

CS 663
Assignment 5
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QS 6.

The first kernel given is as $k_1 = \begin{bmatrix} 0 & 1 & 0 \\ 1 & -4 & 1 \\ 0 & 1 & 0 \end{bmatrix}$

Here, $N = 201$. We zero pad k_1 to get a new k_1 which is an $N \times N$ matrix.

Hence, $\text{DFT}(k_1)$ at a particular frequency (u, v) is given as:

$$\text{DFT1}(u, v) = 2 * \exp(-j2\pi(u+v)(N+1)/2N) \{ \cos(2\pi u N) + \cos(2\pi v N) - 2 \}$$

Similarly, for the kernel $k_2 = \begin{bmatrix} -1 & -1 & -1 \\ -1 & 8 & -1 \\ -1 & -1 & -1 \end{bmatrix}$ with $N=201$, the $\text{DFT}(k_2)$ of the padded kernel k_2 at frequency (u, v) will be given as the equation :

$$\text{DFT2}(u, v) = 2 * \exp(-j2\pi(u+v)(N+1)/2N) \{ 4 - \cos(2\pi u N) - \cos(2\pi v N) - \cos(2\pi(u+v)N) - \cos(2\pi(u-v)N) \}$$

An ideal high pass filter would have frequency response that is cylindrical with low values. Both the plots have circular contours. However kernel k_2 sharpens the image better than k_1 as the cutoff frequency changes as the shape of filter changes. At the end frequencies, they both attain parabolic shape, with k_3 forming a type of paraboloid structure with almost constant magnitude. Therefore, k_2 is better high pass than the kernel k_1 .