## ENV 790.30 - Time Series Analysis for Energy Data | Spring 2024 Assignment 3 - Due date 05/01/24

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### **Directions**

You should open the .rmd file corresponding to this assignment on RStudio. The file is available on our class repository on Github.

Once you have the file open on your local machine the first thing you will do is rename the file such that it includes your first and last name (e.g., "LuanaLima\_TSA\_A02\_Sp24.Rmd"). Then change "Student Name" on line 4 with your name.

Then you will start working through the assignment by **creating code and output** that answer each question. Be sure to use this assignment document. Your report should contain the answer to each question and any plots/tables you obtained (when applicable).

Please keep this R code chunk options for the report. It is easier for us to grade when we can see code and output together. And the tidy opts will make sure that line breaks on your code chunks are automatically added for better visualization.

When you have completed the assignment, **Knit** the text and code into a single PDF file. Submit this pdf using Sakai.

### Questions

Consider the same data you used for A2 from the spreadsheet "Table\_10.1\_Renewable\_Energy\_Production\_and\_Consumpt The data comes from the US Energy Information and Administration and corresponds to the December 2022 Monthly Energy Review. Once again you will work only with the following columns: Total Biomass Energy Production, Total Renewable Energy Production, Hydroelectric Power Consumption. Create a data frame structure with these three time series only.

R packages needed for this assignment: "forecast", "tseries", and "Kendall". Install these packages, if you haven't done yet. Do not forget to load them before running your script, since they are NOT default packages.\

```
#Load/install required package here
library(forecast)

## Registered S3 method overwritten by 'quantmod':
## method from
## as.zoo.data.frame zoo

library(tseries)
library(Kendall)
library(stats)
library(ggplot2)
```

```
library(cowplot)
library(lubridate)
##
## Attaching package: 'lubridate'
## The following object is masked from 'package:cowplot':
##
##
       stamp
## The following objects are masked from 'package:base':
##
##
       date, intersect, setdiff, union
#Importing dataset
Raw_REDataset <- read.csv("Data/Table_10.1_Renewable_Energy_Production_and_Consumption_by_Source.csv",
                  stringsAsFactors = TRUE)
#Subsetting dataset to get the required columns
REDataset <- Raw_REDataset[,c(1, 5:6)]</pre>
head(REDataset)
##
             Month Total.Renewable.Energy.Production
## 1 1973 January
                                              219.839
## 2 1973 February
                                              197.330
## 3
        1973 March
                                              218.686
## 4
        1973 April
                                              209.330
                                              215.982
## 5
          1973 May
         1973 June
                                              208.249
    Hydroelectric.Power.Consumption
##
## 1
                               89.562
## 2
                               79.544
## 3
                               88.284
## 4
                               83.152
## 5
                               85.643
## 6
                               82.060
#Renaming column headings
colnames(REDataset) <- c("Date", "RE", "Hydro")</pre>
head(REDataset)
##
              Date
                        RE Hydro
## 1 1973 January 219.839 89.562
## 2 1973 February 197.330 79.544
        1973 March 218.686 88.284
## 3
        1973 April 209.330 83.152
## 4
## 5
         1973 May 215.982 85.643
         1973 June 208.249 82.060
## 6
```

```
#Converting the Date column to a Date object
REDataset_Date <- REDataset$Date
REDataset$Date <- ym(format(REDataset_Date, format = "%Y %B"))
str(REDataset)

## 'data.frame': 609 obs. of 3 variables:
## $ Date : Date, format: "1973-01-01" "1973-02-01" ...
## $ RE : num 220 197 219 209 216 ...
## $ Hydro: num 89.6 79.5 88.3 83.2 85.6 ...

##NOTE FOR GRADERS: I have not included biomass even though the question mentions
#it based on Luana's message on slack to not include it.</pre>
```

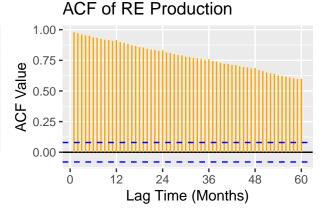
##Trend Component

### $\mathbf{Q}\mathbf{1}$

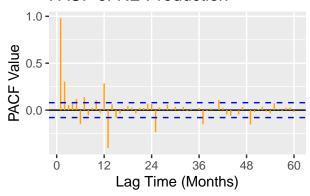
For each time series, i.e., Renewable Energy Production and Hydroelectric Consumption create three plots: one with time series, one with the ACF and with the PACF. You may use the some code form A2, but I want all the three plots side by side as in a grid. (Hint: use function plot\_grid() from the cowplot package)

```
#Converting dataframe into time series
ts_REDataset <- ts(REDataset[,2:3], start=c(1973, 01), frequency = 12)
head(ts_REDataset)
##
                 RE Hydro
## Jan 1973 219.839 89.562
## Feb 1973 197.330 79.544
## Mar 1973 218.686 88.284
## Apr 1973 209.330 83.152
## May 1973 215.982 85.643
## Jun 1973 208.249 82.060
#RE Production Plots
ts_RE_plot <- autoplot(ts_REDataset[,1], col="orange") +</pre>
  xlab("Time") + ylab("RE Production") +
  theme(axis.text.x = element_text(angle = 90, vjust = 0.5, hjust=1))+
  ggtitle("RE Production over time")
ts_RE_ACF <- Acf(ts_REDataset[, 1], lag.max = 60, type = "correlation", plot = FALSE)
ts_RE_ACF <- autoplot(ts_RE_ACF, col = "orange") +</pre>
  xlab ("Lag Time (Months)") + ylab ("ACF Value") +
  ggtitle("ACF of RE Production")
ts_RE_PACF <- Pacf(ts_REDataset[, 1], lag.max = 60, type = "correlation", plot = FALSE)
ts_RE_PACF <- autoplot(ts_RE_PACF, col = "orange") + xlab ("Lag Time (Months)")+
 ylab ("PACF Value") +
  ggtitle("PACF of RE Production")
plot_grid(ts_RE_plot, ts_RE_ACF, ts_RE_PACF )
```

# RE Production over time We have a second of the second of



### PACF of RE Production



```
#Hydroelectric Power Consumption

ts_Hydro_plot <- autoplot(ts_REDataset[,2], col="blue") +
    xlab("Time") + ylab("Hydro Consumption") +
    theme(axis.text.x = element_text(angle = 90, vjust = 0.5, hjust=1))+
    ggtitle("Hydroelectric power consumption over time")

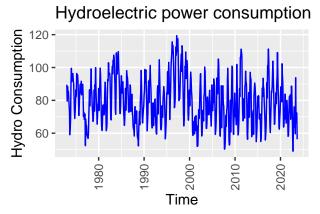
ts_Hydro_ACF <- Acf(ts_REDataset[, 2], lag.max = 60, type = "correlation", plot = FALSE)

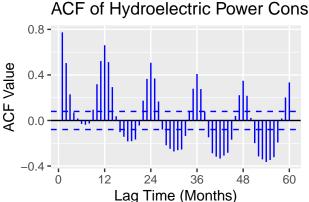
ts_Hydro_ACF <- autoplot(ts_Hydro_ACF, col = "blue") +
    xlab ("Lag Time (Months)") + ylab ("ACF Value") +
    ggtitle("ACF of Hydroelectric Power Consumption")

ts_Hydro_PACF <- Pacf(ts_REDataset[, 2], lag.max = 60, type = "correlation", plot = FALSE)

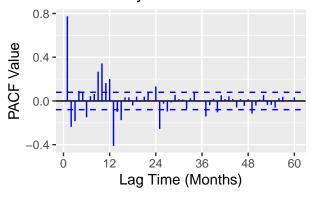
ts_Hydro_PACF <- autoplot(ts_Hydro_PACF, col = "blue") +
    xlab ("Lag Time (Months)") + ylab ("PACF Value") +
    ggtitle("PACF of Hydroelectric Power Consumption")

plot_grid(ts_Hydro_plot, ts_Hydro_ACF, ts_Hydro_PACF)</pre>
```





### PACF of Hydroelectric Power Consumption



### $\mathbf{Q2}$

From the plot in Q1, do the series Total Biomass Energy Production, Total Renewable Energy Production, Hydroelectric Power Consumption appear to have a trend? If yes, what kind of trend?

RE Production has had an overall rising trend from 1973-2020 with steadily declining autocorrelation and almost insignificant PACF beyond the 12th lag mark (with the exception of mildly significant PACF values at the annual 12th, 24th and 36th lag marks). On the other hand, hydroelectric power consumption showcases a seasonal trend with autocorrelation and PACF decreasing over time but maintaining their 6-month positive and negative seasonal trend.

### $\mathbf{Q3}$

Use the lm() function to fit a linear trend to the three time series. Ask R to print the summary of the regression. Interpret the regression output, i.e., slope and intercept. Save the regression coefficients for further analysis.

```
nobs <- nrow(REDataset)
t <- c(1:nobs)

#Fitting the lm() function to the RE column
lm_RE <- lm(ts_REDataset[,1]~t)
print(summary(lm_RE))</pre>
```

```
## Call:
## lm(formula = ts_REDataset[, 1] ~ t)
## Residuals:
      Min
               1Q Median
                               3Q
                                      Max
## -148.27 -35.63
                   11.58 41.51 144.27
## Coefficients:
##
               Estimate Std. Error t value Pr(>|t|)
## (Intercept) 180.98940
                           4.90151
                                     36.92
                                             <2e-16 ***
                0.70404
                           0.01392
                                     50.57
                                             <2e-16 ***
## ---
## Signif. codes: 0 '*** 0.001 '** 0.01 '* 0.05 '.' 0.1 ' 1
##
## Residual standard error: 60.41 on 607 degrees of freedom
## Multiple R-squared: 0.8081, Adjusted R-squared: 0.8078
## F-statistic: 2557 on 1 and 607 DF, p-value: < 2.2e-16
beta0_RE=as.numeric(lm_RE$coefficients[1])
beta0_RE
## [1] 180.9894
beta1_RE=as.numeric(lm_RE$coefficients[2])
beta1_RE
## [1] 0.7040391
#Fitting the lm () function to the hydro column
lm_hydro <- lm(ts_REDataset[,2]~t)</pre>
print(summary(lm_hydro))
##
## Call:
## lm(formula = ts_REDataset[, 2] ~ t)
##
## Residuals:
               1Q Median
##
      Min
                               ЗQ
                                      Max
## -29.818 -10.620 -0.669 9.357 39.528
##
## Coefficients:
##
               Estimate Std. Error t value Pr(>|t|)
## (Intercept) 82.734747
                          1.140265 72.557 < 2e-16 ***
## t
              -0.009849
                          0.003239 -3.041 0.00246 **
## ---
## Signif. codes: 0 '*** 0.001 '** 0.01 '* 0.05 '.' 0.1 ' 1
## Residual standard error: 14.05 on 607 degrees of freedom
## Multiple R-squared: 0.015, Adjusted R-squared: 0.01338
## F-statistic: 9.247 on 1 and 607 DF, p-value: 0.002461
```

```
beta0_Hydro=as.numeric(lm_hydro$coefficients[1])
beta0_Hydro

## [1] 82.73475

beta1_Hydro=as.numeric(lm_hydro$coefficients[2])
beta1_Hydro
```

```
## [1] -0.009849298
```

Interpretation of results: RE regression: Slope (B1) = 0.7 indicating a coherent upward rising trend Intercept (B0) = 180.98 P-value =  $2x10^-16$  indicating strong statistical significance (p-value < 0.05) Rsquared value of 80% signifying that 80% of the variability in the data is determined by time.

Hydro regression: Slope (B1) = -0.0098 indicating no significant upward or downward trend. This is verified by the plot where we can clearly see a seasonal cyclical trend in the data. Intercept (B0) - 82.73 P-value =  $2\times10^{-16}$  indicating strong statistical significance (p-value < 0.05) R squared value = 1.3% indicating that the variability in the data is not really explained by time.

### $\mathbf{Q4}$

##

## 1

## 2

## 3

## 4

## 5

## 6

detrended hydro

6.8371025

-3.1710482

5.5788011

0.4566504

2.9574997

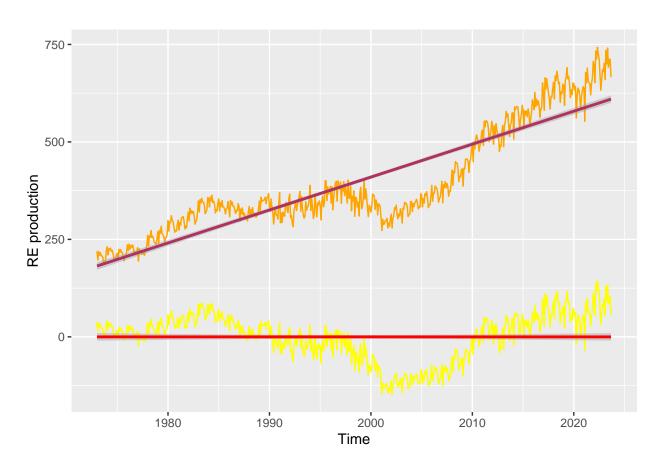
-0.6156510

Use the regression coefficients from Q3 to detrend the series. Plot the detrended series and compare with the plots from Q1. What happened? Did anything change?

```
#Detrending the data
detrend_RE_vector <- REDataset[,2]-(beta0_RE+beta1_RE*t)</pre>
detrend_RE <- data.frame(detrend_RE_vector)</pre>
colnames(detrend_RE)<-"detrended RE"</pre>
head(detrend RE)
##
     detrended RE
## 1
          38.14556
## 2
          14.93252
## 3
          35.58448
## 4
          25.52444
## 5
          31.47240
## 6
          23.03536
detrend_hydro_vector <- REDataset[,3]-(beta0_Hydro + beta1_Hydro*t)</pre>
detrend_hydro <- data.frame(detrend_hydro_vector)</pre>
colnames(detrend_hydro)<- "detrended hydro"</pre>
head(detrend_hydro)
```

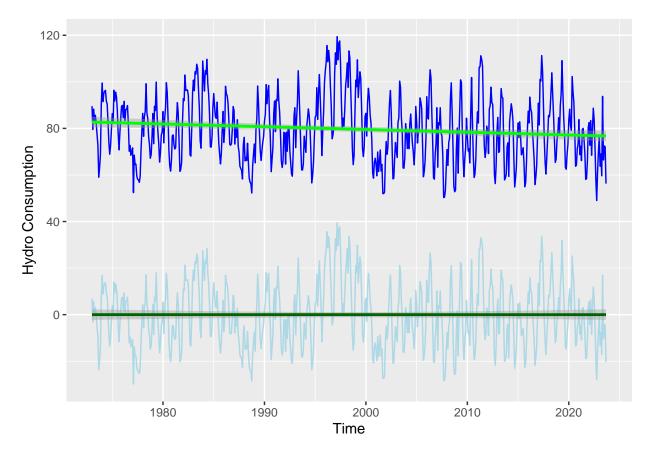
```
#Plotting the original and detrended data for RE with their regression lines
ggplot(REDataset, aes(x=Date, y=RE))+
  geom_line(color="orange")+
  geom_smooth(color="maroon", method="lm")+
  geom_line(aes(y=detrend_RE$^detrended RE^), color = "yellow")+
  geom_smooth(aes(y=detrend_RE$^detrended RE^), color = "red", method="lm")+
  ylab("RE production")+
  xlab("Time")
```

```
## 'geom_smooth()' using formula = 'y ~ x'
## 'geom_smooth()' using formula = 'y ~ x'
```



```
#Plotting the original and detrended data for Hydro with their regression lines
ggplot(REDataset, aes(x=Date, y=Hydro))+
  geom_line(color = "blue")+
  geom_smooth(color="green", method="lm")+
  geom_line(aes(y=detrend_hydro$`detrended hydro`), colour = "lightblue")+
  geom_smooth(aes(y=detrend_hydro$`detrended hydro`), method="lm", color="darkgreen")+
  xlab("Time")+
  ylab("Hydro Consumption")
```

```
## 'geom_smooth()' using formula = 'y ~ x'
## 'geom_smooth()' using formula = 'y ~ x'
```



Analysis: The detrended data shifts the datapoints to around zero (because f the removal of the intercept). In the case of RE, the regression line went from being upward rising in the raw data to horizontal around zero in the detrended data. This indicates that the upward (linear) rising trend in the RE dataset was removed in the detrending process. On the other hand, in hydro, while the data shifted to around zero, the regression line of the raw data is almost parallel to that of the detrended data, and the shape of the time series remains perpetually the same, indicating that it was not detrended sufficiently (if at all).

### $\mathbf{Q5}$

Plot ACF and PACF for the detrended series and compare with the plots from Q1. You may use plot\_grid() again to get them side by side. nut mot mandatory. Did the plots change? How?

```
#Converting detrended datasets into time series
ts_detrend_RE <- ts(detrend_RE$`detrended RE`, start=c(1973, 01), frequency = 12)
head(ts_detrend_RE)
             Jan
                      Feb
                               Mar
                                         Apr
                                                  May
                                                           Jun
## 1973 38.14556 14.93252 35.58448 25.52444 31.47240 23.03536
ts_detrend_hydro <- ts(detrend_hydro$`detrended hydro`, start=c(1973, 01), frequency = 12)
head(ts_detrend_hydro)
##
               Jan
                          Feb
                                     Mar
                                                            May
                                                                        Jun
                                                 Apr
## 1973 6.8371025 -3.1710482
                              5.5788011
                                          0.4566504
                                                      2.9574997 -0.6156510
```

```
#Detrended RE Production Plots

ts_detrend_RE_plot <- autoplot(ts_detrend_RE, col="orange") +
    xlab("Time") + ylab("RE Production") +
    theme(axis.text.x = element_text(angle = 90, vjust = 0.5, hjust=1))+
    ggtitle("Detrended RE Production over time")

ts_detrend_RE_ACF <- Acf(ts_detrend_RE, lag.max = 60, type = "correlation", plot = FALSE)
ts_detrend_RE_ACF <- autoplot(ts_detrend_RE_ACF, col = "orange") +
    xlab("Lag Time (Months)") + ylab("ACF Value") +
    ggtitle("ACF of detrended RE Production")

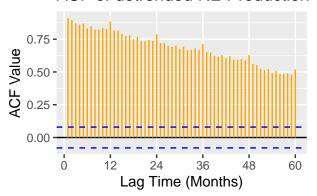
ts_detrend_RE_PACF <- Pacf(ts_detrend_RE, lag.max = 60, type = "correlation", plot = FALSE)
ts_detrend_RE_PACF <- autoplot(ts_detrend_RE_PACF, col = "orange") +
    xlab ("Lag Time (Months)") + ylab ("PACF Value") +
    ggtitle("PACF of detrended RE Production")

plot_grid(ts_detrend_RE_plot, ts_detrend_RE_ACF, ts_detrend_RE_PACF))</pre>
```

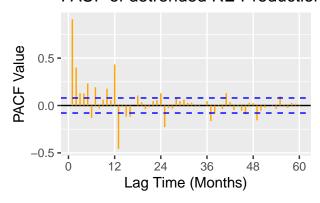
### Detrended RE Production over tir

## Time 2020 - 00- 1000 - 0000 - 0000 - 0000 - 0000 - 0000 - 0000 - 0000 - 0000 - 0000 - 0000 - 0000 - 0000 - 0000 - 0000 - 0000 - 0000 - 0000 - 0000 - 0000 - 0000 - 0000 - 0000 - 0000 - 0000 - 0000 - 0000 - 0000 - 0000 - 0000 - 0000 - 0000 - 0000 - 0000 - 0000 - 0000 - 0000 - 0000 - 0000 - 0000 - 0000 - 0000 - 0000 - 0000 - 0000 - 0000 - 0000 - 0000 - 0000 - 0000 - 0000 - 0000 - 0000 - 0000 - 0000 - 0000 - 0000 - 0000 - 0000 - 0000 - 0000 - 0000 - 0000 - 0000 - 0000 - 0000 - 0000 - 0000 - 0000 - 0000 - 0000 - 0000 - 0000 - 0000 - 0000 - 0000 - 0000 - 0000 - 0000 - 0000 - 0000 - 0000 - 0000 - 0000 - 0000 - 0000 - 0000 - 0000 - 0000 - 0000 - 0000 - 0000 - 0000 - 0000 - 0000 - 0000 - 0000 - 0000 - 0000 - 0000 - 0000 - 0000 - 0000 - 0000 - 0000 - 0000 - 0000 - 0000 - 0000 - 0000 - 0000 - 0000 - 0000 - 0000 - 0000 - 0000 - 0000 - 0000 - 0000 - 0000 - 0000 - 0000 - 0000 - 0000 - 0000 - 0000 - 0000 - 0000 - 0000 - 0000 - 0000 - 0000 - 0000 - 0000 - 0000 - 0000 - 0000 - 0000 - 0000 - 0000 - 0000 - 0000 - 0000 - 0000 - 0000 - 0000 - 0000 - 0000 - 0000 - 0000 - 0000 - 0000 - 0000 - 0000 - 0000 - 0000 - 0000 - 0000 - 0000 - 0000 - 0000 - 0000 - 0000 - 0000 - 0000 - 0000 - 0000 - 0000 - 0000 - 0000 - 0000 - 0000 - 0000 - 0000 - 0000 - 0000 - 0000 - 0000 - 0000 - 0000 - 0000 - 0000 - 0000 - 0000 - 0000 - 0000 - 0000 - 0000 - 0000 - 0000 - 0000 - 0000 - 0000 - 0000 - 0000 - 0000 - 0000 - 0000 - 0000 - 0000 - 0000 - 0000 - 0000 - 0000 - 0000 - 0000 - 0000 - 0000 - 0000 - 0000 - 0000 - 0000 - 0000 - 0000 - 0000 - 0000 - 0000 - 0000 - 0000 - 0000 - 0000 - 0000 - 0000 - 0000 - 0000 - 0000 - 0000 - 0000 - 0000 - 0000 - 0000 - 0000 - 0000 - 0000 - 0000 - 0000 - 0000 - 0000 - 0000 - 0000 - 0000 - 0000 - 0000 - 0000 - 0000 - 0000 - 0000 - 0000 - 0000 - 0000 - 0000 - 0000 - 0000 - 0000 - 0000 - 0000 - 0000 - 0000 - 0000 - 0000 - 0000 - 0000 - 0000 - 0000 - 0000 - 0000 - 0000 - 0000 - 0000 - 0000 - 0000 - 0000 - 0000 - 0000 - 0000 - 0000 - 0000 - 0000 - 0000 - 0000 - 0000 - 0000 - 0000 - 0000 - 0000 - 0000 - 0000 - 0000 - 0000 - 0000 -

### ACF of detrended RE Production



### PACF of detrended RE Production



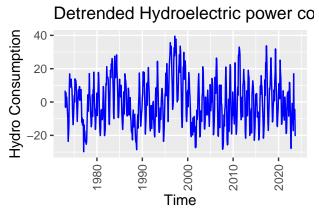
```
#Detrended Hydroelectric Power Consumption

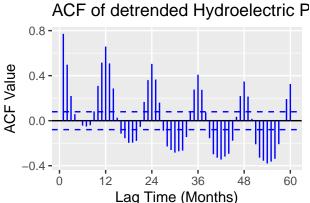
ts_detrend_Hydro_plot <- autoplot(ts_detrend_hydro, col="blue") +
    xlab("Time") + ylab("Hydro Consumption") +
    theme(axis.text.x = element_text(angle = 90, vjust = 0.5, hjust=1))+
    ggtitle("Detrended Hydroelectric power consumption over time")</pre>
```

```
ts_detrend_Hydro_ACF <- Acf(ts_detrend_hydro, lag.max = 60, type = "correlation", plot = FALSE)
ts_detrend_Hydro_ACF <- autoplot(ts_detrend_Hydro_ACF, col = "blue") +
    xlab ("Lag Time (Months)") + ylab ("ACF Value") +
    ggtitle("ACF of detrended Hydroelectric Power Consumption")

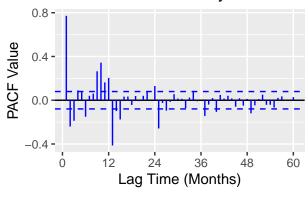
ts_detrend_Hydro_PACF <- Pacf(ts_detrend_hydro, lag.max = 60, type = "correlation", plot = FALSE)
ts_detrend_Hydro_PACF <- autoplot(ts_detrend_Hydro_PACF, col = "blue") +
    xlab ("Lag Time (Months)") + ylab ("PACF Value") +
    ggtitle("PACF of detrended Hydroelectric Power Consumption")

plot_grid(ts_detrend_Hydro_plot, ts_detrend_Hydro_ACF, ts_detrend_Hydro_PACF)</pre>
```

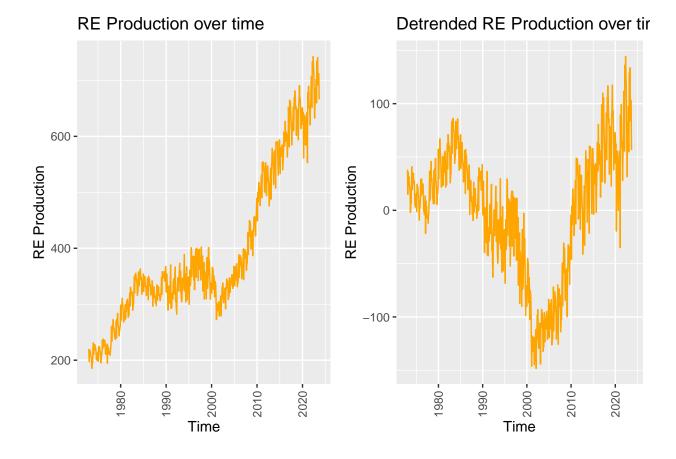




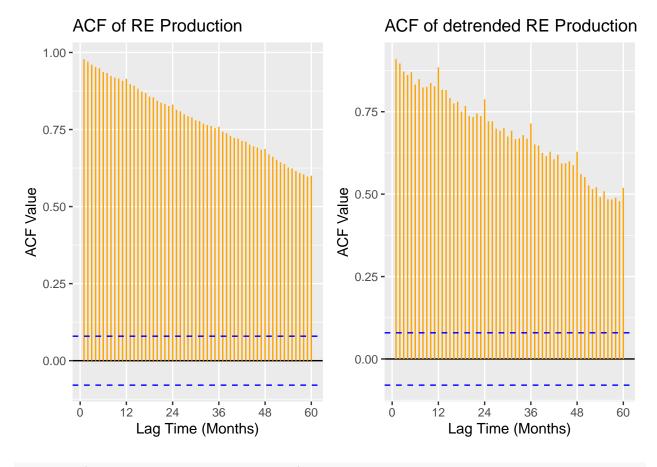
PACF of detrended Hydroelectric Power Consumption



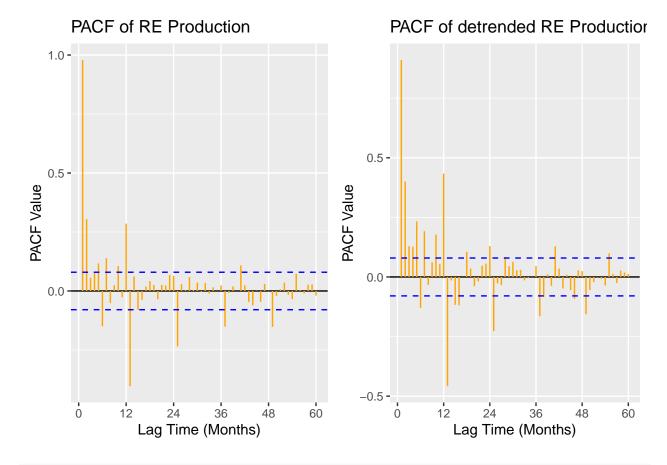
plot\_grid(ts\_RE\_plot, ts\_detrend\_RE\_plot)



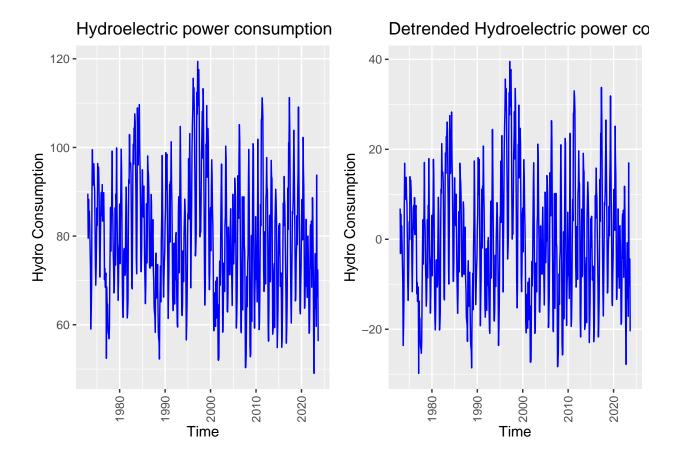
plot\_grid(ts\_RE\_ACF, ts\_detrend\_RE\_ACF)



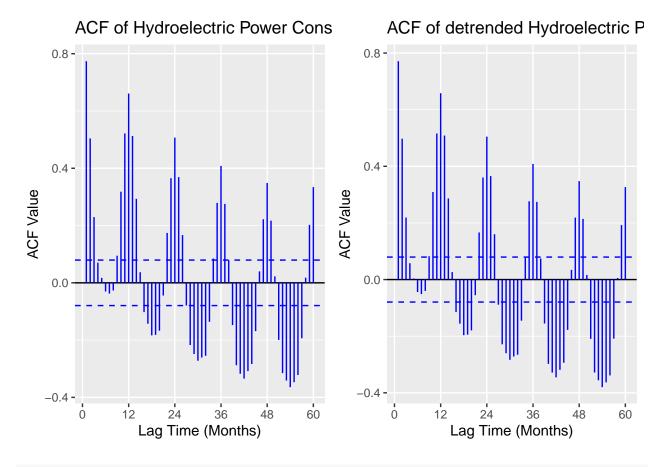
plot\_grid(ts\_RE\_PACF, ts\_detrend\_RE\_PACF)



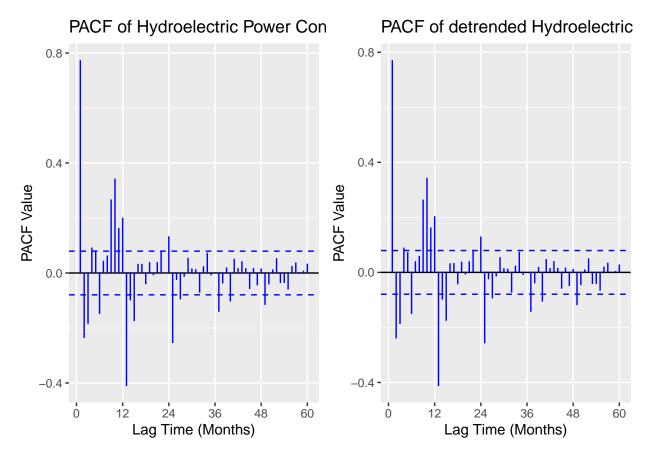
plot\_grid(ts\_Hydro\_plot, ts\_detrend\_Hydro\_plot)



plot\_grid(ts\_Hydro\_ACF, ts\_detrend\_Hydro\_ACF)



plot\_grid(ts\_Hydro\_PACF, ts\_detrend\_Hydro\_PACF)



Analysis: In RE, the almost coherent upward trend changes significantly to cycle around zero although with a one large dip to below -100 in 2000-2015 and then a rise to above 100 from 2015-2020. The ACF also declines by about 0.25 in the initial lags but the shape of the curve remains similar, while PACF remains similar with only a slight decline in the valye in lag 0. In hydro, the trend of the data remains similar, although it now hovers around 0 instead of the intercept of 82. The ACF and PACF both remain the same indicating no impact of the detrending on the data.

### Seasonal Component

Set aside the detrended series and consider the original series again from Q1 to answer Q6 to Q8.

### Q6

Just by looking at the time series and the acf plots, do the series seem to have a seasonal trend? No need to run any code to answer your question. Just type in you answer below.

The hydro consumption dataset has a clear seasonal trend, which is most evident from the ACF plot. However, RE production does not seem to have a seasonal trend, and instead seems to possibly have a linear trend.

### Q7

Use function lm() to fit a seasonal means model (i.e. using the seasonal dummies) the two time series. Ask R to print the summary of the regression. Interpret the regression output. From the results which series have a seasonal trend? Do the results match you answer to Q6?

```
#Creating the seasonal dummies
dummies_RE <- seasonaldummy(ts_REDataset[,1])</pre>
dummies Hydro <- seasonaldummy(ts REDataset[,2])</pre>
#Fitting a linear model to the seasonal dummies
seas_means_model_RE <- lm(REDataset[,2]~dummies_RE)</pre>
summary(seas_means_model_RE)
##
## Call:
## lm(formula = REDataset[, 2] ~ dummies RE)
## Residuals:
##
       Min
                1Q Median
                                3Q
                                       Max
## -199.19 -86.35 -48.84 113.18 331.58
##
## Coefficients:
##
                 Estimate Std. Error t value Pr(>|t|)
## (Intercept)
                  404.526
                              19.574 20.666
                                               <2e-16 ***
## dummies_REJan
                    2.962
                              27.546
                                      0.108
                                                0.914
## dummies_REFeb
                 -34.476
                              27.546 -1.252
                                                0.211
                    3.929
                              27.546
                                                0.887
## dummies_REMar
                                      0.143
                   -8.695
                              27.546 -0.316
                                                0.752
## dummies REApr
## dummies_REMay
                   6.645
                              27.546
                                      0.241
                                                0.809
## dummies REJun
                  -4.198
                              27.546 -0.152
                                                0.879
## dummies_REJul
                   2.460
                              27.546
                                      0.089
                                                0.929
## dummies_REAug
                   -5.026
                              27.546 -0.182
                                                0.855
## dummies RESep -29.119
                              27.546 -1.057
                                                0.291
                              27.682 -0.725
## dummies_REOct -20.068
                                                0.469
## dummies_RENov -20.346
                              27.682 -0.735
                                                0.463
## ---
## Signif. codes: 0 '*** 0.001 '** 0.01 '* 0.05 '.' 0.1 ' 1
## Residual standard error: 138.4 on 597 degrees of freedom
## Multiple R-squared: 0.009296,
                                    Adjusted R-squared:
## F-statistic: 0.5093 on 11 and 597 DF, p-value: 0.8976
seas means model Hydro <- lm(REDataset[,3]~dummies Hydro)</pre>
summary(seas_means_model_Hydro)
##
## Call:
## lm(formula = REDataset[, 3] ~ dummies_Hydro)
##
## Residuals:
##
       Min
                1Q Median
                                3Q
                                       Max
## -31.323 -5.849 -0.468
                             6.243 32.290
##
## Coefficients:
##
                    Estimate Std. Error t value Pr(>|t|)
## (Intercept)
                      80.282
                                  1.470 54.601 < 2e-16 ***
## dummies_HydroJan
                       4.807
                                  2.069
                                          2.323 0.02050 *
```

```
## dummies HydroFeb
                     -2.725
                                 2.069 -1.317 0.18831
## dummies_HydroMar 6.825
                                 2.069 3.298 0.00103 **
## dummies HydroApr 5.319
                                 2.069 2.571 0.01039 *
## dummies_HydroMay 13.922
                                 2.069 6.729 4.02e-11 ***
## dummies_HydroJun 10.650
                                 2.069
                                        5.147 3.60e-07 ***
## dummies HydroJul 3.912
                               2.069 1.891 0.05914 .
## dummies HydroAug -5.677
                               2.069 -2.744 0.00626 **
## dummies_HydroSep -16.797
                               2.069 -8.118 2.72e-15 ***
                                 2.079 -7.920 1.17e-14 ***
## dummies HydroOct -16.468
## dummies_HydroNov -10.885
                                 2.079 -5.235 2.29e-07 ***
## Signif. codes: 0 '*** 0.001 '** 0.01 '* 0.05 '.' 0.1 ' 1
## Residual standard error: 10.4 on 597 degrees of freedom
## Multiple R-squared: 0.4697, Adjusted R-squared: 0.4599
## F-statistic: 48.07 on 11 and 597 DF, p-value: < 2.2e-16
#Storing regression coefficients
BO_RE_seas <- seas_means_model_RE$coefficients[1]
BO_RE_seas
## (Intercept)
      404.5261
##
B1_RE_seas <- seas_means_model_RE$coefficients[2:12]
B1_RE_seas
## dummies_REJan dummies_REFeb dummies_REMar dummies_REApr dummies_REMay
       2.962096
                   -34.476080
                                   3.928880
                                                -8.695335
                                                               6.645116
## dummies_REJun dummies_REJul dummies_REAug dummies_RESep dummies_REOct
      -4.197727
                     2.459508
                                  -5.025904
                                               -29.118512
                                                             -20.068140
##
## dummies RENov
     -20.345560
##
BO Hydro seas <- seas means model Hydro$coefficients[1]
B0_Hydro_seas
## (Intercept)
##
     80.28176
B1 Hydro seas <- seas means model Hydro$coefficients[2:12]
B1 Hydro seas
## dummies_HydroJan dummies_HydroFeb dummies_HydroMar dummies_HydroApr
##
          4.807299
                          -2.725270
                                            6.825024
                                                             5.319044
## dummies_HydroMay dummies_HydroJun dummies_HydroJul dummies_HydroAug
##
         13.922220
                          10.649985
                                            3.912260
                                                            -5.676917
## dummies HydroSep dummies HydroOct dummies HydroNov
##
        -16.797387
                         -16.467980
                                          -10.884780
```

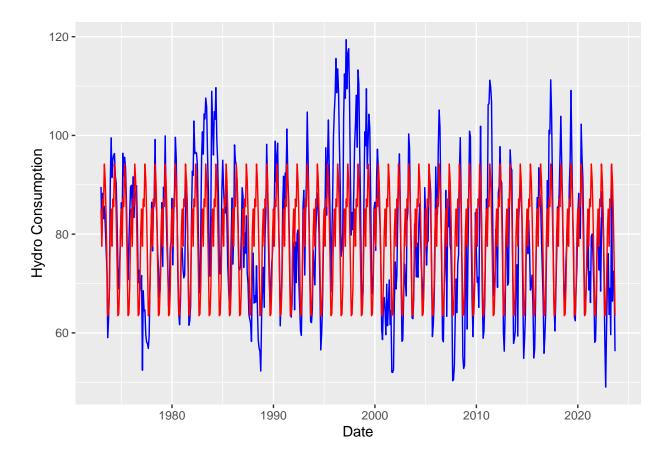
Analysis: The RE seasonal regression model does not give a significant output as the overall p-value is 0.8976 which is >0.05. Further the p-value of all beta values are also > 0.05, indicating that RE does not have a seasonal trend. On the other hand, the overall p=value of hydro seasonal regression model gives a significant output as the overall p-value is  $2.2 \times 10^{\circ}$ -16 which is much < 0.05. Further, all beta values except for that of february are <0.05 indicating that hydro does have a seasonal trend. This matches my results from Qn 6.

### $\mathbf{Q8}$

Use the regression coefficients from Q7 to deseason the series. Plot the deseason series and compare with the plots from part Q1. Did anything change?

```
#computing seasonal component
Hydro_seas_comp <- array(0,nobs)
for(i in 1:nobs){
    Hydro_seas_comp[i] <- (BO_Hydro_seas+B1_Hydro_seas %*% dummies_Hydro[i,])
}
head(Hydro_seas_comp)</pre>
```

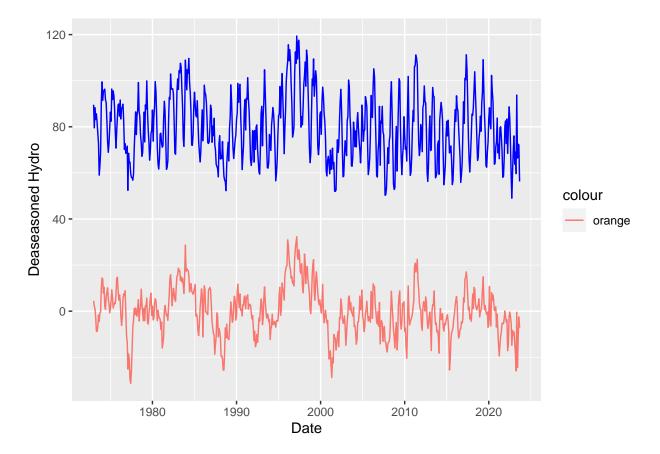
## [1] 85.08906 77.55649 87.10678 85.60080 94.20398 90.93175



```
#Removing seasonal component
deseason_Hydro_data <- REDataset[,3]-Hydro_seas_comp
head(deseason_Hydro_data)</pre>
```

## [1] 4.472941 1.987510 1.177216 -2.448804 -8.560980 -8.871745

```
#Understanding what we did
ggplot(REDataset, aes(x=Date, y=Hydro))+
  geom_line(color="blue")+
  ylab("Deaseasoned Hydro")+
  geom_line(aes(y=deseason_Hydro_data, color="orange"))
```



Analysis: Deseasoning the Hydro dataset did reduce some of its seasonality and shifted it to around zero. However, an element of seasonality does still exist in the plot and it requires additional exploration of the ACF and PACF.

### $\mathbf{Q}\mathbf{9}$

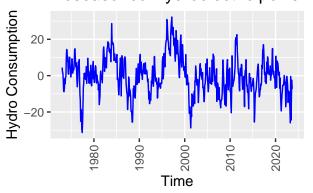
Plot ACF and PACF for the deseason series and compare with the plots from Q1. You may use plot\_grid() again to get them side by side. nut mot mandatory. Did the plots change? How?

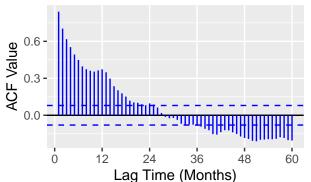
```
#Converting to a time series
ts_deseason_hydro <- ts(deseason_Hydro_data, start=c(1973, 01), frequency = 12 )
head(ts_detrend_hydro)</pre>
```

```
## Jan Feb Mar Apr May Jun
## 1973 6.8371025 -3.1710482 5.5788011 0.4566504 2.9574997 -0.6156510
```

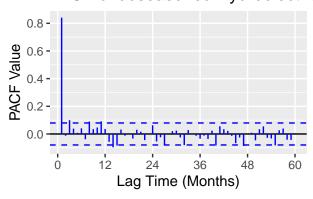
### Deseasoned Hydroelectric power

## ACF of deseasoned Hydroelectric

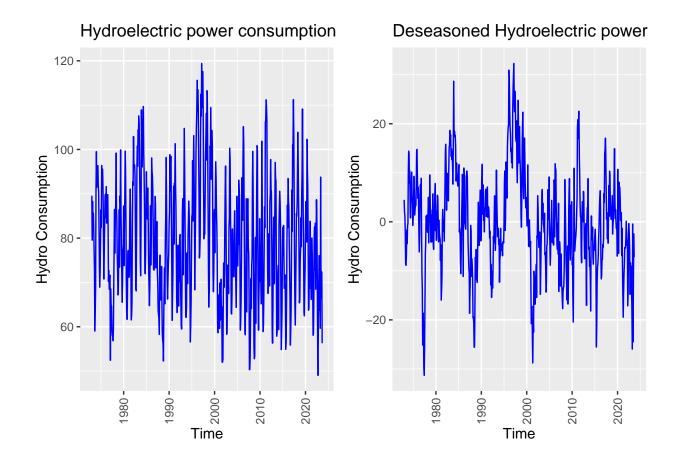




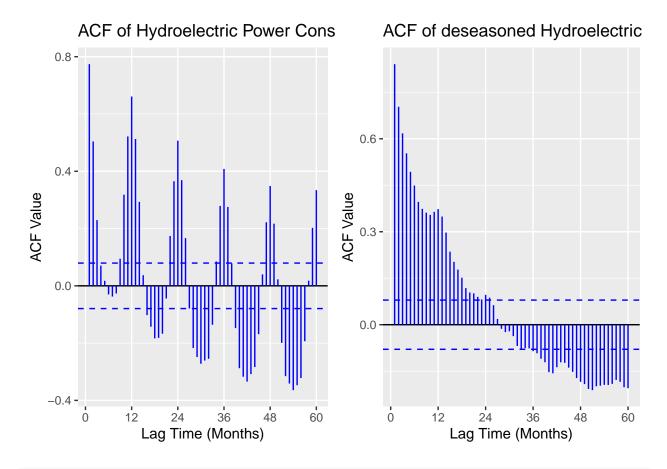
PACF of deseasoned Hydroelectric Power Consumption



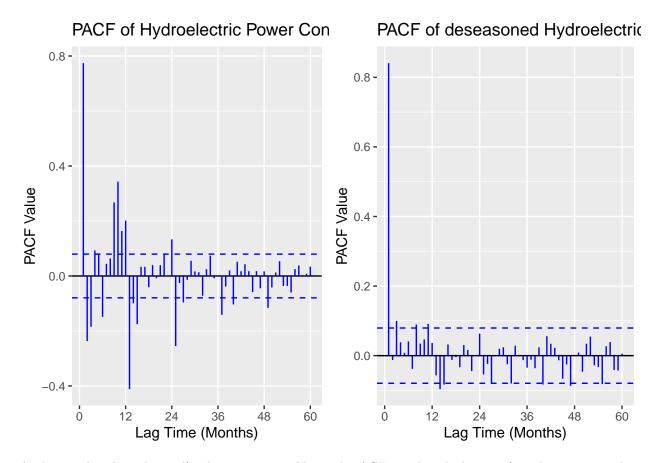
```
plot_grid(ts_Hydro_plot, ts_deseason_Hydro_plot)
```



plot\_grid(ts\_Hydro\_ACF, ts\_deseason\_Hydro\_ACF)



plot\_grid(ts\_Hydro\_PACF, ts\_deseason\_Hydro\_PACF)



Analysis: The plots changed! This is most visible in the ACF graphs which went from being seasonal to linearly declining.