

# Assignment - 1

## Session 9 – Statistical Inference

1. If  $Z$  is norm (mean = 0, sd = 1)

Find  $P(Z > 2.64)$

Find  $P(|Z| > 1.39)$

Ans:

# $P(Z > 2.64)$

#We need to take the whole of the right hand side (area 0.5)

#and subtract the area from  $z = 0$  to  $z = 2.64$ , which we get from the z-table.

#the probability value of  $z = 2.64$  in table is 0.4959

#so  $P(Z > 2.64) = 0.5 - P(0 < z < 2.64) = 0.5 - 0.4959 = 0.0041$

#or we can do like this

```
> #P(|Z| > 1.39)
> #we can find by pnorm function too
> pnorm(1.39)
[1] 0.9177356
> pnorm(-1.39)
[1] 0.08226444
```

# $1 - (pnorm(1.39) - pnorm(-1.39))$

# $1 - (0.9177356 - 0.08226444)$

# $1 - 0.8354712$

#0.1645288 (answer)

2. Suppose  $p$  = the proportion of students who are admitted to the graduate school of the University of

California at Berkeley, and suppose that a public relation officer boasts that UCB has historically had a

40% acceptance rate for its graduate school. Consider the data stored in the table UCBA admissions from

1973. Assuming these observations constituted a simple random sample, are they consistent with the

officer's claim, or do they provide evidence that the acceptance rate was significantly less than 40%?

Use an  $\hat{\alpha} = 0.01$  significance level.

Ans:

```
> -qnorm(0.99)
[1] -2.326348
> #Now to find out our test statistic
> newucb_data <- as.data.frame(UCBA admissions)
```

```
> View(newucb_data)
> dim(newucb_data)
[1] 24 4
> summary(newucb_data$Admit)
Admitted Rejected
      12      12
> phat<-12/(24)
> t <- (phat-0.4)/sqrt(0.4*0.6/(24))
> t
[1] 1
```

#by calculations it is clear that our test statistic is not less than -2.326348

#So we accept our null hypothesis  $H_0$

#hence we say that the observed data are consistent with the officer's claim at  $\alpha = 0.01$ (Level of Significance)