \rightarrow According to Pythagoras

② Manhattan Distance \rightarrow it is a name of city in New York where the representation done in block wise.

③ Minkowski Distance

④ Cosine Distance & etc. \Rightarrow when " θ " angle known

When we use Manhattan we represent points in blocked distances.

