

# Assignment 2

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## 1 Exercise 1

### 1.1 Question 1

Table 1: mean and dispersion

Row.names	Stand dev	Mean	0%	25%	50%	75%	100%
price.PBB_Stk	0.1203319	0.5432103	0.19	0.50	0.58	0.61	1.01
price.PFl_Stk	0.0428952	1.0150201	0.95	0.99	0.99	1.08	1.16
price.PFl_Tub	0.0140545	1.1893758	0.69	1.19	1.19	1.19	1.47
price.PGen_Stk	0.0351661	0.3452819	0.25	0.33	0.33	0.36	0.55
price.PHse_Stk	0.1188312	0.4371477	0.19	0.29	0.45	0.57	0.64
price.PHse_Tub	0.0724550	0.5686734	0.33	0.56	0.59	0.59	1.27
price.PImp_Stk	0.1146461	0.7807785	0.33	0.72	0.75	0.88	2.30
price.PPk_Stk	0.1505174	0.5184362	0.19	0.50	0.58	0.62	0.67
price.PPk_Tub	0.0297261	1.0774094	0.98	1.07	1.09	1.09	1.24
price.PSS_Tub	0.0612116	0.8250895	0.50	0.80	0.85	0.85	0.98

### 1.2 Question 2

Table 2: Market Share

mode	count	share (%)
PBB_Stk	699	15.637584
PFl_Stk	243	5.436242
PFl_Tub	225	5.033557
PGen_Stk	315	7.046980
PHse_Stk	593	13.266219
PHse_Tub	33	0.738255
PImp_Stk	74	1.655481
PPk_Stk	1766	39.507830
PPk_Tub	203	4.541387
PSS_Tub	319	7.136465

Table 3: Average price by choice

	average
PPk_Stk	0.5184
PBB_Stk	0.5432
PFl_Stk	1.0150
PHse_Stk	0.4371
PGen_Stk	0.3453
PImp_Stk	0.7808
PSS_Tub	0.8251
PPk_Tub	1.0774
PFl_Tub	1.1894
PHse_Tub	0.5687

Class:

below or equal to average: below or equal to the average price of the corresponding choice

Table 4: Market Share by Product Characteristics

mode	class	count	share (%)
PBB_Stk	below or equal to average	436	9.7539150
PBB_Stk	over average	263	5.8836689
PFl_Stk	below or equal to average	190	4.2505593
PFl_Stk	over average	53	1.1856823
PFl_Tub	below or equal to average	25	0.5592841
PFl_Tub	over average	200	4.4742729
PGen_Stk	below or equal to average	175	3.9149888
PGen_Stk	over average	140	3.1319911
PHse_Stk	below or equal to average	297	6.6442953
PHse_Stk	over average	296	6.6219239
PHse_Tub	below or equal to average	16	0.3579418
PHse_Tub	over average	17	0.3803132
PImp_Stk	below or equal to average	56	1.2527964
PImp_Stk	over average	18	0.4026846
PPk_Stk	below or equal to average	978	21.8791946
PPk_Stk	over average	788	17.6286353
PPk_Tub	below or equal to average	87	1.9463087
PPk_Tub	over average	116	2.5950783
PSS_Tub	below or equal to average	119	2.6621924
PSS_Tub	over average	200	4.4742729

### 1.3 Question 3

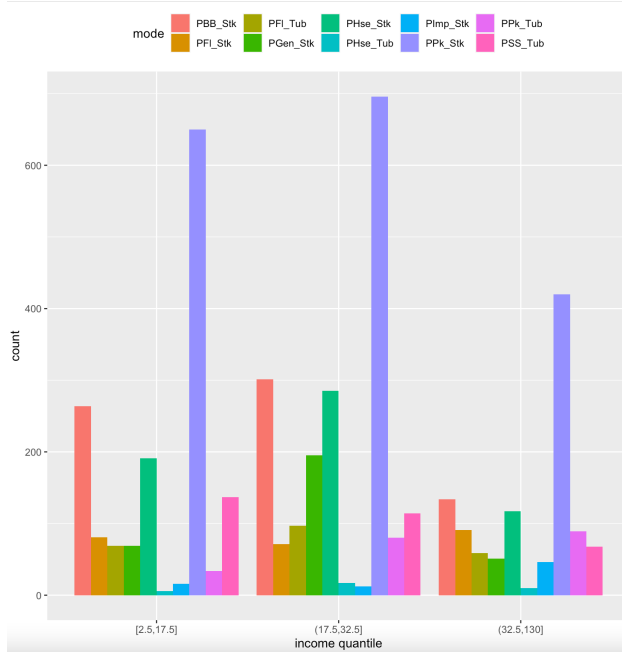


Figure 1: income

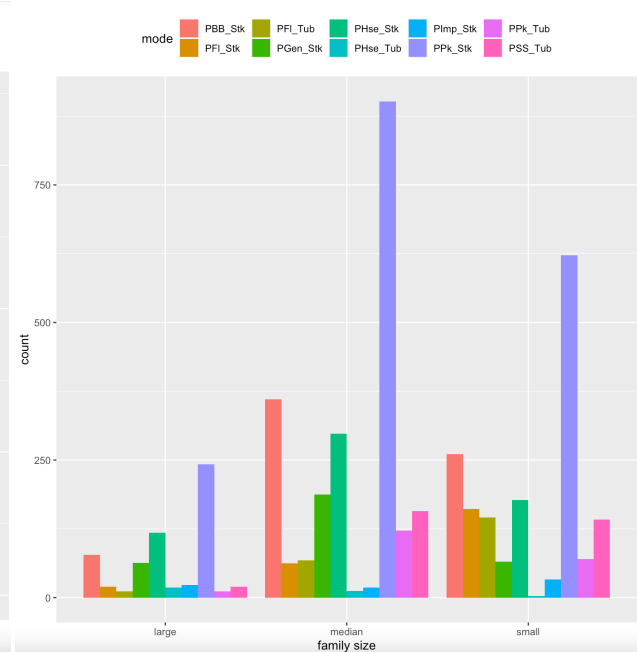


Figure 2: family size

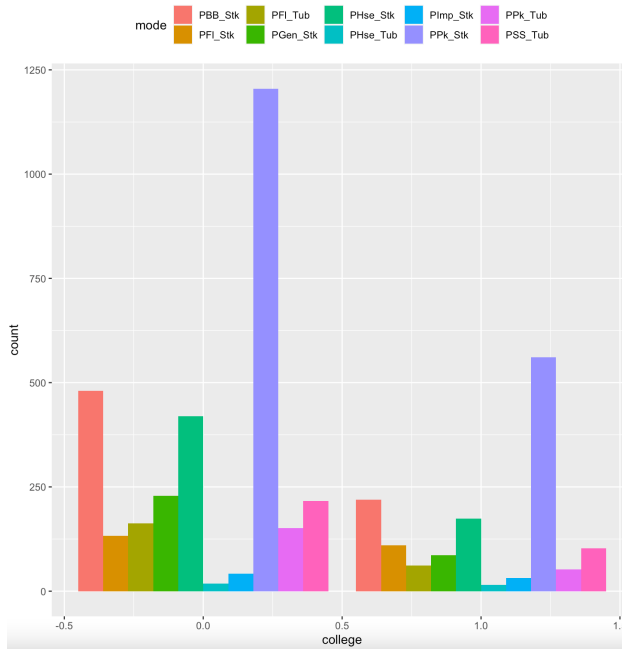


Figure 3: college

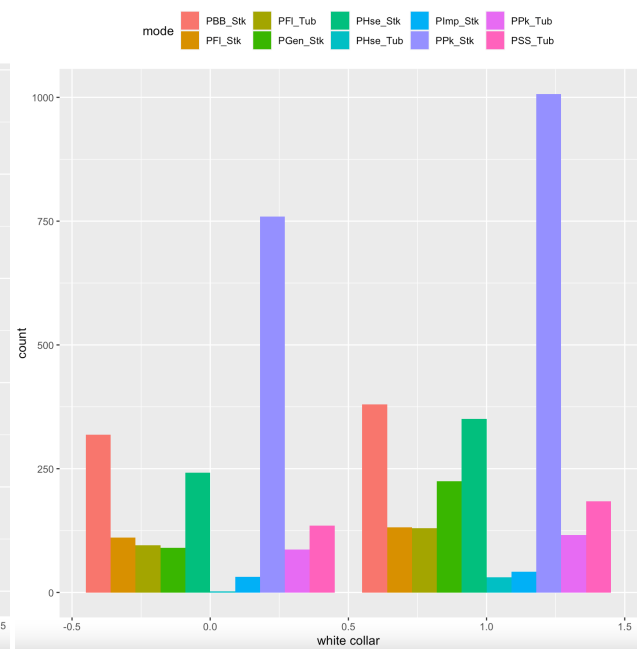


Figure 4: white collar

I counted the amount of transactions by choices and customer attributes. The following bar plots display households' preferences for different choices. Among all results, PPK.stk is always the most popular choice, while PHse.Tub and Plmp.Stk are always the least popular choices.

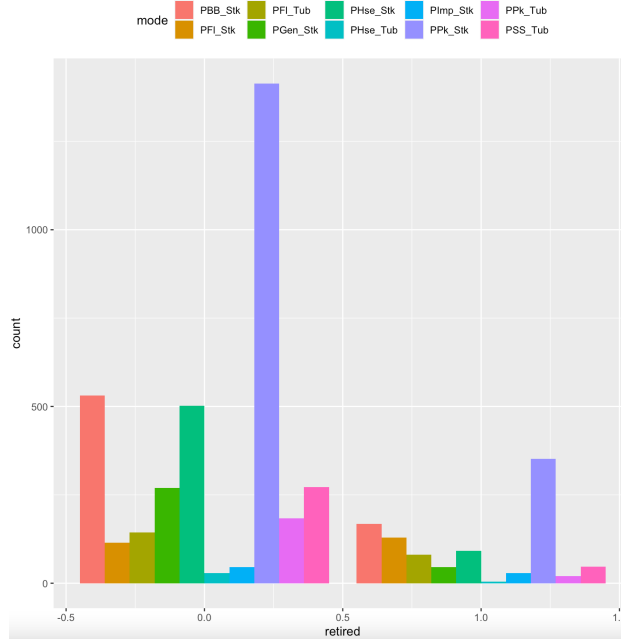


Figure 5: retired

## 2 Exercise 2

### 2.1 Question 1

Since price varies across alternatives, I used a conditional logit model to estimate the effect of price on demand.

### 2.2 Question 2

Table 5: Conditional Logit Model Results

variable_name	own:	mlogit:
(Intercept):PFI_Stk	2.2512752	2.2512752
(Intercept):PFI_Tub	3.3118117	3.3118118
(Intercept):PGen_Stk	-1.9496981	-1.9496981
(Intercept):PHse_Stk	-0.7630255	-0.7630255
(Intercept):PHse_Tub	-2.9422865	-2.9422866
(Intercept):PImp_Stk	-0.5610045	-0.5610044
(Intercept):PPk_Stk	0.9543069	0.9543069
(Intercept):PPk_Tub	2.4191751	2.4191751
(Intercept):PSS_Tub	1.2060752	1.2060752
price	-6.6565795	-6.6565796

### 2.3 Question 3

Holding other conditions the same, an increase in price would cause a decrease in customers' demand for margarine.

### 3 Exercise 3

#### 3.1 Question 1

Income is a family(or individual)-specific variable and doesn't vary across alternatives, so I used a multinomial logit model to estimate the effect of Income on demand.

#### 3.2 Question 2

Table 6: Multinomial Logit Model Results

variable_name	own:	mlogit:
(Intercept):PFl_Stk	-1.5545341	-1.5545334
(Intercept):PFl_Tub	-1.7302736	-1.7302731
(Intercept):PGen_Stk	-0.8452588	-0.8452576
(Intercept):PHse_Stk	-0.3560029	-0.3560023
(Intercept):PHse_Tub	-3.4369486	-3.4369458
(Intercept):PImp_Stk	-3.2944444	-3.2944412
(Intercept):PPk_Stk	0.8453236	0.8453241
(Intercept):PPk_Tub	-2.0030289	-2.0030281
(Intercept):PSS_Tub	-0.6857181	-0.6857174
Income:PFl_Stk	0.0176750	0.0176750
Income:PFl_Tub	0.0208317	0.0208317
Income:PGen_Stk	0.0018352	0.0018351
Income:PHse_Stk	0.0071392	0.0071392
Income:PHse_Tub	0.0138797	0.0138797
Income:PImp_Stk	0.0337008	0.0337007
Income:PPk_Stk	0.0030888	0.0030887
Income:PPk_Tub	0.0259749	0.0259749
Income:PSS_Tub	-0.0038438	-0.0038438

#### 3.3 Question 3

Holding other conditions the same, an increase in households' income would increase households' relative demand for PFl\_stk, PFl\_Tub, PGen\_Stk, PHse\_Stk, PHse\_Tub, PImp\_Stk, PPk\_Tub compared to PBB\_Stk, but decrease households' relative demand for PSS\_Tub compared to PBB\_Stk.

## 4 Exercise 4

### 4.1 Model 1

Table 7: Marginal Effects for Model 1 - Conditional Logit

	PPk_Stk	PBB_Stk	PFL_Stk	PHse_Stk	PGen_Stk	PImp_Stk	PSS_Tub	PPk_Tub	PFL_Tub	PHse_Tub
PPk_Stk	-1.2853	0.2954	0.1207	0.2951	0.1562	0.0373	0.1536	0.0993	0.1108	0.0168
PBB_Stk	0.2954	-0.7454	0.0551	0.1335	0.0728	0.0167	0.0693	0.0452	0.0507	0.0068
PFL_Stk	0.1207	0.0551	-0.3375	0.0505	0.0303	0.0071	0.0293	0.0197	0.0218	0.0030
PHse_Stk	0.2951	0.1335	0.0505	-0.7127	0.0640	0.0166	0.0637	0.0393	0.0442	0.0059
PGen_Stk	0.1562	0.0728	0.0303	0.0640	-0.4281	0.0087	0.0379	0.0251	0.0285	0.0044
PImp_Stk	0.0373	0.0167	0.0071	0.0166	0.0087	-0.1073	0.0085	0.0054	0.0061	0.0008
PSS_Tub	0.1536	0.0693	0.0293	0.0637	0.0379	0.0085	-0.4203	0.0258	0.0279	0.0042
PPk_Tub	0.0993	0.0452	0.0197	0.0393	0.0251	0.0054	0.0258	-0.2825	0.0198	0.0029
PFL_Tub	0.1108	0.0507	0.0218	0.0442	0.0285	0.0061	0.0279	0.0198	-0.3131	0.0033
PHse_Tub	0.0168	0.0068	0.0030	0.0059	0.0044	0.0008	0.0042	0.0029	0.0033	-0.0482

### 4.2 Model 2

Table 8: Marginal Effects for Model 2 - Multinomial Logit

name	own:	mlogit:
PBB_Stk	-0.0008980	-0.0009036
PFL_Stk	0.0006285	0.0006443
PFL_Tub	0.0007356	0.0007460
PGen_Stk	-0.0002773	-0.0002781
PHse_Stk	0.0001694	0.0001849
PHse_Tub	0.0000581	0.0000602
PImp_Stk	0.0004437	0.0004131
PPk_Stk	-0.0010674	-0.0010625
PPk_Tub	0.0008876	0.0008781
PSS_Tub	-0.0006802	-0.0006824

## 5 Exercise 5

### 5.1 Question 1

Table 9: Mixed Logit Model Results

variable_name	own:	mlogit:
(Intercept):PFl_Stk	1.7292656	1.7292804
(Intercept):PFl_Tub	2.7048170	2.7047987
(Intercept):PGen_Stk	-2.0327748	-2.0327371
(Intercept):PHse_Stk	-0.9878331	-0.9878182
(Intercept):PHse_Tub	-3.3021057	-3.3017121
(Intercept):PImp_Stk	-1.6163988	-1.6164452
(Intercept):PPk_Stk	0.8406519	0.8406734
(Intercept):PPk_Tub	1.6437260	1.6437333
(Intercept):PSS_Tub	1.3375013	1.3375425
Income:PFl_Stk	0.0186048	0.0186039
Income:PFl_Tub	0.0212514	0.0212510
Income:PGen_Stk	0.0030780	0.0030771
Income:PHse_Stk	0.0083602	0.0083598
Income:PHse_Tub	0.0130294	0.0130195
Income:PImp_Stk	0.0340684	0.0340689
Income:PPk_Stk	0.0042606	0.0042599
Income:PPk_Tub	0.0262572	0.0262564
Income:PSS_Tub	-0.0049842	-0.0049857
price	-6.6597059	-6.6596694

### 5.2 Question 2

Table 10: Mixed Logit Model Results - drop PPk\_Stk

variable_name	own:	mlogit:
(Intercept):PFl_Stk	1.6364930	1.6364939
(Intercept):PFl_Tub	2.5760207	2.5760219
(Intercept):PGen_Stk	-1.9689330	-1.9689328
(Intercept):PHse_Stk	-0.9428327	-0.9428325
(Intercept):PHse_Tub	-3.2438881	-3.2438745
(Intercept):PImp_Stk	-1.6476828	-1.6476817
(Intercept):PPk_Tub	1.5551281	1.5551291
(Intercept):PSS_Tub	1.2230776	1.2230785
Income:PFl_Stk	0.0184166	0.0184166
Income:PFl_Tub	0.0210461	0.0210461
Income:PGen_Stk	0.0030968	0.0030968
Income:PHse_Stk	0.0075214	0.0075214
Income:PHse_Tub	0.0126704	0.0126704
Income:PImp_Stk	0.0336065	0.0336065
Income:PPk_Tub	0.0259724	0.0259724
Income:PSS_Tub	-0.0043200	-0.0043201
price	-6.4220987	-6.4220997

### 5.3 Question 3

Table 11: Log Likelihood

	$\beta^f$	$\beta^r$
log likelihood	-4885.129	-4884.175

$$MTT = 1.907538$$

### 5.4 Question 4

Since the value of MTT is not significant, we could not reject IIA, which means that excluding “PPk\_Stk” from the model could not be expected to affect the relative risks of the remaining choices.