# Producing the examples in chapters 4 and 5

### 1 Example 4.1

```
mlb0 <- lmer(langPOST ~ (1|schoolnr), data = mlbook_red,</pre>
             REML = FALSE)
summary(mlb0)
## Linear mixed model fit by maximum likelihood ['lmerMod']
## Formula: langPOST ~ (1 | schoolnr)
     Data: mlbook_red
##
##
        AIC
                 BIC
                       logLik deviance df.resid
   26601.3 26620.0 -13297.6 26595.3
                                           3755
##
## Scaled residuals:
                1Q Median
      Min
                                3Q
## -4.1848 -0.6416 0.0909 0.7227
                                    2.5277
##
## Random effects:
## Groups
           Name
                         Variance Std.Dev.
## schoolnr (Intercept) 18.13
                                  4.257
## Residual
                         62.85
                                  7.928
## Number of obs: 3758, groups: schoolnr, 211
## Fixed effects:
              Estimate Std. Error t value
## (Intercept) 41.0046
                            0.3249
                                     126.2
```

## Example 4.3, Table 4.4

```
mlb44 <- lmer(langPOST ~ IQ_verb + sch_iqv
                       + (1|schoolnr), data = mlbook_red,
                       REML = FALSE)
summary(mlb44)
## Linear mixed model fit by maximum likelihood ['lmerMod']
## Formula: langPOST ~ IQ_verb + sch_iqv + (1 | schoolnr)
##
     Data: mlbook red
##
                      logLik deviance df.resid
                BIC
   24898.0 24929.2 -12444.0 24888.0
##
                                          3753
## Scaled residuals:
      Min
               10 Median
                               3Q
## -4.2220 -0.6411 0.0634 0.7059 3.2190
## Random effects:
## Groups
                        Variance Std.Dev.
            Name
## schoolnr (Intercept) 8.68
                                 2.946
## Residual
                        40.43
                                 6.358
```

```
## Number of obs: 3758, groups: schoolnr, 211
##
## Fixed effects:
               Estimate Std. Error t value
## (Intercept) 41.11378
                           0.23181 177.36
## IQ verb
                           0.05549
                                     44.22
                2.45361
## sch iqv
                1.31242
                           0.26160
                                      5.02
##
## Correlation of Fixed Effects:
           (Intr) IQ_vrb
## IQ_verb -0.007
## sch_iqv 0.043 -0.210
```

2.1 The parameters of the random part of the model are in

```
VarCorr(mlb44)
```

```
## Groups Name Std.Dev.
## schoolnr (Intercept) 2.9461
## Residual 6.3584
```

2.2 the estimated intercept variance is

```
VarCorr(mlb44)$schoolnr[1,1]
## [1] 8.679719
```

2.3 For other methods for the objects produced by lmer, see

#### methods(class="merMod")

```
## [1] anova
                    as.function coef
                                              confint
                                                           deviance
## [6] df.residual drop1
                                 extractAIC
                                              family
                                                           fitted
## [11] fixef
                    formula
                                 fortify
                                              getL
                                                           getME
## [16] hatvalues
                    isGLMM
                                 isLMM
                                              isNLMM
                                                           isREML
## [21] logLik
                    model.frame model.matrix ngrps
                                                           nobs
                                 print
## [26] plot
                    predict
                                                           ranef
                                              profile
## [31] refit
                    refitML
                                 residuals
                                              show
                                                           sigma
## [36] simulate
                    summary
                                 terms
                                              update
                                                           VarCorr
## [41] vcov
                    weights
## see '?methods' for accessing help and source code
```

#### 3 Section 4.8.

3.1 The posterior means are obtained as follows: the word ranef stands for "random effects"

```
re.mlb44 <- ranef(mlb44, condVar=TRUE, standard=TRUE)
tbl_df(re.mlb44$schoolnr) %>% glimpse
```

```
## Observations: 211
## Variables: 1
## $ (Intercept) <dbl> 0.7854736, -3.9600743, 0.6766074, 0.6581958, -2.87...
```

3.2 The condVar parameter will also give the posterior variances. What is the structure of this object?

```
str(re.mlb44)
## List of 1
## $ schoolnr:'data.frame': 211 obs. of 1 variable:
## ..$ (Intercept): num [1:211] 0.785 -3.96 0.677 0.658 -2.878 ...
## ..- attr(*, "postVar")= num [1, 1, 1:211] 1.36 3.47 3.19 2.58 4.19 ...
## - attr(*, "class")= chr "ranef.mer"
```

3.3 The posterior means are

```
postmean <- re.mlb44$schoolnr[,1]
str(postmean)
## num [1:211] 0.785 -3.96 0.677 0.658 -2.878 ...</pre>
```

3.4 and the posterior variances are

```
postvar <- attr(re.mlb44$schoolnr,'postVar')[1,1,]
head(postvar)
## [1] 1.363199 3.467994 3.194016 2.582055 4.186157 1.957101</pre>
```

3.5 These are also the comparative variances. The diagnostic variance is calculated using (4.18):

```
diagvar <- VarCorr(mlb44)$schoolnr[1,1] - postvar
diagvar[1:5]
## [1] 7.316520 5.211725 5.485703 6.097663 4.493562</pre>
```

### 4 Comparative standard deviations

```
compsd <- sqrt(postvar)
compsd[1:5]
## [1] 1.167561 1.862255 1.787181 1.606878 2.046010</pre>
```

### 5 Bounds of comparative intervals

```
lower <- postmean - 1.39*compsd
upper <- postmean + 1.39*compsd
lower[1:5]</pre>
```

```
## [1] -0.8374365 -6.5486087 -1.8075742 -1.5753640 -5.7216451
upper[1:5]
## [1] 2.40838377 -1.37153986 3.16078909 2.89175558 -0.03373715
```

#### 5.1 Order

```
perm <- order(postmean, lower, upper)
pm_sort <- postmean[perm]
upper_sort <- upper[perm]
lower_sort <- lower[perm]
pm_sort[1:5]
## [1] -6.717241 -6.469771 -5.887817 -5.760691 -5.316493
upper_sort[1:5]
## [1] -4.972407 -4.818789 -4.291595 -3.861553 -2.832311
pm_sort[1:5]
## [1] -6.717241 -6.469771 -5.887817 -5.760691 -5.316493</pre>
```

#### 5.2 A caterpillar plot like Fig. 4.4 can be produced as follows.

```
library(Hmisc)
errbar(1:211, pm_sort, upper_sort, lower_sort)
```

### 6 Example 5.4

```
form <- langPOST ~
  1 +
  IQ verb +
 ses +
  sch_iqv +
  sch ses +
  IQ verb:ses +
  sch_iqv:sch_ses +
  (1 + IQ_verb|schoolnr)
mlb54sh <- lmer(form, data = mlbook_red,</pre>
                        REML = FALSE)
summary(mlb54sh)
## Linear mixed model fit by maximum likelihood ['lmerMod']
## Formula: langPOST ~ 1 + IQ_verb + ses + sch_iqv + sch_ses + IQ_verb:ses +
##
       sch_iqv:sch_ses + (1 + IQ_verb | schoolnr)
##
     Data: mlbook red
##
##
        AIC
                 BIC
                     logLik deviance df.resid
   24648.8 24717.4 -12313.4 24626.8
##
                                           3747
##
## Scaled residuals:
      Min
                1Q Median
                                30
                                       Max
## -4.2688 -0.6295 0.0783 0.7036 2.8697
##
## Random effects:
## Groups
                         Variance Std.Dev. Corr
           Name
  schoolnr (Intercept) 8.3685 2.8928
##
                          0.1643 0.4054
                                           -0.79
             IQ_verb
## Residual
                         37.3779 6.1137
## Number of obs: 3758, groups: schoolnr, 211
## Fixed effects:
##
                    Estimate Std. Error t value
## (Intercept)
                   41.612180
                             0.247479 168.14
## IQ verb
                               0.063344
                    2.231092
                                          35.22
                    0.174436
                               0.011660
                                          14.96
## ses
## sch_iqv
                    0.760180
                               0.295794
                                           2.57
## sch ses
                   -0.088609
                               0.042280
                                          -2.10
## IQ_verb:ses
                   -0.017341
                               0.004901
                                          -3.54
## sch_iqv:sch_ses -0.119716
                               0.033260
                                          -3.60
##
## Correlation of Fixed Effects:
##
               (Intr) IQ_vrb ses
                                    sch_qv sch_ss IQ_vr:
## IQ_verb
               -0.305
## ses
                0.009 -0.251
              -0.092 -0.167 0.061
## sch_iqv
               0.051 0.054 -0.269 -0.496
## sch_ses
## IQ_verb:ses -0.099 0.076 -0.123 -0.014 -0.140
## sch_qv:sch_ -0.374 -0.010 0.024 0.181 -0.017 -0.126
```

```
mlb54 <- lmer(langPOST ~ IQ_verb*ses + sch_iqv*sch_ses</pre>
                        + (IQ_verb|schoolnr), data = mlbook_red,
                        REML = FALSE)
summary(mlb54)
## Linear mixed model fit by maximum likelihood ['lmerMod']
## Formula:
## langPOST ~ IQ_verb * ses + sch_iqv * sch_ses + (IQ_verb | schoolnr)
##
     Data: mlbook red
##
##
        AIC
                 BIC logLik deviance df.resid
   24648.8 24717.4 -12313.4 24626.8
##
                                           3747
##
## Scaled residuals:
      Min
               1Q Median
                                3Q
                                       Max
## -4.2688 -0.6295 0.0783 0.7036 2.8697
## Random effects:
                         Variance Std.Dev. Corr
## Groups
           Name
## schoolnr (Intercept) 8.3685 2.8928
##
             IQ_verb
                          0.1643 0.4054
                                           -0.79
                         37.3779 6.1137
## Residual
## Number of obs: 3758, groups: schoolnr, 211
## Fixed effects:
##
                   Estimate Std. Error t value
## (Intercept)
                   41.612180
                              0.247479 168.14
## IQ_verb
                   2.231092
                              0.063344
                                          35.22
## ses
                   0.174436
                              0.011660
                                         14.96
## sch_iqv
                   0.760180
                              0.295794
                                          2.57
## sch_ses
                   -0.088609
                              0.042280
                                         -2.10
                   -0.017341
## IQ_verb:ses
                               0.004901
                                          -3.54
## sch_iqv:sch_ses -0.119716
                              0.033260
                                         -3.60
## Correlation of Fixed Effects:
##
              (Intr) IQ_vrb ses
                                    sch_qv sch_ss IQ_vr:
## IQ_verb
              -0.305
## ses
               0.009 - 0.251
## sch_iqv
              -0.092 -0.167 0.061
## sch_ses
               0.051 0.054 -0.269 -0.496
## IQ verb:ses -0.099 0.076 -0.123 -0.014 -0.140
## sch_qv:sch_ -0.374 -0.010 0.024 0.181 -0.017 -0.126
mlb54 <- lmer(langPOST ~ IQ_verb*ses + sch_iqv*sch_ses
                        + (IQ_verb|schoolnr), data = mlbook_red,
                        REML = TRUE)
summary(mlb54)
## Linear mixed model fit by REML ['lmerMod']
## langPOST ~ IQ_verb * ses + sch_iqv * sch_ses + (IQ_verb | schoolnr)
##
      Data: mlbook_red
##
## REML criterion at convergence: 24658.2
##
```

```
## Scaled residuals:
      Min
##
           1Q Median
                                30
                                       Max
## -4.2662 -0.6285 0.0765 0.7014 2.8700
##
## Random effects:
  Groups
                         Variance Std.Dev. Corr
##
           Name
   schoolnr (Intercept) 8.5527 2.9245
                         0.1707 0.4131
##
             IQ_verb
                                           -0.78
## Residual
                         37.3946 6.1151
## Number of obs: 3758, groups: schoolnr, 211
## Fixed effects:
                   Estimate Std. Error t value
## (Intercept)
                              0.249637 166.69
                   41.611567
## IQ_verb
                   2.231943
                               0.063655
                                         35.06
## ses
                   0.174412
                               0.011665
                                          14.95
                              0.298530
## sch_iqv
                   0.762673
                                          2.55
## sch ses
                   -0.088785
                               0.042640
                                         -2.08
                   -0.017302
                              0.004912
                                         -3.52
## IQ_verb:ses
## sch_iqv:sch_ses -0.119733
                              0.033548
                                         -3.57
##
## Correlation of Fixed Effects:
##
              (Intr) IQ_vrb ses
                                    sch_qv sch_ss IQ_vr:
              -0.304
## IQ verb
## ses
               0.009 - 0.250
## sch_iqv
              -0.092 -0.165 0.060
## sch_ses
               0.051 0.054 -0.267 -0.497
## IQ_verb:ses -0.098  0.076 -0.123 -0.014 -0.139
## sch_qv:sch_ -0.375 -0.009 0.024 0.183 -0.017 -0.124
library("R2MLwiN")
## Loading required package: stats4
## Loading required package: lattice
## Loading required package: memisc
## Loading required package: MASS
##
## Attaching package: 'MASS'
## The following object is masked from 'package:dplyr':
##
##
       select
##
## Attaching package: 'memisc'
  The following object is masked from 'package:Matrix':
##
##
       as.array
## The following objects are masked from 'package:dplyr':
##
       collect, query, recode, rename
##
## The following objects are masked from 'package:stats':
```

```
##
##
      contr.sum, contr.treatment, contrasts
## The following object is masked from 'package:base':
##
##
      as.array
## Loading required package: coda
## The MLwiN_path option is currently set to C:/Program Files (x86)/MLwiN v2.36/
## To change this use: options(MLwiN_path="<path to MLwiN>")
library("doBy")
options(MLwiN_path = "C:/Program Files (x86)/MLwiN trial/i386/")
form <- langPOST ~
 1 +
 IQ_verb +
 ses +
 sch iqv +
 sch_ses +
 IQ verb:ses +
 sch_iqv:sch_ses +
 (1 + IQ_verb|schoolnr)
(mymodel1 <- runMLwiN(form, data = mlbook red))</pre>
## MLwiN (version: 2.36) multilevel model (Normal)
## Estimation algorithm: IGLS
                                Elapsed time: 6.68s
## Number of obs: 3758 (from total 3758) The model converged after 4 iterations.
## Log likelihood:
                    -12482.4
## Deviance statistic: 24964.8
## The model formula:
## langPOST ~ 1 + IQ_verb + ses + sch_iqv + sch_ses + IQ_verb:ses +
      sch_iqv:sch_ses + (1 + IQ_verb | schoolnr)
##
## Level 1: schoolnr
## -----
## The fixed part estimates:
                                           Pr(>|z|)
                    Coef.
                          Std. Err.
                                                            [95% Conf.
                                                                      Interval]
                                      z
## Intercept
                 41.73600 0.12250 340.70
                                                              41.49591
                                                                      41.97610
## IQ_verb
                           0.05774 36.82 1.04e-296
                                                                        2.23903
                 2.12585
                                                       ***
                                                              2.01268
                                    13.97 2.247e-44
## ses
                  0.17885
                            0.01280
                                                      ***
                                                              0.15376
                                                                         0.20393
## sch_iqv
                  0.89485
                           0.16525
                                     5.42 6.121e-08
                                                       ***
                                                              0.57097
                                                                        1.21873
## sch_ses
                 -0.09691
                           0.02386
                                     -4.06 4.864e-05
                                                      ***
                                                              -0.14367
                                                                        -0.05015
## IQ_verb:ses
                 -0.02063
                           0.00471
                                      -4.38
                                           1.173e-05
                                                              -0.02985
                                                                        -0.01140
                                                      ***
## sch_iqv:sch_ses
                 -0.11705
                            0.01913
                                      -6.12
                                           9.402e-10
                                                              -0.15453
                                                                        -0.07956
## Signif. codes: 0 '***' 0.001 '**' 0.05 '.' 0.1 ' ' 1
## -----
## The random part estimates at the schoolnr level:
                         Coef.
                                Std. Err.
## var_Intercept
                      46.65785
                                1.19486
## cov_Intercept_IQ_verb -2.29677
                                 0.26798
## var_IQ_verb
                      -0.11155
                                 0.13368
```