

To Help or Disturb: Introduction of Crowdsourced WiFi to 5G Networks

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Pillar of Engineering Systems and Design
Singapore University of Technology and Design (SUTD)

September 12, 2023



About SUTD



- A new public university established in 2009.
- Was established in collaboration with MIT.
- Ranking in the world: 21st in Telecommunication Engineering according to ShanghaiRanking 2023.

Acknowledgement

- This is a joint work with Associate Professor Lingjie Duan.



Prof. Lingjie Duan



Prof. Costas Courcoubetis

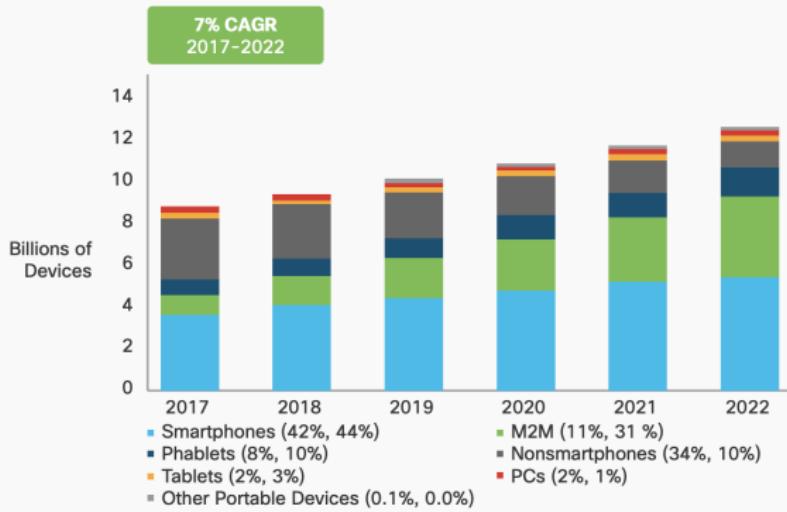
- Results here have been appeared in IEEE TMC.
- **Shugang Hao** and Lingjie Duan, “To Help or Disturb: Introduction of Crowdsourced WiFi to 5G Networks,” IEEE Transactions on Mobile Computing (**IEEE TMC**), vol. 22, no. 9, pp. 5583-5596, 1 Sept. 2023.

Overview

- ① Background: WiFi's Complementarity for 5G Networks
- ② System Model
- ③ Equilibrium Analysis
- ④ Extension to Congested WiFi Case
- ⑤ Summary

Background: Overwhelming Mobile Devices

Figure 4. Global Mobile Devices and Connections Growth



Note: Figures in parentheses refer to 2017, 2022 device share.

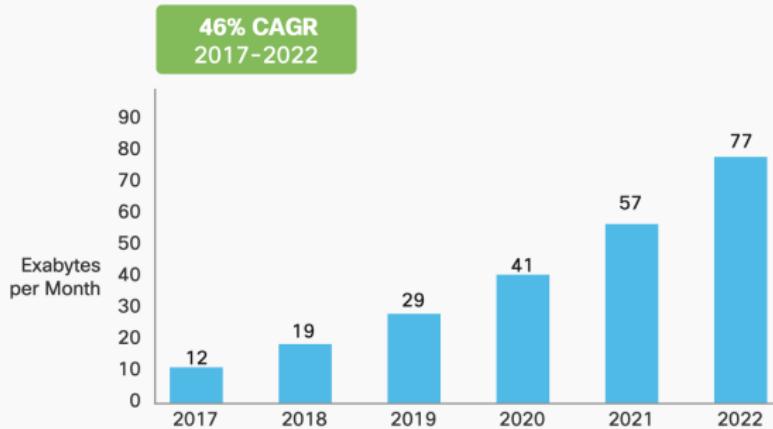
Source: Cisco VNI Mobile, 2019.

Rapid proliferation of mobile devices.

Cisco Visual Networking Index: Global Mobile Data Traffic Forecast Update, 2017–2022, 2019, [online]
<http://media.mediapost.com/uploads/CiscoForecast.pdf>

Background: Overwhelming Mobile Data Traffic

Figure 2. Cisco Forecasts 77 Exabytes per Month of Mobile Data Traffic by 2022



Source: Cisco VNI Mobile, 2019

Mobile data traffic has been **ever-increasing overwhelmingly** with rapid proliferation of mobile devices.

Cisco Visual Networking Index: Global Mobile Data Traffic Forecast Update, 2017–2022, 2019, [online]
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Background: Profile Wireless Technology Issues

To meet overwhelming data traffic demand,

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 - An individual AP has **small** service coverage.
 - It is **difficult** to deploy a **ubiquitous** WiFi network².

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Fon's crowdsourced WiFi network

- has included over **23 million APs**,
- and is fast expanding to cover many **populous and crowded places**.



WiFi hotspots by Fon in London area.

BT Fon WiFi Map, <https://www.btwifi.co.uk/find/>.

Background: WiFi's Complementary for 5G

The crowdsourced WiFi community network's coverage

- is still **not comparable to the ubiquitous 5G coverage,**

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Co-existing 5G and crowdsourced WiFi networks:

- + British Telecom and Fon in the United Kingdom,
- Telenor and OpenSpark in Finland.

Background: WiFi's Complementary for 5G Networks

Features of 5G and crowdsourced WiFi networks:

Features	5G	Crowdsourced WiFi
Coverage	Ubiquitous	Limited
Network Externality	Negative	Positive & Negative

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WiFi's complementarity for 5G:

5G users may add on the crowdsourced WiFi.

Research Questions

We will answer, after the introduction of the crowdsourced WiFi network,

how will 5G users add on the crowdsourced WiFi network?

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how will users' payoffs change?

Related Work on Traffic Offloading

Li et al. (2019), Iosifidis et al. (2015), Lee et al. (2014)

- assumed a cellular network operator's **deploying his own WiFi network** to offload data traffic,
- focused on **central operation**.

Manshaei et al. (2008), Li et al. (2021)

- **ignored** the **negative** network externalities of the 5G network due to congestion.

Gao et al. (2014)

- only studied how a 5G operator bargains with a traditional WiFi network to decide the offloaded traffic amount and associated payment,
- **ignored** the crowdsourced WiFi's **positive** network externality and the users' choices on both service.

Related Work on Network Externalities

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- Negative network externalities in 5G network due to congestion.

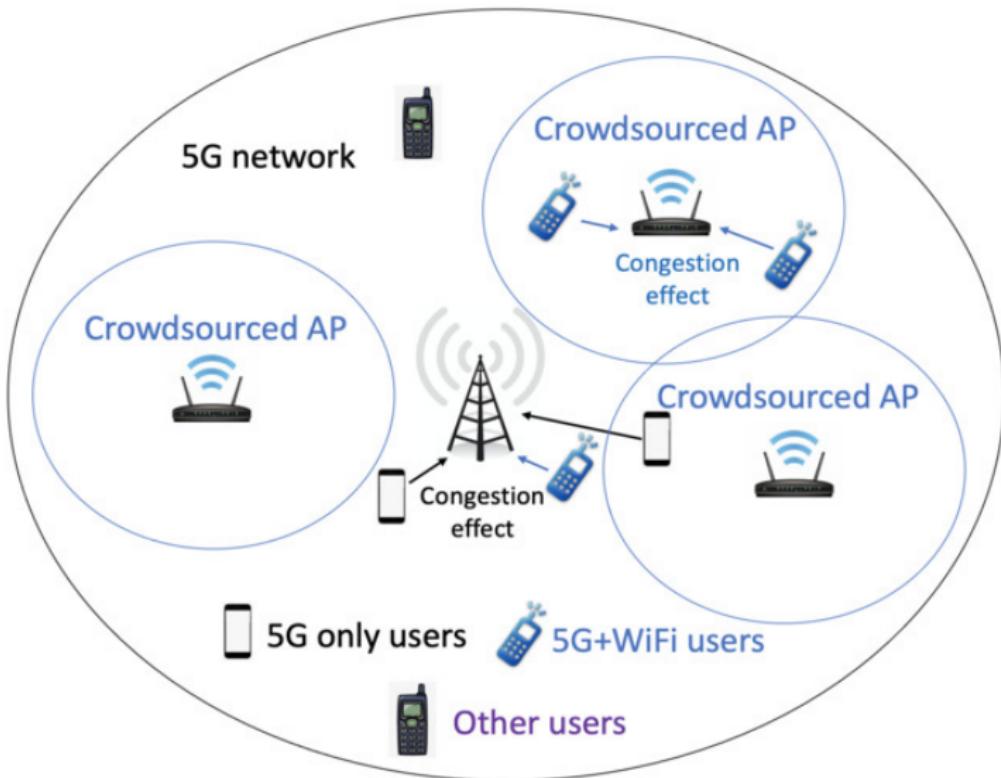
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System Model



Co-existence of the 5G and the crowdsourced WiFi networks.

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5G operator's profit is a **product** of the number of subscribers and the price per subscriber:

$$\pi_1(\bar{p}_1) = N \cdot \bar{x}_1(\bar{p}_1) \cdot \bar{p}_1,$$

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The user's payoff of 5G subscription is given by:

$$\bar{u}_1(\theta) = V_1 - \frac{N\bar{x}_1}{Q}\theta - \bar{p}_1.$$

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Two-stage Stackelberg Game

In practice, the network operators have more power to lead as compared to the users as followers.

Stage I: (Operator's Pricing)

The 5G operator determines price \bar{p}_1 and announces to users.

Stage II: (Users' Subscription)

Each user subscribes (with at least observation payoff \bar{u}) or not.

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We will derive equilibrium with backward induction.

Users' Equilibrium Participation in Stage II

Denote $F^{-1}(\cdot)$ as the inverse function of CDF of users' congestion sensitivity $F(\cdot)$.

Only users of **low** 5G congestion sensitivity will join the 5G network.

We expect the marginal user's payoff is equal to the fixed reservation payoff.

$$\bar{u}_1(\theta = F^{-1}(\bar{x}_1^*)) = \bar{u}.$$

Users' Equilibrium Participation in Stage II

Lemma 1. Equilibrium in Stage II before the introduction of the crowdsourced WiFi

Given any 5G price \bar{p}_1 in Stage I, only users with low congestion sensitivity $\theta \leq F^{-1}(\bar{x}_1^*)$ decide to join the 5G network, where

$$\bar{x}_1^* = \begin{cases} 1, & \text{if } \bar{p}_1 \leq V_1 - \bar{u} - N/Q, \\ F(\bar{\theta}^*), & \text{if } V_1 - \bar{u} - N/Q < \bar{p}_1 < V_1 - \bar{u}, \\ 0, & \text{if } \bar{p}_1 \geq V_1 - \bar{u}, \end{cases}$$

and cutoff $\bar{\theta}^* \in (0, 1)$ is the unique solution to

$$V_1 - \frac{N}{Q}F(\bar{\theta}^*)\bar{\theta}^* - \bar{p}_1 - \bar{u} = 0.$$

The final 5G subscription fraction \bar{x}_1^* **increases** with the 5G network capacity Q and **decreases** with price \bar{p}_1 .

5G Operator's Equilibrium Pricing in Stage I

Now we turn to Stage I to find 5G's best pricing.

With Stage II's user subscription \bar{x}_1^* , the 5G profit objective becomes

$$\bar{\pi}_1 = \begin{cases} N\bar{p}_1, & \text{if } \bar{p}_1 \leq V_1 - \bar{u} - N/Q, \\ N\bar{p}_1 F(\bar{\theta}^*), & \text{if } V_1 - \bar{u} - N/Q < \bar{p}_1 < V_1 - \bar{u}, \\ 0, & \text{if } \bar{p}_1 \geq V_1 - \bar{u}. \end{cases}$$

The problem is still **non-convex** and is difficult to solve analytically given general $F(\theta)$ distribution.

5G Operator's Equilibrium Pricing in Stage I

Proposition 1. Stage I's Equilibrium before the introduction of crowdsourced WiFi

Assume PDF $f(\theta)$ of users' congestion sensitivity is **continuous and non-increasing**, which applies to uniform, exponential and Pareto distributions. At the equilibrium of the Stackelberg game, the 5G price equilibrium in Stage I is:

$$\bar{p}_1^* = \begin{cases} V_1 - \bar{u} - \frac{N}{Q} \bar{\theta}^* F(\bar{\theta}^*), & \text{if } Q < \left(2 + \frac{1}{f(1)}\right) \frac{N}{V_1 - \bar{u}}, \\ V_1 - \bar{u} - \frac{N}{Q}, & \text{if } Q \geq \left(2 + \frac{1}{f(1)}\right) \frac{N}{V_1 - \bar{u}}, \end{cases}$$

and the fraction of 5G subscribers \bar{x}_1^* is:

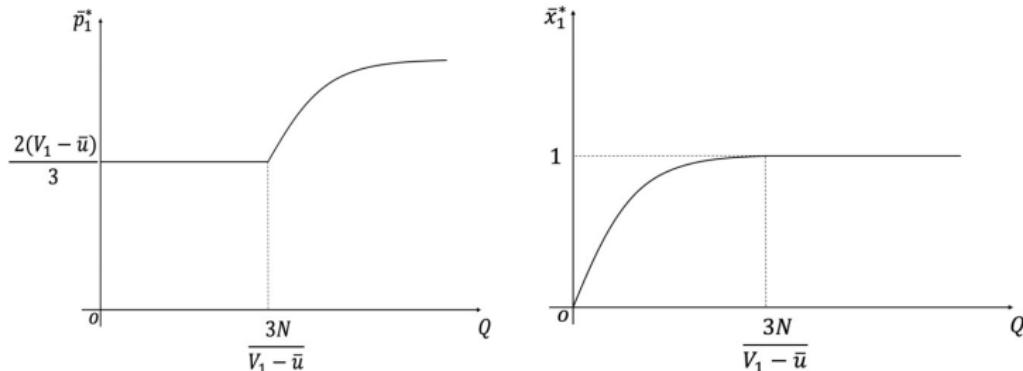
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where $\bar{\theta}^* \in (0, 1)$ is the solution to

$$f(\bar{\theta}^*) \left(V_1 - \bar{u} - \frac{2N}{Q} F(\bar{\theta}^*) \bar{\theta}^* \right) - \frac{N}{Q} F^2(\bar{\theta}^*) = 0.$$

Equilibrium of Two-stage Stackelberg Game

With users' congestion sensitivity $\theta \sim U[0, 1]$, we have equilibrium as follows.



(a) 5G price equilibrium \bar{p}_1^* versus the 5G network capacity Q

(b) Users' subscription \bar{x}_1^* versus capacity Q

- The 5G operator can only charge a **small** price when capacity is **low**.
- Having **non-small** Q , his price **increases**.

System Model after the Introduction of the Crowdsourced WiFi

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- 5G users can further **add on** the crowdsourced WiFi service.

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- $x_1 \in [0, 1]$: the fraction of N users joining the 5G network only,
- $x_2 \in [0, 1]$: the fraction of joining both 5G+WiFi.

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Each 5G+WiFi user

- contributes a **normalized positive addition** $\alpha \in (0, 1)$ to the network coverage (using his home AP),
- the **overall coverage** of the crowdsourced WiFi network is αx_2 .

System Model after the Introduction of the Crowdsourced WiFi

Now the fraction x_2 in the crowdsourced WiFi also affects the 5G congestion.

Each 5G+WiFi user finds himself

- in the WiFi coverage with probability αx_2 ,
- and outside with probability $1 - \alpha x_2$.

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$x_1 + x_2(1 - \alpha x_2)$ fraction of users will share the limited capacity Q .

A 5G-only User's Payoff after the Introduction of the Crowdsourced WiFi

A 5G-only user

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The user's payoff of 5G subscription only is

$$u_1(\theta) = V_1 - \frac{N(x_1 + x_2(1 - \alpha x_2))}{Q} \theta - p_1.$$

A 5G+WiFi User's Payoff after the Introduction of the Crowdsourced WiFi

A 5G+WiFi user

- pays extra price p_2 to add on WiFi,

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The user's payoff of 5G+WiFi subscription is

$$u_2(\theta) = (1 - \alpha x_2)V_1 + \alpha x_2 V_2 - (1 - \alpha x_2) \frac{N(x_1 + x_2(1 - \alpha x_2))}{Q} \theta - p_1 - p_2.$$

We will give analysis on WiFi congestion later to show similar insights.

Operators' Profits after the Introduction of the Crowdsourced WiFi

Both x_1 and x_2 fractions of users pay the 5G operator with price p_1 ,
the 5G operator's profit changes to:

$$\pi_1 = N(x_1 + \textcolor{red}{x}_2)p_1,$$

Li et al., "Optimal Pricing for Peer-to-Peer Sharing With Network Externalities," in IEEE/ACM Transactions on Networking, vol. 29, no. 1, pp. 148-161, 2021.

Operators' Profits after the Introduction of the Crowdsourced WiFi

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the 5G operator's profit changes to:

$$\pi_1 = N(x_1 + \textcolor{red}{x}_2)p_1,$$

The crowdsourced WiFi operator selfishly decides price p_2 to the fraction x_2 of users, and his profit is:

$$\pi_2 = Nx_2(p_2 - \textcolor{red}{c}),$$

c : the deployment cost per user/AP.

Li et al., "Optimal Pricing for Peer-to-Peer Sharing With Network Externalities," in IEEE/ACM Transactions on Networking, vol. 29, no. 1, pp. 148-161, 2021.

Two-stage Dynamic Game

Stage I: (Operators' Pricing)

The 5G and WiFi operators determine and announce prices p_1 and $p_2 \geq c$, respectively.

Stage II: (Users' Subscription)

Each user decides to subscribe to 5G only, 5G+WiFi or neither.

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The 5G and WiFi operators determine and announce prices p_1 and $p_2 \geq c$, respectively.

Stage II: (Users' Subscription)

Each user decides to subscribe to 5G only, 5G+WiFi or neither.

We expect more users' subscription after the introduction of the crowdsourced WiFi.

We will derive equilibrium with backward induction.

Equilibrium Analysis in Stage II

The analysis of a user's decision is involved:

- a user to add on WiFi helps **reduce** the 5G users' **congestion** and **improve** the WiFi network **coverage**.

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To simplify the user choice analysis:

- we first suppose the equilibrium fractions of users in 5G and 5G+WiFi (i.e., x_1^* and x_2^*) are known and stable,

Equilibrium Analysis in Stage II

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To simplify the user choice analysis:

- we first suppose the equilibrium fractions of users in 5G and 5G+WiFi (i.e., x_1^* and x_2^*) are known and stable,
- and derive each user's choice according to his personalized cost congestion θ .

Users' Subscription in Stage II

Lemma 2. Stage II's equilibrium after the introduction of the crowdsourced WiFi

At the equilibrium of Stage II, a user decides his service choice by comparing his personalized congestion cost $\theta \in [0, 1]$ to two cutoff points $F^{-1}(x_1^*)$ and $F^{-1}(x_1^* + x_2^*)$ as in the following two cases.

- If there are a positive number of subscribers to choose 5G+WiFi (i.e., $x_2^* > 0$), a user's equilibrium choice is:

$$\phi(\theta) = \begin{cases} 1 \text{ (5G only)}, & \text{if } \theta \leq F^{-1}(x_1^*) \text{ and } u_1(\theta) \geq \bar{u}, \\ 2 \text{ (5G+WiFi)}, & \text{if } \theta \in (F^{-1}(x_1^*), F^{-1}(x_1^* + x_2^*)) \text{ and } u_2(\theta) \geq \bar{u}, \\ 0 \text{ (Neither)}, & \text{if } \theta \in (F^{-1}(x_1^* + x_2^*), 1], u_1(\theta) < \bar{u}, \text{ and } u_2(\theta) < \bar{u}. \end{cases}$$

- If there is no subscriber to 5G+WiFi (i.e., $x_2^* = 0$), a user's equilibrium choice is:

$$\phi(\theta) = \begin{cases} 1, & \text{if } \theta \leq F^{-1}(x_1^*) \text{ and } u_1(\theta) \geq \bar{u}, \\ 0, & \text{if } \theta \in (F^{-1}(x_1^*), 1], u_1(\theta) < \bar{u}, \text{ and } u_2(\theta) < \bar{u}. \end{cases}$$

Users' Subscription in Stage II

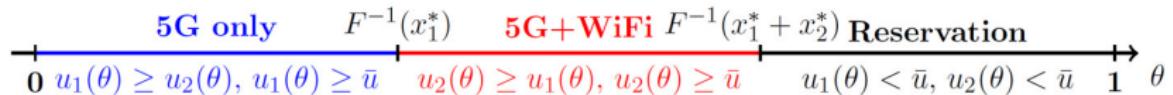


Fig. 3(a)

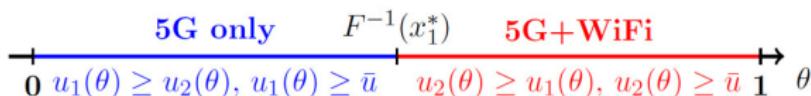


Fig. 3(b)

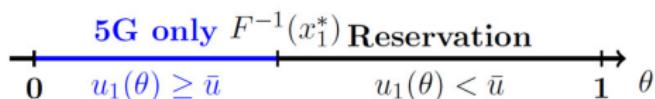


Fig. 3(c)

- Congestion-insensitive users join **5G only** to avoid additional payment.
- Congestion-sensitive users may join **5G+WiFi** for better experience.

Equilibrium in Stage II

Proposition 2.

At the equilibrium of Stage II, user fraction of the 5G and WiFi networks (i.e., x_1^* and x_2^*) are solutions to

$$u_1(F^{-1}(x_1^*)) = u_2(F^{-1}(x_1^*)), \quad u_2(F^{-1}(x_1^* + x_2^*)) = \bar{u},$$

if $x_1^* + x_2^* < 1$, and otherwise

$$u_1(F^{-1}(x_1^*)) = u_2(F^{-1}(x_1^*)), \quad x_1^* + x_2^* = 1,$$

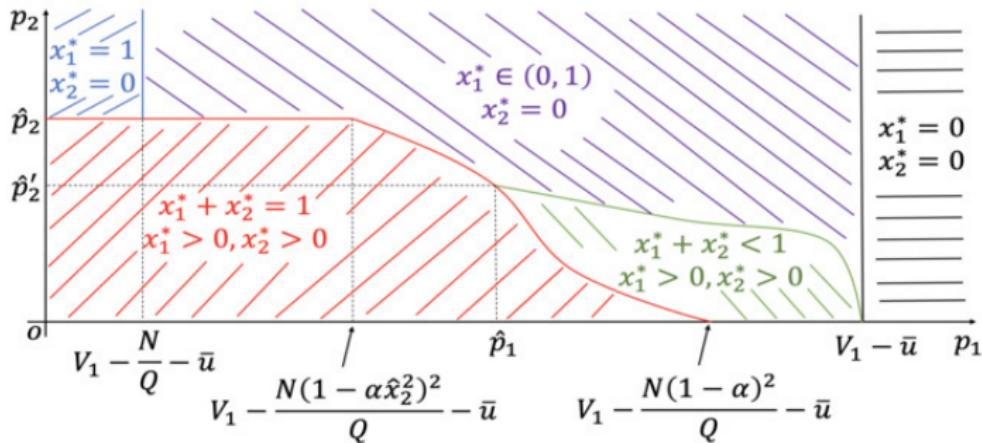
with $u_2(F^{-1}(x_1^* + x_2^*)) \geq \bar{u}$, where $x_2^* \in (0, 1)$ is the largest among all the possible solutions.

Equilibrium in Stage II

To deliver clean engineering insights, We consider

- users obtain the same mobile access profits as $V_1 = V_2$,
- users' congestion sensitivity to follow the uniform distribution:
 $\theta \sim U[0, 1]$.

Later we will show similar insights with θ 's truncated normal distribution.



If both prices of the 5G and the add-on WiFi services are low (see the lower left region), all the users either choose 5G or 5G+WiFi service.

Equilibrium in Stage II

Proposition 2. Stage II's equilibrium

The previous figure summarizes the structural results of the Stage II's equilibrium (x_1^* , x_2^*) in five cases, as functions of any given prices p_1 and p_2 . For example, if both prices of the 5G and the add-on WiFi services are low (see the lower left region), i.e.,

$$p_1 \leq V_1 - \bar{u} - \frac{N}{Q}, \quad p_2 \leq \alpha \hat{x}_2 \frac{N}{Q} (1 - \alpha \hat{x}_2^2) (1 - \hat{x}_2),$$

with $\hat{x}_2 \in [0, 1]$ as the unique solution to

$$4\alpha \hat{x}_2^3 - 3\alpha \hat{x}_2^2 - 2\hat{x}_2 + 1 = 0,$$

then all the users either choose 5G or 5G+WiFi service without leaving the wireless market (i.e., $x_1^* + x_2^* = 1$), and the equilibrium user fraction x_2^* of 5G+WiFi is the greatest root in the range (0,1) to

$$p_2 - \alpha x_2^* \frac{N}{Q} (1 - \alpha (x_2^*)^2) (1 - x_2^*) = 0.$$

In another region (in the lower mid region), where the 5G capacity is small (i.e., $Q < \frac{N}{V_1 - \bar{u}}$) and the WiFi coverage addition per AP is small (i.e., $\alpha < 1 - \sqrt{\frac{V_1 - \bar{u}}{N/Q}}$), at the equilibrium not all the users choose 5G or 5G+WiFi service (i.e., $x_1^* + x_2^* < 1$).

Equilibrium Analysis in Stage I

We do **not** have closed-form solutions of x_1^* and x_2^* in Stage II,

- it is even more difficult to derive the profit objectives π_1 and π_2 .

To make it tractable on 5G profits:

- we first keep the 5G operator's price unchanged after the introduction of the crowdsourced WiFi,
- and we will prove that the 5G operator can still gain from the introduction of the crowdsourced WiFi.

5G Operator's Equilibrium Profit in Stage I

Lemma 3.

At the equilibrium of the whole dynamic game, the 5G operator obtains **at least the same** profit after the introduction of the crowdsourced WiFi, i.e., $\pi_1^* \geq \bar{\pi}_1^*$.

Proposition 4. More profit with non-large capacity regime

At the equilibrium of the whole dynamic game, the 5G operator obtains a **strictly greater** profit after the introduction of the crowdsourced WiFi, i.e., $\pi_1^* > \bar{\pi}_1^*$, as long as **the 5G capacity is small** (i.e., $Q < 3N/(V_1 - \bar{u})$) and **WiFi deployment cost is small**.

Proposition 6. More profit with large capacity regime

At the equilibrium of the whole dynamic game, the 5G operator obtains a **strictly greater** profit after the introduction of the crowdsourced WiFi, i.e., $\pi_1^* > \bar{\pi}_1^*$, as long as **the WiFi deployment cost is small** as in Proposition 5, and **the 5G network capacity is large** (i.e., $Q \geq 3N/(V_1 - \bar{u})$).

5G Operator's Pricing in Large Capacity Regime

Proposition 5.

At the equilibrium, the 5G network operator charges **at least the same** 5G price (i.e., $p_1^* \geq \bar{p}_1^*$ if the 5G capacity is non-small (i.e., $Q \geq 3N/V_1$). Furthermore, the 5G operator charges a **strictly greater price** (i.e., $p_1^* > \bar{p}_1^*$) if **the 5G capacity is non-small** (i.e., $Q \geq 3N/V_1$) and **deployment cost per AP is small**, that is,

$$c \leq \alpha \hat{x}_2 \frac{N}{Q} (1 - \alpha \hat{x}_2^2) (1 - \hat{x}_2),$$

with $\hat{x}_2 \in (0, 1)$ as the unique solution to

$$4\alpha \hat{x}_2^3 - 3\alpha \hat{x}_2^2 - 2\hat{x}_2 + 1 = 0.$$

5G Operator's Pricing in Medium Capacity Regime

Proposition 7.

At the equilibrium, the 5G operator charges users more (i.e., $p_1^* > \bar{p}_1^*$) after the introduction of the crowdsourced WiFi if the 5G network capacity is small (i.e., $3(\frac{\sqrt{17}+23}{32})^2 N/V_1 < Q < 3N/V_1$), the WiFi coverage addition per AP is non-small, that is,

$$\alpha \geq \left(\frac{2\sqrt{1 - \sqrt{\frac{V_1}{3N/Q}}} \left(1 - 2\sqrt{\frac{V_1}{3N/Q}} \right)}{2 - 3\sqrt{\frac{V_1}{3N/Q}}} \right)^2,$$

and deployment cost per user c is small, that is,

$$c \leq \alpha \hat{x}_2 \frac{N}{Q} (1 - \alpha \hat{x}_2^2) (1 - \hat{x}_2),$$

with $\hat{x}_2 \in (0, 1)$ as the unique solution to

$$4\alpha \hat{x}_2^3 - 3\alpha \hat{x}_2^2 - 2\hat{x}_2 + 1 = 0.$$

5G Operator's Pricing in Small Capacity Regime

Proposition 8.

At the equilibrium, the 5G operator **charges users less** (i.e., $p_1^* < \bar{p}_1^*$) after the introduction of the crowdsourced WiFi if the following conditions hold:

- the 5G network capacity is **small** (i.e., $Q < N/V_1$),
- the WiFi coverage addition per AP is **small** (i.e., $\alpha < 1 - \sqrt{\frac{V_1}{N/Q}}$),
- deployment cost per user c is **non-small** as

$$c \in \left(\frac{1 - \sqrt{1 - 3\alpha} \sqrt{\frac{V_1}{3N/Q}}}{3} \frac{N}{Q} \sqrt{\frac{V_1}{3N/Q}} \left(\sqrt{\frac{V_1}{3N/Q}} - \frac{1 - \sqrt{1 - 3\alpha} \sqrt{\frac{V_1}{3N/Q}}}{3\alpha} \left(1 - \frac{1 - \sqrt{1 - 3\alpha} \sqrt{\frac{V_1}{3N/Q}}}{3} \right) \right), \right. \\ \left. \frac{1 - \sqrt{1 - 3\alpha} \sqrt{\frac{V_1}{N/Q}}}{3} \frac{N}{Q} \sqrt{\frac{V_1}{N/Q}} \left(\sqrt{\frac{V_1}{N/Q}} - \frac{1 - \sqrt{1 - 3\alpha} \sqrt{\frac{V_1}{N/Q}}}{3\alpha} \left(1 - \frac{1 - \sqrt{1 - 3\alpha} \sqrt{\frac{V_1}{N/Q}}}{3} \right) \right) \right).$$

Users' Less Payoffs at the Equilibrium

Proposition 9.

At the equilibrium, all the users obtain **strictly less** payoff after the introduction of the crowdsourced WiFi (i.e., $\max\{u_1^*(\theta), u_2^*(\theta)\} < \bar{u}_1^*(\theta)$), if the **5G capacity is non-small** (i.e., $Q \geq 3N/V_1$) and **deployment cost per AP is small**, that is,

$$c \leq \alpha \hat{x}_2 \frac{N}{Q} (1 - \alpha \hat{x}_2^2) (1 - \hat{x}_2),$$

with $\hat{x}_2 \in (0, 1)$ as the unique solution to

$$4\alpha \hat{x}_2^3 - 3\alpha \hat{x}_2^2 - 2\hat{x}_2 + 1 = 0.$$

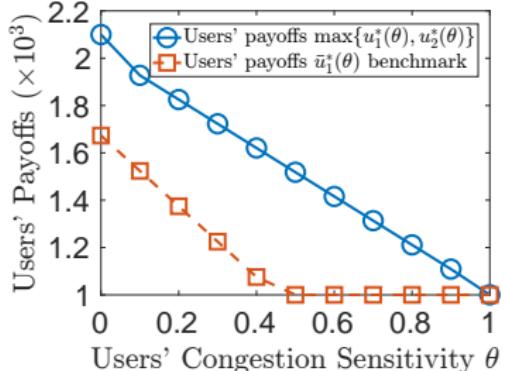
- Users obtain less with **higher** price after the introduction of the crowdsourced WiFi.

Numerical Results

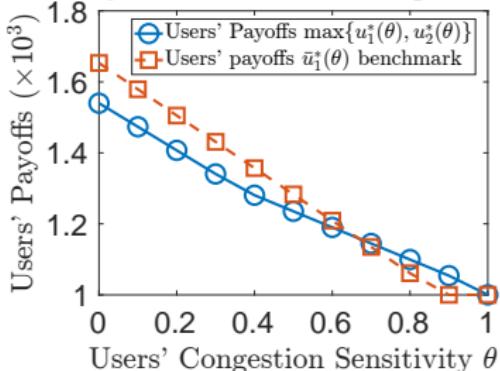
- We consider θ 's **truncated normal distribution** to numerically show similar insights.
- The WiFi deployment cost per access point includes the special router cost in tens or hundreds of dollars: $c = 100$ and 50 .
- We refer the 5G operator's prices as users' annual payment to network operators, ranging from hundreds to thousands of dollars.

AT&T's 5G plan, <https://www.att.com/plans/unlimited-data-plans/>.

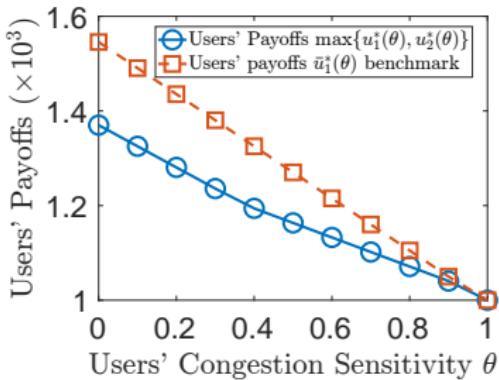
Numerical Results on Users' Equilibrium Payoffs



(c) Small Capacity $Q = 30$

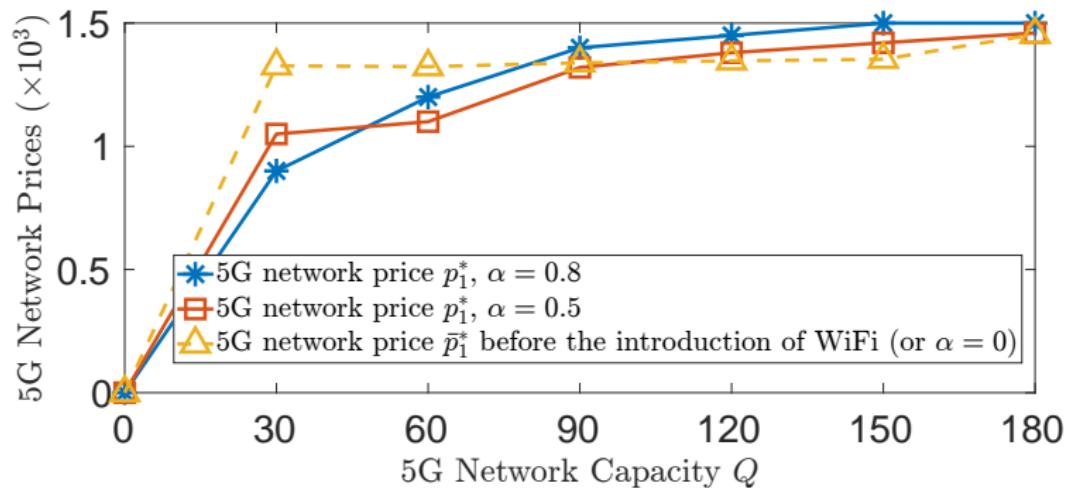


(d) Small Capacity $Q = 120$



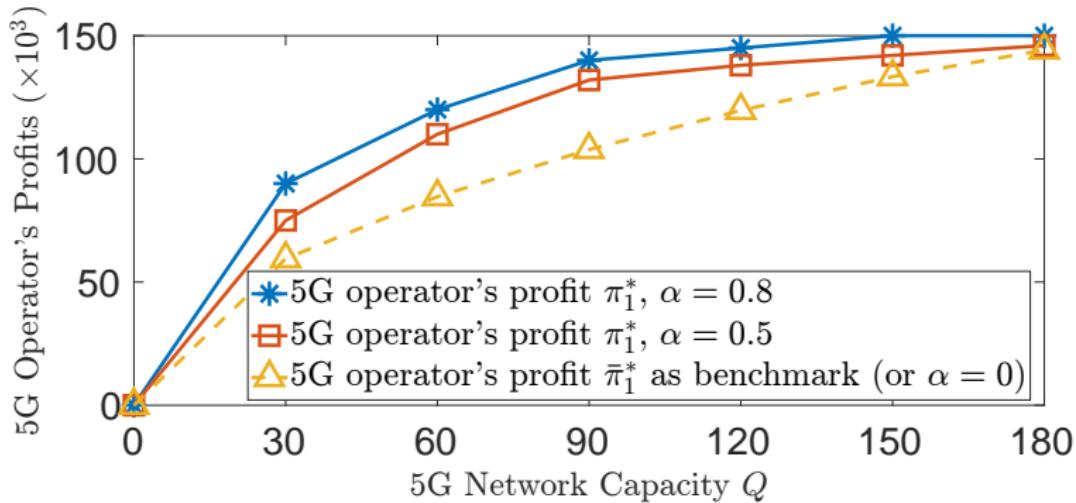
(e) Non-small capacity $Q = 180$

Numerical Results on 5G's Pricing



Small 5G network capacity $Q=30$,
decreased 5G price with increased AP coverage α .

Numerical Results on 5G's Profits



Non-small 5G capacity brings less improvement on 5G profit after the introduction of the crowdsourced WiFi.

Extension to Congested WiFi Case

We suppose $V_1 = V_2 = V$ for ease of exposition.

After we consider WiFi congestion,

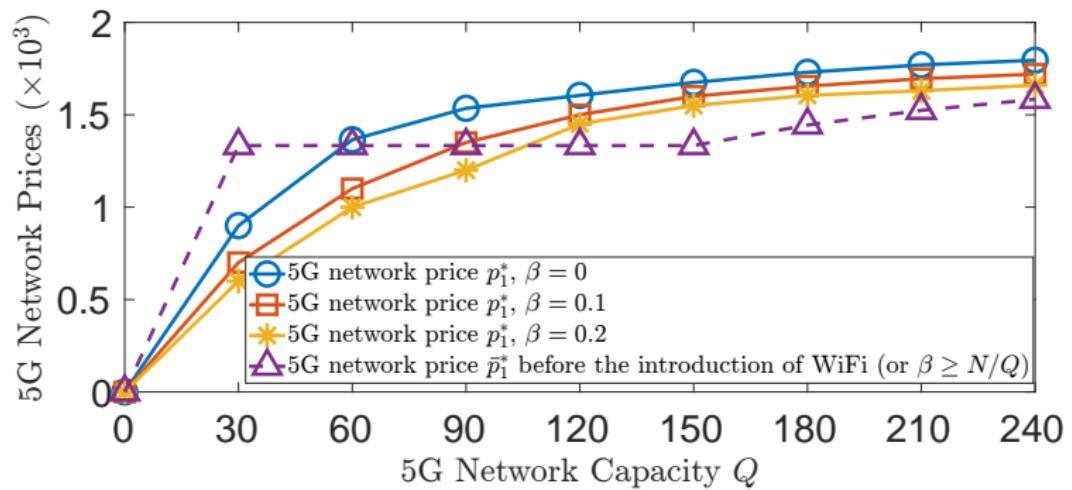
- a 5G-only user's payoff does not change,
- a 5G+WiFi user's becomes

$$\tilde{u}_2(\theta) = V - (1 - \alpha x_2) \frac{N(x_1 + x_2(1 - \alpha x_2))}{Q} \theta - \alpha x_2 \beta \theta - p_1 - p_2.$$

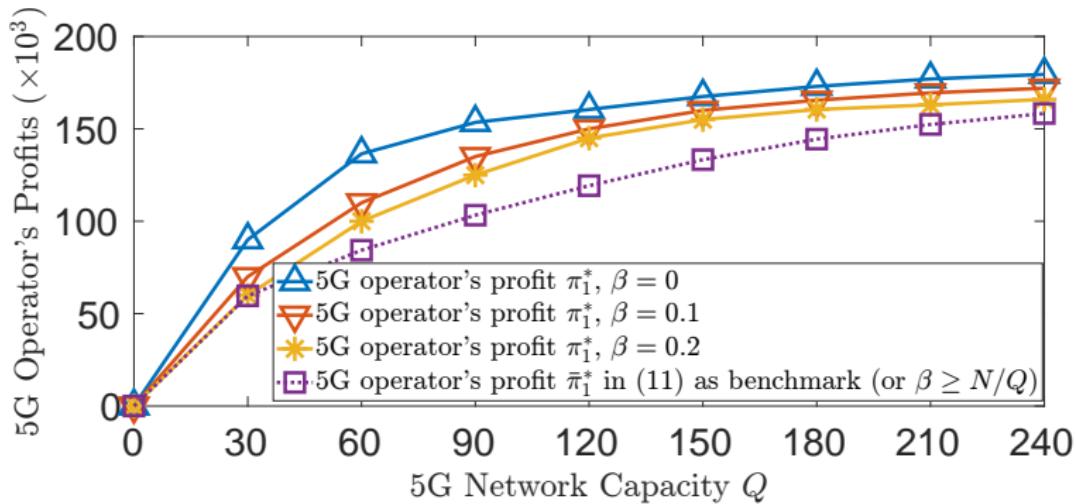
Users' subscription behaviors are the same.

5G operator obtains more after the introduction.

Numerical Results on 5G's Pricing



Numerical Results on 5G's Profits



Summary

We considered

- WiFi's complementarity for 5G networks.
- Both incur diverse network externalities.

We showed that after the introduction of the crowdsourced WiFi,

- 5G operator obtains more profit,
- 5G's structural pricing,
- all the users' payoffs may be worse.

We extended to congested WiFi with similar insights.

Thank You! Q & A